

Self-Check 1, 3, 4

1. Determine how many times the output statement is executed. Indicate whether the algorithm is $O(n^2)$ or $O(n)$.
 - a. $O(n^2)$ – Output statement is executed n^2 times.
 - b. $O(n)$ – Output statement is executed $2n$ times.
 - c. $O(n^2)$ - Output statement is executed $\frac{n(n+1)}{2}$ times
 - d. $O(n^2)$ - Output statement is executed $n - 1$ times

3.

O(f(n))	f(2000)	f(4000)	f(8000)	f(4000)/f(2000)	f(8000)/f(4000)
a. $O(\log n)$	10.966	11.966	12.966	1.091	1.084
b. $O(n)$	2000	4000	8000	2	2
c. $O(n \log n)$	21932	47864	103728	2.182	2.167
d. $O(n^2)$	4,000,000	16,000,000	64,000,000	4	4
e. $O(n^3)$	$8.0 * 10^9$	$6.4 * 10^{10}$	$5.12 * 10^{11}$	8	8

4. When possible, values are estimated from figure 2.9. Otherwise, they are calculated (shown in red)

Growth Type	f(20)	f(40)
Exponential	1,048,576	$1.0995 * 10^{12}$
Cubic	4,000	64,000
Quadratic	2,000	8,000
Log-Linear	2,500	5,000
Linear	2,000	4,000
Logarithmic	1,800	2,000

Programming 1

//CompareGrowth.java output

n = 0	y1 = 10	y2 = 2
n = 10	y1 = 1010	y2 = 502
n = 20	y1 = 2010	y2 = 2002
n = 30	y1 = 3010	y2 = 4502
n = 40	y1 = 4010	y2 = 8002
n = 50	y1 = 5010	y2 = 12502
n = 60	y1 = 6010	y2 = 18002
n = 70	y1 = 7010	y2 = 24502
n = 80	y1 = 8010	y2 = 32002
n = 90	y1 = 9010	y2 = 40502
n = 100	y1 = 10010	y2 = 50002

This result isn't surprising. Because $y2$ contains n^2 (while $y1$ only contains n), as n increases, the constants in $y1$ and $y2$ have less impact on their values.