### BOSTON COLLEGE

### DOCTORAL THESIS

On the use of Coarse Grained Thermodynamic Landscapes to Efficiently Estimate Kinetic Pathways for RNA Molecules

Author: Supervisor: Evan Senter Dr. Peter Clote

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Clote Lab
Department of Biology

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## Ribofinder

#### 1.1 Introduction

In this chapter, we present the Ribofinder program—a pipeline to facilitate the detection of putative guanine riboswitches across genomic data. The Ribofinder tool operates in three stages. First we use Infernal and TransTermHP to detect putative aptamers and expression platforms, two distinct components of riboswitches described in section 1.2. After coalescing this data into a pool of candidate riboswitches, we use RNAfold with constraints based on experimental data to compute the two distinct structural conformations—'gene on' and 'gene off'. In the third and final stage, we leverage FoldAlign to measure the similarity between our candidate pool and a canonical guanine riboswitch well studied in the literature, the xpt G-box riboswitch from Bacillus subtilis.

#### 1.1.1 Organization

This chapter is organized in the following fashion. After providing background on the structural components of a riboswitch alongside their biological significance, we outline the deficiencies in the 'state of the art' software when as it relates specifically to riboswitch detection. We then move on to outline the three stages of Ribofinder: candidate selection, structural prediction, and candidate curation. Having described the approach of the software, we move on to present our findings in using Ribofinder to detect guanine riboswitches across the bacterial RefSeq database. Finally, we provide

brief commentary on possible extensions of the algorithm to locate other flavors of riboswitches, of which adenine-sensitive aptamers are a straightforward extension.

#### 1.2 Background

- 1.3 The Ribofinder pipeline
- 1.3.1 Step 1: Candidate selection
- 1.3.2 Step 2: Structural prediction
- 1.3.3 Step 3: Candidate curation
- 1.4 Using Ribofinder against the RefSeq database
- 1.5 Extending beyond guanine riboswitches

## **FFTbor**

#### 2.1 Introduction

In this chapter, we present the **FFTbor** algorithm and accompanying software. **FFTbor** is a novel algorithm developed with the intent of efficiently computing the Boltzmann probability of those structures whom, for a given input RNA sequence  $\mathbf{s}$ , differ by k base pairs. By leveraging polynomial interpolation via the Fast Fourier Transform, this algorithm runs in  $O(n^4)$  time and  $O(n^2)$  space, a significant improvement over its predecessor. The accompanying software which implements this algorithm has been used to predict the location of expression platforms for putative riboswitches in genomic data, and to evaluate the correlation between kinetic folding speed and landscape ruggedness.

#### 2.1.1 Organization

This chapter is organized in the following fashion. First, we provide background on the problem which FFTbor aims to address, as well as a brief overview of existing approaches. We follow by a formal explanation of the problem, and proceed to describe how the energy landscape is coarsified into discrete bins. We then develop the recursions for the parameterized partition function using the Nussinov-Jacobson energy model, which allows us to exposé the novel aspects of the algorithm. After developing the recursions, we indicate how they can be reformulated as a polynomial whose coefficients  $c_k = \mathbf{Z}_{1,n}^k$ . We then describe how the Fast Fourier Transform can be employed to efficiently compute the coefficients  $c_k$ , finishing our description of the underlying algorithm. Then we proceed to present two applications of FFTbor, an application to RNA kinetics and another

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to riboswitch detection in genomic data. Finally, we give reference to the full recursions using the more accurate Turner energy model, which the underlying implementation actually uses.

#### 2.2 Background

#### 2.3 Formalization of the problem

**FFTbor** aims to compute the coefficients  $p_0, \ldots, p_{n-1}$  of the polynomial

$$p(x) = p_0 + p_1 x + p_2 x^2 + \dots + p_{n-1} x^{n-1},$$
(2.1)

where  $p_k$  is defined as  $p_k = \frac{Z_k}{Z}$ . We employ the Fast Fourier Transform to compute the inverse Discrete Fourier Transform on values  $y_0, \ldots, y_{n-1}$ , where  $y_k = p(\omega^k)$  and  $\omega = e^{2\pi i/n}$  is the principal nth complex root of unity and p(x) is defined in (2.1). By leveraging complex roots of unity in conjunction with the inverse Discrete Fourier Transform the we subvert numeric instability issues observed with both Lagrange interpolation and Gaussian elimination.

Consider an RNA sequence  $\mathbf{s} = s_1, \ldots, s_n$ , where  $s_i \in \{A, C, G, U\}$ , i.e. a sequence of nucleotides. We can describe a secondary structure  $\mathcal{S}$  which is compatible with  $\mathbf{s}$  as a collection of base pair tuples (i, j), where  $1 \le i \le i + \theta < j \le n$  and  $\theta \ge 0$ —generally taken to be 3, the minimum number of unpaired bases in a hairpin loop due to steric constraints.

To more simply develop the underlying recursions for FFTbor, we introduce a number of constraints on the base pairs within S. Firstly, we require that each base pair is either a Watson-Crick or G-U wobble, i.e. base pair (i,j) for sequence  $\mathbf{s}$  has corresponding nucleotides  $(s_i,s_j)$ , which are restricted to the set  $\mathbb{B}=\{(A,U),(U,A),(G,C),(C,G),(G,U),(U,G)\}$ . With this constraint satisfied we say that S is compatible with  $\mathbf{s}$ , and for the remainder of this chapter will only consider those structures which are compatible with  $\mathbf{s}$ . Secondly, we insist that given two base pairs (i,j),(x,y) from S,  $i=x\iff j=y$ —bases have at most one partner. Finally, we require that  $i< x< j\iff i< y< j$ , no pseudoknots are allowed. While pseudoknots have been shown to be present in some biologically relevant RNAs, their inclusion greatly complicates the recursive decomposition of the structure, and thus it is common to ignore them.

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Provided two secondary structures S, T, we can define a notion of distance between them. There are a number of different definitions of distance used across the literature; we will use *base pair distance* for **FFTbor**. Base pair distance is defined as the symmetric difference between the sets S, T

$$d_{BP}(S,T) = |S \cup T| - |S \cap T| \tag{2.2}$$

- 2.4 Derivation of the FFTbor algorithm
- 2.4.1 Definition of the partition function  $\mathbf{Z}_{1,n}^k$
- 2.4.2 Recursions to compute the polynomial  $\mathcal{Z}_{i,j}(x)$
- 2.4.3 Polynomial interpolation to evaluate  $\mathcal{Z}_{i,j}(x)$
- 2.5 Coarse-grained kinetics with FFTbor
- 2.6 Riboswitch detection with FFTbor
- 2.7 Benchmarking and performance considerations

# FFTbor2D

#### 3.1 Introduction

In this chapter, we present the FFTbor2D algorithm and accompanying software. FFTbor2D, like FFTbor described in Chapter 2, is an algorithm which computes the paramerized partition function for an input RNA sequence s. FFTbor2D computes the two-dimensional coarse energy landscape for s given two compatible input secondary structures  $\mathcal{A}$  and  $\mathcal{B}$ , where position (x,y) on the discrete energy landscape corresponds to the Boltzmann probability for those structures  $\mathcal{S}$  which have  $d_{BP}(\mathcal{S},\mathcal{A}) = x$  and  $d_{BP}(\mathcal{S},\mathcal{B}) = y$  (where  $d_{BP}$  is as defined in equation 2.2). By again leveraging the Fast Fourier Transform, FFTbor2D runs in  $O(n^5)$  time and only uses  $O(n^2)$  space—a significant improvement over previous approaches. This permits the output energy landscape to be used in a high-throughput fashion to analyze folding kinetics; a topic covered in detail in Chapter 4.

#### 3.1.1 Organization

This chapter is organized in the following fashion. Because the history for this work arises naturally from the background described in section 2.2, we forego reiteration and instead fall directly into a technical discussion of the underlying algorithm. We first develop the recursions for the Nussinov energy model for expository clarity, the underlying implementation uses the more complicated and robust Turner energy model. Recursions in place, we then move to show how these lead to a single variable polynomial P(x) whose coeffecients can be computed by the inverse Discrete Fourier Transform,

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and map to the 2D energy landscape. We describe two exploitations of P(x), a parity condition and complex conjugates which further reduce the runtime by a factor of 4. Finally, we contrast this software against RNA2Dfold, and outline the performance characteristics of both softwares and highlight the benefits and drawbacks of both.

#### 3.2 Derivation of the FFTbor2D algorithm

- 3.2.1 Definition of the partition function  $\mathbf{Z}_{1,n}^{x,y}$
- 3.2.2 Recursions to compute the polynomial  $\mathcal{Z}_{i,j}(x)$
- 3.2.3 Polynomial interpolation to evaluate  $\mathcal{Z}_{i,j}(x)$
- 3.3 Acceleration of the FFTbor2D algorithm
- 3.3.1 Optimization due to parity condition
- 3.3.2 Optimization due to complex conjugates
- 3.4 Benchmarking and performance considerations
- 3.5 Applications of the FFTbor2D algorithm

# Hermes

## 4.1 Introduction

### 4.1.1 Organization

This chapter is organized in the following fashion.

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4.2	Background	$\mathbf{l}$
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- 4.3 Traditional approaches for kinetics
- 4.3.1 Mean first passage time
- 4.3.2 Equilibrium time
- 4.4 Software within the Hermes suite
- 4.4.1 Exact equilibrium time with RNAeq
- 4.4.2 Approximate equilibrium time with FFTeq
- 4.4.3 Exact mean first passage time with RNAmfpt
- 4.4.4 Approximate mean first passage time with FFTmfpt
- 4.5 Correlations of kinetics data across software
- 4.6 Population occupancy curves with FFTeq