

PRICE, ANCHORING, & SUBSTITUTION
IN
THE MARKET FOR FINE ART AUCTIONS

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ABSTRACT

Joan Miro and Salvador Dali are two Surrealists painters often featured together at auction. Can the past price of a Miro painting drive up the current price of a Dali piece? We examine the existence and behavior of these “anchoring” cross-effects between prices of related art pieces sold at auction. Our research generalizes the anchoring model of Beggs & Graddy (2009) in order to study related art pieces. We draw upon insights from conversations with art specialists and experts at Sotheby’s, and construct a new dataset of recent auction sales for assorted art (2006-2015). We find significant evidence of anchoring cross-effects. Our findings are of interest to art researchers, auction house specialists, and those who wish to understand where price signals travel in the art auction world.

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1. INTRODUCTION

Imagine you are heading to Christie's to bid on a Monet painting, which experts believe is worth \$1 million based on its size and medium. However, you're unaware of those experts' estimates and you have no idea how much the Monet is worth, so you look up recent sales of other Impressionist paintings. You find out a Van Gogh sold for \$20 million last week. With that number in mind, you start to believe the Monet is also worth \$20 million, and that's how much you bid - even if that amount reflects more the price of the Van Gogh than the Monet itself.

This is known as the *anchoring effect* - a well-studied cognitive bias in which the first value you hear (the "anchor") can shape your perception of what sorts of values are normal. This was first demonstrated in a landmark experiment by Tversky & Kahneman (1974). In that study, participants were given five seconds to mentally calculate the product of the numbers 1 through 8, visually written out for them on a blackboard. It was found that if the numbers were displayed as "1x2x3x4x5x6x7x8", participants would read the lower numbers first and give a median estimate of 512 for the product. On the other hand, if the numbers were displayed as "8x7x6x5x4x3x2x1", then participants would first see the higher numbers and give a much higher median estimate of 2250. Thus, it seems that first impressions do affect judgement, at least in quantitative scenarios.

This bias also appears in the market for fine art auctions, which in 2014 saw a sales volume of approximately \$7.35 billion (Christie's Figures 2014). To the best of our knowledge, Beggs & Graddy (2009) were the first to formally study anchoring in the context of art auctions. In their model, the hedonic value of an artwork, say a painting, is assumed to be determined by its hedonic characteristics such as the artist, medium, and degree of authenticity. These features do not change

over time², which means that if buyers were perfectly rational, they would pay only according to their (time-dependent) demand for these features. If however, buyers learn that the painting previously sold for a very high price, they may internalize that previous high price as a reference point – the “anchor” – and be willing to pay much more as a result. Past price could legitimately inform current price since it reflects hedonic value, as well as other relevant, non-hedonic influences such as bidder wealth and artwork reputation. However, if we control for those, then past price becomes an irrelevant signal in this context, and its impact on current price can be interpreted as an anchoring effect. Thus, anchoring is said to occur when past price biases current price, controlling for hedonic value and non-hedonic price determinants.

Of course, the ways in which auction participants internalize and act upon past price cannot be inferred from just observing prices. Hence in our research and in much of the literature, including Beggs & Graddy (2009), this is treated as a black box. The mere observation of this effect, i.e. past price biasing current price, suffices for our definition of anchoring (discussed further in Section 2).

Using a regression model that carefully separates out anchoring, Beggs & Graddy (2009) identified and analyzed resales of Impressionist and Contemporary paintings, finding significant evidence of anchoring effects. However, as mentioned in their paper, it is very difficult to identify multiple sales of the same art piece. This method of testing for anchoring effects cannot be applied to new works or works that have never been brought to auction. Moreover, in practice, it turns out that auction specialists appraise an art piece based primarily on past sales of related pieces³. The anchoring research of Beggs & Graddy (2009) is limited in its analysis and applicability.

² Age is not considered a hedonic feature, because for us it represents time-dependent demand for art rather than intrinsic characteristics of the work.

³ Interview, Raphaëlle Benabou.

In this paper, we study whether the sales of similar paintings (substitutes) display anchoring cross-effects – for example, whether the past price of a Monet can bias the current price of a Van Gogh. Our data consists of two datasets of Impressionist and Contemporary art, used not only in Beggs & Graddy (2009) but also in many other econometric papers on art auctions, as well as a new dataset of assorted art sales between 2006 and 2015 specifically collected for this project. We begin by successfully replicating the general anchoring findings from Beggs & Graddy (2009). Our success is surprising and noteworthy because, as discussed later in Section 6, we do not know exactly which observations in their data were originally used. Next, we introduce our expanded version of their model, which tests for anchoring cross-effects by controlling for similarity across pieces. We introduce two quantitative measures of similarity. Running our model on these three datasets, we discover significant evidence of anchoring cross-effects for Impressionist and assorted art. To ensure robustness, we also run our model on a subset of our assorted art dataset for three specific artist pairs who we already know to be similar or dissimilar. This selection, explained in Section 6, includes Joan Miro & Salvador Dali, Pablo Picasso & Marc Chagall, and Edvard Munch & Henri de Toulouse-Lautrec. In those three comparisons, we find the extent of artistic similarity (or dissimilarity) really is accurately reflected in whether our model detects anchoring.

This research makes several major contributions to the existing literature on art auctions. First, to the best of our knowledge, no econometric work has attempted to quantify hedonic similarity between art pieces. Thus, this study is useful not only for appraising art, but also for other tasks where art pieces must be compared, such as constructing price indices across heterogeneous artworks. We hope our two measures of similarity may provide a starting point for such analysis. Second, much of the econometric work on art auctions has relied on the same two Impressionist and Contemporary art datasets that only include sales until 1991 and 1994, respectively. Our new dataset of approximately 500,000 assorted art sales (2006-2015), constructed by writing a Python

program to scrape an online art database for 10 straight days, is a larger and more up-to-date collection of auction data (Blouin Art Sales Index). Lastly, our discovery of anchoring cross-effects is notable because it adds to the growing body of research on how price signals implicitly propagate around the art auction market. Our work allows researchers to account for hidden biases such as anchoring when comparing sales of different art pieces, and demonstrates how Beggs & Graddy’s original anchoring model may be successfully customized. For auction houses and professionals, our work provides a practical regression model for estimating an artwork’s price in light of related sales. Beggs & Graddy’s original model has been extensively applied in other domains such as corporate finance, real estate, and horse racing (Dougal et al. 2015; Leung & Tsang 2013; McAlvanah & Moul 2013). Our approach is more general than Beggs & Graddy’s, and may find application in other fields as well.

As part of our research, we conducted interviews with several specialists and experts in the field. To learn about the art market and how auction specialists appraise pieces, we talked with Mark Best, a former financial analyst who is now a specialist in American, Modern, and Contemporary prints at Sotheby’s NYC. For insight into artistic similarity, we talked with Hadley Newton, who formerly worked at Sotheby’s with Impressionist art. The three artist pairs we examine in Section 6 were suggested by Hadley. We also talked extensively with Raphaëlle Benabou, who is an administrator of art collections, estates, and valuations at Bonham’s in London. Raphaëlle provided us with many of our anecdotes and fact-checked our description of the auction system. We draw upon these interviews for both our discussion and our quantitative analysis.

Determining artistic similarity is not trivial: we were told that no two art pieces are the same⁴. Even in the case of prints, where 100-200 copies (editions) of the same art piece are manufactured

⁴ Interview, Mark Best.

and numbered in order of production, an edition with a lower number (i.e. produced earlier) may sell for more than an edition with a higher number. Furthermore, drivers of similarity can vary at different price points, and whether art is purchased as a decoration or as an investment. In this paper, we provide a starting point for quantitatively measuring similarity between pieces, but acknowledge that better measures could be constructed.

This thesis proceeds as follows. In Section 2, we give a brief overview of the art auction system and process, followed by a discussion of anchoring and its role in this market. Section 3 surveys the literature relevant to anchoring in the art market and explains the importance of our research. Section 4 describes the original data of Beggs & Graddy, as well as our new dataset, and explains the motivation behind constructing the latter. Section 5 describes our methodology, which includes the original regressions of Beggs & Graddy (2009), our expanded regression models, and our measures of substitution. Section 6 gives our results. This includes our replication of the anchoring work of Beggs & Graddy, followed by our findings on anchoring cross-effects. We then present the results of our experiments on the three artist pairs suggested to us by Hadley Newton. Finally, Section 7 concludes with a summary of our research and directions for future work.

2. OVERVIEW OF ART AUCTIONS & ANCHORING

The Art Auction System

In perhaps one of the world's oldest duopolies, approximately 42% of the global art auction market is controlled by two major houses: Christie's and Sotheby's, established in 1766 and 1744 respectively (Baker & Kazakina 2015). The former, headquartered in London, is privately held by French multimillionaire Francois-Henri Pinault and only reports sales figures twice a year. Sotheby's, headquartered in New York City, is publicly traded and reports detailed revenues and costs. While both houses deal in art, often sourced from museum or private collections, in recent years Christie's has become the larger player. In the first six months of 2015, Christie's realized \$4.5 billion in art sales, while Sotheby's only pulled \$3.5 billion (Reyburn 2015). That said, both houses have enjoyed their share of record-breaking auctions: Picasso's *Les Femmes d'Alger ("Version O")* sold for \$179 million at Christie's in 2015, while Pollock's *No. 5, 1948* went for \$164 million at Sotheby's in 2006. The whole spectrum of art can be found at Christie's and Sotheby's, ranging from Impressionist oil paintings to Chinese ceramics. Auctions are usually themed around a certain artist, medium, time period, or represent a private collection. Often individual events are part of a series, such as Christie's "First Open" series (launched in 2005) for post-war and contemporary art. Other smaller but well-known auction houses include Bonham's and Phillip's, both headquartered in the United Kingdom.

In addition to art, both houses run auctions for other goods such as jewelry, automobiles, and furniture. Many believe, however, these houses play to different strengths. To sell photographs, go to Sotheby's; to sell books and manuscripts, go to Christie's (Rohleder 2001). For classic automobiles, go to Sotheby's or Bonham's (Reyburn 2015). Specialization is not limited to product selection, either. According to Raphaele Benabou, Bonham's (as a smaller house) appeals to many

sellers because lower sales volume ensures pieces will be better noticed at auction. Competition between auction houses is fierce, and each tries to capture the best consignments by luring sellers with benefits such as higher guaranteed prices and waived house commission fees (Baker & Kazakina 2015). Yet, the two houses have cooperated and even colluded at times. In the early 2000's, both houses were convicted of fixing commission fees charged to sellers, and were required to pay back \$256 million each (O'Connell 2000).

The actual auction process is as follows. First, a client (prospective seller) will request an estimate from the auction house for their item of interest, either by submitting photographs or scheduling an in-person appointment with a specialist. If the item is deemed appropriate for auction, the house and the seller will enter negotiations and draw up a seller's contract. The item then travels to the house to be officially photographed, catalogued, and stored before the auction event ("How to Sell" n.d.). Clients may visit more than one auction house to compare arrangements.

Three quantities are decided by the seller and the house before any auction: a low and a high presale estimate for the art piece, and a reserve price. The low and high estimates represent the range of possible values the piece might go for, and are usually suggested by a committee of in-house art experts. As shown empirically by Ashenfelter (1989), these estimates do generally seem to accurately predict sale price. Some cross-house differences may exist: Bauwens and Ginsburgh (2000), for instance, show that in certain art categories, Sotheby's tends to undervalue expensive pieces and overvalue inexpensive ones (while Christie's does the opposite). In negotiations, the seller and the house also determine a reserve price known only to those two parties. The reserve price, which designates the minimum price the seller will accept for an item, is a closely guarded secret in the art auction world. However, according to estimates by Ashenfelter, Graddy and Stevens (2002), the reserve price may be set around 70-80% of the low estimate. It is unclear why the reserve is

concealed, but Vincent (1995) suggests that under certain circumstances, announcing the reserve may discourage potential bidders from participating and could lower overall bids.

Before the auction event, the house will typically publish a presale catalog for the art pieces, available both in print and online. For each piece to be sold, the catalog includes photographs and the presale estimates, as well as information on the artist, the materials and a condition report, signs of authenticity such as a signature, and who previously owned the work (provenance). Houses also host pre-auction viewings where both potential bidders and the public can examine items in person. Bidders must register before an auction, and for particularly opulent events, must show proof of their assets.

Auctions are almost always conducted in an ascending first price format. Unless starting bids have been pre-placed, the auctioneer starts low (somewhere below the secret reserve price) and calls increasing prices until the bidding stops, upon which the item is declared to be “knocked down” or “hammered down” (Ashenfelter 1989).⁵ The final sale price is the “hammer price.” On top of this, the house adds “buyer’s premium” commission fee, usually 20% to 25% of the hammer price, before the winning bidder receives the item (Ashenfelter & Graddy 2003).⁶ At Sotheby’s and Christie’s, the seller receives payment approximately 35 days after the auction, minus a “seller’s premium” which is usually around 10% of the hammer price (“Selling at Christie’s” n.d.; Ashenfelter & Graddy 2003). If an item does not meet its reserve price, it goes unsold and is said to have been “bought in.” The auction house, however, rarely purchases the item: instead, it may be resold later at a lower estimate or taken off the market. Historically, auction houses did not publish records of whether items went unsold. However, since the 1980s, auction houses in NYC have been legally required to report this

⁵ The auctioneer will call out prices around 10% higher than the current bid (“Sotheby’s – Glossary” n.d.).

⁶ Interview, Raphaëlle Benabou.

information. And, according to Ashenfelter & Graddy (2003), houses in other locations are following this trend as well.

How Anchoring Affects Art Auctions

The art auction market is especially vulnerable to unobserved psychological and behavioral biases, because on both sides of the market, participants must rely on subjective judgement, past experience, and personal preferences to evaluate artwork. The ever-changing heterogeneity of art pieces, buyers, and sellers makes it intractable for both auction houses and economists to perfectly estimate demand for art. Thus, the auction format, designed to set prices by discovering private valuations, seems fitting for this context. Yet, auction outcomes can be shaped drastically by behavioral phenomena. Competition can become fierce between bidders who wish to win the same item (“bidding wars”), driving up hammer prices far beyond an artwork’s estimated value (Gleadell 2016). Auctions are very emotional experiences, as we learned firsthand when we attended an auction for Chinese ceramics at Christie’s NYC. When one sculpture got caught in a bidding war and ended up selling for nearly \$500,000, the room erupted in applause.

Anchoring is one of the most-studied biases in the behavioral sciences: it is at once trivial to demonstrate and difficult to explain away. The effect occurs when first (quantitative) impressions distort future outcomes, even when the initial information is irrelevant (Tversky & Kahneman 1974; Sugden et al. 2013). As described in our introduction, we can identify anchoring through the impact of past sale price on current price, controlling for hedonic quality and non-hedonic influences on current price. The assumption of constant hedonic quality across sales is foundational for Beggs & Graddy (2009), and this quality must clearly be controlled for since it informs price at every time step. Yet, non-hedonic influences may also shape current price. For instance, if buyers believe an artwork will sell for more in the future, then they may pay more at time $t - 1$. These high

expectations may carry forward to later buyers, driving up the current price further at time t . Thus, controlling for both hedonic and non-hedonic determinants of current price is necessary if we wish to study how past price anchors current price.

As mentioned earlier, the exact behavioral mechanism by which this occurs is a black box: the overall effect may be attributed to buyers, sellers, auctioneers, or some combination of all three (Graddy et al. 2014). Below, we briefly describe what this could look like for those different groups.

Bidders may anchor on numbers provided prior to auction: this can include presale estimates and past prices for an artwork, as well as estimates and prices for related pieces. Estimates are expected to anchor bidder perceptions, because by definition, they give a general idea of how much a piece is worth. As discussed, past prices can reflect not only hedonic value but unobserved past factors such as bidding activity, the wealth of individual buyers, and even exogenous factors such as the weather (De Silva et al. 2012). It is worth noting that anchoring is difficult to avoid, though more expertise in the given area helps to guard against this bias (Northcraft & Neale 1987).

Sellers may anchor on past sales prices when setting the reserve. Some research finds that anchoring is more powerful for sellers than for buyers, but weakens with increased seller experience (Sugden et al. 2013; Alevy et al. 2011). Auctioneers can actively anchor bidder perceptions of value through the numbers they call out, particularly at the start of an auction. While this can be a powerful tool for the auctioneer, Brandly (2015) warns against setting anchors too high (to drive up future bids) or too low (to attract starting bids). Go too high, and your numbers lose credibility; go too low, and bidders will suspect something is wrong with the item.

We learned that auction houses are aware of anchoring effects, not only between resales of the same item, but between sales of related pieces.⁷ When internal departments formulate presale

⁷ Interview, Raphaëlle Benabou.

estimates for a work of art, a single specialist will research past sales of comparable pieces (similar size, artist, medium, etc.) to get a ballpark idea of the current work's value. Next, the specialist describes the current work to others in the department, but without revealing any numbers from those past sales (which would introduce anchoring). Every person volunteers an estimate for the current work, and only then does the specialist reveal what related works went for in the past. From there presale estimates are formed, presumably as a combination of information from past sales of related pieces (the anchors) and more up-to-date knowledge of the art piece in question. These anchoring cross-effects between related goods are the primary focus of our study, and discussed further in the next section.

The question of what makes two art pieces similar (i.e., substitutes) is therefore of enormous interest to those in the field. Before one can appraise a piece of art, one must identify past sale precedents, which requires understanding what makes art pieces similar. Only then is it possible to properly analyze anchoring and other biases that can distort prices and sales.

3. REVIEW OF THE LITERATURE

Anchoring

Anchoring is a cognitive bias that has been studied in psychology and behavioral sciences for over 40 years. A comprehensive survey of the anchoring literature is given by Furnham & Boo (2011). The seminal work on anchoring was first authored by Tversky & Kahneman (1974), who conducted experiments such as the one in the introduction to this paper. In another experiment that demonstrated anchoring, those authors gave participants a random number between 0 and 100. Then, the participants were asked to estimate the percentage of African countries in the United Nations. Tversky & Kahneman found that those who initially received a low number underestimated the correct percentage, while those who received a high number overestimated the correct percentage. This showed that a numerical first impression could serve as a starting point (an “anchor”) for quantitative judgment, even if that first impression was entirely arbitrary or irrelevant.

The anchoring effect is extremely complex, and many studies have attempted to understand its nature and implications. For instance, some research shows people formulate estimates more quickly when provided with numbers to anchor on (Strack & Mussweiler). Some studies show that anchoring decreases, but does not altogether vanish, with increased cognitive ability (Bergman et al. 2010).

Within economics, much of the anchoring work focuses on historical market data. Some studies test for anchoring by examining changing prices and demand for unchanging goods (Rajendran & Tellis 1994; Greenleaf 1995; Bokhari & Geltner 2011; Dougal et al. 2012). Much of the anchoring research in economics uses experiments, surveys, or multiple-choice tests to find out how individuals form estimates and judgments in the presence of an anchor (Frykblom & Shogren

2000; Winter 2002; Flachaire & Hollard 2007). Anchoring has been studied in many socioeconomic contexts such as accounting, real estate, the courtroom, public goods, and international finance (Kinney & Uecker 1982; Buccianeri & Minson 2013; Mussweiler 2001; Green et al. 1998; Nianhang & Shinong 2007).

In addition, anchoring has been researched in the context of auctions (Lucking-Reiley et al. 2007; Ku et al. 2006). For example, one bizarre experiment was conducted by Ariely & Prelec (2006). Students were first asked to write down the last two digits of their Social Security number, then bid for various items such as chocolate, computer equipment, or a textbook. The students who had higher digits submitted significantly higher bids, even when explicitly reminded that Social Security numbers are random quantities that carry no inherent meaning. Wolk and Spann (2008) study bidding for online auctions in the presence of an anchor. They found that bidders respond strongly to internalized anchors such as knowledge of past prices for a good, while they respond to external anchors (such as advertiser-suggested bids) just moderately, and only when those numbers are not implausibly high.

Anchoring & Art Auctions

Anchoring is also present in the art market. The literature shows that first numerical impressions do impact prices, auctioneer estimates, and sale volume. Here, we provide an overview of research that studies anchoring in the art market, which is still a highly nascent topic.

To our knowledge, a discussion paper by Beggs & Graddy (2005) is the first to examine anchoring effects (i.e. “reference dependence”) in the art auction market. This paper is described as a working paper for Beggs & Graddy (2009). To identify anchoring, they examine resales within two datasets of Impressionist and Contemporary paintings, which contain not only hammer price but also hedonic characteristics such as artist and medium. Both the Impressionist and Contemporary

art datasets are used in our research, and are described in detail in Section 4. The regression model of Beggs & Graddy (2005) detects anchoring by first controlling for hedonic value and non-hedonic biases on price, then testing for the impact of past price on current price. This model is formalized in Beggs & Graddy (2009), except that this model tests separately for positive (gains) and negative impacts (losses) of anchoring on current price. The authors find strongly significant evidence for anchoring in both Impressionist and Contemporary genres. They find no evidence that positive impacts of anchoring are significantly different from negative ones.

Beggs & Graddy (2009), using the same resale approach and data, dive deeper into the impact of anchoring effects on price, presale estimates, and the probability of a sale. Their model, which we apply and expand, does not test asymmetrically for gains and losses. For price, they find that anchoring effects are stronger for Impressionist art pieces than for Contemporary ones, particularly for items that are resold quickly after a first sale. They also find significant anchoring effects for the presale low estimates, noting that low estimates tend to gravitate toward past price as the anchor. Beggs & Graddy do not find anchoring significantly affects the probability of sale. The anchoring models developed by Beggs & Graddy (2009) have been used in later anchoring research such as Leung et. al (2013), and forms the basis of our own approach. We attempt to replicate selected results from Beggs & Graddy (2009) in Section 6. Beggs & Graddy believe anchoring effects on the sale price may primarily be attributed to the buyers, since buyers primarily determine price, but beyond that treat anchoring as a black box. Graddy et al. (2014) use more data and mostly corroborate the anchoring results of Beggs & Graddy (2009). However, they express more uncertainty about whether anchoring effects should be attributed to buyers, sellers, or auctioneers.

Bruno & Nocera (2008) study how anchoring affects presale estimates using a unique dataset of nearly 1,000 Italian paintings that have been sold at least twice (1985-2006). They regress the range of presale estimates on a multi-level dummy variable for anchoring to account for multiple

past prices (anchors). The authors find significant evidence of anchoring. First, the existence of past prices makes the presale estimate range narrower, presumably because auction houses become more confident in their estimates of the item's value.⁸ Second, Bruno & Nocera find that if a past price exists for an item, the presale estimate range will be more closely centered on actual sale price. Hence, both the bias and variance of the presale estimate range, an estimator of the actual sale price, seem to decrease in the presence of anchors. These findings are consistent with what we heard through interviews, namely, that specialists at auction houses research past sales before formulating estimates.⁹

Even the order in which art pieces are auctioned can beget anchoring effects, as shown in Hong et al. (2015). For the semiannual Auction Week, a two-week auction series held every spring and fall across New York City,¹⁰ Sotheby's and Christie's have a handshake arrangement to alternate who holds their auction first. Using 26 years of Auction Week data and an adapted version of the resale model in Beggs & Graddy (2009), Hong et al. find that average opening sale revenues significantly anchor later sales during the rest of an Auction Week. Specifically, they discover that if more expensive paintings are sold first, then Sotheby's and Christie's will pull in higher total revenue (+21% higher), and more works will sell overall (+11% more sales). They state that their anchoring coefficients are quantitatively comparable to those from Beggs & Graddy (2009). This is the only work we found that does not examine anchoring across resales of the same art piece. However, since they only analyze mean revenues of auction houses and do not consider individual art pieces, their approach cannot be applied in our context.

⁸ Specifically, both the relative and absolute range between low and high estimates.

⁹ Interview, Raphaëlle Benabou.

¹⁰ For more about Auction Week, see Goldstein (2014).

Other behavioral research on art auctions exists, though much of it is more tangential to anchoring. In the art trade, there is the belief that if an art piece goes unsold at auction, it becomes “burned” and will sell for less in the future. To test this quantitatively, Beggs & Graddy (2008) use an even smaller sample of repeat sales from the Impressionist and Contemporary datasets in Beggs & Graddy (2005). The authors find that on average, burned paintings do seem to sell for significantly less (-30%), particularly if they are resold at the same auction house within 2 years (-37%). Whether this is directly due to buyer perceptions of failure, however, is ambiguous. Sentiment, emotion, and mood are also growing areas of research. For instance, Canals-Cerdá (2012) analyze art auctions and seller reputations on eBay, and discover that negative feedback significantly lowers sale price and the probability of sale. Penasse et al. (2014) collect survey data on sentiment toward selected artists in the art community, and find that strong confidence on the part of auction houses and art collectors can predict art returns in the short run. Furthermore, De Silva et al. (2012) examine if weather, a proxy for mood, significantly impacted art auctions at Sotheby’s and Christie’s during the period 1990–2007. They find a weakly significant effect, suggesting that external emotional shocks do affect art auction activity.

In the aforementioned literature, the exact process by which past quantities anchor future ones is treated as a black box: only the impact is noted. This is what we described earlier, and the view of anchoring we adopt in this research.

Contribution of This Research

It is clear that anchoring is pervasive in the art auction market, especially since psychological and behavioral factors seem to be significant drivers of auction activity. However, the research to date (except Hong et al. 2015; see above) has studied anchoring only in the context of resale. This is problematic because as Beggs & Graddy (2009) acknowledge, it is extremely uncommon to

encounter multiple sales of the same artwork. This is further limited by large time gaps between sales, which weaken anchoring effects (Graddy et al. 2014; Hong et al. 2015). Additionally, it is difficult to show resale observations refer to the same art piece, since an artist may create multiple pieces with the same medium, dimensions, and so forth. Beggs & Graddy (2009) manually cross-checked their resale data against presale catalogs.

More importantly, a shared but flawed assumption across much of the aforementioned literature on anchoring is that hedonic quality does not change across auction sales. In talking with Mark Best at Sotheby's, we were surprised to hear how much artwork can deteriorate over time. Prints may tear accidentally, fade under glass, or become punctured, if tacked to the wall for decoration. The canvas of a painting can weaken over time, and must be "relined" with a new canvas attached to the back for extra support. Restoration (often by an unwitting owner) can also harm the value of an art piece: protective glaze must be scraped off, retouched paintings must be scrutinized under ultraviolet light, and so forth. We suspect these factors explain why Beggs & Graddy (2009) find stronger anchoring effects for Impressionist artworks than for Contemporary ones. Paintings in the former category mostly belong to renowned Impressionists artists such as Renoir and Monet, and are orders of magnitude more valuable in both presale estimates and prices (Beggs & Graddy 2009; see Table 1 and 2). Thus, they are probably far better maintained, which better preserves their hedonic quality, allowing past sales to better anchor future ones.

If the hedonic quality of a painting changes across sales, then we can still identify anchoring, given we control for those intertemporal differences. Yet, if we have to control for hedonic differences anyway, why not look at different art pieces altogether? This observation allows us to generalize the anchoring work of Beggs & Graddy (2009) beyond resales of the same good to sales of related (substitute) goods. In all previous literature we are aware of, the anchor is always a previous sale of the same good. However, if we control adequately for quality changes between the anchor

and the current art piece, then we may use sales of a related piece as the anchor instead of a past sale. We introduce this formally in Section 5.

4. DATA

We use three datasets on auction sales in this paper: Impressionist art (1980-1991), Contemporary art (1982-1994), and recent assorted art sales (2006-2016). The Impressionist and Contemporary art datasets have been used extensively in the literature and described in detail elsewhere (Richardson 1992; Beggs & Graddy 1997; Ashenfelter & Graddy 2003; Beggs & Graddy 2009). Both of those datasets are available on the Brandeis academic website of Kathryn Graddy.¹¹ However, the last is a new dataset constructed specifically for this paper.

Impressionist Art (1980-1991)

The Impressionist art dataset (1980-1991) was constructed at Princeton University for the undergraduate thesis of Andrew Richardson under the guidance of Orley Ashenfelter, and covers sales at Christie's and Sotheby's in both London and New York (Richardson 1992). There are well over 16,000 observations of art piece sales, which were compiled by manually scouring presale catalogs. Each observation contains the painting title, the artist name, the sale price and date, the auction house and location, the presale low and high estimates, and hedonic characteristics such as the piece dimensions and the presence of a signature. In-depth attribute details are unavailable in this dataset: for example, dimensions are called "DIM_A" and "DIM_B". The dataset contains 58 major artists whose work is often featured at auction, and among the most frequent are Pablo Picasso (1,155 sales), Pierre Renoir (829 sales), and Raoul Dufy (763 sales). Approximately half the auction sales in this dataset are split between Christie's and Sotheby's, as well as between London and New

¹¹ <http://people.brandeis.edu/~kgraddy/data.html>

York. Table 1 shows summary statistics for selected attributes. 29% of observations in this dataset are bought in, i.e. represent a no-sale. The highest sale in this dataset goes to Vincent Van Gogh's *Portrait of Dr. Gachet* (1890), which netted approximately \$82.5 million on May 15, 1990. Conversely, the lowest sale is a work by Paul Cesar Helleu that went for a mere \$1,888 on March 25, 1986.

Many of these quantities have distributions that are roughly log-normal (i.e., without the log transformation, skewed heavily right), showed in Figure 1. In general, we see very high variation: sales price, for example, reflects both works with record-high sales as well as works that sold for minimal amounts or were bought in. This is because the majority of paintings exhibit middle-market sale price, estimates, size, and so forth, while relatively few reach the highest ranges. The two painting dimensions have the most irregular distributions, particularly in the middle ranges. However, as seen in Figure 2, the large portion of paintings do not tend to be lopsided in their physical dimensions. Finally, we see that auction sales in this dataset have generally risen over time (Figure 3), though there are some years with record numbers of sales.

Contemporary Art (1982-1994)

The Contemporary art dataset represents every Contemporary art piece sold from 1982 to 1994 at Christie's primary King Street location in London, for a total of approximately 4,500 observations (Beggs & Graddy 2005). The dataset was compiled by Kathryn Graddy, who manually examined auction catalogs and sifted through internal data in the archives of Christie's. Similar to the Impressionist dataset, each observation lists the artist, the auction sale price and date, the presale low and high estimates, the lot number, whether or not the item sold, and hedonic characteristics such as the artist and medium. Various currency exchange quantities are included, such as the UK CPI at the time, and monetary quantities are given in thousands of pounds. The data comes with a

STATA .do file, which gives more detailed information on the attributes. Roughly 22.5% of observations in this dataset are bought in. Nearly 600 artists are represented, with Lucio Fontana (157 sales), Karel Appel (151 sales), and Alexander Calder (141 sales) being the most frequent.

Table 2 gives summary statistics for this dataset. As with the Impressionist dataset, and shown in Figure 4, quantitative dimensions such as sale price and size also show roughly a log-normal shape, though auctions sales seem to be more uniform over time (Figure 5). As shown in Figure 6, Impressionist pieces are generally orders of magnitude more expensive than Contemporary pieces. However, Contemporary pieces do tend to be physically larger (Figure 7) and have far more unbalanced dimensions, though as with Impressionist pieces large width and length do seem to scale together (Figure 8).

Assorted Art (2006-2015)

A major contribution of this research is the construction of a large dataset of 500,000 recent auctions sales of assorted artworks (2006-2015). To do this, we wrote a Python program to scrape recent listings on the Blouin Art Sales Index, a frequently updated online database of art auction sales (Blouin Art Sales Index). The Blouin Art Sales Index was suggested to us by Bobray Bordelon, a economics & finance librarian at Princeton University. We ran our program for 10 nonstop days in December 2015. The motivation behind collecting and using a new dataset is threefold. First, the time gaps between auction sales in this dataset are much shorter, compared to our other datasets. The average time gap between sales in the Impressionist and Contemporary art datasets are 5.57 and 0.98 days, respectively, while the average gap here is only 0.0072 days – indicating most sales occur on the same day. This is more conducive to studying anchoring. Second, this dataset consists of a very wide range of artists and artistic styles, while the Impressionist and Contemporary datasets are more limited in their artistic scope. More variety allows us to identify more substitutes, and better

test our measures of substitution. Finally, as mentioned earlier, sales in this dataset are more recent and could better reflect the current auction climate.

The full, raw dataset consists of approximately 500,000 observations (paintings and non-paintings), covering primarily 19th and 20th century art. It also includes some works from earlier time periods, going back to 1000 CE for works by Song Dynasty artist Yi Yuanji. Nearly 90,000 artists are included, with the best represented being Pablo Picasso (3,440 sales), Andy Warhol (2,573 sales), and Salvador Dali (1,508 sales). However, we did not identify any resales. We only examine paintings, of which there are approximately 250,000 observations. The most expensive sale is an untitled crayon work by Cy Twombly (1928-2001), which went for \$70.5 million at Sotheby's in NYC in November 2015. The artists whose works sell for the most, on average, include Kazimir Malevich of the Suprematist movement (1879-1935), the Abstract Expressionist Mark Rothko (1903-1970), Vincent Van Gogh (1853-1890), and also Song Dynasty artists such as Emperor Huizong (1082-1135) and Yi Yuanji. As before, sale prices and other quantitative characteristics seem to follow a roughly log-normal distribution (Figures 9-12). Most of the paintings in this dataset sell for low 5 or 6 figure sums, while only a minority sell for higher figures reflected in the gradually diminishing right tail. It is clear that artists who sell more works through auction will enjoy higher revenue on average (regression slope: 0.52. p-val: <2E-16), as they become better-known in auction circles through higher representation.

Each observation in this new dataset includes the artwork title, the artist, artwork category as described by the auction house, a textual description of the materials, the lot number, sale date, auction house, and the USD sale price. Information on the materials were given in the form of unstructured text data, which might be attributed to freeform data entry on the part of Blouin. Hence, simple keyword extraction was used to extract hedonic characteristics such as height and width; more

sophisticated textual extraction methods should be employed in future work. Some summary statistics for the full raw dataset are provided in Table 3.

5. METHODOLOGY

Detecting Anchoring Across Sales of the Same Good

A two-stage regression model for detecting anchoring is specified in Beggs & Graddy (2009). The same model is used to detect anchoring effects in later papers such as Hong et al. (2015), and in general, may be estimated for goods that exhibit unchanging hedonic quality over time. That hedonic quality for artwork would not change is thus a key assumption of their work. Intuitively, their model identifies anchoring by looking at two sales of an item, say a painting, at different points in time. After controlling for hedonic value and non-hedonic price biases at all time points, current price may be regressed on past price. That impact of past price is identified as the anchoring effect.

Hedonic regressions are commonly used to estimate demand for highly heterogeneous items such as art, wine, and real estate as a function of their constituent attributes (Edmonds 1984; Costanigro et al. 2007). For example, the value of a painting may depend on its dimensions and authenticity, while a bottle of wine may be appraised based on its age and where it was grown. In the first stage of the model, Beggs & Graddy (2009) regress the sale prices $P \in R^{[n,1]}$ of n resold paintings¹² on their k hedonic and temporal variables $X \in R^{[n,(k+1)]}$ ¹³, while also including temporal effects $\delta_t \in R^{[n,1]}$. This yields a hedonic price prediction $\pi_t \in R^{[n,1]}$ for each observation of a

¹² The data here consists of all sale observations that correspond to the set of paintings that have been resold multiple times. Beggs & Graddy have painstakingly verified each observation against presale catalogs. Because those are not available, in our replication work we make the assumption that duplicate observations in their Impressionist and Contemporary data refer to multiple sales of the same item.

¹³ Each sale observation includes the auction date, hence the $k + 1$ dimensions in the data.

painting sale. The resulting equation, which both Beggs & Graddy and we use, is given below. We denote the current period as t and the previous period as $t - 1$.

$$\pi_t = \mathbf{X}\mathbf{B} + \delta_t$$

For our replication work on the Impressionist and Contemporary datasets, we use the same hedonic variables that Beggs & Graddy used. For Impressionist art this includes painting date, length, width, medium of the artwork, indicators of authenticity (signed, monogrammed, stamped), and artist.¹⁴ For Contemporary art this includes painting date, length, width, medium, and artist. The temporal effects are modelled by half-year time dummies.

In the same manner as Beggs & Graddy, we use the natural log of prices and hedonic price predictions, which allows us to interpret the regression results as relative effects (percent changes). For unsold items, we proxy value with 80% of the low estimate as they do (see Section 4). It is important to note that hedonic price predictions for a single painting $\pi_t, t \in \{1, 2, 3 \dots\}$ may vary with respect to time, since these are estimated based on prices for the painting at different times. These prices reflect demand for art, which may change over time. The k hedonic variables, however, are assumed to remain constant across sales.

In the second stage of the model, Beggs & Graddy specify the following regression – for each unique painting – in order to separate out anchoring from other effects. Their equation (which we also use) is given below.

¹⁴ Besides the artist’s hand-drawn signature, monograms and stamps may also be used to mark an artwork as authentic. A monogram is a stylized symbol of the artist (sometimes an artistic rendering of their initials) that may be put onto a work. Artists may also have a custom stamp for their work, which may include their printed name.

$$\omega = a_0 + a_1\pi_t + a_2(P_{t-1} - \pi_t) + a_3(P_{t-1} - \pi_{t-1})$$

- ω is the response variable. Beggs and Graddy fit several regressions where the response ω represents either the hammer price, the presale estimator, or an indicator for whether the item sells, which involves a probit transformation. In our replication work, we only examine ω as hammer price.
- π_t is the current hedonic valuation of bidders, i.e. the hedonic price prediction in the current period t . To detect anchoring effects, hedonic valuations π_t must be controlled for. Otherwise, one would not be able to separate hedonic and non-hedonic influences in the current period.
- $(P_{t-1} - \pi_t)$ identifies the anchoring effect. This specifies how past hammer price P_{t-1} , the anchor, differs from π_t , the current hedonic valuations of bidders. Since we have already controlled for the latter, as well as non-hedonic components of past price that could possibly affect current price – see $(P_{t-1} - \pi_{t-1})$ below – this term measures the extent to which past price irrelevantly impacts current price.
- $(P_{t-1} - \pi_{t-1})$ is the past residual, i.e. non-hedonic inputs into past price. This controls for any other components of past price that could, conceivably, affect current price.¹⁵ For example, past price might be a function of unobservable bidder excitement for the work. This would not only drive up past price, but could also drive up current price. Hence, we control for such non-hedonic price biases in this term.

¹⁵ One example would be a work's reputation, which could drive up both past and current price. This component of quality, however, cannot be modeled as another hedonic attribute like size, medium, etc., since reputation is not an intrinsic property of an art piece.

In the case of the dependent variable P_t (i.e., when ω is hammer price), we see that those non-hedonic inputs, usually captured by $(P_t - \pi_t)$, would instead be contained in the residuals. One should also note that because hedonic prices may vary over time, $(P_{t-1} - \pi_t)$ is distinct from $(P_{t-1} - \pi_{t-1})$. Additionally, the intercept α_0 represents the value of ω in the absence of other predictors. For example, if ω represents hammer (sale) price, then a high intercept could suggest a high average price for paintings across the given market.

Identifying Substitutes

As we discussed earlier and as Beggs & Graddy (2009) note, it is extremely difficult to track down multiple sales of the same item. The same art piece can become a drastically different hedonic object within its lifetime due to deterioration or restoration. Also, many years or decades may elapse between sales of the same art piece – far too long to reliably measure anchoring biases.

It is reasonable to believe that buyers, when bidding on an artwork, make judgments based not only on that piece's past sales, but also what similar pieces went for. This allows for more versatile approach to identifying anchoring effects, or if between different goods, cross-effects, as long as we control adequately for hedonic differences. Before measuring similarity, however, we must identify related pieces for the current good, since many pieces may be entirely irrelevant. Thus, to identify substitutes for the sale of an art piece, we search through our data for past sales of other pieces with the same artist, medium, and signs of authenticity. We also omit observations where no substitutes were found. This gives us a list of related sales to consider for the current good. Only then may we proceed to measure similarity and test for anchoring cross-effects, as described below.

Detecting Anchoring Across Substitutes

Here, we build on the two-stage regression model presented earlier. Suppose, as before, we have our same design matrix $\mathbf{X} \in R^{[n,k+1]}$ and our hammer prices $P_t \in R^{[n,1]}$. We run the first hedonic regression as before, except that we are not concerned specifically with resale.

$$\pi = \mathbf{X}\mathbf{B} + \delta_t$$

We next depart from the original model. Denote the sale observation of our current good as x_c and the sale observation of a single substitute as x_s , such that the hedonic predictions estimated above are π_c, π_s , and P_c, P_s are the respective hammer prices. Then our second regression is:

$$\omega_c = b_0 + b_1\pi_c + b_2(P_s - \pi_c) + b_3(P_s - \pi_s) + b_4Q$$

Here, the subscripts for the past and current sales $t - 1$ and t are replaced by subscripts for the substitute s and current good c . In other words, instead of considering a current sale and past sale of the same painting (which corresponds to hedonic matrices \mathbf{X}_t and \mathbf{X}_{t-1}), we consider the current sale of the painting and the past sale of a substitute (thus replacing \mathbf{X}_t and \mathbf{X}_{t-1} with \mathbf{X}_c and \mathbf{X}_s). The previous regression model assumed that there was no unobserved quality changes in the painting across sales, such that $\mathbf{X}_t = \mathbf{X}_{t-1} = \mathbf{X}$. Hedonic prices π_t could still change due to time-dependent demand. However, in this generalized framework, we assume that characteristics do differ across goods, such that $\mathbf{X}_c \neq \mathbf{X}_s$. Thus, we control for those hedonic differences by including a measure of substitution Q in our regression model, which may be constructed from either π or \mathbf{X} . This allows us identify anchoring effects in $(P_s - \pi_c)$, as before.

What if a painting has multiple substitutes - the multivariate case? Let a given good x_c have a vector of substitutes $X_s = \{x_{s1}, x_{s2}, \dots, x_{sd}\}$. We can write:

$$w_c = b_1\pi_c + b_{i2}(P_{RS} - \pi_c) + b_{i3}(P_{RS} - \pi_{RS}) + b_3Q$$

$$P_{RS} = \frac{1}{d} \sum_{i=1}^d P_{si} \quad \pi_{RS} = \frac{1}{d} \sum_{i=1}^d \pi_{si}$$

Two goods c_1 and c_2 may have different numbers of substitutes d_1, d_2 , which is why for our regression model it is necessary to aggregate them into a “representative substitute” via a summarizing function such as the mean or maximum (we use the former). This produces a representative price P_{RS} and hedonic prediction π_{RS} . Hence, this multivariate regression tests whether there exists anchoring effects for the sale of the current good with respect to the “average” substitute - a conglomerate of all substitutes together. The marginal effect of Q on w_c , then, represents how strongly the dependent variable (such as price) is affected by our quality of substitution. The measure of substitution Q may be calculated from the multivariate π or \mathbf{X} . Finally, if we omit Q and use the current good’s previous sale instead of its average substitute, this reduces to the original model of Beggs & Graddy.

Measuring Substitution Across Art Pieces

In this paper, we experiment with two simple measures of substitution Q_1 and Q_2 between art pieces. The first is derived from the hedonic predictions, and represents unobserved quality differences. The second is formulated from our interviews with art experts and specialists. These measure do

not and cannot perfectly capture differences between artworks, but they do provide a starting point for quantitatively measuring art similarity.

Measure #1: Second Moment of Hedonic Price Differences

Consider the current good x_c and d substitute art pieces $X_s = \{x_{s1}, x_{s2}, \dots, x_{sd}\}$, which are aggregated into an “average substitute.” One way we can measure substitution is by examining how much, on average, the hedonic price predictions of the substitutes differ from that of the current good. This corresponds to hedonic value differences that are not captured in our hedonic regression model. It is not, however, sufficient to just capture the average magnitude of these hedonic differences. If some substitutes have hedonic values below that of the current good, and some have hedonic values above, then our “average substitute” may have the same hedonic value as the current good, indicating perfect substitution! It is preferable to have uniformly substitutable goods rather than a polarized mix of good substitutes and bad substitutes. Thus, we use the following measure of similarity, which is essentially a second moment estimator about the current good’s hedonic prediction¹⁶:

$$Q_1 = -\log \frac{1}{d} \sum_{i=1}^d (\pi_c - \pi_{si})^2$$

This measure captures both the hedonic differences $(\pi_c - \pi_{si})$ as well as the variability of such differences (indicated in the squared term). As described before, we work in logs for relative

¹⁶ We do not subtract the other term $E[X = (\pi_c - \pi_s)]^2$ typically used in calculating variance $V[X] = E[X^2] - E[X]^2$, since that (squared) mean term reflects the absolute hedonic differences $X = (\pi_c - \pi_s)$. Our measure represents $E[X^2]$, the summation of $V[X]$ and $E[X]^2$, and this is how we account for both spread and magnitude.

effects, and the negative sign allows a higher Q_1 (smaller hedonic differences and lower variation in those differences) to correspond to higher substitutability.

Measure #2: Domain Knowledge of Similarity

For our second measure of substitution, we draw upon domain knowledge from our expert interviews. We found the most commonly mentioned and important determinants of artwork similarity (substitutability) were artist, medium, signs of authenticity, size of the artwork, and how recently the artwork was auctioned. The opinions of our interviewees on more complex factors, such as subject matter and artistic style, seemed to be mixed: some said these were key to measuring similarity between pieces, while others did not believe they were as relevant¹⁷. One thing we were surprised to learn about size in particular was that its importance in determining similarity varies at different price points. For the lower and middle price ranges, people usually purchase art as a decoration, and usually purchase pieces of similar sizes that can be displayed side-by-side. As price increases, people tend to value artwork more as an investment, and so the importance of size in determining similarity decreases.

To capture these anecdotal observations about art similarity, we present a second measure of substitution between a current piece x_c and its substitutes $X_s = \{x_{s1}, x_{s2}, \dots, x_{sd}\}$. This measure of substitution depends on size S_i , hedonic price π_i , and auction date t_i .

$$Q_2 = -\log \frac{1}{d} \sum_{i=1}^d \left[\frac{(S_c - S_{si})^2}{1 + (\pi_c + \pi_{si})} + \Delta days(t_c, t_{si}) \right]$$

¹⁷ For further discussion: <http://www.jstor.org/stable/pdf/20715780.pdf?acceptTC=true>

Greater differences in size between the current good and its substitutes correspond to decreased similarity and thus decreased substitutability¹⁸. However, this effect decreases as the hedonic values of the current good or its substitutes rise. Consistent with the anchoring literature discussed earlier, the farther the anchor (the sale of a substitute) is in the past, the weaker the anchoring effect is. Note that we use hedonic prices to indicate increasing value. This is because P_{si} and P_c can reflect not only π_{si} and π_c but also non-hedonic determinants of price, and furthermore, P_c is the dependent variable to be determined in our main anchoring regression. No possible past anchoring effects are considered with the hedonic prices here: we assume buyers are myopic, as captured in the time difference effect, and assess similarity primarily based on hedonic factors.

The hedonic price predictions enter into both Q_1 and Q_2 , but the two measures are considerably different. Hedonic differences are the primary focus of Q_1 , while for Q_2 they only serve the implicit purpose of scaling size. The measure Q_2 also includes temporal differences, which do not explicitly enter into the hedonic regressions. Hence, we may consider Q_1 a very broad measure of hedonic similarity, while Q_2 is a narrower measure formulated from domain knowledge. It is surprising that these two divergent measures yield similar evidence of anchoring effects, and given that we apply these broadly, detect anchoring effects at all. We show this in the next section.

¹⁸ We add one in the denominator of the first term to protect against results exploding toward infinity. Empirically, however, this is negligible compared to the magnitude of our hedonic prices.

6. RESULTS

We begin by fitting a hedonic regression model to all three datasets. Next, we replicate the original anchoring findings of Beggs & Graddy (2009) for their two Impressionist and Contemporary datasets. Then, we apply their same model to our new dataset of assorted art sales. Finally, we run our anchoring cross-effects regression on all three datasets. As a final experiment to ensure the robustness of our model, we also run our cross-effects regressions on three selected pairs of artists.

Hedonic Regressions

We begin by fitting a hedonic regression model to our three datasets in order to construct a measure of artistic value for each piece. For Impressionist Art, as Beggs & Graddy (2009) did, we fit separate hedonic regressions for Impressionist art depending on whether it was auctioned in NYC or London (due to currency differences). We then recombine the regression results and renormalize for the currency differences. Tables 4 through 7 below show the results of the hedonic predictions.

Overall, hedonic characteristics such as the painting dimensions, the presence of a signature, medium, and artist and time effects (both omitted for brevity; both significant) have a significant impact on the sale price of the painting. It is surprising that a painting's date of creation is generally not significant, which may be explained by the importance of artist variables. For Impressionist Art and Contemporary Art, much of the variation in price is explained by our regression model, indicated by generally high R^2 values. For our new dataset, however, the R^2 value is extremely low although variables are significant. This is to be expected: our dataset covers a very large variety of paintings, and so we should see very high variance across prices in our regression model (though far lower bias, as indicated by our highly significant hedonic variables). The F-statistic is extremely

significant in all cases, which shows that our regression variables are relevant as a whole. In general, the most impactful variables are those for the art medium and the dimensions. This may be attributed to large pieces and pieces from specialized mediums selling for more, as indicated by large, significant coefficients for certain mediums and not for others. Despite a high R^2 value for Impressionist art, the intercept is highly significant. This suggests that non-hedonic factors likely play a large role in determining value for Impressionist pieces, which is understandable given the relatively more pronounced age and renown of those works. Additionally, the presence of a signature specifically, rather than other signs of authenticity such as a monogram, generally seems to be more important to determining hedonic value. We do note that signature is more significant for Impressionist art auctioned in NYC, while medium is more significant factor for that auctioned in London. As a further note, regressing on only artist and time dummies corresponds to a reduction in R^2 in the Impressionist and Contemporary datasets, as noted in Beggs & Graddy (regressions not included). Generally, it is clear that hedonic factors such as size and medium do play a large role in determining value for the works we examine.

Replicating Beggs & Graddy (2009)

Here, we attempt to replicate some of the work of Beggs & Graddy (2009), who analyze the same Impressionist and Contemporary datasets to test whether the first sale of a painting produces an anchoring effect on its later sales. In this research we only consider sale price, but Beggs & Graddy did also run regressions for presale estimate and the probability of sale. As mentioned earlier, they identified resale observations in the Impressionist and Contemporary datasets by cross-checking them against presale catalogs, which we do not have. Hence, we make the assumption that duplicate hedonic observations refer to multiple sales of the same item, which is clearly too lenient since even different art pieces may have the same characteristics. However, as discussed below, we are still able

to reproduce their general findings even without knowing which exact observations were originally used.

Tables 8 and 9 show our results, alongside the original tables (Tables 8b and 9b) of Beggs & Graddy. We were able to reproduce the discovery of highly significant anchoring effects in Impressionist art, and the more weakly significant effects in Contemporary art. However, our anchoring coefficients are not nearly as large as theirs. For Impressionist art, a 10% increase in the difference between past price and current hedonic prediction (anchoring) only corresponds to a 1.7% increase in the current sale price (Beggs & Graddy: 6.2-8.5%), while for Contemporary art the same 10% increase only corresponds to a 1.3% predicted increase in current sale price (Beggs & Graddy: 5%). On the other hand, our regressions show that the residuals from past price (unobserved inputs into past price, such as the thrill of bidding) are much stronger than anchoring in the case of Impressionist art (5% increase for Impressionist), which differs from the results of Beggs & Graddy. One explanation could be that the reputation of Impressionist pieces grows over time as these pieces trade ownership across collectors and museums, so that reputation effects tend to drive up buyer demand beyond hedonic value or even past price anchors. This would be captured in the past residuals.

We do find a weaker impact of the past residuals on current price in the case of Contemporary art, a result which is shared by Beggs & Graddy. They attribute this to the heavy time-dependent variation in prices in this Contemporary art dataset (not shown here), which suggests past prices would not serve as meaningful anchors. We also replicated their discovery of relatively small time coefficients, particularly for Contemporary art. This indicates that the specific number of months between sales seems to not be a major influence in determining the current price of a work (at least in the context of resale). Finally, our anchoring regressions also share the very high R^2 and

adjusted R^2 values of Beggs & Graddy, indicating that much of the variation in hammer prices is explained by this model.

In addition to Impressionist and Contemporary art, we also ran Beggs & Graddy’s original anchoring regression on our new dataset of recent assorted painting sales (Table 10). Because our dataset does not seem to have identifiable multiple sales of the same item, we used the average substitute of an item (constructed as described in our methodology) instead of a past sale as a point of comparison for the anchoring effect. This reduces to running our regression for anchoring cross-effects without the measure of substitution, i.e. the control term Q . Despite this simplistic approach that does not control for substitution, we can still discover some insight.

We discovered strong and highly significant anchoring effects in this context (5.9% increase), although, just as in our findings for Contemporary art, the residual from past price seemed to be relatively unimportant. This preliminary evidence suggests, although we have not controlled for substitution yet, anchoring is at work in this dataset. The R^2 value is much lower due to the very high variation in our data, but the F-statistic is extremely high indicating that our regression variables do seem to be relevant. As in both the original results of Beggs & Graddy and our replication of their work, we found that time effects seemed to be relatively weak, though they are highly significant. Hence, our next Q_1 and Q_2 regressions, designed to control for substitution, should yield more precise and accurate insight into anchoring effects.

Anchoring Cross-effects for Impressionist, Contemporary, & Assorted Art

In this section, we describe our regression results that control for substitution. We employ our measures Q_1, Q_2 which describe how similar a current good is to its “average substitute,” a representative good constructed from all other identified substitutes. As discussed earlier, the

measure Q_1 represents the (log) second moment of hedonic prices of substitutes about that of the current good. This allows Q_1 to capture both the spread of hedonic differences as well as the magnitude of those differences. Conversely, the variable Q_2 measures similarity across art pieces according to insight from our interviews, and represents the importance of size, price, and time effects.

Q1: Second Moment of Hedonic Price Differences

$$\omega_c = b_0 + b_1\pi_c + b_2(P_s - \pi_c) + b_3(P_s - \pi_s) + b_4 \left[Q_1 = -\log \frac{1}{d} \sum_{i=1}^d (\pi_c - \pi_{si})^2 \right]$$

Tables 11 through 13 show the results of running the above regression for our Impressionist, Contemporary, and assorted art datasets. There are several results particularly worth noting here.

First, after controlling for substitution, anchoring effects lose significance for Contemporary art, and only retain significance for Impressionist and recent assorted art. It is possible that anchoring is no longer significant for Contemporary art because it tends to be especially diverse. For instance, based on our interviews, we learned that over time the boundaries between art mediums have become finer as mediums are combined in “mixed media” formats. These unusual Contemporary artworks do seem to fetch competitive sums at auction.¹⁹ As a result, a Contemporary artwork to be auctioned may lack obvious precedents for the determination of its value. Thus, current price will be determined by the piece’s own characteristics as well as unobserved inputs into price such as general demand for Contemporary art. This seems to be confirmed by the highly significant hedonic

¹⁹ For instance, Matt Lamb’s “Figures” fetched \$24K at Christie’s, London on June 22, 2010. (Christie’s Lotfinder)

price prediction, as well as the highly significant, non-negative substitute residual. The lack of anchoring effects for Contemporary art goes hand-in-hand with the insignificance of the substitution measure, which indicates that price does not seem to be determined by substitution phenomena.

On the other hand, anchoring effects and substitution are significant for Impressionist art. In general, Impressionist works tend to have better-defined mediums such as oil and watercolor, which likely makes it easier to identify similar sale precedents. Hence, anchoring is significant (though not particularly strong): a 10% gap between the substitute's sale price and the current piece's hedonic value corresponds to 0.3% change in the current price. More impactful is the substitute sale residual, which exhibits a highly significant and stronger coefficient. We believe this may be due to reputation effects. Impressionist pieces, which tend to be much older, scarcer, and well-known, seem to be purchased more as an investment rather than a decoration (Bittar n.d.; Beggs & Graddy 2009, see price indices). Hence, we would expect their non-hedonic value to rise as their provenance and auction history becomes more and more illustrious over time. As a result, the sale prices of these pieces begin to reflect their historical reputation more than their hedonic value. Historical reputation may be tied to general attributes such as the artist and provenance, which may of course be shared by multiple works. Thus, we should expect buyers of a piece to draw upon price signals from sales of similarly reputable works, which are captured in the significant substitute residual here.

Finally, our assorted art dataset exhibits strong and highly significant anchoring effects. We believe this is partially due to the far smaller time gaps between sales, which as discussed in our literature review, seem to be more conducive to anchoring. However, in addition to containing both Impressionist and Contemporary works, the assorted art dataset is much larger and diverse. This means that for a given art piece, it may be possible to find closer substitutes, which is suggested here by the highly significant coefficient for the substitution measure.

Time effects (months since last sale) have small coefficients across the board, and are insignificant for Impressionist art. From our interviews, we learned that buyers of art tend to be myopic, in that they do not tend to internalize the full range of historical prices (only recent prices, e.g. anchoring). This seems to be confirmed by the price indices and small time coefficients in Beggs & Graddy (2009), which suggest that prices can climb up dramatically over long stretches of time. Here, for assorted art, a 100 month (8.3 year) time interval between sales only corresponds to an 8% decrease in the current price. For Contemporary art, the same gap corresponds to a 5% decrease, while for Impressionist art the association is almost nonexistent. Nevertheless, the fact Contemporary and assorted art have somewhat larger coefficients suggest that smaller time intervals between sales can counteract buyer nearsightedness.

The R^2 values are generally in line with our results for the original anchoring regression: there is much less variation in the Impressionist and Contemporary datasets than in our assorted art one. High F-statistics confirm the relevance of our variables, as before.

Q2: Domain Knowledge of Similarity

$$\omega_c = b_1\pi_c + b_2(P_s - \pi_c) + b_3(P_s - \pi_s) + b_4 \left[Q_2 = -\log \frac{1}{d} \sum_{i=1}^d \left(\frac{(S_c - S_{si})^2}{1 + (\pi_c + \pi_{si})} + \Delta days(t_c, t_{si}) \right) \right]$$

Tables 14 through 16 show the results of using Q_2 as a control for substitution. Even though the design and focus of Q_2 is considerably different from those of Q_1 , we reach similar results, which further confirms our overall discovery of anchoring effects.

First, as in the Q_1 case, anchoring is significant for Impressionist and assorted art, but insignificant for Contemporary art. This is what we found in the Q_1 case, which is surprising since Q_2 only focuses on a couple of key variables (size, time) that were carefully suggested by our experts. Nevertheless, anchoring coefficients are weaker across the board, which suggests that Q_1 might be a more stringent control.

Although Q_2 becomes a significant predictor of price across all three datasets, the impact of Q_2 on price is mixed, compared to the Q_1 case. For Impressionist art, Q_2 has a larger coefficient (in absolute value) than Q_1 did; on the other hand, for Contemporary art Q_2 is weaker. This suggests that when buyers of a given art piece research sales of comparable pieces, they base their hedonic value judgments primarily on size, and do not delve into sales too far in the past. For Contemporary art, we see that Q_2 is significant as opposed to the Q_1 case, indicating that domain knowledge of artistic similarity does seem to be legitimately helpful in predicting price. This is consistent with our discussion of Contemporary art pieces in the Q_1 case, and the lower R^2 for Impressionist art in our hedonic regression model (Tables 5 and 6). Compared to Impressionist pieces, Contemporary art

pieces do seem to generally have a more limited provenance and history, and so derive much of their value from hedonic factors. That said, here the quality of substitution Q_2 is still comparatively stronger for Impressionist art than for Contemporary art. This is because time effects are stronger for Contemporary art than for Impressionist art: some of the predictive ability of Q_2 is sapped by the significant time coefficient also included in the regression (-0.05039). Prices for Impressionist pieces generally seem to be somewhat resistant to long intervals between sales, as indicated by the lower and nonsignificant time coefficient (0.8457).

While both Q_1 and Q_2 are significant for assorted art, Q_2 is a hugely more impactful measure of substitution: a 10% improvement in substitution quality corresponds to a 3.0% increase in sales price. Focusing on size and time duration seems to be far more effective as a control, since for this assorted art dataset, it is possible that Q_1 (as a more general hedonic measure of similarity) may capture too much noise to be helpful for measuring substitution. Nevertheless, regardless of which measure we use, we are still accounting for a lot of variation in the data, as evidenced by moderate-low R^2 values.

Three Experiments

Hadley Newton (formerly of Sotheby's) helped us to sift through our assorted art dataset for pairs of artists to compare. This includes Joan Miro & Salvador Dali, Pablo Picasso & Marc Chagall, and Edvard Munch & Henri de Toulouse-Lautrec. The first two artist pairs produced artistically similar work, and so should be expected to exhibit anchoring cross-effects. However, while they were historically similar (as explained below), Munch and Toulouse-Lautrec had fairly divergent artistic styles. Thus, they should not be expected to display anchoring effects. This allows us to ensure the robustness of our model, specifically, that it does not falsely detect anchoring in light of non-artistic similarity.

In this section, we run our Q_1 and Q_2 regressions on those three pairs of artists for comparison. Specifically, we test whether one artist serves as an anchor for the other, and vice-versa: an artist may not be their own anchor. This allow us directly test our anchoring regressions on known substitutes, and evaluate our results more thoroughly.

Substitution Experiment #1:

Joan Miro (1893-1983) & Salvador Dali (1904-1989)

Miro and Dali were two of the most iconic Spanish Surrealists, and created pieces that are at once abstract, imaginative, and occasionally absurd. The work of Miro draws heavily on well-defined geometric shapes and lines, filled with bright colors and political overtones (Danto n.d.). Dali's work, which ranges from bizarre scenes to nightmarish landscapes, is dreamlike yet shows an appreciation for the realistic nature of classical and Renaissance art ("Salvador Dali Biography" n.d.). Overall, their artistic styles only seem to be moderately similar, given Miro's focus on geometry and Dali's emphasis on realism. That said, works by both Surrealists have sold at auction for 6- and 7-figure

sums, and the two Surrealists are sometimes paired together at museum and gallery exhibitions (Galerie Michael n.d.). We were also told that works by these two artists tend to also attract the same kinds of clients.²⁰

Tables 18 and 19 show the anchoring regression results for Miro and Dali (in our assorted art dataset) with our respective controls Q_1 and Q_2 . First, it is notable that anchoring is entirely insignificant with Q_1 , but gains a highly significant p-value and becomes much stronger when Q_2 is used. However, the substitution measure in the Q_1 case is highly significant and impactful while that in the Q_2 case is not. This relationship between the anchoring effect and the measure of substitution in this dataset suggests that Q_2 is not an appropriate control, which would indicate that the anchoring effects in the Q_2 case may be illusory. Either way, there is a large amount of variation that our model cannot explain, as evidenced by our low R^2 values. It is also surprising that the hedonic price predictions are relatively weak and insignificant, and that unobserved inputs into the substitute's price (the substitute's residual) are impactful and highly significant. Even further, the intercept term is very large and significant. Together, all these observations suggest that there are other influential inputs at work (in the error term) beyond our identified variables. Thus, a substitution control better tailored to Dali and Miro might be required in this scenario, as anchoring effects between Dali and Miro pieces are inconclusive here. However, this experiment does highlight the importance of controlling for substitution to prevent anchoring effects from being falsely detected.

As confirmed by our earlier regressions, time effects are significant and influential for both Dali and Miro who (as Surrealists) may be classified as Contemporary artists. Despite the variation in our data, high F-statistics in both the Q_1 and Q_2 cases ensures the relevance of our model.

²⁰ Interview, Hadley Newton.

However, we cannot say there are conclusive anchoring effects between Dali and Miro - which makes sense given their somewhat divergent styles, even within the larger Surrealist movement.

Substitution Experiment #2:

Pablo Picasso (1881-1973) & Marc Chagall (1887-1985)

Picasso and Chagall, former friends turned opponents and two of the best-known Contemporary artists, spanned multiple artistic traditions (“Pablo Picasso Paintings” n.d.). The works of Picasso range from Cubist nude portraits to Neoclassical and Surrealist paintings, and frequently depict real life in abstract forms. Chagall drew upon a variety of movements including Surrealism, Cubism, and Expressionism for his works, many of which focus on scenes from Eastern Europe. Overall, the styles of Picasso and Chagall seem to be relatively similar, and some research even suggests that price indices for those two artists tend to move together (Finkelstein 2002). The two painters are frequently featured together at exhibitions (Opera Gallery 2009; Brandstatter 2015), more often than Dali and Miro are, and the works of Picasso and Chagall often fetch 7- and even 8-figure sums at auction.

Overall, for this comparison we see similar results whether we use Q_1 or Q_2 (Tables 20 and 21). Anchoring is strong and significant in this comparison between Picasso and Chagall. It is also associated with the presence of significant control terms this time, which suggests that even after controlling for substitution, anchoring is still very much at play. Also, the coefficients are large: if the price of the substitute is 10% higher than the hedonic value of the current good, we should expect to see a 15% increase in the current good’s price due to anchoring (if we use Q_1 ; 25% increase if we use Q_2). In the Q_2 case, the intercept is also much stronger and highly significant, compared to that of Q_1 . There is a lot of variation in the data, as evidenced by the extremely low R^2 values. This indicates that for Picasso and Chagall, prices for their artwork are probably affected by other

influences, and that our two measures of substitution, although significant and generally a step in the right direction, could be improved. Time effects are fairly small, and do not seem to affect price much if at all.

While anchoring effects were less conclusive for Miro and Dali than for Picasso and Chagall, we do see here highly significant evidence of strong anchoring cross-effects, which makes sense given their artistic similarity. Thus, we should expect prices for one artist's works to noticeably impact those for the other's pieces.

Substitution Experiment #3:

Edvard Munch (1863-1944) & Henri de Toulouse-Lautrec (1864-1901)

We were suggested to pair together Munch and Toulouse-Lautrec because, as contemporaries in Europe, they met with similar levels of economic and critical success during their lifetimes. However, their artistic styles seem to somewhat differ. Munch, a Norwegian artist associated with Expressionism and Symbolism, is known for the intensely psychological and brooding themes he imbued into his paintings and prints (“Edvard Munch Biography” n.d.). On the other hand, Toulouse-Lautrec is known for his Post-Impressionist, drawing-like depictions of people, often those from lower-class, urban environments (“Henri de Toulouse-Lautrec Biography” n.d.). It seems that Munch and Toulouse-Lautrec are featured together less frequently: a quick Google search only turns up a 1965 exhibition at the Metropolitan Museum of Art (“Metropolitan Museum” 1965). Nevertheless, both artists pull in hefty sums: Toulouse-Lautrec’s work “Au Lit: Le Baiser” fetched \$16.3 million at Sotheby’s in early 2015, and Munch’s Internet-famous “The Scream” sold for nearly \$120 million at Sotheby’s in 2012 (Ellis-Petersen 2015; Vogel 2012).

Tables 22 and 23 show the respective Q_1 and Q_2 anchoring regression results for Munch and Toulouse-Lautrec in our assorted art dataset. As expected, no significant or strong anchoring effects appear this time, regardless of whether we use Q_1 or Q_2 . Even if the two artists did enjoy comparable success during their concurrent lifetimes, which would be reflected in similar prices, their artistic styles seem to be too different to permit anchoring cross-effects. Our measure of substitution is insignificant in both the Q_1, Q_2 cases, which seems to further suggest that Munch and Toulouse-Lautrec are not particularly close hedonic substitutes. That said, Q_2 has a somewhat larger coefficient, which could be due to its inclusion of near-significant time effects (p-value: 5.38). The R^2 value indicates that we do seem to explain more variation in the data than we did for other artist

pairs, but relatively low F-statistics confirms that anchoring is not at play between the Munch/Toulouse-Lautrec pair. In fact, the only significant variable is the hedonic price prediction. Hence, we do not find any evidence of anchoring between Munch and Toulouse-Lautrec – which is understandable, given their relatively divergent artistic styles. This is encouraging, because it means our model is relatively robust and does not detect anchoring too leniently.

7. CONCLUSION AND FUTURE DIRECTIONS

If a Picasso painting fetches a high sum at auction, will a similar painting by Dali also sell for more? In this research, we set out to examine the existence of these anchoring cross-effects, building upon the original anchoring work of Beggs & Graddy (2009). To accomplish this, we developed a more general model to control for similarity between art pieces, effectively allowing us to consider related goods instead of past sales of an item. With modern computer programming tools, we also constructed a new dataset consisting of 500,000 recent auction sales of assorted art (including 250,000 paintings) spanning the years 2006-2015. This is itself a major contribution to the art economics literature, much of which has relied on the same Impressionist and Contemporary auction data compiled in the 1990's.

We were able to replicate the general findings of Beggs & Graddy (2009) on their original dataset, despite not knowing exactly which observations they used. This included the discovery of significant anchoring effects across the resales of Impressionist and Contemporary art pieces, as well as various other results (similarly high R^2 values, insignificant time coefficients, etc.). Such replication work ensured we were applying their model correctly before modifying it for our substitution work.

Our model, which generalizes the original model of Beggs & Graddy (2009), allows one to test for anchoring cross-effects across sales of similar art pieces. For our model, we introduced two quantitative measures of similarity (substitution) between art pieces, drawing upon insights from our interviews with experts and specialists in the art world. Quantitative measures of artistic similarity, to our knowledge, has not previously appeared in the art econometric literature. Running our model, we were able to find significant evidence of anchoring cross-effects in our Impressionist and assorted art datasets. To ensure our model's robustness, we also ran three experiments on three pairs of

artists with differing degrees of similarity. We identified strong and significant anchoring between Picasso and Chagall, inconclusive effects between Miro and Dali, and no significant anchoring between Munch and Toulouse-Lautrec. This showed that our anchoring model successfully accounts for artistic similarity when it is obviously strong (Picasso and Chagall), and at the other extreme, is robust against false detection of anchoring when there is clear artistic dissimilarity (Munch and Toulouse-Lautrec).

Overall, our discovery of anchoring cross-effects was surprising given that the similarity measures we constructed were considerably different and broadly applied. Measuring similarity across art pieces is an enormously difficult challenge, even for art experts. In our interviews, we sometimes received very divergent opinions on the relative importance of various hedonic characteristics. Yet assessing artistic similarity is vital to properly appraising works, and as we surmised from our interviews, something that those in the field must continually address. Hence, there are many directions for future work.

First, the exact mechanism by which past price can bias current price is still a black box. The mere observation of this sufficed for our definition of anchoring, but it would be worthwhile to dig deeper into this regard in order to understand how price signals flows across auction sales. To better understand how past price biases current price, it may be useful to conduct further interviews with buyers, auctioneers, and sellers to understand how they formulate their estimates of pieces.

Second, one could further develop measures of similarity between art pieces. While in this research we have optimized for breadth and generality, one should examine the art market more closely to understand how similarity is defined for different styles, artists, and price points. It is well-known that many artists pass through multiple artistic phases during their careers, and their styles can often change dramatically. Hence, future research may wish to take a complementary approach

to our general survey by focusing on several artists in depth, and studying how anchoring cross-effects between them change based on different points in their careers.

Finally, one could examine other applications of anchoring. While we have only focused on the impact of anchoring on sale (hammer) price, Beggs & Graddy (2009) also discuss how it can impact auctioneer presale estimates for a piece, as well as the probability of even selling the work. As in their paper, our regression model can easily be adapted for these by changing the dependent variable or applying a probit transformation. One could also test for asymmetric anchoring cross-effects between similar pieces, i.e. if gains in the price of a substitute affects a good's sale price differently than losses do. However, when Beggs & Graddy (2005) examined this for resales of the same work, they found no significant evidence of asymmetric effects.

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9. FIGURES AND TABLES

FIGURES

Figure 1: Distribution of selected quantities in the Impressionist art dataset. Y-axis is number of observations. The dimensions in this dataset were not specified beyond “DIM_A” and “DIM_B.”

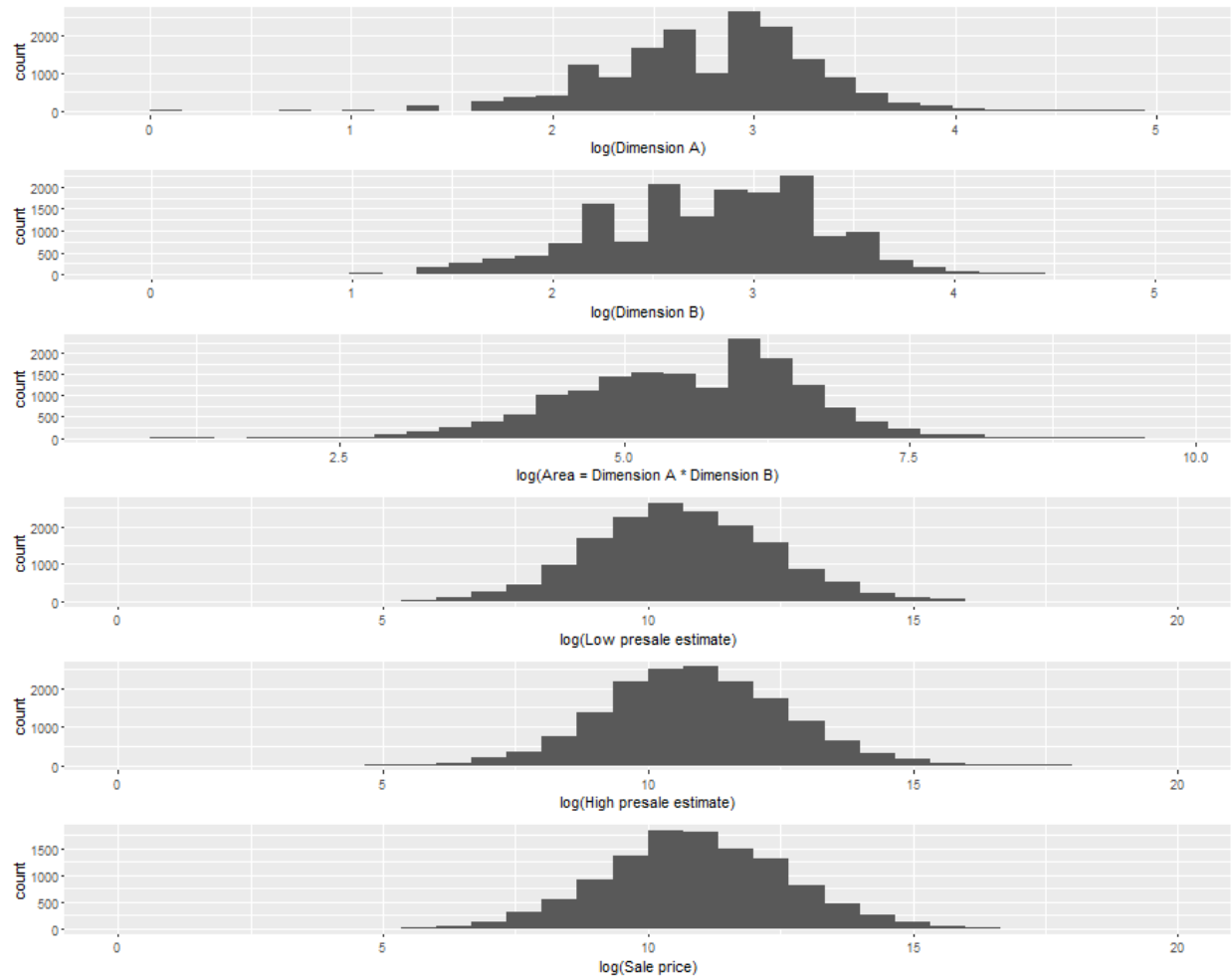


Figure 2: Comparison of painting dimensions, Impressionist art. The least squares regression line is shown.

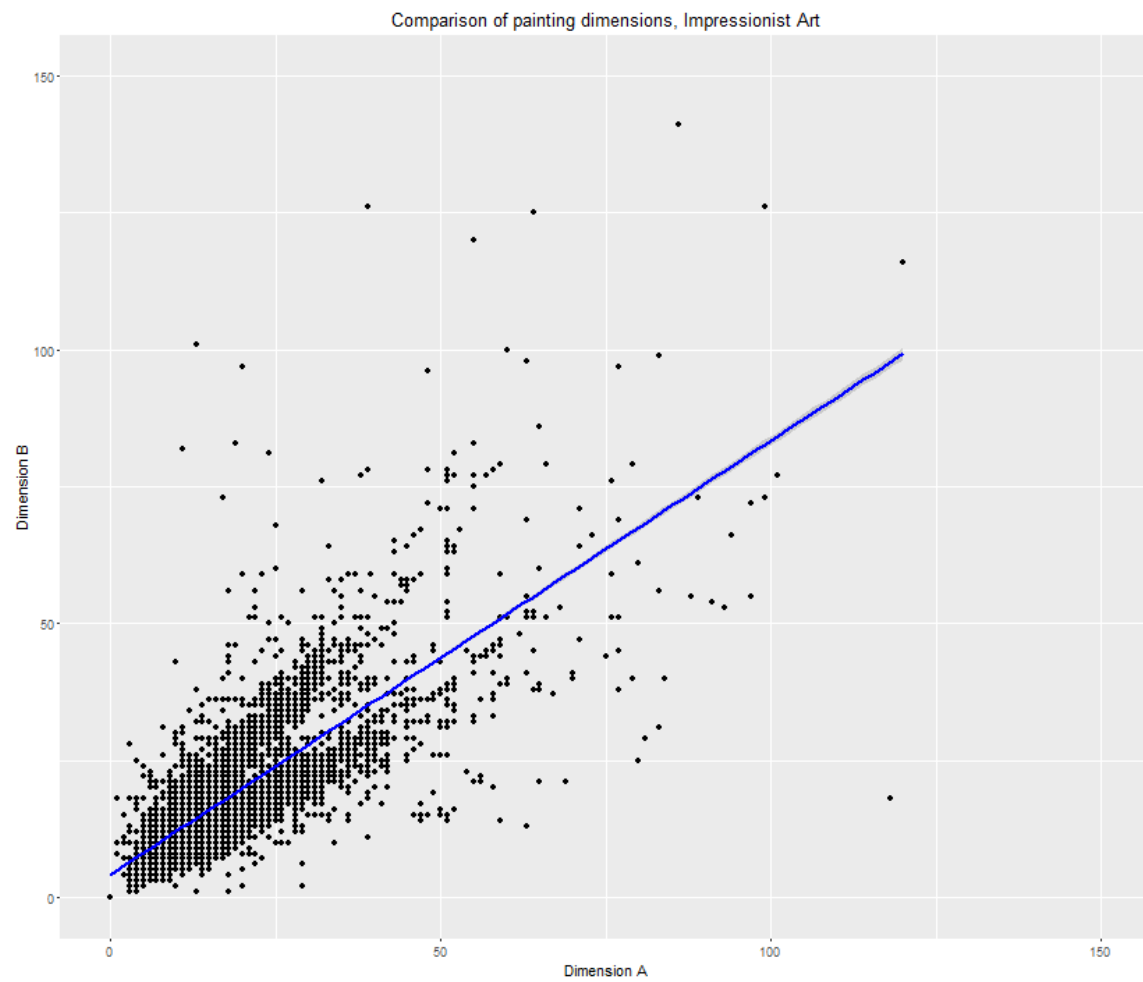


Figure 3: Impressionist art, auction sales over time.

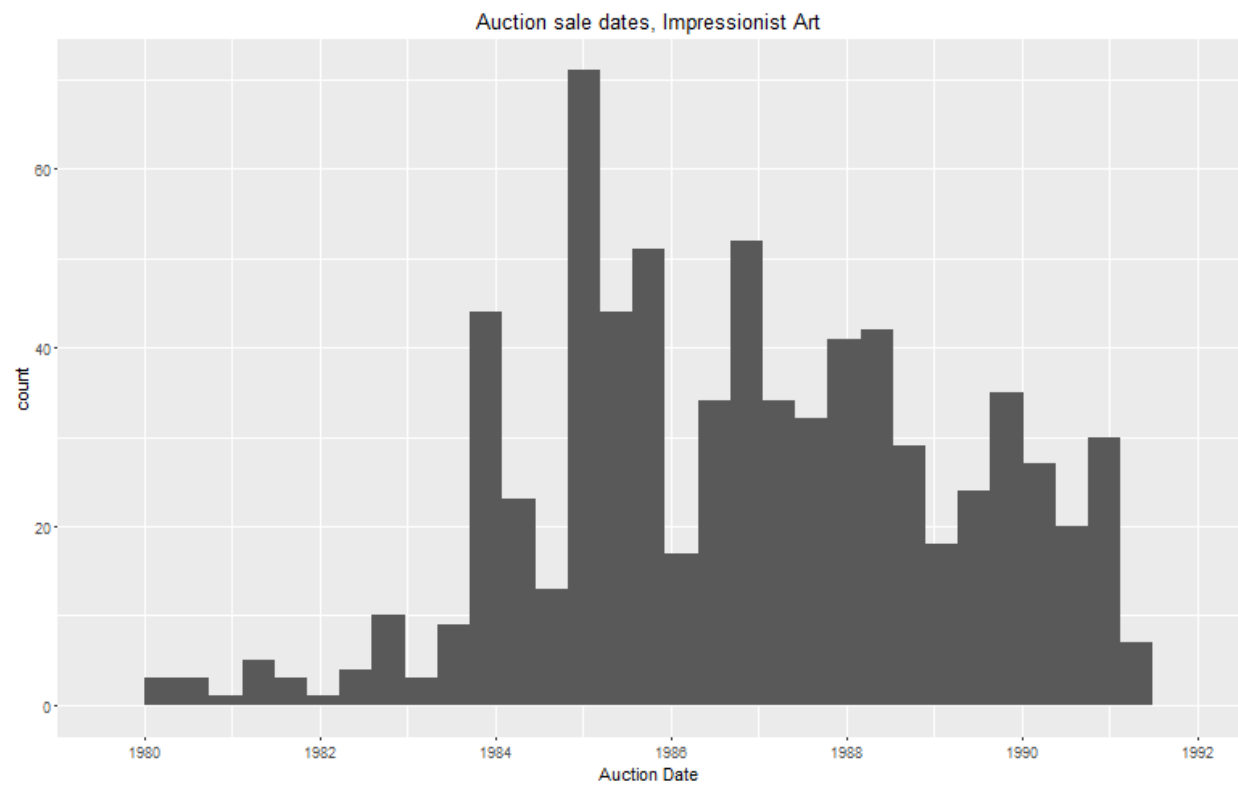


Figure 4: Distribution of selected quantities in the Contemporary art dataset.

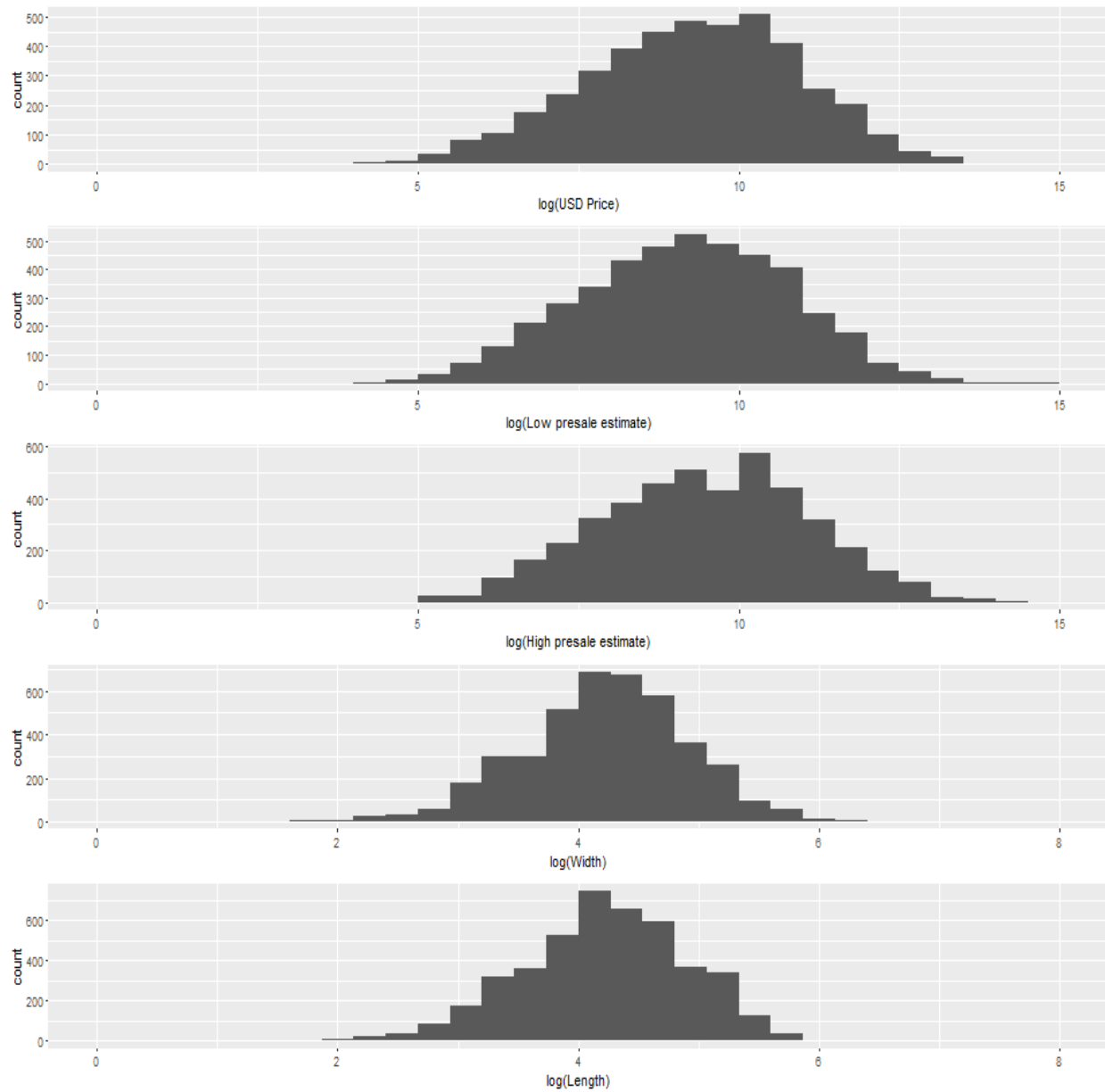


Figure 5: Auction sales over time, Contemporary art.

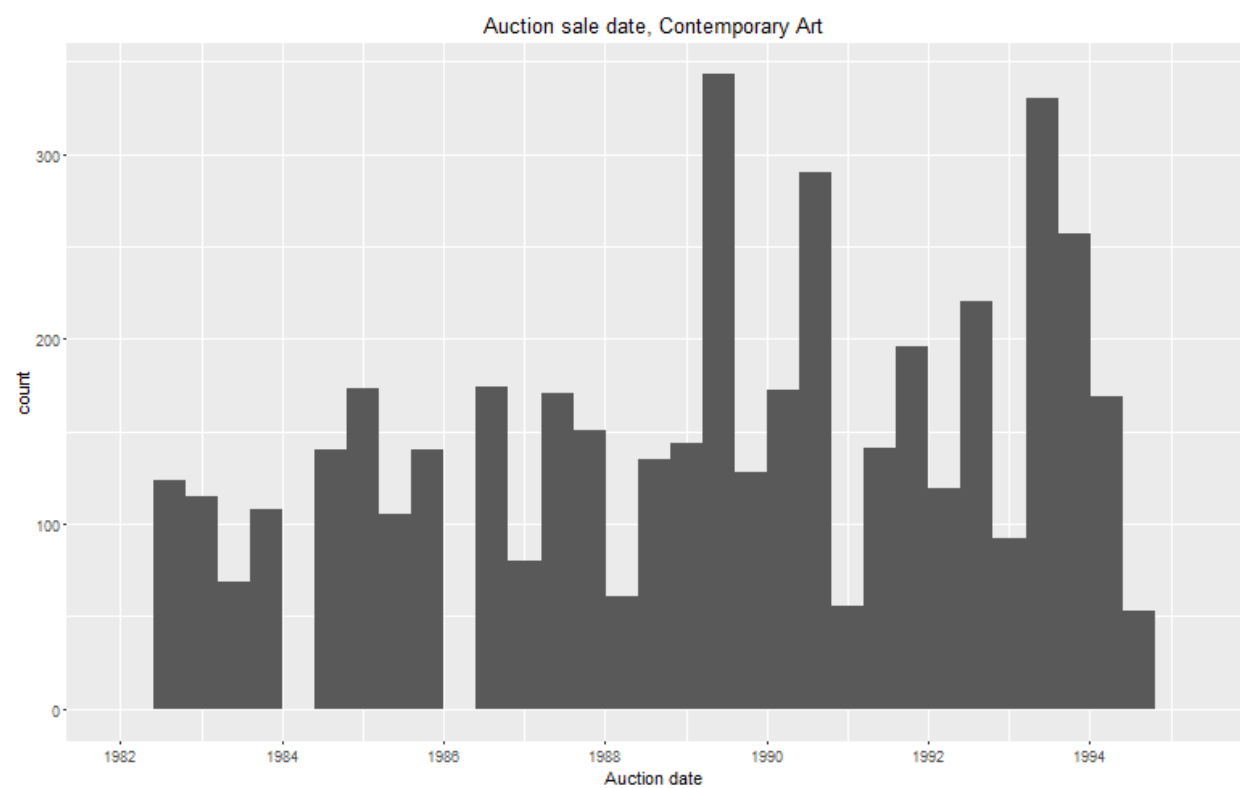


Figure 6: Comparison of log prices, Impressionist and Contemporary art.

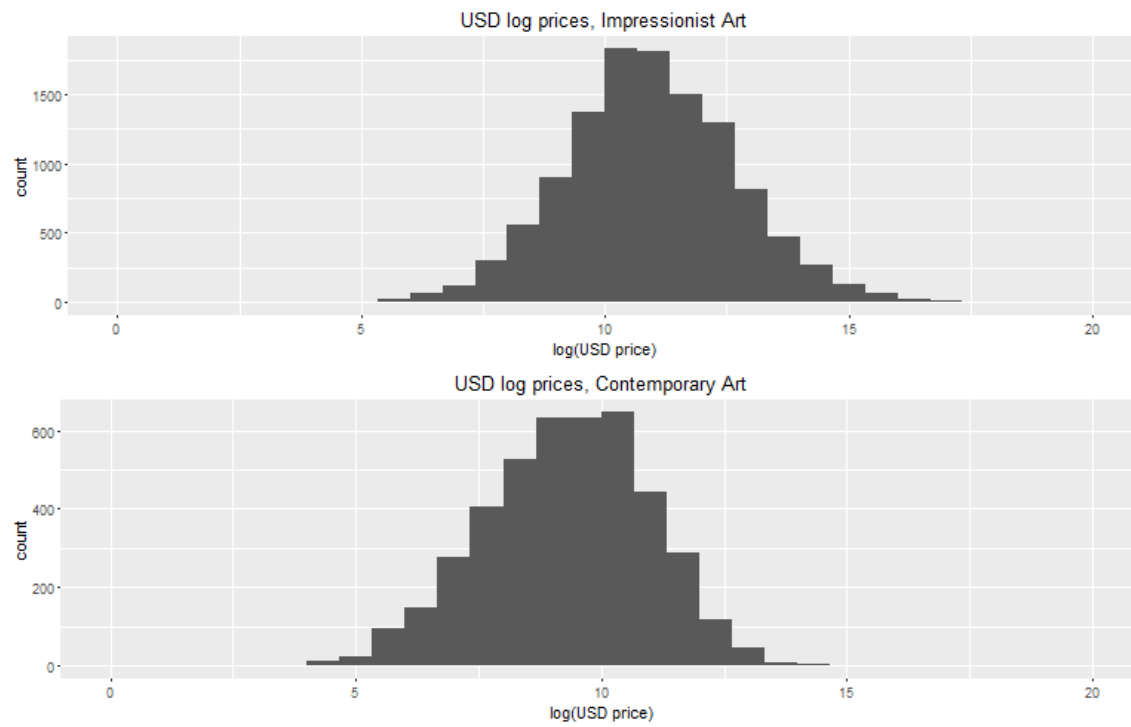


Figure 7: Comparison of log area, Impressionist and Contemporary art.

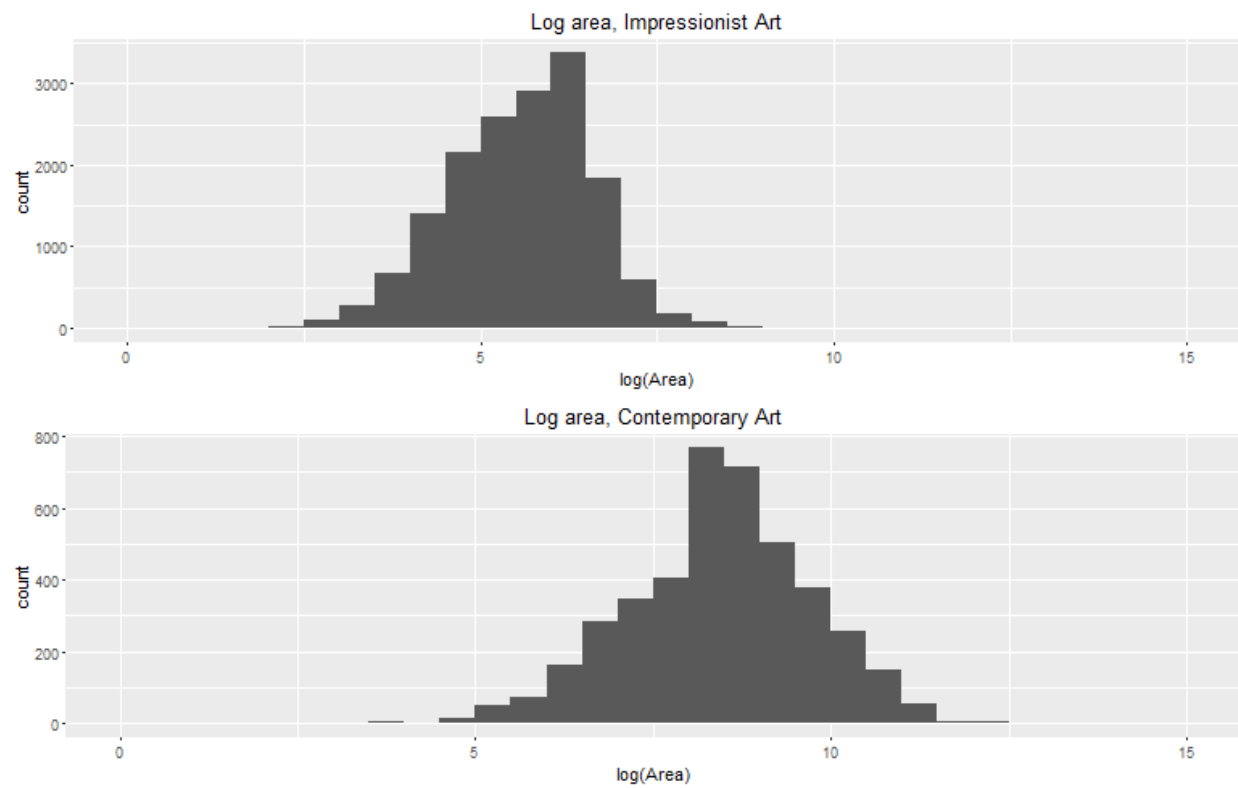
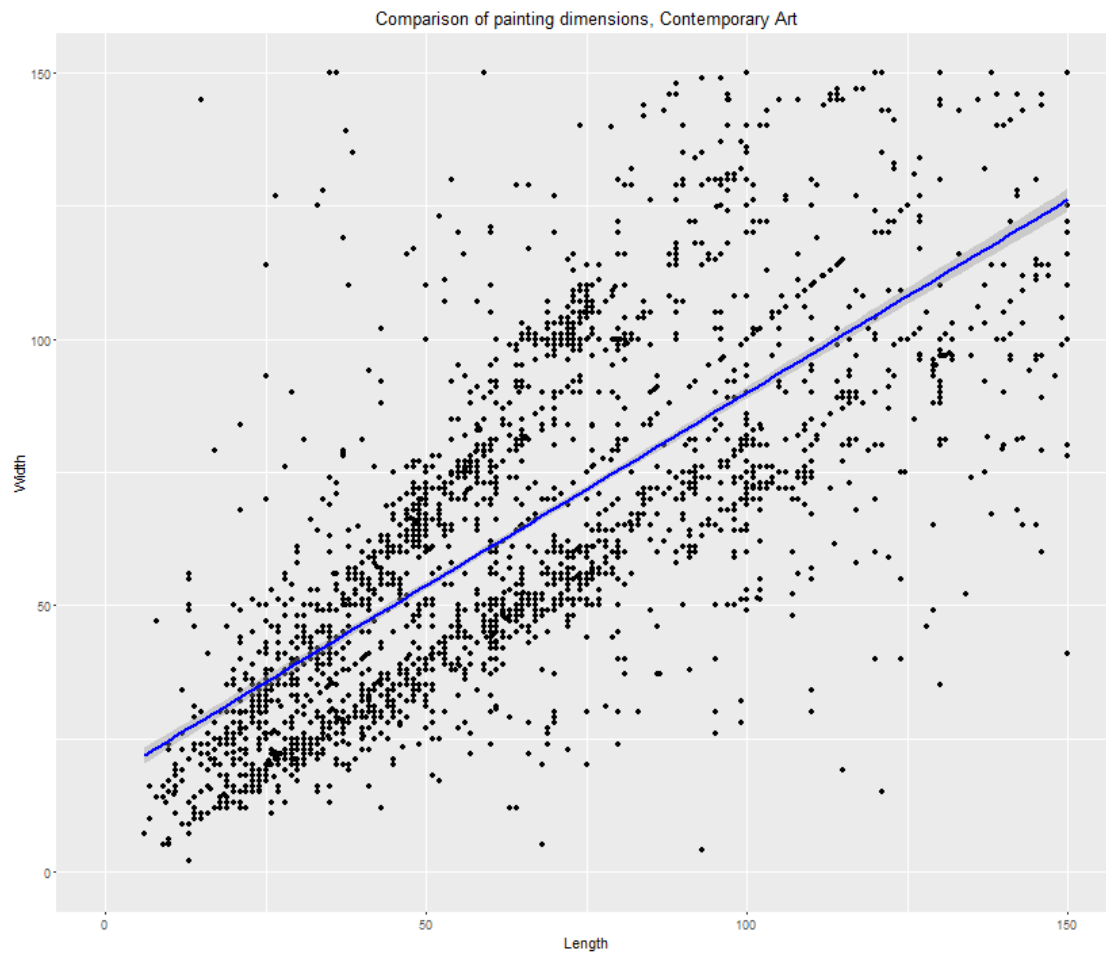
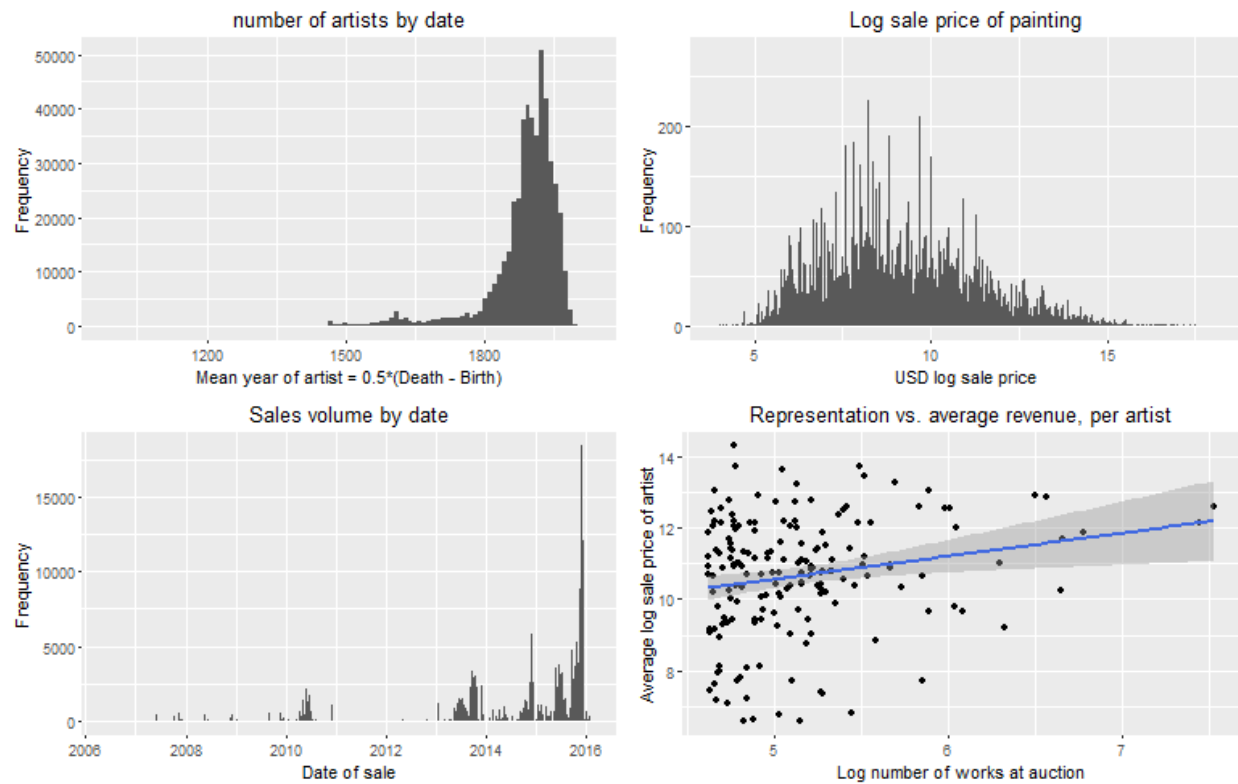


Figure 8: Comparison of painting dimensions, Contemporary art.



Figures 9-12: Plots for recent assorted art dataset.



TABLES

Table 1: Impressionist art (16,253 observations), summary statistics for selected continuous features. Units unknown for the dimensions. The # of NA values (missing values) for Sale Price indicate observations where the work of interest did not sell. 91% of works have signs of authenticity (indicated in a multi-level variable SIGN for different signs of authenticity. It equals 0 if no signs are present).

Variable	Min	1st Qu.	Median	Mean	3rd Qu.	Max	# NA vals
Date of Auction	3/26/1980	2/21/1985	11/20/1986	12/01/1986	10/19/1988	5/9/1991	0
Dimension A	0	11	17	18.31	23.00	120.00	37
Dimension B	0	11	18	18.69	24	141	37
Low Estimate (USD)	102	14,000	40,000	196,023	132,800	40,000,000	0
High Estimate (USD)	128	18,000	50,000	257,967	168,300	50,000,000	0
Sale Price (USD)	126	18,700	53,856	285,428	176,000	82,500,000	4,696
Date of Painting's Creation	1823	1902	1922	1921	1938	1983	3,950
Diameter of Painting	1	6.75	11.50	15.10	24.50	36.00	16,243

Table 2: Contemporary art (4,456 observations), summary statistics for selected continuous variables. There already exists a dummy variable **SOLD** which indicates whether or not a painting has sold, so here, **Sale Price (USD)** reflects either the final sale price of the work (if it has sold) or the final highest bid (if it is bought in). Additionally, the .do information file that accompanied this dataset did not provide the exact units for length and width. This dataset did not included indicators of authenticity such as a signature.

Variable	Min	1st Qu.	Median	Mean	3rd Qu.	Max	# NA vals
Date of Auction	6/29/1982	6/26/1986	6/29/1989	5/15/1989	7/2/1992	6/30/1994	0
Low Estimate (USD)	81	3,078	10,248	32,619	30,681	3,491,100	45
High Estimate (USD)	145	4,316	13,342	43,613	40,545	5,042,700	45
Sale Price (USD)	0	3,024	11,055	35,179	34,030	3,297,150	2
Length	5.40	44.50	70	84.53	105	957	73
Width	2	46	70	84.71	105	602	293

Table 3: Assorted art (264,115 observations, only paintings), summary statistics for selected continuous variables. Approximately 72% of the works are signed. Other hedonic characteristics not included in this table are artist and materials. We do not consider presale estimates, since they are not the focus of our research.

Variable	Min	1st Qu.	Median	Mean	3rd Qu.	Max	# NA vals
Date of Auction	6/9/2006	9/28/2013	2/14/2015	7/4/2014	10/16/2015	12/22/2015	0
Sale Price (USD)	1	989	3,007	50,497	12,435	70,530,000	0
Height (Inches)	0.04	11.89	19.49	23.51	29.53	358.27	0
Width (Inches)	0.15	12.20	19.57	23.58	28.74	355.71	0

HEDONIC REGRESSIONS

P-values that are significant at the 5% level (or lower) are **bolded**.

Table 4: Hedonic predictions, Impressionist Art (London). Half-year time dummies omitted for brevity. Multiple signs of authenticity accounted for; medium is also a categorical variable. The regression software we used (R programming language) dropped certain columns for estimation purposes.

Variable	Estimate	Std. Error	t-value	p-value
Constant	10.667	6.704	1.591	0.113
Date of Painting	-0.002	0.004	-0.604	0.546
Dimension A	0.027	0.008	3.519	0.001
Dimension B	0.017	0.006	2.595	0.010
Authenticity #1	0.267	0.251	0.760	0.448
Authenticity #2	-0.065	0.434	-0.149	0.881
Authenticity #3	-0.430	0.413	-1.04	0.298
Medium 6	1.780	0.680	2.625	0.009
Medium 9	0.349	0.684	0.510	0.610
Medium 12	2.270	0.674	3.368	0.001
Medium 15	1.470	0.698	2.110	0.036
Medium 18	2.950	0.643	4.595	0.000
Medium 24	1.460	0.770	1.889	0.060
Medium 27	1.094	0.661	1.655	0.010
Medium 30	0.490	0.659	0.745	0.456
Medium 33	1.280	0.846	1.512	0.132
Medium 39	1.767	0.660	2.677	0.008
R^2	0.866			
Adjusted R^2	0.825			
F-Statistic	21.01 on 79 and 256 DF (p-value: < 2.2E-16)			

Table 5: Hedonic predictions, Impressionist Art (NYC). Half-year time dummies omitted for brevity.

Variable	Estimate	Std. Error	t-value	p-value
Constant	20.536	5.800	3.541	0.000
Date of Painting	-0.006	0.003	-2.013	0.045
Dimension A	0.041	0.007	5.447	0.000
Dimension B	0.013	0.007	1.771	0.077
Authenticity #1	1.059	0.157	6.757	0.000
Authenticity #2	0.301	0.245	1.228	0.220
Authenticity #3	0.203	0.217	0.936	0.350
Medium 6	-0.365	0.687	-0.531	0.596
Medium 9	-0.060	0.642	-0.094	0.925

Medium 12	1.014	0.618	1.640	0.102
Medium 15	-0.131	0.665	-0.197	0.844
Medium 18	1.248	0.615	2.029	0.043
Medium 21	0.773	0.877	0.882	0.379
Medium 24	0.361	0.661	0.546	0.585
Medium 27	-0.342	0.657	-0.522	0.602
Medium 30	-0.075	0.646	-0.117	0.907
Medium 38	-0.404	0.808	-0.500	0.617
Medium 39	0.645	0.631	1.023	0.307
R^2	0.837			
Adjusted R^2	0.800			
F-Statistic	22.24 on 74 and 319 DF (p-value: < 2.2E-16)			

Table 6: Hedonic predictions, Contemporary Art. Half-year time dummies omitted for brevity.

Variable	Estimate	Std. Error	t-value	p-value
Constant	-1.542	1.918	-0.804	0.422
log(Date of Painting)	-0.672	0.427	-1.574	0.116
log(Length)	0.592	0.116	5.111	0.000
log(Width)	0.616	0.118	5.235	0.000
Medium a	0.379	0.368	1.031	0.303
Medium br	-1.004	0.470	-2.134	0.034
Medium chk	-0.512	0.506	-1.013	0.312
Medium col	-2.011	0.543	-3.700	0.000
Medium cr	-0.856	0.376	-2.279	0.023
Medium f	-1.196	0.490	-2.442	0.015
Medium g	-0.923	0.407	-2.271	0.024
Medium ik	-0.666	0.383	-1.738	0.083
Medium o	0.339	0.315	1.076	0.283
Medium pas	-0.764	0.551	-1.388	0.166
Medium pg	3.843	0.644	5.964	0.000
Medium ph	-2.974	0.720	-4.132	0.000
Medium pl	1.436	0.660	2.176	0.030
Medium pn	0.733	0.796	0.921	0.358
Medium s	-0.303	0.491	-0.618	0.537
Medium sk	2.781	0.579	4.804	0.000
Medium t	-0.773	0.390	-1.980	0.049
Medium tp	0.253	0.554	0.457	0.648
Medium w	-0.419	0.367	-1.143	0.254
R^2	0.923			
Adjusted R^2	0.889			

F-Statistic	27.17 on 146 and 330 DF (p-value: < 2.2E-16)
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Table 7: Hedonic predictions, assorted art. Half-year time dummies omitted for brevity. Artist and medium were omitted due to computational constraints.

Variable	Estimate	Std. Error	t-value	p-value
Constant	6.224	0.018	345.782	<2e-16
log(Height)	0.614	0.008	76.454	<2e-16
log(Width)	0.230	0.008	28.431	<2e-16
Signed	-0.635	0.008	-79.255	<2e-16
Monogrammed	-0.203	0.022	-9.089	<2e-16
Stamped	0.086	0.016	5.391	0.000
R^2	0.101			
Adjusted R^2	0.101			
F-Statistic	5907 on 5 and 264109 DF (p-value: < 2.2E-16)			

ANCHORING EFFECTS (REPLICATION)

Throughout this paper, we are only interested in regressions where price is the dependent variable. This is reflected in all following tables for anchoring effects.

Table 8: Replicated anchoring effects, Impressionist Art. In the original anchoring regression, the current hedonic prediction (at time t) represents π_t , the anchoring effect represents $(P_{t-1} - \pi_t)$, and the past residual represents $(P_{t-1} - \pi_{t-1})$.

	Estimate	Std.Error	t-value	p-value
Constant	-0.338	0.193	-1.755	0.080
Current hedonic prediction	1.018	0.019	53.327	<2e-16
Anchoring effect	0.174	0.072	2.410	0.017
Past residual	0.503	0.077	6.533	0.000
Months since last sale	0.008	0.002	4.219	0.000
R^2	0.923			
Adjusted R^2	0.922			
F-Statistic	1047 on 4 and 349 DF (p-value: < 2.2E-16)			

Table 8b: Original anchoring results for Impressionist Art, Beggs & Graddy (2009). This corresponds to the full sample with price as the dependent variable. Findings of anchoring were significant (not shown).

	Estimate	Std. Error
Constant	0.246	0.436
Current hedonic prediction	0.982	0.036
Anchoring effect	0.625	0.131
Past residual	0.323	0.141
Months since last sale	0.011	0.0003
R^2	0.90	

Table 9: Replicated anchoring effects, Contemporary Art

	Estimate	Std.Error	t-value	p-value
Constant	-0.115	0.050	-2.316	0.022
Current hedonic prediction	1.034	0.020	50.799	0.000
Anchoring effect	0.131	0.074	1.773	0.078
Past residual	0.191	0.095	2.009	0.046
Months since last sale	-0.001	0.003	-0.341	0.734
R^2	0.941			
Adjusted R^2	0.940			
F-Statistic	698 on 4 and 176 DF (p-value: < 2.2E-16)			

Table 9b: Original anchoring results for Contemporary art, Beggs & Graddy (2009).

	Estimate	Std. Error
Constant	-0.292	0.408
Current hedonic prediction	1.015	0.047
Anchoring effect	0.183	0.091
Past residual	0.379	0.146
Months since last sale	0.0002	0.0004
R^2	0.91	

Table 10: Anchoring effects, assorted art.

	Estimate	Std.Error	t-value	p-value
Constant	-1.599	0.010	-16.467	0.000
Current hedonic prediction	1.148	0.012	98.054	0.000

Anchoring effect	0.591	0.011	51.626	0.0000
Past residual	-0.020	0.012	-1.683	0.092
Months since last sale	-0.042	0.005	-8.837	0.000
R^2	0.414			
Adjusted R^2	0.414			
F-Statistic	3.04E4 on 4 and 172189 DF (p-value: < 2.2E-16)			

ANCHORING CROSS-EFFECTS (Q1)

Table 11: Anchoring cross-effects (Q_1) for Impressionist art. In our anchoring cross-effects regression, the current hedonic prediction is represents π_c , the anchoring cross-effect represents $(P_s - \pi_c)$, the substitute residual represents $(P_s - \pi_s)$, and the substitute measure represents Q which is Q_1 here. Again, the substitute here represents the “average substitute” for the current good.

	Estimate	Std.Error	t-value	p-value
Constant	-0.105	0.067	-1.558	0.119
Current hedonic prediction	1.020	0.012	84.393	0.000
Anchoring cross-effect	0.034	0.014	2.419	0.016
Substitute residual	-0.284	0.021	13.405	0.000
Substitute measure	0.008	0.004	2.055	0.040
Months since substitute sale	-0.001	0.001	-1.035	0.301
R^2	0.775			
Adjusted R^2	0.775			
F-Statistic	8004 on 5 and 11608 DF (p-value: < 2.2E-16)			

Table 12: Anchoring cross-effects (Q_1) for Contemporary art.

	Estimate	Std.Error	t-value	p-value
Constant	0.60	0.090	0.659	0.510
Current hedonic prediction	1.034	0.025	41.781	0.000
Anchoring cross-effect	-0.030	0.029	-1.039	0.299
Substitute residual	0.298	0.044	6.791	0.000
Substitute measure	-0.013	0.009	-1.465	0.143
Months since substitute sale	-0.050	0.014	-3.529	0.000
R^2	0.831			
Adjusted R^2	0.830			
F-Statistic	938 on 5 and 952 DF (p-value: < 2.2E-16)			

Table 13: Anchoring cross-effects (Q_1) for assorted art.

	Estimate	Std.Error	t-value	p-value
Constant	-1.995	0.221	-9.043	0.000
Current hedonic prediction	1.241	0.026	47.959	0.000
Anchoring cross-effect	0.661	0.025	26.414	0.000
Substitute residual	-0.102	0.026	-3.869	0.000
Substitute measure	0.027	0.005	5.366	0.000
Months since substitute sale	-0.089	0.016	-5.594	0.000
R^2	0.461			
Adjusted R^2	0.461			
F-Statistic	3030 on 5 and 17693 DF (p-value: < 2.2E-16)			

ANCHORING CROSS-EFFECTS (Q2)

Table 14: Anchoring cross-effects (Q_2) for Impressionist art.

	Estimate	Std.Error	t-value	p-value
Constant	0.009	0.074	0.116	0.9079
Current hedonic prediction	0.999	0.006	162.044	0.000
Anchoring cross-effect	0.026	0.013	1.965	0.050
Substitute residual	0.286	0.021	13.572	0.000
Substitute measure	0.015	0.008	1.871	0.061
Months since substitute sale	-0.0001	0.001	-0.195	0.8457
R^2	0.775			
Adjusted R^2	0.775			
F-Statistic	8004 on 5 and 11608 DF (p-value: < 2.2E-16)			

Table 15: Anchoring cross-effects (Q_2) for Contemporary art.

	Estimate	Std.Error	t-value	p-value
Constant	-0.092	0.115	-0.797	0.426
Current hedonic prediction	1.056	0.019	58.124	0.000
Anchoring cross-effect	-0.021	0.027	-0.775	0.439
Substitute residual	0.292	0.044	6.680	0.000
Substitute measure	-0.012	0.006	-2.022	0.0435
Months since substitute sale	-0.050	0.014	-3.545	0.000
R^2	0.8316			
Adjusted R^2	0.8307			
F-Statistic	940.3 on 5 and 952 DF (p-value: < 2.2E-16)			

Table 16: Anchoring cross-effects (Q_2) for assorted art.

	Estimate	Std.Error	t-value	p-value
Constant	-2.036	0.176	-11.541	0.000
Current hedonic prediction	1.272	0.019	66.215	0.000
Anchoring cross-effect	0.519	0.022	23.632	0.000
Substitute residual	0.081	0.023	3.586	0.000
Substitute measure	0.296	0.015	19.504	0.000
Months since last sale	0.072	0.010	7.093	0.000
R^2	0.398			
Adjusted R^2	0.398			
F-Statistic	3936 on 5 and 29784 DF (p-value: < 2.2E-16)			

Table 17: Summary of results, anchoring (cross-effects).

Variable	Anchoring coef (& p-val), Q_1	Anchoring coef (& p-val), Q_2
Impressionist art	0.034 (0.016)	0.026 (0.0495)
Contemporary art	-0.03 (0.299)	-0.02 (0.438)
Assorted art	0.66 (0.000)	0.52 (0.000)

THREE EXPERIMENTS

Table 18: Miro vs. Dali (Q_1)

	Estimate	Std.Error	t-value	p-value
Constant	7.150	2.161	3.309	0.001
Current hedonic prediction	0.519	0.271	1.919	0.055
Anchoring cross-effect	-0.370	0.252	-1.466	0.143
Substitute residual	0.488	0.254	1.919	0.055
Substitute measure	0.18523	0.020	9.149	0.000
Months since last sale	-0.0825	0.044	-1.865	0.0623
R^2	0.126			
Adjusted R^2	0.123			
F-Statistic	41.84 on 5 and 1458 DF (p-value: < 2.2E-16)			

Table 19: Miro vs. Dali (Q_2)

	Estimate	Std.Error	t-value	p-value
Constant	8.677	2.233	3.886	0.000
Current hedonic prediction	-0.061	0.275	-0.221	0.825
Anchoring cross-effect	-0.973	0.254	-3.836	0.000
Substitute residual	1.032	0.258	4.005	0.000
Substitute measure	0.012	0.037	0.317	0.751
Months since last sale	-0.106	0.047	-2.245	0.025
R^2	0.075			

Adjusted R^2	0.072
F-Statistic	23.76 on 5 and 1458 DF (p-value: < 2.2E-16)

Table 20: Picasso vs. Chagall (Q_1)

	Estimate	Std.Error	t-value	p-value
Constant	-2.880	3.353	-0.859	0.391
Current hedonic prediction	2.027	0.340	5.959	0.000
Anchoring cross-effect	1.546	0.325	4.754	0.000
Substitute residual	-1.126	0.328	-3.432	0.001
Substitute measure	0.362	0.022	16.116	0.000
Months since last sale	-0.057	0.0366	-1.550	0.121
R^2	0.179			
Adjusted R^2	0.177			
F-Statistic	102.9 on 5 and 2359 DF (p-value: < 2.2E-16)			

Table 21: Picasso vs. Chagall (Q_2)

	Estimate	Std.Error	t-value	p-value
Constant	-21.895	3.230	-6.779	0.000
Current hedonic prediction	3.479	0.341	10.218	0.000
Anchoring cross-effect	2.537	0.332	7.639	0.000
Substitute residual	-2.242	0.333	-6.733	0.000
Substitute measure	0.551	0.0837	6.582	0.000
Months since last sale	0.205	0.0579	3.549	0.000
R^2	0.105			
Adjusted R^2	0.103			
F-Statistic	55.39 on 5 and 2359 DF (p-value: < 2.2E-16)			

Table 22: Munch vs. Toulouse-Lautrec (Q_1)

	Estimate	Std.Error	t-value	p-value
Constant	2.212	2.302	0.961	0.337
Current hedonic prediction	0.856	0.205	4.179	0.000
Anchoring cross-effect	-0.219	0.199	-1.101	0.272
Substitute residual	0.140	0.213	0.656	0.512
Substitute measure	0.043	0.46	0.930	0.353
Months since last sale	0.053	0.071	0.754	0.452
R^2	0.2927			
Adjusted R^2	0.2811			
F-Statistic	25.24 on 5 and 305 DF (p-value: < 2.2E-16)			

Table 23: Munch vs. Toulouse-Lautrec (Q_2)

	Estimate	Std.Error	t-value	p-value
Constant	2.724	2.187	1.245	0.214
Current hedonic prediction	0.815	0.206	3.953	0.000
Anchoring cross-effect	-0.273	0.202	-1.353	0.177
Substitute residual	0.196	0.215	0.909	0.364
Substitute measure	0.369	0.211	1.744	0.082
Months since last sale	0.262	0.135	1.936	0.054
R^2	0.298			
Adjusted R^2	0.286			
F-Statistic	25.86 on 5 and 305 DF (p-value: < 2.2E-16)			