HW 1

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1.5

a

$$A(4) = 1000 \times (1 - 0.06 \times 4)$$
$$= 1000 \times (1.24)$$
$$= $1240.00$$

b

$$A(4) = 1000 \times (1 - 0.06 \times 4)$$
$$= 1000 \times (0.76)$$
$$= $760.00$$

 \mathbf{c}

$$A(4) = 1000 \times (1 + 0.06)^4$$
$$= 1000 \times (1.262)$$
$$= $1262.48$$

 \mathbf{d}

$$r^{(4)} = 0.06i(t) = 1 + \frac{r^{(m)}}{m}^{m} - 1$$

$$= 1 + \frac{0.06^{4}}{4} - 1$$

$$= 1 + 0.015^{4} - 1$$

$$= 0.0614A(4) = 1000 \times (1 + 0.0614)^{4}$$

$$= 1000 \times (1.269)$$

$$= \$1268.99$$

 \mathbf{e}

$$d^{(12)} = 0.06i(t) = 1 - \frac{d^{(m)}}{m}^{-m} - 1$$

$$= 1 - \frac{0.06}{12}^{-12} - 1$$

$$= 1 - 0.005^{-12} - 1$$

$$= 0.0620A(4) = 1000 \times (1.272)$$

$$= $1272.01$$

 \mathbf{f}

$$A(4) = 1000 \times e^{\delta t}$$

$$= 1000 \times e^{0.06 \times 4}$$

$$= 1000 \times e^{0.24}$$

$$= 1000 \times (1.271)$$

$$= $1271.25$$

1.9

Present Value

$$A(0) = \sum_{i=1}^{5} C_t \times (1+i)^{-t}$$

$$= \sum_{i=1}^{5} C_t \times (1.02)^{-t}$$

$$= 950 \times (1.02)^0 + 800 \times (1.02)^{-1} + 150 \times (1.02)^{-2} + 400 \times (1.02)^{-3} + 120 \times (1.02)^{-4}$$

$$= 950 \times 1 + 800 \times 0.9804 + 150 \times 0.9612 + 400 \times 0.9423 + 120 \times 0.9239$$

$$= 950 + 784.314 + 144.175 + 376.9289 + 110.8615$$

$$= $2366.28$$

A(5)

To calculate the value in 5 years, we could begin as above, and accumulate each cash flow individually to t = 5 rather that t = 0. However, it is equivalent to simply accumulate the sum as a whole.

$$A(5) = A(0) \times 1.02^5$$

$$= $2366.28 \times 1.10408$$

$$= $2612.56$$

1.36

To solve for the interest earned in the fifth year, we can subtract A(5) - A(4)

$$\begin{split} A(5) &= A(0) \times \int_0^5 \frac{1}{10(1+t)^3} dt \\ A(4) &= A(0) \times \int_0^4 \frac{1}{10(1+t)^3} dt \\ A(5) - A(4) &= A(0) \times \int_0^5 \frac{1}{10(1+t)^3} dt - A(0) \times \int_0^4 \frac{1}{10(1+t)^3} dt \\ &= A(0) \times (\int_0^5 \frac{1}{10(1+t)^3} dt - \int_0^4 \frac{1}{10(1+t)^3} dt) \\ &= A(0) \times (\int_4^5 \frac{1}{10(1+t)^3} dt) \\ &= A(0) \times (\int_4^5 \frac{1}{10(1+t)^3} dt) \\ &= 100 \times \frac{1}{10} \times \int_4^5 (1+t)^{-3} dt \\ &= 10 \times \frac{-(1+t)^{-2}}{2} |_4^5 \\ &= 10 \times (\frac{-(1+5)^{-2}}{2} - \frac{-(1+4)^{-2}}{2}) \\ &= 5 \times ((1+4)^{-2} - (1+5)^{-2}) \\ &= 5 \times (0.0122) \\ &= \$0.0611 \end{split}$$