## Untitled

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```
library(MASS);
library(nlme);
source("D:/WPI/prediction/Lib_Prediction.R");
source("D:/WPI/prediction/Lib_simu_genetic_data.R");
## Rlab 2.15.1 attached.
## Attaching package: 'Rlab'
## The following object is masked from 'package:MASS':
##
##
       michelson
## The following objects are masked from 'package:stats':
##
##
       dexp, dgamma, dweibull, pexp, pgamma, pweibull, qexp, qgamma,
       qweibull, rexp, rgamma, rweibull
## The following object is masked from 'package:datasets':
##
##
       precip
source("D:/WPI/prediction/generate response formula.R");
###Parameter setting
###Parameters on the effects / coefficients
beta0 = -0.5;
#For binary trait, the risk at X=0 is 1/(1+exp(-beta0)). The average risk (prevalence) at given coeffic
# Y = array(NA, length(Xbeta));
# for (i in 1:length(Y)) {
    Py1x = 1/(1 + exp(-Xbeta[i]) - beta0); #P(y=1 | x) based on logistic model
     Y[i] = ifelse(runif(1) < Py1x, 1, 0);
# }
# mean(Y); #prevalance of Y.
\#beta0 = -7; \# for binary trait. Risk when X=0 is 1/(1+exp(7))=0.0009110512. Also, at the given coeffic
\#beta0 = -3; \# for binary trait. Risk when X=0 is 1/(1+exp(3))=0.04742587. Also, at the given coefficie
raceN = 3; #Number of racial groups
```

```
sigma.race = 1; #pair-wise covariance among individuals in the same racial group
beta.race = 1; #treat the "coefficient" of the mix-effect b_i be 1.
beta.acup = log(4.9); #6; #Coeff of acupuncture
beta.mbsr = log(4.9); #6; #Coeff of mbsr
beta.sex = log(1.1); #1;
beta.age = log(1.25); #-1;
beta.edu = log(1.26); #1;
beta.len = log(1.13); #1;
beta.bas = log(0.80); #1;
beta.conc = log(0.77); #1;
markerN = 10; #The # of PainMarkers
beta.biom.v = 2; #=1; #The value of the coeff of the biomarkers
beta.biom = rep(beta.biom.v, markerN); #Coeff of the biomarkers
names.xbiom = paste("xbiom", 1:markerN, sep=""); #variable names for biomarkers
mdfN.acup = 4; #The # of modifiers for acupuncture
beta.mdf.acup.v=2; #The value of the coeff of accupunctur's modifiers
beta.mdf.acup = rep(beta.mdf.acup.v, mdfN.acup); #Vector of coeffs of accupunctur's modifiers
gama.acup.v = 2; #The value of the coeff of the modifier*acupucture interaction terms.
gama.acup = rep(gama.acup.v, mdfN.acup); #Vector of coeffs of the modifier*acupucture interaction terms
names.mdf.acup = paste("zmdfAcup", 1:mdfN.acup, sep=""); #variable names of the modifiers for acupunctu
mdfN.mbsr = 4; #The # of modifiers for MBSR
beta.mdf.mbsr.v=2; #The value of the coeff of MBSR's modifiers
beta.mdf.mbsr = rep(beta.mdf.mbsr.v, mdfN.mbsr); #Vector of coeffs of accupunctur's modifiers
{\tt gama.mbsr.v = 2;} \ \textit{\#The value of the coeff of the modifier*MBSR interaction terms.}
gama.mbsr = rep(gama.mbsr.v, mdfN.mbsr); #Vector of coeffs of the modifier*MBSR interaction terms.
names.mdf.mbsr = paste("zmdfMBSR", 1:mdfN.mbsr, sep=""); #variable names of the modifiers for MBSR
errSD=1; #The SD of error term
###Parameters on prodiction process
isRandomCV=T; #Random cross-validation in prediction
nfold=5; #The number of folds in cross-validation
nrepeat=2; #number of repeats of cross-validation
###Parameters on simulations
simuN = 100; #The number of simulations.
###Data simulation and prediction outcomes
predProp = c(0, 0.25, 0.5, 0.75, 1); #Proportion of true predictors besides names.basic that are includ
models = vector(mode = "list", length(predProp)); #prediction models .
outputs = vector(mode = "list", length(predProp)); #prediction outputs .
###Parameters on data
groupSampleSizes = seq(20, 400, by=20);
#qroupSampleSizes = seq(500, 2000, by=100);
\#groupSampleSizes = seq(150, 500, by=50);
AUC = array(NA, dim=c(length(groupSampleSizes), length(predProp)));
```

```
\#Store\ AUC\ over\ sample\ sizes\ and\ proportions\ of\ predictors\ used.
for(gi in 1:length(groupSampleSizes))
  groupSampleSize = groupSampleSizes[gi];
  #sample size for each of the three groups: control, mbsr, and acupuncture.
  ###Looping through simulations
  R2.controls = array(NA, simuN); #Store the R2 of the controlling predictors.
  for(i in 1:simuN)
    ###Generate data
   x0 = rep(1, groupSampleSize*3);
    #The mixed-effect term for racial group
   xrace = sample(1:raceN, size=groupSampleSize*3, replace=T, prob=rep(1/raceN, raceN));
    #Assume equal chance for each racial group to be sampled.
   b.xrace = array(NA, dim=groupSampleSize*3); #b.xrace is the vector of b_i values.
   for (racei in 1:raceN)
     b.xrace[which(xrace==racei)] = rnorm(1, sd=sigma.race);
    #assign the same b_i value for the all in the ith racial group.
    #The "basic" factors
   xacup = c(rep(0, groupSampleSize*2), rep(1, groupSampleSize));
    #acupuncture group indicator
   xmbsr = c(rep(0, groupSampleSize), rep(1, groupSampleSize), rep(0, groupSampleSize)); #MBSR group i
   xsex = rbinom(n=groupSampleSize*3, size=1, prob=0.5); #50% recruited are males??
   xage = rnorm(n=groupSampleSize*3, mean=0, sd=1); #standardized age.
   xedu = rbinom(n=groupSampleSize*3, size=1, prob=0.5);
   xlen = rbinom(n=groupSampleSize*3, size=1, prob=0.5);
   xbas = rnorm(n=groupSampleSize*3, mean=0, sd=1);
   xconc = rbinom(n=groupSampleSize*3, size=1, prob=0.5);
    #PainMarker data
   xbiom = data.frame(matrix(rnorm(n=groupSampleSize*3*markerN), ncol=markerN)); #Assume biomarker val
   names(xbiom) = names.xbiom;
    #acupuncture-modifier data
   zmdfAcup = data.frame(matrix(rnorm(n=groupSampleSize*3*mdfN.acup), ncol=mdfN.acup));
    #Assume acupuncture-modifier values are N(0,1);
   names(zmdfAcup) = names.mdf.acup;
    #mbsr-modifier data
   zmdfMBSR = data.frame(matrix(rnorm(n=groupSampleSize*3*mdfN.mbsr), ncol=mdfN.mbsr)); #Assume acupun
   names(zmdfMBSR) = names.mdf.mbsr;
   Xmatrix = cbind(x0, b.xrace, xacup, xmbsr, xsex, xage, xedu, xlen, xbas, xconc, xbiom, zmdfAcup, zm
    #### Generate response
   names.mainEff = c("x0", "b.xrace", "xacup", "xmbsr", "xsex", "xage", "xedu", "xlen", "xbas", "xcon
    coeffs.mainEff = c(beta0, beta.race, beta.acup, beta.mbsr, beta.sex, beta.age, beta.edu, beta.len,
```

```
names.trt = c("xacup", "xmbsr"); #variable names of the treatments
names.mdf = list(names.mdf.acup, names.mdf.mbsr); #variable names of the modifiers corresponding to
coeffs.interaction = list(gama.acup, gama.mbsr); #coefficients of the treatment-modifier interactio
# ####----Quantitative Response----
resp = get.Y.reg(XData=Xmatrix, names.mainEff, coeffs.mainEff, names.trt, names.mdf, coeffs.interac
#print(resp$R2); #proportion of variation explained by all predictors
\# Calculate the R^2 of the controlling predictors
vars.control = c(varBeta0=0, varRace=sigma.race^2, varAcup=(1/3)*(1-1/3), varMbsr=(1/3)*(1-1/3), varRace=sigma.race^2, varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3), varAcup=(1/3)*(1-1/3)*(1-1/3), varAcup=(1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3)*(1-1/3
betas.control = c(beta0, beta.race, beta.acup, beta.mbsr, beta.sex, beta.age, beta.edu, beta.len, b
R2.controls[i] = sum(vars.control*betas.control^2)/var(resp$Y);
####----Binary Response-----
\#resp = get.Y.logit(XData=Xmatrix, names.mainEff, coeffs.mainEff, names.trt, names.mdf, coeffs.inte
####Combine data for analysis
xrace = as.factor(xrace); #Convert race into factor variable, which is used in data analysis.
dat = data.frame(Y=resp$Y, Xmatrix, xrace);
####Predictive analysis
names.control = c("xrace", "xacup", "xmbsr", "xsex", "xage", "xedu", "xlen", "xbas", "xconc"); #Con
{\tt names.trt.all = c("xacup", "xmbsr"); \textit{\#All possible treatments that could have interaction effects.}}
for (mi in 1:length(predProp)){
    ##Create model formula based on proportion of predictors used.
                           = round(length(names.xbiom)*predProp[mi]);
   mdf.acup.used = round(length(names.mdf.acup)*predProp[mi]);
   mdf.mbsr.used = round(length(names.mdf.mbsr)*predProp[mi]);
   names.main=c(names.control, names.xbiom[0:xbiom.used], names.mdf.acup[0:mdf.acup.used], names.mdf
   if (predProp[mi] == 0)
      names.trt = NULL;
   }
   else{
      names.trt = names.trt.all;
      names.mdf = list(names.mdf.acup[0:mdf.acup.used], names.mdf.mbsr[0:mdf.mbsr.used]);
   models[[mi]] = formula.f.r(names.main=names.main, names.trt=names.trt, names.mdf=names.mdf, names.
   # ### ---- Predict quantitative outcome ----
   out = meanPredEvaluCV.lme(fixed=models[[mi]]$fixed, dat=dat, randomf=models[[mi]]$random, model R
    #out = meanPredEvaluCV.lme(fixed=models[[mi]]$fixed, dat=dat, randomf=NULL, model_R='lm', loopn=n
   outputs[[mi]] = rbind(outputs[[mi]], t(c(MSE=out[1], L2normRatio=out[2], L1normRatio=out[3], corr
    ### ---- Predict binary outcome ----
    #out = predEvaluCV.qlm(formula=models[[mi]]$fixed, dat=dat, nfold=nfold, nrepeat=nrepeat, isRando
    \#outputs[[mi]] = rbind(outputs[[mi]], t(c(prob=out[1], sensi=out[2], speci=out[3], AUC=out[4])));
    #outputs[[mi]] = rbind(outputs[[mi]], t(unlist(out)));
}
```

```
# #True underlying model
  print(c(sampleSize=groupSampleSize*3, raceN=raceN, sigma.race = sigma.race, beta.acup = beta.acup,
          beta.mbsr = beta.mbsr, beta.sex = beta.sex, beta.age = beta.age, beta.edu=beta.edu, beta.len=
          mdfN.acup=mdfN.acup, beta.mdf.acup.v=beta.mdf.acup.v, gama.acup.v=gama.acup.v,
          mdfN.mbsr=mdfN.mbsr, beta.mdf.mbsr.v=beta.mdf.mbsr.v, gama.mbsr.v=gama.mbsr.v));
  # #R2 of controlling predictors
  mean(R2.controls):
  #Prediction accuracies
  for (mi in 1:length(predProp)){
   print(predProp[mi]);
   print(models[[mi]]$fixed);
   print(apply(outputs[[mi]], 2, mean));
   print(apply(outputs[[mi]], 2, quantile, probs=c(0.05, 0.95)));
    AUC[gi, mi] = apply(outputs[[mi]], 2, mean)[4];
  }
}
##
        sampleSize
                             raceN
                                         sigma.race
                                                          beta.acup
                                                                           beta.mbsr
##
       60.0000000
                        3.00000000
                                         1.00000000
                                                         1.58923521
                                                                          1.58923521
##
          beta.sex
                          beta.age
                                           beta.edu
                                                           beta.len
                                                                            beta.bas
        0.09531018
                        0.22314355
                                         0.23111172
##
                                                         0.12221763
                                                                         -0.22314355
##
         beta.conc
                           markerN
                                        beta.biom.v
                                                          mdfN.acup beta.mdf.acup.v
                                         2.00000000
                                                         4.0000000
##
       -0.26136476
                       10.00000000
                                                                          2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
##
        2.00000000
                        4.00000000
                                         2.00000000
                                                         2.00000000
## [1] 0
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
##
  <environment: 0x0000000212b1878>
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
##
             MSF.
                                  1.15632582
##
   136.54566192
                    1.14642420
                                                 0.01292311
                                                               1.37450210
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        91.96583
                    1.054085
                                1.053518 -0.2490554
                                                           1.104876
## 95% 189.05535
                    1.240469
                                1.280388
                                            0.2546717
                                                           1.666102
  [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x00000002150ca50>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
     126.7743004
                     1.1230934
                                    1.1292502
                                                  0.2902731
                                                                1.3512454
##
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                               0.9500355 0.03936745
## 5%
       87.33891
                   0.9489917
                                                           0.965194
## 95% 166.11695
                   1.2947249
                               1.3054324 0.49846641
                                                           1.752660
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
```

```
## <environment: 0x0000000214fac48>
##
            MSF.
                  L2normRatio L1normRatio correlation MSEoverObsVar
                     1.0365428
                                                 0.4989935
##
     105.9666183
                                  1.0383108
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       70.04285
                 0.8116581
                              0.8120248 0.2886566
                                                         0.7066068
                              1.2996542
## 95% 157.36826
                  1.2895822
                                           0.7101413
                                                         1.7793186
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
## <environment: 0x000000021149858>
##
             MSE
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      73.6503324
                     0.8572437
                                   0.8598638
                                                 0.6867223
                                                               0.8352344
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                   0.603905
## 5%
       38.47027
                              0.5786745
                                           0.5413456
                                                         0.3880001
## 95% 115.78980
                    1.068846
                              1.0792554
                                           0.8283352
                                                         1.3588999
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
      xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
## <environment: 0x0000000130a3920>
##
                                L1normRatio
                                               correlation MSEoverObsVar
             MSE
                  L2normRatio
##
                    0.21628644
                                  0.21762518
                                                0.97658990
                                                              0.05444491
      4.74210565
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 2.422776
                 0.1531011
                              0.1523401
                                          0.9571292
                                                       0.02558233
  95% 7.926379
                 0.2852162
                              0.2939072
                                                       0.09628849
                                          0.9885314
##
       sampleSize
                                                                         beta.mbsr
                             raceN
                                        sigma.race
                                                        beta.acup
      120.00000000
##
                        3.00000000
                                        1.00000000
                                                       1.58923521
                                                                        1.58923521
##
         beta.sex
                                          beta.edu
                                                         beta.len
                                                                          beta.bas
                         beta.age
##
       0.09531018
                        0.22314355
                                        0.23111172
                                                      0.12221763
                                                                       -0.22314355
##
        beta.conc
                           markerN
                                       beta.biom.v
                                                        mdfN.acup beta.mdf.acup.v
                                                      4.00000000
                                                                        2.00000000
##
       -0.26136476
                       10.00000000
                                        2.00000000
##
       gama.acup.v
                        mdfN.mbsr beta.mdf.mbsr.v
                                                     gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
## <environment: 0x000000021756a28>
            MSE
                               L1normRatio
                                               correlation MSEoverObsVar
##
                  L2normRatio
   128.69272176
                                  1.10832479
                                                0.01793359
                    1.10155958
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       95.57048
                   1.009412
                                1.006838 -0.2231301
                                                          1.044707
## 95% 169.44238
                   1.229048
                                           0.2499454
                                1.245699
                                                          1.589165
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
      zmdfAcup1 + xmbsr * zmdfMBSR1
##
```

```
## <environment: 0x0000000216f7bd0>
##
             MSF.
                   L2normRatio
                                L1normRatio
                                              correlation MSEoverObsVar
                                                  0.3299756
##
     113.6774627
                     1.0466775
                                   1.0522049
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        79.80428
                   0.8888998
                               0.8869343
                                            0.0795105
                                                          0.8169517
## 95% 160.38497
                   1.2476467
                               1.2625942
                                            0.5193088
                                                          1.6581825
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x00000002218d9e8>
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
             MSE
##
      88.8194203
                     0.9300289
                                   0.9332456
                                                  0.5551843
                                                                0.9501085
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        57.81135
                   0.7337457
                               0.7320315
                                            0.3272781
                                                          0.5745168
## 95% 141.93207
                   1.2472225
                               1.2331401
                                            0.7100326
                                                          1.6594624
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
## <environment: 0x000000021a13660>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
##
      55.6089780
                     0.7280071
                                   0.7317077
                                                  0.7505058
                                                                0.6069440
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
                               0.5312196
                                            0.5681458
## 5%
        29.28022
                   0.5306355
                                                          0.2985309
## 95% 103.31903
                   1.0235771
                               1.0377748
                                            0.8596700
                                                          1.2200916
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
   <environment: 0x000000012fb4a38>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
##
      3.19389560
                    0.17117253
                                  0.17276090
                                                 0.98430021
                                                               0.03568463
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
                  0.1057920
                              0.1093468
                                           0.9641423
## 5% 1.299669
                                                        0.01222983
  95% 6.609331
                  0.2717204
                              0.2711917
                                           0.9942733
                                                        0.08490755
##
        sampleSize
                             raceN
                                         sigma.race
                                                          beta.acup
                                                                          beta.mbsr
##
      180.00000000
                        3.00000000
                                         1.00000000
                                                         1.58923521
                                                                          1.58923521
##
          beta.sex
                          beta.age
                                           beta.edu
                                                           beta.len
                                                                           beta.bas
##
        0.09531018
                                                         0.12221763
                                                                        -0.22314355
                        0.22314355
                                         0.23111172
##
         beta.conc
                           markerN
                                        beta.biom.v
                                                          mdfN.acup beta.mdf.acup.v
                                                                         2.00000000
##
       -0.26136476
                       10.00000000
                                         2.00000000
                                                         4.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
        2.00000000
                                                         2.00000000
##
                        4.00000000
                                        2.00000000
## [1] O
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
```

```
##
      xconc
## <environment: 0x000000021cba310>
##
            MSE
                 L2normRatio L1normRatio
                                             correlation MSEoverObsVar
                   1.07727004
                               1.08337149
                                              0.03079011
##
   123.94964275
                                                            1 19276145
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       94.30026 1.001264 0.992818 -0.1974337
                                                         1.011933
## 95% 161.80516
                 1.217442 1.231317 0.2388405
                                                        1.558790
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
      xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
      zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x0000000221494a0>
                               L1normRatio correlation MSEoverObsVar
            MSE
                 L2normRatio
##
    106.5728726
                    1.0071074
                                 1.0119565
                                                0.3593132
                                                              1.0655087
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       78.29164
                 0.8744335 0.8794402 0.1198600
                                                       0.7789709
## 95% 153.21413
                 1.2262239
                             1.2379232
                                         0.5229105
                                                        1.5912633
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
      zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
      zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x0000000121ed7b8>
            MSE
                 L2normRatio L1normRatio correlation MSEoverObsVar
##
                                                0.5855331
##
     80.7296358
                    0.8796100
                                  0.8831715
                                                              0.8410189
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       55.96547 0.7188839 0.7211196 0.3562986
                                                       0.5334663
## 95% 132.54699
                 1.1809567
                             1.1641421 0.7154732
                                                       1.5645450
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
      xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
      zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
      xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
      xmbsr * zmdfMBSR3
## <environment: 0x000000022191600>
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
     47.7772252
                    0.6687295
                                  0.6725551
                                                0.7803190
                                                              0.5087151
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       27.42875 0.4998923 0.5041949 0.5864327
                                                       0.2571254
## 95% 100.64732 1.0140227
                              0.9996541 0.8722298
                                                       1.1553164
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
      xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
##
      zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
      zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
      zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
      zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
## <environment: 0x000000013060790>
##
            MSE
                  L2normRatio
                               L1normRatio correlation MSEoverObsVar
      2.58324792
                                0.15354913
                                              0.98736209
                                                             0.02829394
##
                   0.15211553
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 1.178284 0.1013397 0.1024842 0.9669743 0.01087165
```

```
## 95% 6.304024 0.2597652
                            0.2683676 0.9947940
                                                       0.07537719
##
                                    sigma.race
                                                                       beta.mbsr
       sampleSize
                            raceN
                                                       beta.acup
      240.00000000
                                                       1.58923521
                                                                       1.58923521
##
                        3.00000000
                                       1.00000000
##
         beta.sex
                         beta.age
                                         beta.edu
                                                         beta.len
                                                                          beta.bas
##
       0.09531018
                       0.22314355
                                       0.23111172
                                                      0.12221763
                                                                       -0.22314355
##
                                                       mdfN.acup beta.mdf.acup.v
        beta.conc
                          markerN
                                      beta.biom.v
       -0.26136476
                      10.00000000
                                       2.00000000
                                                      4.00000000
                                                                        2.00000000
##
##
       gama.acup.v
                        mdfN.mbsr beta.mdf.mbsr.v
                                                      gama.mbsr.v
##
        2.00000000
                        4.00000000
                                       2.00000000
                                                      2.00000000
## [1] 0
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
## <environment: 0x000000004d2f100>
                               L1normRatio
                                              correlation MSEoverObsVar
##
            MSE
                 L2normRatio
##
   120.93248090
                   1.06327967
                                 1.06795018
                                                0.03531787
                                                              1.15742273
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
                 0.9961337
                               0.992818 -0.1698643
       94.72979
                                                          1.006925
## 95% 158.30786
                 1.2017580
                               1.211115
                                          0.2197862
                                                          1.515562
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x00000002164a080>
            MSE
                 L2normRatio L1normRatio
                                              correlation MSEoverObsVar
##
##
     102.1642922
                    0.9833754
                                  0.9875855
                                                 0.3774975
                                                               1.0096487
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       75.21338
                 0.863949
                              0.8648351 0.1531471
                                                         0.7608891
## 95% 149.30516
                   1.214998
                             1.2120889
                                          0.5276432
                                                         1.5379377
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x000000021c0c678>
##
            MSE
                  L2normRatio
                               L1normRatio
                                              correlation MSEoverObsVar
##
      75.6137608
                    0.8479126
                                  0.8515320
                                                 0.6056587
                                                               0.7752872
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       53.55757
                  0.7136841
                              0.7057709
                                          0.3867494
                                                        0.5158598
## 95% 126.85443
                  1.1680998 1.1430165
                                          0.7186331
                                                         1.4572362
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
##
## <environment: 0x000000021f44c10>
##
                                L1normRatio
                                              correlation MSEoverObsVar
            MSE
                  L2normRatio
##
      43.2774320
                    0.6342540
                                  0.6378611
                                                 0.7978682
                                                               0.4536856
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
                                         0.6066871
                 0.4894472
                            0.4954767
                                                        0.2451666
## 5% 26.13820
                              0.9794394
## 95% 91.92657
                 0.9842721
                                         0.8758392
                                                        1.0683940
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
```

```
xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
##
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
   <environment: 0x00000001ae6f030>
##
             MSF.
                   L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
                                                               0.02426175
##
      2.24994824
                    0.14131436
                                  0.14247567
                                                0.98904404
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
  5% 1.118394
                  0.1003227
                              0.1006063
                                          0.9702935
                                                        0.01037084
  95% 5.954362
                  0.2513181
                              0.2648494
                                          0.9950368
##
                                                        0.07056757
        sampleSize
                             raceN
                                        sigma.race
                                                         beta.acup
                                                                          beta.mbsr
##
      300.00000000
                        3.00000000
                                        1.00000000
                                                                         1.58923521
                                                        1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                           beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                       beta.biom.v
                                                        mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                        4.00000000
                                                                         2.00000000
##
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
       gama.acup.v
                                                        2.00000000
##
        2.00000000
                        4.00000000
                                        2.00000000
## [1] O
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
  <environment: 0x000000013508388>
                  L2normRatio
             MSF.
                                L1normRatio
                                              correlation MSEoverObsVar
##
   118.76044652
                    1.05384289
                                  1.05791592
                                                0.03561046
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        94.31835
                  0.9934304
                                0.991697 -0.1546277
                                                          0.9984578
                   1.1971796
                                1.195285
                                           0.2123922
                                                          1.4798751
## 95% 153.54214
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
  <environment: 0x00000002192d6a0>
##
                                 L1normRatio
##
             MSE
                   L2normRatio
                                               correlation MSEoverObsVar
##
      99.0237070
                     0.9670847
                                   0.9704792
                                                  0.3909426
                                                                0.9723542
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       74.64659
                   0.8604633
                               0.8586869
                                           0.1636685
                                                          0 7544239
## 95% 145.07737
                   1.1964952
                               1.1878465
                                           0.5288133
                                                          1.5227434
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
  <environment: 0x0000000020e4f868>
##
             MSE
                                 L1normRatio
                                               correlation MSEoverObsVar
                   L2normRatio
      72.1895953
                                   0.8296586
                                                  0.6190605
##
                     0.8271039
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       51.82047
                    0.701045
                               0.6994593
                                           0.4194947
                                                          0.5008501
## 95% 121.58712
                    1.133552
                               1.1269051
                                           0.7211866
                                                          1.4055370
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
```

```
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
##
  <environment: 0x0000000217279c0>
##
                   L2normRatio L1normRatio
##
             MSE
                                               correlation MSEoverObsVar
##
      40.3986966
                     0.6121273
                                   0.6150316
                                                 0.8090522
                                                                0.4188456
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 25.52711
                  0.4865269
                              0.4876445
                                          0.6197787
                                                         0.2403093
## 95% 86.51238
                  0.9618673
                              0.9586943
                                          0.8767488
                                                         1.0127461
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
##
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
  <environment: 0x000000016bf68d0>
                                 L1normRatio
##
             MSE
                   L2normRatio
                                               correlation MSEoverObsVar
                     0.1343669
                                   0.1353302
                                                 0.9900972
##
       2.0380459
                                                                0.0217352
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 1.087068 0.09974947 0.09983171
                                          0.9716956
                                                       0.01018413
## 95% 5.600268 0.24498279 0.24753684
                                          0.9950832
                                                       0.06651975
##
        sampleSize
                             raceN
                                        sigma.race
                                                                          beta.mbsr
                                                         beta.acup
                                                        1.58923521
##
      360.00000000
                        3.00000000
                                        1.00000000
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                          beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
                           markerN
                                                         mdfN.acup beta.mdf.acup.v
         beta.conc
                                       beta.biom.v
##
                       10.00000000
                                        2.00000000
                                                         4.00000000
                                                                         2.00000000
       -0.26136476
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                         2.00000000
## [1] 0
##
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
  <environment: 0x000000021774670>
##
                                 L1normRatio
##
             MSE
                 L2normRatio
                                               correlation MSEoverObsVar
##
   117.20075180
                    1.04604684
                                  1.04976180
                                                0.04217519
                                                               1.11569354
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        94.7840
                   0.991942
                              0.9885276 -0.1441941
                                                        0.9930453
## 95% 152.2625
                   1.186478
                              1.1864756
                                          0.2091505
                                                         1.4586896
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
  <environment: 0x000000016725bd8>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
      96.9898739
                                   0.9585683
                                                 0.4000611
##
                     0.9558098
                                                                0.9468545
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       74.64659
                    0.859705
                               0.8554358
                                           0.1859726
                                                          0.7514403
## 95% 140.47270
                    1.186728
                                           0.5268071
                               1.1765112
                                                          1.4716820
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
```

```
zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x000000012e942c0>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
      69.6704343
                     0.8109898
                                   0.8128921
                                                  0.6301047
                                                                0.7008779
##
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        51.00415
                   0.6930274
                               0.6919083
                                           0.4302787
                                                          0.4903502
## 95% 119.16888
                   1.1155268
                               1.1027852
                                           0.7252534
                                                          1.3339920
## [1] 0.75
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
##
       xmbsr * zmdfMBSR3
##
   <environment: 0x000000015cbe7f0>
##
             MSE
                   L2normRatio
                                L1normRatio
                                                correlation MSEoverObsVar
##
      38.3120927
                     0.5953272
                                   0.5976710
                                                  0.8175253
                                                                0.3935707
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 25.28955
                  0.4809833
                              0.4807411
                                          0.6298229
                                                         0.2360761
                                                         0.9954052
  95% 84.73013
                  0.9360496
                              0.9483609
                                          0.8791120
##
  Γ1 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
   <environment: 0x000000021f2b268>
##
                                 L1normRatio
                                               correlation MSEoverObsVar
##
             MSE
                   L2normRatio
##
       1.8903709
                     0.1293195
                                   0.1302659
                                                  0.9908401
                                                                0.0199612
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
     1.065605 0.09801175 0.09848996
                                          0.9731320
                                                       0.009809009
   95% 5.442072 0.23727017 0.23654921
                                          0.9952117
                                                       0.059800640
##
        sampleSize
                             raceN
                                        sigma.race
                                                          beta.acup
                                                                          beta.mbsr
##
      420.00000000
                        3.00000000
                                         1.00000000
                                                         1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                           beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                         0.12221763
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                        beta.biom.v
                                                          mdfN.acup beta.mdf.acup.v
                                                         4.00000000
                                                                         2.00000000
##
       -0.26136476
                       10.00000000
                                        2.00000000
##
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
       gama.acup.v
                        4.00000000
##
        2.00000000
                                        2.00000000
                                                         2.00000000
##
  Γ1] 0
##
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
   <environment: 0x0000000130af530>
##
                                 L1normRatio
##
             MSE
                   L2normRatio
                                                correlation MSEoverObsVar
                    1.04053682
                                  1.04384564
                                                 0.04419673
                                                               1.10227298
##
   115.76167388
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        94.86596
                   0.9913769
                               0.9890882 -0.1374240
                                                          0.9922454
## 95% 149.77630
                   1.1703603
                               1.1689170
                                           0.2027249
                                                          1.4308225
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
```

```
zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x00000000498f960>
                   L2normRatio
                                 L1normRatio
##
             MSE
                                                correlation MSEoverObsVar
##
      95.0947272
                     0.9466857
                                   0.9491626
                                                  0.4081965
                                                                0.9263409
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        74.30626
                   0.8573784
                                0.855231
                                           0.2143425
                                                          0.7450967
## 95% 136.25072
                 1.1628483
                                1.170385
                                           0.5268071
                                                          1.4467234
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
   <environment: 0x0000000051f2280>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      67.8144608
                     0.8001491
                                   0.8019099
                                                  0.6372417
                                                                0.6789808
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        50.97243
                   0.6892703
                               0.6898185
                                           0.4389945
                                                          0.4884077
## 95% 115.15323
                   1.0907749
                               1.0880531
                                           0.7266161
                                                          1.3137785
  [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
##
  <environment: 0x0000000131268d8>
##
             MSF.
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
      36.7423225
                     0.5833330
                                   0.5854477
                                                  0.8235877
##
                                                                0.3752849
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
                              0.4802803
## 5% 24.84593
                  0.4793657
                                           0.6386113
                                                         0.2331463
                                          0.8795203
## 95% 81.66066
                  0.9286796
                              0.9310946
                                                         0.9373414
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
  <environment: 0x0000000051e3ea8>
##
                                               correlation MSEoverObsVar
##
             MSE
                  L2normRatio
                                 L1normRatio
      1.77990837
                                                0.99138330
##
                    0.12561685
                                  0.12651886
                                                               0.01866406
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
  5% 1.040534 0.09721199 0.09787781
                                          0.9754821
                                                       0.009671658
   95% 5.260327 0.23130662 0.22777204
                                           0.9952732
                                                       0.058246012
##
        sampleSize
                             raceN
                                         sigma.race
                                                          beta.acup
                                                                          beta.mbsr
      480.0000000
                        3.00000000
                                         1.00000000
##
                                                         1.58923521
                                                                         1.58923521
##
                                                           beta.len
          beta.sex
                          beta.age
                                           beta.edu
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                         0.12221763
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                        beta.biom.v
                                                          mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                         4.00000000
                                                                         2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
## [1] 0
```

```
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
## <environment: 0x00000002205f2f8>
                 L2normRatio L1normRatio correlation MSEoverObsVar
##
            MSE
   114.96915732
                   1.03601602
                                 1.03889654
                                               0.04699353
                                                             1.09159700
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
       95.02079
                 0.9909023 0.9884135 -0.1337960
## 95% 146.44366
                  1.1583908
                              1.1642086 0.1986798
                                                         1.404463
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
##
## <environment: 0x000000012f4c248>
##
            MSE
                  L2normRatio
                               L1normRatio
                                             correlation MSEoverObsVar
##
      93.8690656
                     0.9393479
                                  0.9416579
                                                0.4148566
                                                              0.9101706
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       74.93277
                  0.8567774
                               0.853729
                                          0.2199774
                                                        0.7411693
## 95% 131.49955
                 1.1429676
                               1.162212
                                          0.5268071
                                                        1.4031188
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
##
## <environment: 0x000000012fd4038>
##
            MSF.
                 L2normRatio L1normRatio
                                             correlation MSEoverObsVar
      66.4117617
                    0.7905939
                                  0.7922178
                                                0.6439486
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
       50.84033
                 0.6879751 0.6884102 0.4536217
                                                        0.4833912
## 5%
                 1.0651559 1.0656885
                                          0.7277258
## 95% 112.30262
                                                        1.2434861
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
## <environment: 0x000000004bcb350>
##
            MSF.
                  L2normRatio L1normRatio
                                              correlation MSEoverObsVar
##
      35.5111162
                    0.5728515
                                  0.5746031
                                                0.8289088
                                                              0.3600467
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.50829 0.4768962 0.4727782
                                         0.6582759
## 95% 77.10680
                            0.9138840
                 0.9017274
                                         0.8807591
                                                       0.8757602
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
## <environment: 0x000000021c70f10>
            MSE
                 L2normRatio
                               L1normRatio
                                              correlation MSEoverObsVar
##
##
      1.69590801
                   0.12261832
                                 0.12349666
                                               0.99181196
                                                             0.01764601
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
```

```
## 5% 1.022026 0.09661797 0.09692946
                                          0.9759925
                                                      0.009546699
                                          0.9953313
## 95% 4.933305 0.21973004 0.22439389
                                                      0.056958956
##
        sampleSize
                             raceN
                                        sigma.race
                                                         beta.acup
                                                                         beta.mbsr
##
      540.00000000
                        3.00000000
                                        1.00000000
                                                        1.58923521
                                                                        1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                          beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                       -0.22314355
##
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
         beta.conc
                           markerN
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                        4.00000000
                                                                        2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc
  <environment: 0x0000000020ee8f10>
##
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
   114.08831399
                    1.03219790
                                  1.03471416
                                                0.04964828
                                                               1.08284607
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        95.07655
                  0.9890429
                               0.9864975 -0.1264213
                                                         0.9896632
## 95% 143.20298
                   1.1507220
                               1.1593284
                                          0.1944839
                                                         1.3712246
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
##
##
   <environment: 0x00000000494b8c8>
##
             MSF.
                   L2normRatio
                                 L1normRatio
                                              correlation MSEoverObsVar
##
      92.7886261
                     0.9337271
                                   0.9356459
                                                 0.4196217
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        74.82615
                  0.8561248
                               0.8526013
                                           0.2274564
                                                         0.7408537
## 95% 129.53638
                   1.1387568
                               1.1510655
                                           0.5267839
                                                         1.3889970
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x00000000489f288>
##
             MSE
                  L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      65.2275369
                     0.7832130
                                   0.7846551
                                                 0.6489627
                                                               0.6460758
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        50.47343
                   0.6873736
                               0.6852668 0.4704411
                                                         0.4826305
## 95% 105.56177
                  1.0525822
                               1.0541508
                                           0.7279976
                                                         1.2047296
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
## <environment: 0x0000000047ec478>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
                                   0.5666881
##
      34.5544843
                     0.5651836
                                                 0.8327286
                                                               0.3487291
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
                 0.4740906
                            0.4715606
                                         0.6861312
## 5% 24.4511
                                                       0.2291115
## 95% 75.8100
                 0.8789601
                             0.8879304
                                         0.8810797
                                                       0.8213100
## [1] 1
```

```
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
   <environment: 0x00000001ac46660>
##
##
             MSF.
                   L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      1.62976018
                    0.12033101
                                  0.12119416
                                                0.99213999
                                                               0.01686274
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 1.012343 0.09627202 0.09642401
                                          0.9774709
                                                      0.009402423
   95% 4.629851 0.21624868 0.21645206
                                          0.9953636
                                                      0.054147886
##
                                                                          beta.mbsr
        sampleSize
                             raceN
                                        sigma.race
                                                         beta.acup
##
      600.00000000
                        3.00000000
                                        1.00000000
                                                         1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                          beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                                        0.12221763
                                                                        -0.22314355
                                        0.23111172
##
         beta.conc
                           markerN
                                       beta.biom.v
                                                        mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                        4.00000000
                                                                         2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
## [1] O
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
## <environment: 0x0000000131532f0>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
                                                 0.0508404
##
     113.3625420
                     1.0292873
                                   1.0316238
                                                                1.0758753
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                 0.9889425
## 5%
        95.22892
                              0.9862177 -0.1176213
                                                         0.9899214
## 95% 141.46913
                   1.1470003
                                           0.1896817
                               1.1513490
                                                          1.3543267
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x000000012ee4340>
             MSE
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      91.8690537
                     0.9291401
                                   0.9308613
                                                 0.4237590
                                                                0.8875006
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        74.83237
                   0.8567774
                               0.8526013
                                          0.2375858
                                                         0.7415471
                               1.1408225
## 95% 127.61156
                                           0.5243251
                   1.1238107
                                                          1.3553958
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x0000000130cf000>
                                 L1normRatio
##
             MSE
                   L2normRatio
                                               correlation MSEoverObsVar
##
      64.2952163
                     0.7775845
                                   0.7789362
                                                 0.6528310
                                                                0.6348191
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        50.42017
                   0.6888514
                               0.6856537
                                           0.4805887
                                                          0.4833916
## 95% 102.59978
                   1.0407695
                               1.0358405
                                           0.7265507
                                                          1.1589678
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
```

```
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
##
##
  <environment: 0x00000001698e4a0>
                                               correlation MSEoverObsVar
##
             MSE
                  L2normRatio
                                L1normRatio
##
      33.7849044
                     0.5591299
                                   0.5604081
                                                 0.8357743
                                                                0.3396745
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
## 5% 24.41772
                  0.4740906
                              0.4715655
                                          0.7010415
                                                        0.2291115
                                          0.8809952
## 95% 74.54924
                  0.8622082
                              0.8747674
                                                        0.8133414
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
##
  <environment: 0x0000000021a52058>
                                L1normRatio
                                               correlation MSEoverObsVar
##
            MSE
                  L2normRatio
##
      1.57501804
                    0.11844000
                                  0.11927565
                                                0.99240921
                                                               0.01622073
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
                              0.0962184
## 5% 1.008075 0.09603563
                                          0.9782126
                                                      0 009379423
  95% 4.352296 0.21239783
                              0.2116662
                                          0.9953875
                                                      0.052359557
##
        sampleSize
                             raceN
                                        sigma.race
                                                         beta.acup
                                                                          beta.mbsr
##
      660.00000000
                        3.00000000
                                        1.00000000
                                                        1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                          beta.len
                                                                           beta.bas
        0.09531018
                        0.22314355
##
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
         beta.conc
                           markerN
                       10.00000000
                                        2.00000000
                                                        4.00000000
##
       -0.26136476
                                                                         2,00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2,00000000
                                                        2.00000000
## [1] 0
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
## <environment: 0x000000013c84628>
##
            MSE
                  L2normRatio L1normRatio
                                               correlation MSEoverObsVar
##
   112.77444917
                    1.02649788
                                  1.02854690
                                                0.05291181
                                                               1.06957850
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        95.59263
                  0.9869918
                               0.9852865 -0.1145384
## 5%
                                                           0.988670
## 95% 140.34774
                 1.1401253
                               1.1446893
                                         0.1882218
                                                           1.335186
## [1] 0.25
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x000000012fd70a0>
                                 L1normRatio
##
             MSE
                   L2normRatio
                                               correlation MSEoverObsVar
##
      91.1007323
                     0.9249603
                                   0.9265222
                                                 0.4276213
                                                                0.8785615
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        74.96176
                  0.8561248
                               0.8514937
                                           0.2501457
                                                         0.7411693
                                                         1.3005086
## 95% 127.03303
                   1.1148952
                               1.1378827
                                           0.5239596
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
```

```
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x000000012fe85b0>
                                 L1normRatio
                                              correlation MSEoverObsVar
##
             MSE
                   L2normRatio
##
      63.4961162
                     0.7724320
                                   0.7736942
                                                 0.6563837
                                                               0.6250280
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.40528
                  0.6879901
                              0.6856537
                                          0.4991268
                                                        0.4832254
                              1.0203655
## 95% 97.52841
                                          0.7265507
                                                        1.1218433
                  1.0132550
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
## <environment: 0x0000000050f69d8>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      33.1110295
                     0.5535139
                                   0.5547563
                                                 0.8386099
                                                               0.3316218
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.41289
                  0.4733328
                              0.4715655
                                          0.7100058
                                                        0.2268638
## 95% 70.52752
                  0.8452747
                              0.8627123
                                          0.8810163
                                                        0 7614605
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
  <environment: 0x000000012f66f78>
##
             MSE
                  L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      1.52933521
                    0.11680285
                                  0.11763011
                                                0.99263656
                                                              0.01568021
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 1.002658 0.09551907 0.09562391
                                          0.9797304
                                                      0.009265568
   95% 4.244901 0.20917163 0.20830466 0.9954425
##
                                                      0.048452011
##
        sampleSize
                             raceN
                                       sigma.race
                                                         beta.acup
                                                                         beta.mbsr
##
      720.00000000
                        3.00000000
                                        1.00000000
                                                        1.58923521
                                                                         1.58923521
##
          beta.sex
                                          beta.edu
                                                          beta.len
                                                                           beta.bas
                          beta.age
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
                                                        mdfN.acup beta.mdf.acup.v
        beta.conc
                           markerN
                                       beta.biom.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                        4.00000000
                                                                        2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
  <environment: 0x0000000021923080>
                                 L1normRatio
                                               correlation MSEoverObsVar
##
            MSE
                   L2normRatio
   112.22331388
##
                    1.02417532
                                  1.02607945
                                                0.05462993
                                                              1.06428805
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        95.59263
                   0.9857676
                               0.9844618 -0.1068859
                                                         0.9876282
                               1.1383467
## 95% 139.65868
                   1.1258990
                                           0.1862391
                                                         1.3220761
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
```

```
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
  <environment: 0x0000000164f9580>
##
##
                                 L1normRatio
                                              correlation MSEoverObsVar
             MSE
                   L2normRatio
##
      90.4281279
                     0.9215387
                                   0.9229639
                                                  0.4307361
                                                                0.8711577
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        74.99955
                   0.8561248
                               0.8513607
                                            0.2651877
                                                          0.7415526
## 95% 125.41868
                   1.1076274
                               1.1247445
                                            0.5227542
                                                          1.2949138
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
##
  <environment: 0x000000012db95e0>
##
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
##
      62.7852018
                     0.7680529
                                   0.7692112
                                                  0.6594334
                                                                0.6166716
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.47343
                  0.6888790
                              0.6863932
                                          0.5066570
                                                         0.4832254
## 95% 95.38926
                  0.9778694
                              0.9959889
                                          0.7257605
                                                         1.0427246
## [1] 0.75
##
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
## <environment: 0x0000000146b3b38>
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
##
                                   0.5502100
                     0.5491435
                                                  0.8407926
                                                                0.3252211
##
      32.5673217
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
## 5% 24.44142
                  0.4735505
                              0.4711119
                                          0.7192610
                                                         0.2277301
  95% 67.22976
                  0.8139767
                              0.8024255
                                           0.8809787
                                                         0.7201790
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
   <environment: 0x00000000504f678>
                                 I.1normRatio
                                               correlation MSEoverObsVar
##
             MSF.
                   L2normRatio
                    0.11545180
                                  0.11627524
                                                 0.99282541
##
      1.49112643
                                                               0 01523041
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 0.9964019 0.09531349 0.09545183
                                            0.9804827
                                                        0.009225161
  95% 4.0775060 0.20002113 0.20247510
                                            0.9954523
                                                        0.045207014
##
        sampleSize
                             raceN
                                         sigma.race
                                                          beta.acup
                                                                          beta.mbsr
##
      780.00000000
                        3.00000000
                                         1.00000000
                                                                         1.58923521
                                                         1.58923521
##
          beta.sex
                          beta.age
                                           beta.edu
                                                           beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                         0.23111172
                                                         0.12221763
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                        beta.biom.v
                                                          mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                         4.00000000
                                                                         2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
       2.00000000
                        4.00000000
##
                                        2.00000000
                                                         2.00000000
```

```
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
## <environment: 0x000000013e52870>
                                             correlation MSEoverObsVar
##
            MSE
                 L2normRatio L1normRatio
##
    111.8573575
                    1.0222949
                                  1.0240499
                                                0.0556047
                                                              1.0598573
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
       95.80323 0.9849914 0.9842386 -0.09827819
## 5%
                                                        0.9875528
## 95% 137.20717 1.1190667
                              1.1321349 0.18563726
                                                        1.3038038
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
      zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x00000001312ee28>
##
            MSE
                  L2normRatio
                               L1normRatio
                                              correlation MSEoverObsVar
##
     89.8737676
                    0.9183715
                                  0.9197457
                                                0.4339877
                                                              0.8642849
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
       75.06494
                 0.8560122
                             0.8513607
                                         0.2778590
                                                        0.7408537
## 95% 123.05508
                 1.0965709 1.1105987
                                          0.5222558
                                                        1.2733867
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
      zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
      zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x000000021a19fa0>
            MSE
                  L2normRatio
                                L1normRatio
                                             correlation MSEoverObsVar
##
     62.1939834
                    0.7641338
                                  0.7651710
                                                0.6622521
                                                              0.6092026
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
               0.6888790
                            0.6853587
                                         0.5164674
## 5% 50.56267
                                                       0.4826567
## 95% 93.65305 0.9702537
                                         0.7256592
                             0.9802467
                                                       0.9946195
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
      xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
      zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
      xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
      xmbsr * zmdfMBSR3
## <environment: 0x00000001ae7b1d0>
##
            MSE
                 L2normRatio L1normRatio
                                             correlation MSEoverObsVar
                                  0.5460972
                                                0.8428745
##
     32.0890364
                    0.5450749
                                                              0.3193725
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
## 5% 24.39335 0.4733328 0.4704420 0.7253116
                                                       0.2266166
## 95% 63.22196
                 0.8045203
                            0.7914044
                                         0.8811286
                                                       0.6744573
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
      xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
##
      zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
      zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
      zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
      zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
## <environment: 0x000000021f698f8>
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
     1.45884326
                               0.11508539
                                             0.99298915 0.01484087
##
                  0.11427474
```

```
MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 0.993315 0.09520359 0.09529691
                                          0.9818166
                                                      0.009185678
  95% 3.935210 0.19112440 0.19831706
                                                      0.041094050
                                          0.9954576
##
        sampleSize
                             raceN
                                                         beta.acup
                                                                         beta.mbsr
                                        sigma.race
##
      840.00000000
                        3.00000000
                                        1.00000000
                                                        1.58923521
                                                                         1.58923521
##
                                                                           beta.bas
          beta.sex
                          beta.age
                                          beta.edu
                                                          beta.len
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                        4.00000000
                                                                         2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
##
        2.00000000
                        4.0000000
                                        2.00000000
                                                        2.00000000
##
  [1] 0
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
##
  <environment: 0x00000000488b1b0>
##
             MSE
                  L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
   111.50996956
                    1.02069264
                                  1.02240410
                                                0.05635232
                                                               1.05603024
##
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
       96.17706
                  0.9853087
                               0.9847934 -0.09542643
                                                         0.9876282
                               1.1234896 0.18214018
## 95% 136.46720
                   1.1117186
                                                         1.2817498
  [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
  <environment: 0x0000000050aee78>
##
            MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      89.3780307
                     0.9157012
                                   0.9169984
                                                 0.4366861
                                                                0.8584330
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                                           0.2885776
## 5%
        75.25397
                    0.855487
                               0.8513607
                                                         0.7394918
## 95% 121.56247
                               1.0907204
                    1.082645
                                           0.5222699
                                                          1.2404727
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
  <environment: 0x000000021da2b28>
##
            MSE
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      61.6652217
                     0.7607350
                                   0.7617716
                                                 0.6647317
                                                                0.6027027
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.73544
                  0.6891826
                              0.6859347
                                          0.5278237
                                                        0.4824997
  95% 91.00982
                  0.9619501
                              0.9727103
                                          0.7251923
                                                         0.9639861
  [1] 0.75
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
##
       xmbsr * zmdfMBSR3
  <environment: 0x0000000134435c8>
##
                                L1normRatio
                                               correlation MSEoverObsVar
##
             MSE
                  L2normRatio
##
      31.6495394
                     0.5413818
                                   0.5423408
                                                 0.8447693
                                                                0.3141439
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
## 5% 24.29510
                  0.4723799
                              0.4699223
                                          0.7386903
                                                        0.2260033
                                          0.8815523
## 95% 57.92987
                  0.7778325
                              0.7776614
                                                        0.6577517
```

```
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
   <environment: 0x000000013c93a58>
##
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
             MSE
##
      1.42981672
                    0.11321622
                                  0.11402638
                                                0.99313393
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
                   0.0948139 0.09507398
## 5% 0.9872754
                                           0.9834732
                                                        0.009142014
  95% 3.7441018
                   0.1895341 0.18917562
                                           0.9954905
                                                        0.037330785
##
                             raceN
        sampleSize
                                        sigma.race
                                                         beta.acup
                                                                          beta.mbsr
##
      900.00000000
                        3.00000000
                                        1.00000000
                                                         1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                          beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
        beta.conc
                           markerN
                                                                         2.00000000
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                         4.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
  <environment: 0x000000012eebfc0>
##
             MSE
                   L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
                    1.01922998
                                  1.02082428
                                                0.05767138
   111.20606953
                                                               1.05252218
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                               0.9849672 -0.08871843
        96.40281
                   0.9857676
                                                          0.9872153
                               1.1163650 0.17507879
## 95% 135.27595
                   1.1081946
                                                          1.2689355
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x000000021299d80>
##
             MSE
                   L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      88.9523199
                     0.9133442
                                   0.9145950
                                                  0.4391333
                                                                0.8532330
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
       75.46271
                   0.8553168
                               0.8514778
                                           0.2934114
                                                          0.7388885
## 95% 119.19542
                 1.0756663
                               1.0783783
                                           0.5220513
                                                          1.2156088
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
##
  <environment: 0x000000006139870>
##
                   L2normRatio
                                               correlation MSEoverObsVar
             MSE
                                 L1normRatio
##
      61.2227859
                     0.7578459
                                   0.7588613
                                                 0.6668305
                                                                0.5971227
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.75103
                  0.6891894
                              0.6859347
                                          0.5347799
                                                         0.4815856
## 95% 89.31894
                  0.9415892
                              0.9532571
                                          0.7253369
                                                         0.9497742
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
```

```
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
##
       xmbsr * zmdfMBSR3
##
   <environment: 0x000000021294ec8>
             MSE
                   L2normRatio L1normRatio
                                               correlation MSEoverObsVar
##
                     0.5383313
      31.2856652
                                   0.5391806
                                                  0.8463244
                                                                0.3097497
##
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
       24.27470
                              0.4698055
                                          0.7455128
## 5%
                  0.4722308
                                                         0.2255632
  95% 54.03879
                  0.7609081
                              0.7670783
                                          0.8815819
                                                         0.6126453
## [1] 1
##
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
  <environment: 0x00000002103e710>
##
##
             MSF.
                  L2normRatio
                                L1normRatio
                                              correlation MSEoverObsVar
##
      1.40485778
                    0.11230409
                                  0.11309475
                                                0.99325935
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 0.9855819 0.09458935 0.09489052 0.9842186
                                                        0.009079441
   95% 3.5108300 0.18524200 0.18106207
                                           0.9955066
                                                        0.035956490
        sampleSize
                             raceN
                                        sigma.race
                                                         beta.acup
                                                                          beta.mbsr
##
      960.00000000
                        3.00000000
                                        1.00000000
                                                         1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                           beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                         0.12221763
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                         4.00000000
                                                                         2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                         2.00000000
## [1] 0
##
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc
  <environment: 0x0000000021e3c878>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
   110.92002563
                    1.01780539
                                  1.01933788
                                                0.05914792
                                                               1.04929919
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        96.72355
                  0.9853107
                               0.9845353 -0.07969608
                                                          0.9865221
## 5%
## 95% 134.35571
                   1.1034775
                               1.1130489 0.17475051
                                                          1.2543716
  [1] 0.25
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
##
  <environment: 0x00000000d120068>
##
                                 L1normRatio
                                               correlation MSEoverObsVar
             MSE
                   L2normRatio
##
      88.5628423
                     0.9111443
                                   0.9124272
                                                 0.4414224
                                                                0.8485433
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
        75.56413
                   0.8549717
                               0.8515476
                                           0.3002882
                                                          0.7388396
## 5%
                   1.0591407
                               1.0602862
## 95% 118.50722
                                           0.5217325
                                                          1.1704144
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
```

```
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
##
  <environment: 0x0000000216f53c0>
##
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      60.8133794
                     0.7551356
                                   0.7561515
                                                  0.6687775
                                                                0.5920401
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.71563
                  0.6889495
                              0.6853587
                                          0.5398605
                                                         0.4813296
## 95% 88.05612
                  0.9351168
                              0.9386240
                                           0.7255506
                                                         0.9234208
  [1] 0.75
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
##
   <environment: 0x00000000616a600>
                                                correlation MSEoverObsVar
##
             MSE
                   L2normRatio
                                 L1normRatio
##
      30.9684443
                     0.5356155
                                   0.5364356
                                                  0.8477086
                                                                0.3058790
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.27166
                  0.4722308
                              0.4699223
                                          0.7525350
                                                         0.2255411
## 95% 52.12567
                  0.7365354
                              0.7389937
                                          0.8817498
                                                         0.5748757
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
   <environment: 0x000000012f289b8>
##
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
       1.3831468
                                   0.1122772
                                                  0.9933693
##
                     0.1115025
                                                                0.0139376
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
   5% 0.9828191 0.09448588 0.09479721
                                           0.9850075
                                                        0.009059877
   95% 3.2552178 0.17722921 0.17756736
                                           0.9955124
                                                        0.034505533
##
        sampleSize
                             raceN
                                         sigma.race
                                                          beta.acup
                                                                          beta.mbsr
##
     1020.00000000
                        3.00000000
                                         1.00000000
                                                         1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                           beta.edu
                                                           beta.len
                                                                           beta.bas
                                                         0.12221763
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                                        -0.22314355
##
         beta.conc
                           markerN
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                         4.00000000
                                                                         2.00000000
                         mdfN.mbsr beta.mdf.mbsr.v
                                                        gama.mbsr.v
       gama.acup.v
##
        2.00000000
                        4.00000000
                                        2.00000000
                                                         2.00000000
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
   <environment: 0x000000005032360>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
                                  1.01807686
                                                 0.06035145
##
   110.68460491
                    1.01661292
                                                               1.04644936
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                             0.9844315 -0.07547824
## 5%
        96.72355
                   0.9850179
                                                          0.9859939
## 95% 132.86467
                   1.1006093
                               1.1093391 0.17407379
                                                          1.2418824
## [1] 0.25
```

```
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
       zmdfAcup1 + xmbsr * zmdfMBSR1
##
  <environment: 0x000000022261138>
##
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      88.2325069
                     0.9092659
                                   0.9104222
                                                  0.4433866
                                                                0.8444328
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5%
        75.67444
                   0.8549717
                               0.8516864
                                           0.3027217
                                                          0.7385903
## 95% 116.03598
                   1.0428678
                               1.0432800
                                           0.5216589
                                                          1.1375727
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
##
  <environment: 0x000000005702258>
##
             MSE
                   L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      60.4576326
                     0.7527715
                                   0.7536822
                                                  0.6705185
                                                                0.5875400
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.73544
                  0.6883231
                              0.6852984
                                          0.5467236
                                                         0.4799444
## 95% 86.28021
                              0.9246445
                                                         0.9014126
                  0.9192270
                                          0.7258170
  [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
## <environment: 0x000000004950e18>
##
                  L2normRatio
                                 L1normRatio
                                                correlation MSEoverObsVar
             MSE
      30.6825667
                     0.5331558
                                   0.5338796
                                                  0.8489662
                                                                0.3023705
##
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.26471
                  0.4719607
                              0.4696097
                                          0.7577779
                                                         0.2253459
## 95% 51.24125
                  0.7043478
                              0.7116643
                                          0.8818429
                                                         0.5358712
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
## <environment: 0x000000012fe0b60>
             MSF.
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      1.36294684
                    0.11074721
                                  0.11151101
                                                0.99347154
                                                               0.01369659
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                                                         0.00903264
## 5% 0.9806561 0.09441193 0.09479695
                                           0.9856790
   95% 3.0821079 0.17128419 0.16817498
                                           0.9955181
                                                         0.03210787
##
        sampleSize
                             raceN
                                        sigma.race
                                                         beta.acup
                                                                          beta.mbsr
##
     1080.00000000
                        3.00000000
                                        1.00000000
                                                        1.58923521
                                                                         1.58923521
##
          beta.sex
                          beta.age
                                          beta.edu
                                                           beta.len
                                                                           beta.bas
##
        0.09531018
                        0.22314355
                                        0.23111172
                                                        0.12221763
                                                                        -0.22314355
##
        beta.conc
                           markerN
                                       beta.biom.v
                                                         mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                       4.00000000
                                                                         2.00000000
##
       gama.acup.v
                         mdfN.mbsr beta.mdf.mbsr.v
                                                       gama.mbsr.v
```

```
2.00000000
                       4.00000000
                                      2.00000000
                                                      2.00000000
## [1] O
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
      xconc
## <environment: 0x000000013ca0900>
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
   110.45938620
                 1.01550030
                               1.01690115
                                              0.06141977
                                                            1.04388708
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
## 5%
       96.96092 0.9849798 0.9841101 -0.07224594
                                                       0.9855105
1.2234657
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
      zmdfAcup1 + xmbsr * zmdfMBSR1
##
## <environment: 0x000000004cc1260>
##
            MSE
                  L2normRatio
                              L1normRatio correlation MSEoverObsVar
##
     87.9224419
                    0.9075299
                                  0.9086653
                                               0.4451890
                                                             0.8407002
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
       75.77675
                 0.8549499
                              0.851754 0.3092697
                                                       0.7383961
## 5%
## 95% 113.63847
                1.0300064
                               1.037196
                                       0.5214448
                                                       1.1152295
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
      zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
      zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
##
## <environment: 0x0000000020e098f0>
##
            MSE
                  L2normRatio
                               L1normRatio
                                            correlation MSEoverObsVar
      60.1412990
                    0.7506784
                                  0.7515494
                                               0.6720166
##
                                                             0.5835825
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
                 0.6879930
## 5% 50.72764
                             0.6853587
                                        0.5570864
                                                      0.4796532
                                        0.7258170
## 95% 84.91559
                 0.9138958
                             0.9117110
                                                      0.8664344
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
      xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
      zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
      xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
      xmbsr * zmdfMBSR3
## <environment: 0x000000021256a48>
                              L1normRatio
##
            MSE
                  L2normRatio
                                             correlation MSEoverObsVar
##
      30.4206478
                    0.5309047
                                 0.5315929
                                               0.8501087
                                                             0.2992091
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.24103 0.4716447
                           0.4694695
                                        0.7636376
                                                      0.2246247
## 95% 48.30941 0.6962780
                             0.7004694
                                        0.8819791
                                                      0.4987612
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
      xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
      zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
      zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
##
      zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
      zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
## <environment: 0x00000001ae99e70>
                 L2normRatio L1normRatio correlation MSEoverObsVar
##
            MSF.
```

```
1.34473391
                    0.11006426
                                 0.11082053
                                                0.99356285
##
                                                              0.01348053
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                                                      0.009008581
## 5% 0.9773481 0.09432475 0.09473636 0.9871409
  95% 2.7711936 0.16344856 0.16423025
                                           0.9955293
                                                       0.029936107
                             raceN
##
        sampleSize
                                        sigma.race
                                                         beta.acup
                                                                        beta.mbsr
                       3.00000000
##
     1140.00000000
                                        1.00000000
                                                        1.58923521
                                                                       1.58923521
##
                                          beta.edu
                                                          beta.len
         beta.sex
                         beta.age
                                                                          beta.bas
##
       0.09531018
                                        0.23111172
                                                       0.12221763
                                                                       -0.22314355
                       0.22314355
##
         beta.conc
                           markerN
                                       beta.biom.v
                                                        mdfN.acup beta.mdf.acup.v
##
       -0.26136476
                       10.00000000
                                        2.00000000
                                                       4.00000000
                                                                        2.00000000
##
       gama.acup.v
                        mdfN.mbsr beta.mdf.mbsr.v
                                                     gama.mbsr.v
        2.00000000
                        4.00000000
                                        2.00000000
                                                        2.00000000
##
## [1] 0
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc
   <environment: 0x000000015b49f58>
##
             MSE
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
   110.21625985
                   1.01448709
                                 1.01583461
                                               0.06264865
                                                              1.04152398
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                 0.9849215 0.9842386 -0.07013254
## 5%
       96.96092
                                                         0.9851682
## 95% 131.19767
                 1.0920259 1.0985514 0.17247017
                                                         1.2170126
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
       zmdfAcup1 + xmbsr * zmdfMBSR1
  <environment: 0x000000013047948>
##
             MSE
                  L2normRatio
                                L1normRatio correlation MSEoverObsVar
      87.6426203
                     0.9061179
                                   0.9072673
                                                 0.4465725
##
                                                               0.8375847
##
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
                              0.8526405
## 5%
       75.88986
                  0.8551324
                                           0.3113864
                                                         0.7385903
## 95% 112.35757
                   1.0251833
                              1.0293764
                                           0.5209742
                                                         1.0874460
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
       zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
##
##
       zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x00000001346f840>
##
             MSF.
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      59.8302683
                     0.7487650
                                   0.7496153
                                                 0.6734212
                                                               0.5799581
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 50.73596
                 0.6877737
                              0.6853587
                                          0.5599805
                                                        0.4789185
## 95% 83.52957
                 0.8994547
                              0.9061743
                                         0.7258170
                                                        0.8540360
## [1] 0.75
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
##
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
       xmbsr * zmdfMBSR3
## <environment: 0x000000012e48fa8>
##
                  L2normRatio
                               L1normRatio
                                               correlation MSEoverObsVar
             MSF.
                     0.5289003
                                   0.5295492
                                                 0.8511352
                                                               0.2963680
##
      30.1779903
##
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.22747 0.4713831 0.4694262 0.7723189
                                                       0.2246247
```

```
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
      xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
##
      zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
      zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
      zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
##
      zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
  <environment: 0x00000002172c218>
##
##
            MSE
                  L2normRatio
                                L1normRatio
                                             correlation MSEoverObsVar
      1.32860157
                   0.10947715
                                 0.11022840
                                              0.99364242
                                                             0.01329152
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 0.9773481 0.09426938 0.09461809
                                          0.9879516
                                                      0.009007546
  95% 2.4428944 0.15712207 0.15662860
                                          0.9955293
                                                      0.026557993
##
       sampleSize
                            raceN
                                       sigma.race
                                                        beta.acup
                                                                       beta.mbsr
##
    1200.00000000
                       3.00000000
                                       1.00000000
                                                       1.58923521
                                                                      1.58923521
##
         beta.sex
                         beta.age
                                         beta.edu
                                                         beta.len
                                                                         beta.bas
##
       0.09531018
                       0.22314355
                                       0.23111172
                                                      0.12221763
                                                                     -0.22314355
##
        beta.conc
                          markerN
                                      beta.biom.v
                                                       mdfN.acup beta.mdf.acup.v
##
      -0.26136476
                      10.00000000
                                       2.00000000
                                                      4.00000000
                                                                      2.00000000
##
      gama.acup.v
                        mdfN.mbsr beta.mdf.mbsr.v
                                                     gama.mbsr.v
       2.00000000
                       4.00000000
                                       2.00000000
                                                      2.00000000
##
## [1] 0
  Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
## <environment: 0x0000000050ce1b8>
                 L2normRatio
                                L1normRatio
                                              correlation MSEoverObsVar
            MSE
                   1.01355890
                                 1.01485873
                                               0.06342896
                                                             1.03942630
##
   110.03756973
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
##
                              0.9841667 -0.06639098
## 5%
       97.06425
                 0.9844857
                                                        0.9848646
## 95% 130.57298
                  1.0867805
                              1.0925213 0.17215250
                                                        1.2070592
## [1] 0.25
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
      xconc + xbiom1 + xbiom2 + zmdfAcup1 + zmdfMBSR1 + xacup *
##
      zmdfAcup1 + xmbsr * zmdfMBSR1
## <environment: 0x000000000d0284c8>
##
            MSF.
                  L2normRatio
                                L1normRatio
                                              correlation MSEoverObsVar
##
     87.4043302
                    0.9047315
                                  0.9058993
                                                0.4479553
                                                              0.8346220
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
       75.92762
                 0.8549499
                            0.8526405
                                          0.3192320
                                                        0.7384262
## 95% 110.90563
                                          0.5209399
                 1.0225634
                            1.0211042
                                                        1.0758728
## [1] 0.5
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
      xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + zmdfAcup1 +
##
      zmdfAcup2 + zmdfMBSR1 + zmdfMBSR2 + xacup * zmdfAcup1 + xacup *
      zmdfAcup2 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2
## <environment: 0x000000006b38290>
##
            MSE
                  L2normRatio
                                L1normRatio
                                              correlation MSEoverObsVar
                                  0.7477983
                                                0.6747622
##
      59.5612270
                    0.7469393
                                                              0.5765728
           MSE L2normRatio L1normRatio correlation MSEoverObsVar
                            0.6850565
                                         0.5647692
## 5% 50.73596
                 0.6877153
                                                       0.4785674
## 95% 82.31456
                 0.8868399
                             0.8958081
                                         0.7260486
                                                       0.8245268
## [1] 0.75
```

```
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
##
       xbiom7 + xbiom8 + zmdfAcup1 + zmdfAcup2 + zmdfAcup3 + zmdfMBSR1 +
       zmdfMBSR2 + zmdfMBSR3 + xacup * zmdfAcup1 + xacup * zmdfAcup2 +
##
##
       xacup * zmdfAcup3 + xmbsr * zmdfMBSR1 + xmbsr * zmdfMBSR2 +
##
       xmbsr * zmdfMBSR3
## <environment: 0x0000000213be098>
             MSF.
##
                  L2normRatio
                                 L1normRatio
                                               correlation MSEoverObsVar
##
      29.9607656
                     0.5269985
                                   0.5276466
                                                 0.8521039
                                                               0.2937285
##
            MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 24.22162
                  0.4710245
                              0.4690547
                                          0.7813860
                                                        0.2243183
## 95% 45.62316
                              0.6668161
                                          0.8820633
                                                        0.4530929
                  0.6585545
## [1] 1
## Y ~ xrace + xacup + xmbsr + xsex + xage + xedu + xlen + xbas +
##
       xconc + xbiom1 + xbiom2 + xbiom3 + xbiom4 + xbiom5 + xbiom6 +
##
       xbiom7 + xbiom8 + xbiom9 + xbiom10 + zmdfAcup1 + zmdfAcup2 +
##
       zmdfAcup3 + zmdfAcup4 + zmdfMBSR1 + zmdfMBSR2 + zmdfMBSR3 +
##
       zmdfMBSR4 + xacup * zmdfAcup1 + xacup * zmdfAcup2 + xacup *
##
       zmdfAcup3 + xacup * zmdfAcup4 + xmbsr * zmdfMBSR1 + xmbsr *
       zmdfMBSR2 + xmbsr * zmdfMBSR3 + xmbsr * zmdfMBSR4
##
## <environment: 0x0000000216df940>
##
             MSE
                  L2normRatio
                                L1normRatio
                                               correlation MSEoverObsVar
##
      1.31430665
                    0.10893719
                                 0.10969078
                                                0.99371489
                                                              0.01311959
             MSE L2normRatio L1normRatio correlation MSEoverObsVar
## 5% 0.9773289 0.09430026 0.09463756
                                           0.9889092
                                                       0.009007546
## 95% 2.1871619 0.15067731 0.15132287
                                           0.9955271
                                                       0.023950812
cbind(groupSampleSizes*3, AUC);
##
         [,1]
                    [,2]
                              [,3]
                                        [,4]
                                                  [,5]
           60 0.01292311 0.2902731 0.4989935 0.6867223 0.9765899
##
   [1,]
   [2,] 120 0.01793359 0.3299756 0.5551843 0.7505058 0.9843002
   [3,] 180 0.03079011 0.3593132 0.5855331 0.7803190 0.9873621
##
   [4,] 240 0.03531787 0.3774975 0.6056587 0.7978682 0.9890440
  [5,] 300 0.03561046 0.3909426 0.6190605 0.8090522 0.9900972
##
```

```
[6,] 360 0.04217519 0.4000611 0.6301047 0.8175253 0.9908401
   [7,] 420 0.04419673 0.4081965 0.6372417 0.8235877 0.9913833
##
   [8,] 480 0.04699353 0.4148566 0.6439486 0.8289088 0.9918120
##
  [9,] 540 0.04964828 0.4196217 0.6489627 0.8327286 0.9921400
## [10.] 600 0.05084040 0.4237590 0.6528310 0.8357743 0.9924092
## [11,] 660 0.05291181 0.4276213 0.6563837 0.8386099 0.9926366
## [12,] 720 0.05462993 0.4307361 0.6594334 0.8407926 0.9928254
## [13,] 780 0.05560470 0.4339877 0.6622521 0.8428745 0.9929891
## [14,] 840 0.05635232 0.4366861 0.6647317 0.8447693 0.9931339
## [15,] 900 0.05767138 0.4391333 0.6668305 0.8463244 0.9932593
## [16,] 960 0.05914792 0.4414224 0.6687775 0.8477086 0.9933693
## [17,] 1020 0.06035145 0.4433866 0.6705185 0.8489662 0.9934715
## [18,] 1080 0.06141977 0.4451890 0.6720166 0.8501087 0.9935629
## [19,] 1140 0.06264865 0.4465725 0.6734212 0.8511352 0.9936424
## [20,] 1200 0.06342896 0.4479553 0.6747622 0.8521039 0.9937149
```