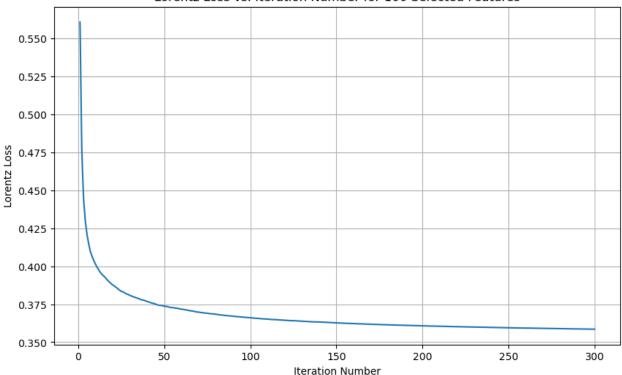
```
In [ ]: import pandas as pd
          \textbf{import} \text{ numpy } \textbf{as} \text{ np}
          {\color{red}\textbf{import}} \ {\color{blue}\textbf{matplotlib.pyplot}} \ {\color{blue}\textbf{as}} \ {\color{blue}\textbf{plt}}
          \textbf{from} \  \, \textbf{sklearn.preprocessing} \  \, \textbf{import} \  \, \textbf{StandardScaler}
          from scipy.special import expit
          from sklearn.metrics import accuracy_score, roc_curve
In [ ]: X = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Gisette\gisette_train.data', sep = ' ', header= None)
         y = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Gisette\gisette_train.labels', header = None)
Xt = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Gisette\gisette_valid.data', sep = ' ', header = None)
          yt = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Gisette\gisette_valid.labels', header= None)
          X = X.drop(5000, axis = 1)
          Xt = Xt.drop(5000, axis = 1)
          scaler = StandardScaler()
          Xs = scaler.fit_transform(X)
          Xts = scaler.transform(Xt)
          Xs = np.hstack([np.ones((Xs.shape[0], 1)), Xs])
          Xts = np.hstack([np.ones((Xts.shape[0], 1)), Xts])
          y = np.where(y == -1, 0, 1)
         yt = np.where(yt == -1, 0, 1)
In [ ]: def grad(X, y, w):
              ywx = y * np.matmul(w, X.T)
              dl = (2*(ywx - 1)/(1 + (ywx - 1)**2))
              dl = np.where(ywx > 1, 0, dl)
              g = (1/X.shape[0])*np.matmul(dl * y, X ) + 2*s*w
              return g
In [ ]: def loss(X,y,w):
              yxw = y * np.matmul(w, X.T)
              toadd = np.log(1 + (yxw - 1)**2)
              toadd = np.where(yxw > 1, 0, toadd)
              tot = (1/X.shape[0])*np.sum(toadd) + s*(np.linalg.norm(w)**2)
In [ ]: def schedule(k, p, mu, iter):
              sch = []
              for i in range(iter):
                   mi = k + (p-k)*np*max([0, (iter - 2*i)/(2*i*mu + iter)])
                   mi = np.min([p - 1, mi])
                   sch.append(round(mi))
              return sch
In []: s = 0.001
          def fit(X,y, eta, des_feat):
              w = np.zeros(X.shape[1])
              y = y.squeeze()
              feat_ind = range(X.shape[1])
              sch = schedule(des_feat, X.shape[1] + 1, 300, 300)
              for i in range(300):
                   w[feat_ind] = w[feat_ind] - eta*grad(X[:, feat_ind], y, w[feat_ind])
                   feat_ind = np.abs(w).argsort()[-(sch[i]):]
                   w1 = np.zeros(X.shape[1])
                   w1[feat_ind] = w[feat_ind]
                   w = w1
              return w
In [ ]: #from hw4
          def score(X, y, w):
              Xw = np.matmul(X,w)
              p = np.where(expit(Xw) > 0.5, 1, 0)
              return accuracy_score(p, y)
In []: w0 = fit(Xs,y, 0.01, 500)
          score(Xs, y, w0)
Out[ ]: 0.9105
In [ ]: def loss_v_iter(X,y,eta):
              liter = []
              w = np.zeros(X.shape[1])
              y = y.squeeze()
              feat_ind = range(X.shape[1])
```

```
sch = schedule(100, X.shape[1] + 1, 300, 300)
for i in range(300):
    w[feat_ind] = w[feat_ind] - eta*grad(X[:, feat_ind], y, w[feat_ind])
    feat_ind = np.abs(w).argsort()[-(sch[i]):]
    w1 = np.zeros(X.shape[1])
    w1[feat_ind] = w[feat_ind]
    w = w1
    liter.append(loss(X,y,w))
return liter
```

```
In []: gis_liter = loss_v_iter(Xs, y, 0.01)

In []: plt.figure(figsize=(10,6))
    plt.plot(range(1,301), gis_liter)
    plt.ylabel('Lorentz Loss')
    plt.xlabel('Iteration Number')
    plt.title('Lorentz Loss vs. Iteration Number for 100 Selected Features')
    plt.grid()
    plt.show()
```

Lorentz Loss vs. Iteration Number for 100 Selected Features

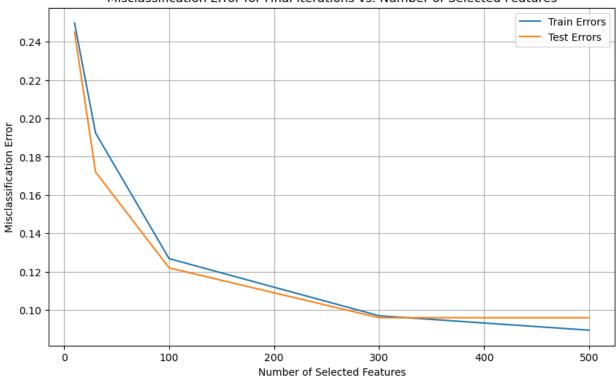


```
In [ ]: desired_features = [10, 30, 100, 300, 500]

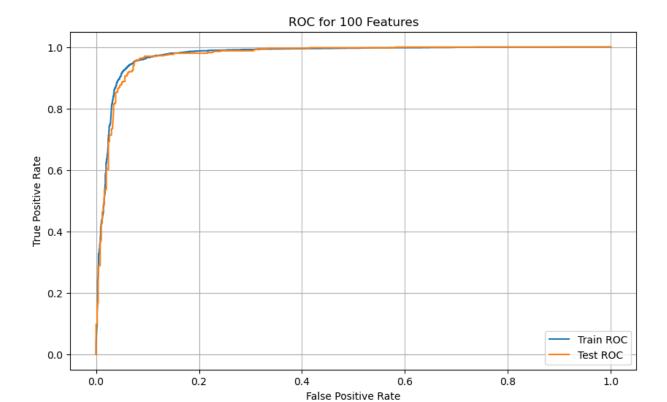
In [ ]: misclass_train = []
    misclass_test = []
    for d in desired_features:
        w = fit(Xs, y, 0.01, d)
        wt = fit(Xts, yt, 0.01, d)
        misclass_train.append(1 - score(Xs, y, w))
        misclass_train.append(1 - score(Xts, yt, wt))

In [ ]: plt.figure(figsize=(10,6))
    plt.plot(desired_features, misclass_train, label = 'Train Errors')
    plt.plot(desired_features, misclass_test, label = 'Test Errors')
    plt.title('Misclassification Error for Final Iterations vs. Number of Selected Features')
    plt.ylabel('Number of Selected Features')
    plt.glabel('Number of Selected Features')
    plt.glabel('Misclassification Error')
    plt.legend()
    plt.legend()
    plt.legend()
    plt.show()
```

Misclassification Error for Final Iterations vs. Number of Selected Features



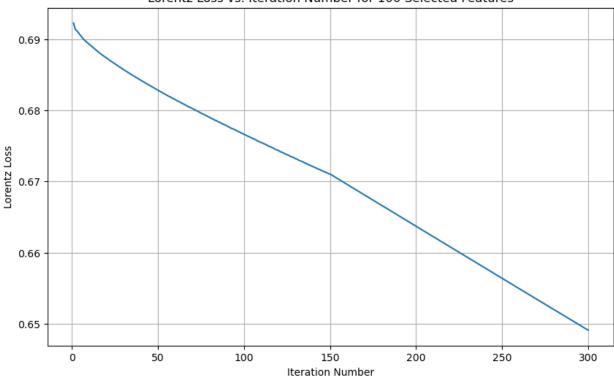
```
In [ ]: misclass_train
Out[]: [0.249666666666667,
          0.19233333333333336,
           0.126833333333333335,
          0.0969999999999998,
          0.0895000000000000002]
In [ ]: misclass_test
         [0.245, 0.1720000000000000, 0.122, 0.09599999999997, 0.09599999999999]
Out[ ]:
In [ ]: w_100 = fit(Xs,y,0.01,100)
In [ ]: prob_y_100 = expit(np.matmul(Xs, w_100))
          prob_yt_100 = expit(np.matmul(Xts, w_100))
         fpr_train, tpr_train, _ = roc_curve(y, prob_y_100)
fpr_test, tpr_test, _ = roc_curve(yt, prob_yt_100)
In [ ]: plt.figure(figsize=(10,6))
         plt.plot(fpr_train, tpr_train, label= 'Train ROC')
plt.plot(fpr_test, tpr_test, label = 'Test ROC')
          plt.xlabel('False Positive Rate')
          plt.ylabel('True Positive Rate')
          plt.title('ROC for 100 Features')
          plt.grid()
          plt.legend()
          plt.show()
```



Dexter dataset

```
In [ ]: X = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Dexter\dexter_train.csv', header= None)
        y = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Dexter\dexter_train.labels', header = None)
        Xt = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Dexter\dexter_valid.csv', header= None)
        yt = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\Dexter\dexter_valid.labels', header = None)
        scaler = StandardScaler()
        Xs = scaler.fit_transform(X)
        Xts = scaler.transform(Xt)
        Xs = np.hstack([np.ones((Xs.shape[0], 1)), Xs])
        Xts = np.hstack([np.ones((Xts.shape[0], 1)), Xts])
        y = np.where(y == -1, 0, 1)
        yt = np.where(yt == -1, 0, 1)
In [ ]: w0 = fit(Xs,y, 0.0001, 100)
        score(Xs, y, w0)
        0.896666666666666
Out[]:
In [ ]: dex_liter = loss_v_iter(Xs, y, 0.0001)
        plt.figure(figsize=(10,6))
        plt.plot(range(1,301), dex_liter)
        plt.ylabel('Lorentz Loss')
        plt.xlabel('Iteration Number')
        plt.title('Lorentz Loss vs. Iteration Number for 100 Selected Features')
        plt.grid()
        plt.show()
```

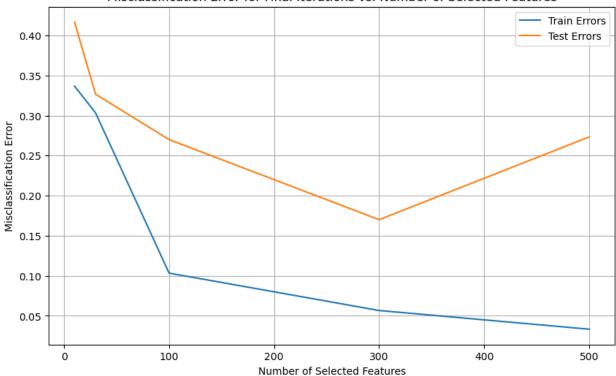




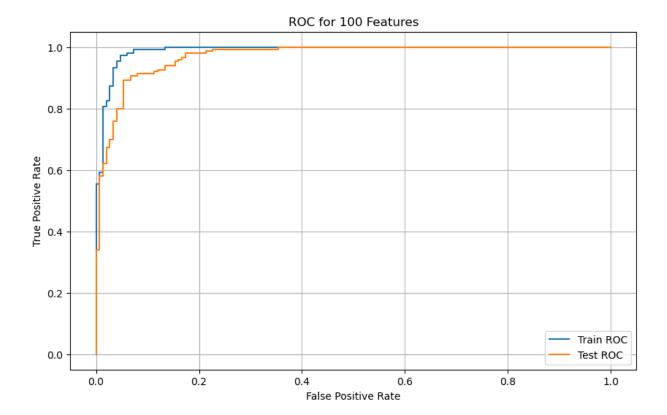
```
In [ ]: misclass_train = []
    misclass_test = []
    for d in desired_features:
        w = fit(Xs, y, 0.0001, d)
        wt = fit(Xts, yt, 0.0001, d)
        misclass_train.append(1 - score(Xs, y, w))
        misclass_test.append(1 - score(Xts, yt, wt))
In [ ]: plt.figure(figsize=(10,6))
```

```
In []: plt.figure(figsize=(10,6))
    plt.plot(desired_features, misclass_train, label = 'Train Errors')
    plt.plot(desired_features, misclass_test, label = 'Test Errors')
    plt.title('Misclassification Error for Final Iterations vs. Number of Selected Features')
    plt.xlabel('Number of Selected Features')
    plt.ylabel('Misclassification Error')
    plt.grid()
    plt.legend()
    plt.show()
```

Misclassification Error for Final Iterations vs. Number of Selected Features



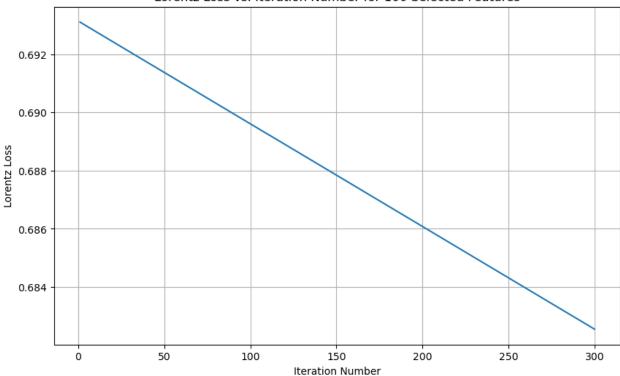
```
In [ ]: misclass_train
0.30333333333333334,
          0.10333333333333339,
         0.05666666666666664,
         0.0333333333333333333
In [ ]: misclass_test
0.27,
         0.1700000000000000004,
         0.27333333333333333]
In [ ]: w_100 = fit(Xs,y,0.0001,100)
         prob_y_100 = expit(np.matmul(Xs, w_100))
         prob_yt_100 = expit(np.matmul(Xts, w_100))
         fpr_train, tpr_train, _ = roc_curve(y, prob_y_100)
fpr_test, tpr_test, _ = roc_curve(yt, prob_yt_100)
In [ ]: plt.figure(figsize=(10,6))
         plt.plot(fpr_train, tpr_train, label= 'Train ROC')
plt.plot(fpr_test, tpr_test, label = 'Test ROC')
         plt.xlabel('False Positive Rate')
         plt.ylabel('True Positive Rate')
         plt.title('ROC for 100 Features')
         plt.grid()
         plt.legend()
         plt.show()
```



Madelon Dataset

```
In [ ]: X = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\MADELON\madelon_train.data', sep = ' ', header= None)
          y = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\MADELON\madelon_train.labels', header = None)
         Xt = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\MADELON\madelon_valid.data', sep = ' ', header = None)
yt = pd.read_csv('D:\School\Applied ML FSU\Applied-ML-FSU\Data\MADELON\madelon_valid.labels', header= None)
          X = X.drop(500, axis = 1)
          Xt = Xt.drop(500, axis= 1)
          scaler = StandardScaler()
          Xs = scaler.fit_transform(X)
         Xts = scaler.transform(Xt)
          Xs = np.hstack([np.ones((Xs.shape[0], 1)), Xs])
         Xts = np.hstack([np.ones((Xts.shape[0], 1)), Xts])
         y = np.where(y == -1, 0, 1)
yt = np.where(yt == -1, 0, 1)
In [ ]: w0 = fit(Xs,y, 0.0001, 100)
         score(Xs, y, w0)
Out[ ]: 0.5735
In [ ]: mad_liter = loss_v_iter(Xs, y, 0.0001)
         plt.figure(figsize=(10,6))
          plt.plot(range(1,301), mad_liter)
          plt.ylabel('Lorentz Loss')
         plt.xlabel('Iteration Number')
          plt.title('Lorentz Loss vs. Iteration Number for 100 Selected Features')
          plt.grid()
          plt.show()
```

Lorentz Loss vs. Iteration Number for 100 Selected Features

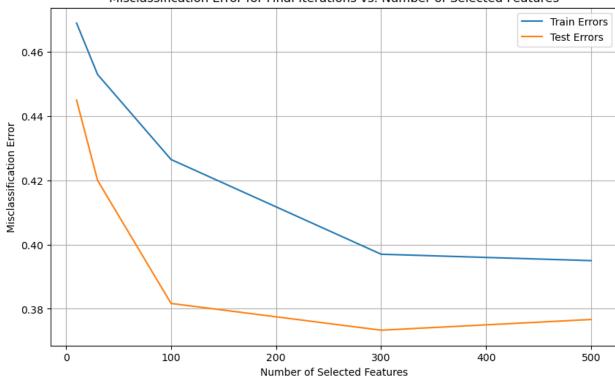


```
In []: misclass_train = []
    misclass_test = []
    for d in desired_features:
        w = fit(Xs, y, 0.0001, d)
        wt = fit(Xts, yt, 0.0001, d)
        misclass_train.append(1 - score(Xs, y, w))
        misclass_test.append(1 - score(Xts, yt, wt))
In []: plt.figure(figsize=(10,6))
    plt.plot(desired_features, misclass_train, label = 'Train Errors')
    plt.plot(desired_features, misclass_test, label = 'Test Errors')
    plt.title('Misclassification Error for Final Iterations vs. Number of Selected Features')
```

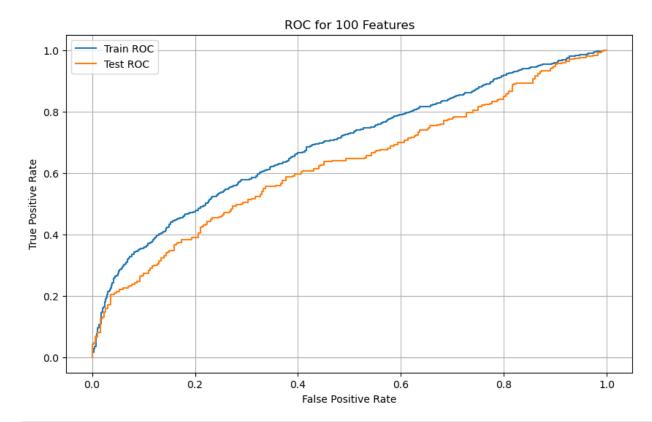
plt.xlabel('Number of Selected Features')
plt.ylabel('Misclassification Error')

plt.grid()
plt.legend()
plt.show()

Misclassification Error for Final Iterations vs. Number of Selected Features



```
In [ ]: misclass_train
        [0.469, 0.452999999999999, 0.4265, 0.397, 0.395]
Out[]:
In [ ]: misclass_test
0.420000000000000004,
          0.381666666666666666667,
          0.3766666666666667]
In [ ]: w_100 = fit(Xs,y,0.0001,100)
         prob_y_100 = expit(np.matmul(Xs, w_100))
         prob_yt_100 = expit(np.matmul(Xts, w_100))
         fpr_train, tpr_train, = roc_curve(y, prob_y_100)
fpr_test, tpr_test, = roc_curve(yt, prob_yt_100)
In [ ]: plt.figure(figsize=(10,6))
         plt.plot(fpr_train, tpr_train, label= 'Train ROC')
         plt.plot(fpr_test, tpr_test, label = 'Test ROC')
         plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
         plt.title('ROC for 100 Features')
         plt.grid()
         plt.legend()
         plt.show()
```



Tn []: