

### Problem 1

```
const int n = 50;
int tally;

void Inc() {
    int count;
    for (count = 1; count<n; count++)
        tally++
}

void Dec() {
    int count;
    for (count = 1; count<n; count++)
        tally--
}
```

```
void main() {
    tally = 0;
    parbegin(Inc(),Dec()); // parbegin executes the functions in parallel
    write tally;
}
```

(a) What is the lower bound and upper bound on the final value of the shared variable *tally* in this concurrent program. Assume processes can execute at any relative speed and that the value can only be incremented/decremented after it has been loaded into a register by a separate machine instruction.

$$n = 60$$

Inc  $\rightarrow$  ① regl = tally  
② regl = regl + 1  
③ tally = regl

Dec  $\rightarrow$  ④ reg1 = tally  
⑤ reg1 = reg1 - 1  
⑥ tally = reg1

①	②	③	④	⑤	⑥	⑦
0		1	1		0	0

Case 1)

①	④	⑤	⑥	②	③	1
0	0	-1		1		
①	④	⑤	⑥	②	③	2
1	1	0		2		
⋮						
①	②	⑤	②	③		50
49	49	41	50	50		

Case 2)

④	①	②	③	⑤	⑥	-1
0	0	1	1	1	-1	
④	①	②	③	⑤	⑥	-2
-1	-1	0	0	-2	-2	
⋮						
④	①	②	③	⑤	⑥	-50
-19	-19	48	48	-50	-50	

Lower bound for tally :  $-50$   
Upper bound for tally :  $50$

$$\text{tally}_{\text{count}} = 0$$

(14) What is the lower and upper bounds if we consider the following process?

```
void main() {
    tally = 0;
    parbegin(&inc,&inc); // parbegin executes the functions in parallel
    write tally;
}
```

Incl)  $\rightarrow$

- ①  $regl = tally$
- ②  $regl = regl + 1$
- ③  $tally = regl$

```

④ regl = tally
⑤ regl = regl + 1
⑥ tally = regl

```

Case 1)	①	②	⑤	⑥	②	③	⑦
regl	0	0	1	1	1	1	
tally	0	0	0	1	0	1	1
regl	1	1	2	1	2	2	
tally	1	1	1	2	1	2	2
regl	2	2	3	3	3	3	
tally	2	2	2	3	2	3	3
regl	...						⋮
tally							

So

Case 2)	4	0	2	3	5	6	T
regl	0	0	1	1	1	1	
tally	0	0	0	1	0	1	1
regl	1	1	2	2	2	2	
tally	1	1	1	2	1	2	2
regl							⋮
tally							⋮
regl							⋮
tally							⋮
							So

Incl)  $\rightarrow$

- ① reg1 = tally
- ② reg1 = reg1 + 1
- ③ tally = reg1

- ④ regl = tally
- ⑤ regl = regl + 1
- ⑥ tally = regl

Case 8)	0	1	2	3	4	5	6	7
reg1	0	1	1	1	2	2		
tally	0	0	1	1	1	2		2
reg1	2	3	3	3	4	4		
tally	2	2	3	3	3	4		4
reg1	4	5	5	5	6	6		
tally	4	4	5	5	5	6		6
reg1								
tally								:
								:

100

Case 4)

$P_1$  ①

$P_2$  ①③⑤ — 49 times tally = 49

$P_1$  ②③ — tally = 1

$P_2$  ④⑤ — tally = 1

① ①②③ — 49 times tally = 50

$P_2$  ⑥ — tally = 2

Lower bound for tally: 50



100

Lower bound for tally: 50  
Upper bound for tally: 2

2)

Problem 2  
Show that, if the wait() and signal() semaphore operations are not executed atomically, then mutual exclusion may be violated. [20 pts]

atomic ops: finish Entirely

Mutual Exclusion: no two processes can exist in the critical section at any given time

```
wait(s)
{
    while(s <= 0);
    s--;
}

signal(s)
{
    s++;
}
```

Atomic on:  $S=1$

P1	main	P2	main
	wait()		wait()
	$S=0$		blocked

**CS**

Signal()

$S=1$

$S=0$   
**CS**

Signal  
 $S=1$

Atomic off:  $S=1$

P1	main	P2	main
	wait()		
	Preempt		

$S=-1$       wait()  
 $S=0$

**VIOLATION** →

**CS** **CS**

above shows if wait isn't atomic P1 gets preempted before it decrements then P2 is able to decrement then P1 comes back & decrements, now  $S=-1$  & P1 & P2 are in the critical section @ the same time.

p3)

Problem 3

The Under-equipped Mechanic Shop problem is a synchronization problem in which 3 mechanics work in an under-equipped shop and are forced to share 3 available tools (A, B and C). The 3 mechanics continuously repair parts and take breaks after fixing a part. Mechanic 1 needs the 3 tools to repair a part, Mechanic 2 only needs A and C to repair a part, and Mechanic 3 only needs B and C to repair a part. Write a program/pseudocode to synchronize between these 3 mechanics. Explain whether a deadlock can occur or not in your program. [20 pts]

need  
Mech 1: A B C



program/pseudocode to synchronize between these 3 mechanics. Explain whether a deadlock can occur or not in your program. [20 pts]

need  
 Mech 1 : A B C  
 Mech 2 : A C  
 Mech 3 : B C

Sem toolA, toolB, toolC

Void Mech1work()

While(working)

{

wait(toolA)

wait(toolB)

wait(toolC)

fix()

Signal(toolA)

Signal(toolB)

Signal(toolC)

break()

}

}

int main()

{

mech mech1, mech2, mech3

toolA, toolB, toolC = 1

mech1.mech1work()

mech2.mech2work()

mech3.mech3work()

While(!workDayOver);

return 0;

}

Void Mech2work()

While(working)

{

wait(toolA)

wait(toolC)

fix()

Signal(toolA)

Signal(toolC)

break()

}

}

Void Mech3work()

While(working)

{

wait(toolB)

wait(toolC)

fix()

Signal(toolB)

Signal(toolC)

break()

}

}

A deadlock may occur Because there exist a Circular wait which happens when

mech1 wait(a)

mech2 wait(b)

mech3 wait(c)

mech1 signal(a)

mech1 signal(b)

mech2 wait(a)

mech3 wait(b)

mech3 wait(c) Lock



P4)

#### Problem 4

Consider the following snapshot of a system. Answer the following questions: [24 pts]

Current available:	R1	R2	R3	R4
	2	1	0	0

  

Current Allocation:	P-R	R1	R2	R3	R4
	P1	0	0	1	2
	P2	2	0	0	0
	P3	0	0	3	4
	P4	2	3	5	4
	P5	0	3	3	2

  

Maximum Claim:	P-R	R1	R2	R3	R4
	P1	0	0	1	2
	P2	2	7	5	0
	P3	6	6	5	6
	P4	4	3	5	6
	P5	0	6	5	2

(a) What are the total number of resources present in the system?

a)  $tot = allocation + available$

R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>	R <sub>4</sub>
6	7	12	12

b) (b) Compute what each process might still need.

Need = Max - allocation

ALLOCATION					MAX					Need				
	R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>	R <sub>4</sub>		R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>	R <sub>4</sub>		R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>	R <sub>4</sub>
✓ P <sub>1</sub>	0	0	1	2	P <sub>1</sub>	0	0	1	2	P <sub>1</sub>	0	0	0	0
P <sub>2</sub>	2	0	0	0	P <sub>2</sub>	2	7	5	0	P <sub>2</sub>	0	7	5	0
P <sub>3</sub>	0	6	3	4	P <sub>3</sub>	0	6	5	6	P <sub>3</sub>	6	6	2	2
✓ P <sub>4</sub>	2	3	5	4	P <sub>4</sub>	4	3	5	6	P <sub>4</sub>	2	0	0	2
✓ P <sub>5</sub>	0	3	3	2	P <sub>5</sub>	0	6	5	2	P <sub>5</sub>	0	3	2	0

c) Is this system in a safe or unsafe state? Why?

① work = available

① Find i st

- finish<sub>i</sub> != true  
- need<sub>i</sub> ≤ work

if no i → ④

③ work = work + allocation

① work = 2 1 0 0

② need<sub>i=1</sub> = 0 0 0 0

③ work = 2 1 0 0  
+ 0 1 2 2  
= 2 2 2 2  
finish<sub>i=1</sub> = TRUE

② need<sub>i=4</sub> = 2 0 0 2

③ work = 2 2 2 2  
+ 1 2 5 4

② need<sub>i=5</sub> = 0 3 2 0

③ work = 4 5 7 6  
+ 0 6 5 2  
= 4 11 12 8  
finish<sub>i=5</sub> = true

② need<sub>i=2</sub> = 0 7 5 0

③ work = 4 11 12 8  
+ 2 0 0 0  
= 6 11 12 8

② need<sub>i=3</sub> = 6 6

③ work = 6 11  
+ 0 0  
= 6 11  
finish<sub>i=3</sub> = true

④ all finish<sub>i</sub> = true

2 2

12 8  
3 4  

---

15 12  
we

-TRUE



if no  $i \rightarrow (4)$

③  $work = work + allocation$   
 $Finish[i] = TRUE$   
 $\rightarrow$  ②

④ all  $Finish[i] = TRUE$ ?  
 SAFE

$$\begin{array}{r} \textcircled{3} \text{ work} = \begin{array}{cccc} 2 & 2 & 2 & 2 \\ + & 2 & 3 & 5 & 4 \\ \hline & 4 & 5 & 7 & 6 \end{array} \\ \text{Finish}_i = 4 = TRUE \end{array}$$

$$\begin{array}{r} + 2000 \\ = 61128 \end{array} \left. \begin{array}{l} \\ \end{array} \right\} \text{Finish}_i = 2 = TRUE$$

The system is safe b/c it passed BANKERS SAFETY TEST  $P_1 \Rightarrow P_4 \Rightarrow P_5 \Rightarrow P_2 \Rightarrow P_3$

(d) Is this system currently deadlocked? Why or why not?

NO b/c if the system runs in the sequence

$P_1 \Rightarrow P_4 \Rightarrow P_5 \Rightarrow P_2 \Rightarrow P_3$

it will remain safe

(e) Which processes, if any, are or may become deadlocked?

NONE when system follows sequence

(f) If a request from  $P_3$  arrives (0,1,0,0), can that request be safely granted? If granted, what would be the resulting state (safe, unsafe, deadlocked)? Which processes, if any, are or may become deadlocked if this request was immediately granted?

2100

Request

① if  $Request_i > Need_i \rightarrow ERROR$

② if  $Request_i \leq available$  goto ③ else wait

③  $ALLOCATION_i = ALLOCATION_i + REQUEST_i$   
 $Need_i = Need_i - Request_i$   
 $available = available - Request_i$

④ Run SAFE, if safe: grant? deny

① ✓  
 ② ✓  
 ③

$$\begin{array}{r} + \begin{array}{cccc} 0 & 0 & 3 & 4 \\ 0 & 1 & 0 & 0 \\ \hline 0 & 1 & 3 & 4 \end{array} \end{array}$$

$$\begin{array}{r} - \begin{array}{cccc} 2 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ \hline 2 & 0 & 0 & 0 \end{array} \end{array}$$

$$\begin{array}{r} - \begin{array}{cccc} 6 & 6 & 2 & 2 \\ 0 & 1 & 0 & 0 \\ \hline 6 & 5 & 2 & 2 \end{array} \end{array}$$

	ALLOCATION					MAX					Need			
	$R_1$	$R_2$	$R_3$	$R_4$		$R_1$	$R_2$	$R_3$	$R_4$		$R_1$	$R_2$	$R_3$	$R_4$
$P_1$	0	0	1	2	$P_1$	0	0	1	2	$P_1$	0	0	0	0
$P_2$	2	0	0	0	$P_2$	2	7	5	0	$P_2$	0	7	5	0
$P_3$	0	1	3	4	$P_3$	0	6	5	1	$P_3$	6	5	2	2



$P_2$	2	0	0	0
$P_3$	0	1	3	4
$P_4$	2	3	5	4
$P_5$	0	3	3	2

$P_2$	2	7	5	0
$P_3$	0	6	5	6
$P_4$	4	3	5	0
$P_5$	0	6	5	2

$P_2$	0	7	5	0
$P_3$	6	5	2	2
$P_4$	2	0	0	2
$P_5$	0	3	2	0

AVAILABLE = 2000

① work = 2000

Need<sub>i</sub> = 5

① work = available

② need<sub>i</sub> ≤ P<sub>i</sub>

Work = 4366

10332

4698

NOT SAFE

③ work = 2000  
- 0012  
2012

② Need<sub>i</sub> = 4

work = 2012  
2354  
4366

① Find i st

- Finish<sub>i</sub> != true

- Need<sub>i</sub> ≤ work

if no i → ④

② work = work + allocation  
Finish<sub>i</sub> = true  
→ ②

③ all Finish<sub>i</sub> = true?  
SAFE

Request cannot be safely given  
if request given, DEADLOCKED

$P_2 + P_3$  would be deadlocked if  
sequence  $P_1 \rightarrow P_4 \rightarrow P_5 \rightarrow$  NO NOT  
ENOUGH RESOURCES

## Problem 5

Write a program/pseudo-code to show how solving the dining philosophers problem can be done by allowing each philosopher to grab both chopsticks at once. Discuss any drawbacks of your solution. [10 pts]

int Mutex;

int main()

{

Mutex = 1;

do {

wait(mutex)

grab\_both()

signal(mutex)

DRAWBACKS:

① ONLY ONE Philo  
can eat at a time

② Can lead to starvation



eat()  
think()  
3 while(1);

### Problem 6

(a) Three processes share  $M$  resources units that can be reserved and released only one at a time. Each process needs a maximum of 3 units. What is the minimum value of  $M$  so that a deadlock cannot occur? [5pts]

	allocation	max	need
$P_1$	$x$	3	$3-x$
$P_2$	$x$	3	$3-x$
$P_3$	$x$	3	$3-x$

$$m = \text{tot} \\ \text{allocation} = 3x \\ \text{avail} = m - 3x$$

$$M - 3x \geq 3$$

$$M - 3 \geq 3$$

$$M \geq 6$$

$x=1$ , Max num proc hold while still allowing 1 proc to rec all units to finish

With  $M=6$ , a process can request max & complete op & release resources so no deadlock

(b)  $N$  processes share  $M$  resource units that can be reserved and released only one at a time. The maximum need of each process does not exceed  $M$ , and the sum of all maximum needs is less than  $M+N$ . Show that a deadlock cannot occur. [5 pts]

$$\text{need} < M+N$$

$$\sum_{i=1}^N \text{Need}_i < M+N$$

ASSUME ALL Procs holding some resources but fewer than max

$$\text{ALLOCATION} = \sum_{i=1}^N \text{Need}_i - N$$

$$\sum_{i=1}^N \text{need}_i = M+N - N$$

$$= \sum_{i=1}^N \text{need}_i = M$$

$$\text{AVAILABLE} = M - \left( \sum_{i=1}^N \text{Need}_i - N \right) \geq 0$$



Because sum of max needs of all procs  
is less than  $M+N$  & each process has at  
most  $Need_i - 1$  resources the remaining available  
resources will always be enough to satisfy  
the max needs of one process

Since there's always sufficient resources  
to meet max needs of at least one  
process, a sequence of allocations will  
always avoid a deadlock, c

EACH Proc can eventually be allocated  
its max resources, complete work, release  
& allow another proc to proceed

THUS deadlock cannot occur

