

**I apologize that it is not as well put together this week. I did not have time to make it look better. Thanks!**

### Problem 1

- The variable sex is significant at a 0.05 significance level. The variable income is significant at a 0.01 significance level.
- As the variable "sex" is increased by one unit, it is estimated that the gamble variable will change by -22.11833 units (as long as all other variables are held constant). Because the variable only takes values of 0 and 1, this means that it is estimated to drop -22.11833 as it switches from sex = 0 to sex = 1 (as long as all other variables are held constant).
- $F = 4.1338$ ,  $p\text{-value} = 0.01177$ . Statistically significant at significance level 0.05.

### Problem 2

- $H_0: \beta_{\text{salary}} = 0$ ;  $H_A: \beta_{\text{salary}} \neq 0$

$$T = -1.878$$

$$P\text{val} = 0.0667$$

Statistically significant at the 0.10 significance level

$$H_0: \beta_{\text{salary}} = \beta_{\text{ratio}} = \beta_{\text{expend}} = 0; H_A: \text{at least one is not } 0$$

$$F = 4.0662$$

$$P\text{val} = 0.01209$$

Statistically significant at the 0.05 significance level

- $H_0: \beta_{\text{salary}} = 0$ ;  $H_A: \beta_{\text{salary}} \neq 0$

$$T = 0.686$$

$$P\text{val} = 0.496$$

Fail to reject null. We do not have statistically significant evidence that  $\beta_{\text{salary}} \neq 0$

$$F = 52.88$$

Pval is approximately 0.

Reject the null, statistically significant at and reasonable significance level.

The F-Test and t-test are not equivalent. Different decisions are made between rejecting the null and failing to reject the null at different significance levels.

### Problem 3

Lcavol only: Residual standard error = 0.7875 and R-squared = 0.5394

Lweight added: Residual standard error = 0.7506 and R-squared = 0.5859

SVI added: Residual standard error = 0.7168 and R-squared = 0.6264

Lpbh added: Residual standard error = 0.7108 and R-squared = 0.6366

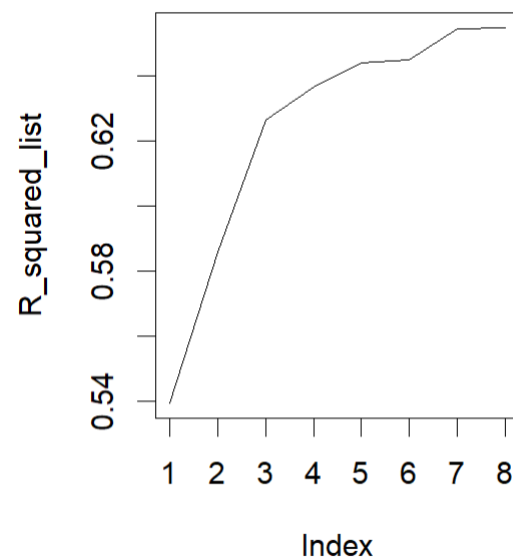
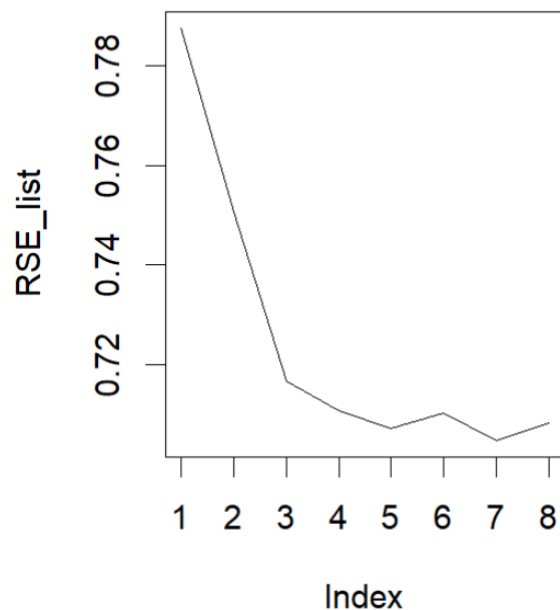
Age added: Residual standard error = 0.7073 and R-squared = 0.6441

LCP added: Residual standard error = 0.7102 and R-squared = 0.6451

PGG45 added: Residual standard error = 0.7048 and R-squared = 0.6544

Gleason added: Residual standard error = 0.7084 and R-squared = 0.6548

As the number of variables increased the RSE decreased on average, but  $R^2$  increased. Generally, as one of the quantities went up, the other went down.



#### Problem 4

$$y_{ij} \sim N(\mu + \alpha_i, \sigma^2)$$

$$\mu = 0 \text{ and } \alpha_1 = \frac{y_{1\cdot}}{5}$$

$$\text{Var}(\hat{\mu} + \hat{\alpha}_1) = \frac{\sigma^2}{5}$$

$$\hat{\mu} + \hat{\alpha}_1 \sim N(\mu + \alpha_1, \frac{\sigma^2}{5})$$

R Code:

```
library(faraway)
```

```
#Problem 1
```

```
out_full <- lm(gamble ~ sex + status + income + verbal, data = teengamb)
summary(out_full)
RSS_full <- sum(out_full$residuals^2)
```

```
out_red <- lm(gamble ~ income, data = teengamb)
summary(out_red)
RSS_red <- sum(out_red$residuals^2)
```

```
anova(out_full, out_red)
```

```
F <- ((RSS_red - RSS_full)/3) / (RSS_full/42)
F
```

```
p_value <- pf(F, lower.tail = FALSE, df1 = 3, df2 = 42)
p_value
```

```
#Problem 2
```

```
out_1 <- lm(total ~ expend + ratio + salary, data = sat)
out_2 <- lm(total ~ 1, data = sat)
```

```
anova(out_1, out_2)
```

```
out_3 <- lm(total ~ expend + ratio + salary + takers, data = sat)
summary(out_3)
```

```
#Problem 3
```

```
out_pro_1 <- lm(lpsa ~ lcavol, data = prostate)
summary(out_pro_1)
```

```
out_pro_2 <- lm(lpsa ~ lcavol + lweight, data = prostate)
summary(out_pro_2)
```

```
out_pro_3 <- lm(lpsa ~ lcavol + lweight + svi, data = prostate)
summary(out_pro_3)
```

```
out_pro_4 <- lm(lpsa ~ lcavol + lweight + svi + lbph, data = prostate)
summary(out_pro_4)
```

```
out_pro_5 <- lm(lpsa ~ lcavol + lweight + svi + lbph + age, data = prostate)
summary(out_pro_5)
```

```
out_pro_6 <- lm(lpsa ~ lcavol + lweight + svi + lbph + age + lcp, data = prostate)
summary(out_pro_6)
```

```
out_pro_7 <- lm(lpsa ~ lcavol + lweight + svi + lbph + age + lcp + pgg45,
               data = prostate)
summary(out_pro_7)
```

```
out_pro_8 <- lm(lpsa ~ lcavol + lweight + svi +
               lbph + age + lcp + pgg45 + gleason,
               data = prostate)
summary(out_pro_8)
```

```
RSE_list <- c(0.7875, 0.7506, 0.7168, 0.7108, 0.7073, 0.7102, 0.7048, 0.7084)
plot(RSE_list, type = "l")
```

```
R_squared_list <- c(0.5394, 0.5859, 0.6264, 0.6366, 0.6441, 0.6451, 0.6544, 0.6548)
```

```
plot(R_squared_list, type = "l")
```