

12

Interpreters

The tools we use have a profound (and devious!) influence on our thinking habits, and, therefore, on our thinking abilities.

Edsger Dijkstra, *How do we tell truths that might hurt?*

Languages are powerful tools for thinking. Different languages encourage different ways of thinking and lead to different thoughts. Hence, inventing new languages is a powerful way for solving problems. We can solve a problem by designing a language in which it is easy to express a solution, expressing the solution in that language, and implementing an interpreter for that language.

An *interpreter* is just a program. As input, it takes a specification of a program in some language. As output, it produces the output of the input program. By designing a new interpreter, we can invent a new language.

In this chapter, we explore how to implement an interpreter. We also introduce the Python programming language, and describe a Python program that implements an interpreter for a subset of the Scheme language. Implementing an interpreter further blurs the line between *data* and *programs*, that we first crossed in Chapter 3 by passing procedures as parameters and returning new procedures as results. Now that we are implementing an interpreter, all programs are just data input for the interpreter program. The meaning of the program is determined by the interpreter.

12.1 Building Languages

To implement an interpreter for a given target language we need to:

1. Implement a *parser* that takes as input a string representation of a program in the target language and produces a structural parse of the input program. The parser should break the input string into its language components, and form a parse tree data structure that represents the input text in a structural way. Section 12.3 describes our

evaluator

parser implementation.

2. Implement an *evaluator* that takes as input a structural parse of an input program, and evaluates that program. The evaluator should implement the target language's evaluation rules. Section 12.4 describes our evaluator.

Our target language is a simple subset of Scheme we call *Charme*.¹



The Charme language is very simple, yet is powerful enough to express all computations (that is, it is a universal programming language). Its evaluation rules are a subset of the statefull evaluation rules for Scheme. Charme includes the application expression, if expression, lambda expression, name expression, and definitions. It supports integral numbers, and provides the basic arithmetic and comparison primitives with the same meanings as they have in Scheme.

The full grammar and evaluation rules for Charme are given in Section 12.4. The evaluator implements those evaluation rules.

Before describing our interpreter implementation, the next section introduces Python, the programming language we use to implement the interpreter (and for most of the rest of the programs in this book).

12.2 Python

We could implement a Charme interpreter using Scheme (or any other universal programming language), but choose to implement it using the programming language Python. Python is a popular programming language initially designed by Guido van Rossum in 1991.² Python is freely available from <http://www.python.org>.

Python is widely used to develop dynamic web applications and as a scripting language for applications. Python was used to manage special effects production for Star Wars: Episode II, and is used extensively in many organizations including Google, reddit.com, and NASA.³

We use Python instead of Scheme to implement our Charme interpreter for

¹The original name of Scheme was “Schemer”, a successor to the languages “Planner” and “Conniver”. Because the computer on which “Schemer” was implemented only allowed six-letter file names, its name was shortened to “Scheme”. In that spirit, we name our snake-charming language, “Charmer” and shorten it to Charme. Depending on the programmer’s state of mind, the language name can be pronounced either “charm” or “charme”.

²The name *Python* alludes to Monty Python’s Flying Circus.

³See <http://www.python.org/about/quotes/> for more descriptions of Python uses.

a few reasons. The first reason is pedagogical: it is instructive to learn new languages. As Dijkstra's quote at the beginning of this chapter observes, the languages we use have a profound effect on how we think. This is true for natural languages, but also true for programming languages. Different languages make different styles of programming more convenient, and it is important for every programmer to be familiar with many different styles of programming.

All of the major concepts we have covered so far apply to Python nearly identically to how they apply to Scheme, but seeing them in the context of a different language should make it clearer what the fundamental concepts are and what are artifacts of a particular programming language. Another reason for using Python is that it provides some features that enhance expressiveness that are not available in Scheme. These include built-in support for objects and imperative control structures.

The grammar for Python is quite different from the Scheme grammar, so Python programs look very different from Scheme programs. In most respects, however, the evaluation rules are quite similar to the evaluation rules for Scheme. This chapter does not describe the entire Python language, but instead introduces the grammar rules and evaluation rules for different Python constructs as we need them to implement our interpreter. For more complete documentation on Python see <http://www.python.org>.

Like Scheme, Python is a *universal programming language*: both languages are capable of expressing *all* mechanical computations. For any computation we can express in Scheme, there is a Python program that defines the same computation. Conversely, every Python program has an equivalent Scheme program.

One piece of evidence that every Scheme program has an equivalent Python program is the interpreter we develop in this chapter. Since we can implement an interpreter for a Scheme-like language in Python, we know we can express every computation that can be expressed by a program in that language with an equivalent Python program (that is, the Charm interpreter implemented in Python with the original Charm program as input).

Tokenizing. We introduce Python using one of the procedures in our interpreter implementation. We divide the job of parsing into two procedures that are combined to solve the problem of transforming an input string into a list describing the input program's structure. The first part is the *tokenizer* which *tokenizes* an input string. Its input is the input string in the target programming language, and its output is a list of the tokens in that string.

A *token* is an indivisible syntactic unit. For example, the Charm expression, `(define square (lambda (x) (* x x)))`, contains the tokens: `(`, `define`,



square, (, lambda, (, x,), (, *, x, x,),), and). The tokens are separated by whitespace (spaces, tabs, and newlines). Punctuation marks such as the left and right parentheses are tokens by themselves; even when they are adjacent to non-whitespace characters these marks are considered independent tokens.

The *tokenize* procedure below takes as input a string *s* in the Charmé target language, and produces as output a list of the tokens in *s*. We describe the Python language constructs it uses next.

```
def tokenize(s):
    current = " # the empty string (two single quotes)
    tokens = [] # the empty list
    for c in s: # for each character, c, in the string s
        if c.isspace(): # if c is a whitespace
            if len(current) > 0: # if the current token is non-empty
                tokens.append(current) # add it to the list
                current = " # reset current token to empty string
            elif c in '()': # else, if c is a parenthesis
                if len(current) > 0: # end the current token
                    tokens.append(current)
                    current = "
                tokens.append(c) # add the parenthesis to the token list
            else: # otherwise (it is an alphanumeric)
                current = current + c # add the character to the current token
    # end of the for loop (by indentation); reached the end of s
    if len(current) > 0: # if there is a current token add it
        tokens.append(current)
    return tokens # the result is the list of tokens
```

12.2.1 Python Programs

Whereas Scheme programs are composed of expressions and definitions, Python programs are mostly sequences of statements. Unlike expressions which (mostly) evaluate to values, a statement has no value. The emphasis on statements reflects (and impacts) the style of programming used with Python. It is more imperative than that used with Scheme: instead of composing expressions in ways that pass the result of one expression as an operand to the next expression, Python programs typically consist of a sequence of statements, each of which alters the state in some way towards reaching the goal state. Nevertheless, it is possible (but not recommended) to program in Scheme using an imperative style (emphasizing **begin** and **set!** expressions), and it is possible (but not recommended) to program in

Python using a functional style (emphasizing procedure applications and eschewing the assignment statement).

Defining a procedure in Python is similar to defining a procedure in Scheme, except the grammar rule is different:

```

ProcedureDefinition ::= def Name ( Parameters ) : Block
Parameters          ::=  $\epsilon$ 
Parameters          ::= SomeParameters
SomeParameters      ::= Name
SomeParameters      ::= Name , SomeParameters

Block                ::= Statement
Block                ::= <newline> indented(Statements)
Statements          ::= Statement <newline> MoreStatements
MoreStatements      ::= Statement <newline> MoreStatements
MoreStatements      ::=  $\epsilon$ 

```

Unlike in Scheme, the whitespace (such as new lines) has meaning in Python. Statements cannot be separated into multiple lines, and only one statement may appear on a single line. Indentation within a line also matters. Instead of using parentheses to provide code structure, Python uses the indentation to group statements into blocks. The Python interpreter will report an error if the indentation of the code does not match its structure.

Since whitespace matters in Python, we include newlines (<**newline**>) and indentation in our grammar. We use *indented(elements)* to indicate that the *elements* are indented. For example, the rule for *Block* is a newline, followed by one or more statements. The statements are all indented one level inside the block's indentation. This means it is clear when the block's statements end because the next line is not indented to the same level.

The evaluation rule for a procedure definition is similar to the rule for evaluating a procedure definition in Scheme.

Python Procedure Definition. The procedure definition,

```
def Name (Parameters ) : Block
```

defines *Name* as a procedure that takes as inputs the *Parameters* and has the body expression *Block*.

The procedure definition

```
def tokenize(s): ...
```

defines a procedure named *tokenize* that takes a single parameter, *s*.

Assignment. The body of the procedure uses several different types of Python statements. Following Python’s more imperative style, five of the statements in *tokenize* are assignment statements. For example, the assignment statement, *tokens* = [] assigns the value [] (the empty list) to the name *tokens*.

The grammar for the assignment statement is:

<i>Statement</i>	$::\Rightarrow$	<i>AssignmentStatement</i>
<i>AssignmentStatement</i>	$::\Rightarrow$	<i>Target</i> = <i>Expression</i>
<i>Target</i>	$::\Rightarrow$	<i>Name</i>

For now, we use only a *Name* as the left side of an assignment, but since other constructs can appear on the left side of an assignment statement, we introduce the nonterminal *Target* for which additional rules can be defined to encompass other possible assignees. Anything that can hold a value (such as an element of a list) can appear as the target of an assignment.

The evaluation rule for an assignment statement is similar to Scheme’s evaluation rule for set expressions: the meaning of *x* = *e* in Python is similar to the meaning of (set! *x* *e*) in Scheme, except that the target *Name* need not exist before the assignment. In Scheme, evaluating (set! *x* 7) where the name *x* was not previously defined is an error; in Python, if *x* is not already defined, evaluating *x* = 7 creates a new place named *x*.

Python Evaluation Rule: Assignment. To evaluate an assignment statement, evaluate the expression, and assign the value of the expression to the place identified by the target. If no such place exists, create a new place with that name.

Arithmetic and Comparison Expressions. Like Scheme, Python supports many different kinds of expressions for performing arithmetic and comparisons. Since Python does not use parentheses to group expressions, the grammar provides the grouping by breaking down expression in several steps. This defines an order of *precedence* for parsing expressions. If a complex expression includes many expressions, the grammar specifies how they will be grouped. For example, consider the expression 3+4*5. In Scheme, the expressions (+ 3 (* 4 5)) and (* (+ 3 4) 5) are clearly different and the parentheses group the subexpressions. The meaning of the Python

expression $3+4*5$ is $(+ 3 (* 4 5))$, that is, it evaluates to 23. The expression $4*5+3$ also evaluates to 23.

This makes the Python grammar rules more complex since they must deal with $*$ and $+$ differently, but it makes the meaning of Python expressions match our familiar mathematical interpretation, without needing all the parentheses needed in Scheme expressions. The way this is done is by defining the grammar rules so an *AddExpression* can contain a *MultExpression* as one of its subexpressions, but a *MultExpression* cannot contain an *AddExpression*. This makes the multiplication operator have *higher precedence* than the addition operator. If an expression contains both $+$ and $*$ operators, the $*$ operator attaches to its operands first. The replacement rules that happen first have lower precedence, since their components must be built from the remaining pieces.

Here are the grammar rules for Python expressions for comparison, multiplication, and addition expressions that achieve this:

<i>Expression</i>	$::\Rightarrow$ <i>CompExpr</i>
<i>CompExpr</i>	$::\Rightarrow$ <i>CompExpr</i> <i>Comparator</i> <i>CompExpr</i>
<i>Comparator</i>	$::\Rightarrow$ $< \mid > \mid == \mid <= \mid >=$
<i>CompExpr</i>	$::\Rightarrow$ <i>AddExpression</i>
<i>AddExpression</i>	$::\Rightarrow$ <i>AddExpression</i> $+$ <i>MultExpression</i>
<i>AddExpression</i>	$::\Rightarrow$ <i>AddExpression</i> $-$ <i>MultExpression</i>
<i>AddExpression</i>	$::\Rightarrow$ <i>MultExpression</i>
<i>MultExpression</i>	$::\Rightarrow$ <i>MultExpression</i> $*$ <i>PrimaryExpression</i>
<i>MultExpression</i>	$::\Rightarrow$ <i>PrimaryExpression</i>
<i>PrimaryExpression</i>	$::\Rightarrow$ <i>Literal</i>
<i>PrimaryExpression</i>	$::\Rightarrow$ <i>Name</i>
<i>PrimaryExpression</i>	$::\Rightarrow$ $($ <i>Expression</i> $)$

The last rule allows parentheses to be used to group expressions. For example, $(3 + 4) * 5$ is parsed as the *PrimaryExpression*, $(3 + 4)$, times 5, so it evaluates to 35; without the parentheses, $3 + 4 * 5$ is parsed as 3 plus the *MultExpression*, $4 * 5$, so it evaluates to 23.

A *Literal* can be a numerical constant. Numbers in Python are similar (but not identical) to numbers in Scheme. In the example program, we use the integer literal 0.

A *PrimaryExpression* can also be a name, similar to names in Scheme. The

evaluation rule for a name in Python is similar to the stateful rule for evaluating a name in Scheme⁴.

Exercise 12.1. Do comparison expressions have higher or lower precedence than addition expressions? Explain why using the grammar rules.

Exercise 12.2. Draw the parse tree for each of the following Python expressions and provide the value of each expression.

- a. `1 + 2 + 3 * 4`
- b. `3 > 2 + 2`
- c. `3 * 6 >= 15 == 12`
- d. `(3 * 6 >= 15) == True`

12.2.2 Data Types

Python provides many built-in data types. We describe three of the most useful data types here: lists, strings, and dictionaries.

Lists. Python provides a list datatype similar to lists in Scheme, except instead of building list from simpler parts (that is, using *cons* pairs in Scheme), the Python list type is provided as a built-in datatype. The other important difference is that Python lists are mutable.

Lists are denoted in Python using square brackets. For example, `[]` denotes an empty list, and `[1, 2]` denotes a list containing two elements. As in Scheme, the elements of a list can be of any type (including another list).

Elements can be selected from a list using the list subscription expression:

$$\begin{aligned} \text{PrimaryExpression} &::\Rightarrow \text{SubscriptExpression} \\ \text{SubscriptExpression} &::\Rightarrow \text{PrimaryExpression} [\text{Expression}] \end{aligned}$$

If the first primary expression evaluates to a list, the subscript expression selects the element indexed by value of the inner expression from the list. For example,

```
>>> a = [1, 2, 3]
>>> a[0]
1
```

⁴There are some subtle differences and complexities (see Section 4.1 of the Python Reference Manual, however, which we do not go into here).


```

>> a[1+1]
3
>> a[3]
IndexError: list index out of range

```

So, the expression $p[0]$ in Python is analogous to $(car\ p)$ in Scheme.

We can also use negative selection indexes to select elements from the back of the list. The expression $p[-1]$ selects the last element in the list p .

The running time of a list selection operation in Python is approximately constant: it does not depend on the length of the list even if the selection index is the end of the list. The reason for this is that Python stores lists internally differently from how Scheme stores them as arbitrary pairs. The elements of a List are stored as a block in memory, so the location of the k^{th} element can be calculated by adding Sk to the location of the start of the list where S is a constant representing the size of each element in the list.

A subscript expression can also select a range of elements from the list:

$$\begin{aligned} \text{SubscriptExpression} &::\Rightarrow \text{PrimaryExpression} [\text{Bound}_{Low} : \text{Bound}_{High}] \\ \text{Bound} &::\Rightarrow \text{Expression} \mid \epsilon \end{aligned}$$

The subscript expression evaluates to a list containing the elements between the low bound and the high bound. If the low bound is missing, the low bound is the beginning of the list. If the high bound is missing, the high bound is the end of the list. For example,

```

>> a = [1, 2, 3]
>> a[:1]
[1]
>> a[1:]
[2, 3]
>> a[4-2:3]
[3]
>> a[:]
[1, 2, 3]

```

So, the expression $p[1:]$ in Python is analogous to $(cdr\ p)$ in Scheme.

Python lists are mutable (the value of a list can change after it is created). We can use list subscripts as the targets for an assignment expression:

$$\text{Target} ::\Rightarrow \text{SubscriptExpression}$$

For example,

```
>>> a = [1, 2, 3]
>>> a[0] = 7
>>> a
[7, 2, 3]
>>> a[1:4] = [4, 5, 6]
>>> a
[7, 4, 5, 6]
>>> a[1:] = [6]
>>> a
[7, 6]
```

Note that assignments can not only be used to change the values of elements in the list, but also to change the length of the list.

In the *tokenize* procedure, we use *tokens = []* to initialize *tokens* to an empty list, and use *tokens.append(current)* to append an element to the *tokens* list. The Python *append* procedure is similar to the *mlist-append!* procedure (except it works on the empty list, where there is no way in Scheme to modify the null input list).

Strings. The other datatype used in *tokenize* is the string datatype, named *str* in Python. As in Scheme, a String is a sequence of characters. Unlike Scheme Strings and Python Lists, which are mutable, the Python *str* datatype is immutable. So, once a string is created its value cannot change. This means all the string methods that seem to change the value of a string actually return a new string (for example, *capitalize()* returns a copy of the string with its first letter capitalized).

Strings are enclosed in quotes, which (unlike in Scheme where single quotes cannot be used) can be either single quotes (e.g., 'hello') or double quotes (e.g., "hello"). In our example program, we use the assignment expression, *current = "* (two single quotes), to initialize the value of *current* to the empty string. The input, *s*, is a string object.

Dictionaries. A dictionary is a lookup-table where values are associated with keys. The keys can be any immutable type (strings and numbers are commonly used as keys); the values can be of any type. We did not use the dictionary type in *tokenize*, but it is very useful for implementing frames in the evaluator.

A dictionary is denoted using curly brackets. The empty dictionary is *{}*. We can add a key-value pair to the dictionary using an assignment where the left side is a subscript expression that specifies the key and the right side is the value assigned to that key. For example,

```
birthyear = {}  
birthyear['Euclid'] = '300BC'  
birthyear['Ada Lovelace'] = 1815  
birthyear['Alan Turing'] = 1912  
birthyear['Alan Kay'] = 1940
```

defines *birthdays* as a dictionary containing four entries. The keys are all strings; the values are numbers, except for Euclid's entry which is a string.

We can obtain the value associated with a key in the dictionary using a subscript expression. For example, *birthyear*['Alan Turing'] evaluates to 1912. We can replace the value associated with a key using the same syntax as adding a key-value pair to the dictionary. The statement,

```
birthyear['Euclid'] = -300
```

replaces the value of *birthyear*['Euclid'] with the number -300 .

The dictionary type also provides a method *has_key* that takes one input and produces a Boolean indicating if the dictionary object contains the input value as a key. For the *birthyear* dictionary, *birthyear.has_key*('John Backus') evaluates to False and *birthyear.has_key*('Ada Lovelace') evaluates to True.

The dictionary type lookup and update operations have approximately constant running time in most cases: the time it takes to lookup the value associated with a key does not scale as the size of the dictionary increases. This is done by computing a number based on the key that determines where the associated value would be stored (if that key is in the dictionary). The number is used to index into a structure similar to a Python list (so it has constant time to retrieve any element). Mapping keys to appropriate numbers to avoid many keys mapping to the same location in the list is a difficult problem, but one the Python dictionary object does well for typical sets of keys.

12.2.3 Objects and Methods

In Python, every data value, including lists and strings, is an object. This means the way we manipulate data is to invoke methods on objects. The list datatype provides methods for manipulating and observing lists. The grammar rules for expressions that call procedures are:

$$\begin{aligned}
\text{PrimaryExpression} &::\Rightarrow \text{CallExpression} \\
\text{CallExpression} &::\Rightarrow \text{PrimaryExpression (ArgumentList)} \\
\text{ArgumentList} &::\Rightarrow \text{SomeArguments} \\
\text{ArgumentList} &::\Rightarrow \epsilon \\
\text{SomeArguments} &::\Rightarrow \text{Expression} \\
\text{SomeArguments} &::\Rightarrow \text{Expression , SomeArguments}
\end{aligned}$$

To invoke a method we use the same rules, but the *PrimaryExpression* of the *CallExpression* specifies an object and method:

$$\begin{aligned}
\text{PrimaryExpression} &::\Rightarrow \text{AttributeReference} \\
\text{AttributeReference} &::\Rightarrow \text{PrimaryExpression . Name}
\end{aligned}$$

The name *AttributeReference* is used since the same syntax is used for accessing the internal state of objects as well.

The *tokenize* procedure includes five method applications, four of which are *tokens.append(current)*. The object reference is *tokens*, the list of tokens in the input. The list *append* method takes one parameter and adds that value to the end of the list.

The other method invocation is *c.isspace()* where *c* is a string consisting of one character in the input. The *isspace* method for the string datatype returns true if the input string is non-empty and all characters in the string are whitespace (either spaces, tabs, or newlines).

The *tokenize* procedure also uses the built-in function *len*. The *len* function takes as input an object of a collection datatype (including a list or a string), and outputs the number of elements in the collection. It is a procedure, not a method; the input object is passed in as a parameter. In *tokenize*, we use *len(current)* to find the number of characters in the current token.

12.2.4 Control Statements

Python provides control statements for making decisions, looping, and for returning from a procedure.

If. Python's if-statement is similar to both the if-expression and conditional-expression in Scheme:

```

Statement ::= IfStatement
IfStatement ::= if Expressionpredicate : Block Elifs OptElse
Elifs ::=  $\epsilon$ 
Elifs ::= elif Expressionpredicate : Block Elifs
OptElse ::=  $\epsilon$ 
OptElse ::= else : Block

```

The evaluation rule is similar to Scheme's conditional expression. First, the *Expression_{predicate}* of the *if* is evaluated. If it evaluates to a true value, the consequent *Block* is evaluated, and none of the rest of the *IfStatement* is evaluated. Otherwise, each of the *elif* predicates is evaluated in order. If one evaluates to a true value, its *Block* is evaluated and none of the rest of the *IfStatement* is evaluated. If none of the *elif* predicates evaluates to a true value, the *else Block* is evaluated (if there is one).

The main if-statement in *tokenize* is:

```

if c.isspace():
    ...
elif c in '()':
    ...
else:
    current = current + c

```

The first if predicate tests if the current character is a space. If so, the end of the current token has been reached. The consequent *Block* is itself an *IfStatement*:

```

if len(current) > 0:
    tokens.append(current)
    current = ""

```

If the current token has at least one character, it is appended to the list of tokens in the input string and the current token is reset to the empty string. This *IfStatement* has no *elif* or *else* clauses, so if the predicate is false, there is nothing to do. Unlike in Scheme, there is no need to have an alternate clause, since the Python if-statement does not need to produce a value.

If the predicate for the main if-statement is false, evaluation proceeds to the *elif* clause. The predicate for this clause tests if *c* is in the set of characters given by the literal string '()'. That is, it is true if *c* is either an open or close parentheses. As with spaces, a parenthesis ends the previous token, so the first statement in the *elif* clauses is identical to the first consequent clause. The difference is unlike spaces, we need to keep trace of the parentheses, so it is added to the token list by *tokens.append(c)*.

The final clause is an *else* clause, so its body will be evaluated if neither the **if** or **elif** predicate is true. This means the current character is not a space or a parenthesis, so it is some other character. It should be added to the current token. This is done by the assignment expression, *current* = *current* + *c*. The addition operator in Python works on strings as well as numbers (and some other datatypes). For strings, it concatenates the operands into a new string. Recall that strings are immutable, so there is no equivalent to the list *append* method. Instead, appending a character to a string involves creating a new string object.

For. A **for** statement provides a way of iterating through a set of values, carrying out a body block for each value.

$$\begin{aligned} \text{Statement} &::\Rightarrow \text{ForStatement} \\ \text{ForStatement} &::\Rightarrow \text{for } \text{Target} \text{ in } \text{Expression} : \text{Block} \end{aligned}$$

The *Target* (as was used in the assignment statement) is typically a variable name. The value of the *Expression* is a collection of elements. To evaluate a for statement, each value of the *Expression* collection is assigned to the *Target* in order, and the *Block* is evaluated once for each value.

Other than the first two initializations, and the final two statements, the bulk of the *tokenize* procedure is contained in a **for** statement. The for-statement in *tokenize* header is **for** *c* **in** *s*. The string *s* is the input string, a collection of characters. So, the loop will repeat once for each character in *s*, and the value of *c* is each character in the input string (represented as a singleton string), in turn.

Return. In Scheme, the body of a procedure is an expression and the value of that expression is the result of evaluating an application of the procedure. In Python, the body of a procedure is a block of one or more statements. Statements have no value, so there is no obvious way to decide what the result of a procedure application should be. Python's solution is to use a return statement.

The grammar for the return statement is:

$$\begin{aligned} \text{Statement} &::\Rightarrow \text{ReturnStatement} \\ \text{ReturnStatement} &::\Rightarrow \text{return } \text{Expression} \end{aligned}$$

A return statement finishes execution of a procedure, returning the value of the *Expression* to the caller as the result.

The last statement of the *tokenize* procedure is:

```
return tokens
```

It returns the value of the *tokens* list to the caller.

12.3 Parser

The parser takes as input a Charme program string, and produces as output a Python list that encodes the structure of the input program. The first step is to break the input string into tokens; this is what the *tokenize* procedure defined in the previous section does.

The next step is to take the list of tokens and produce a data structure that encodes the structure of the input program. Since the Charme language is built from simple parenthesized expressions, we can represent the parsed program as a list. But, unlike the list returned by *tokenize* which is a flat list containing the tokens in order, the list returned by *parse* is a structured list that may have lists (and lists of lists, etc.) as elements.

Charme's syntax makes implementing the parser fairly simple, since the grammar rules for Scheme are very simple since we can break an expression into its components just by using the parentheses and whitespace. The parser needs to balance the open and close parentheses that enclose expressions. For example, if the input string is "(define square (lambda (x) (* x x)))" the output of *tokenizer* is the list:

```
[('(', 'define', 'square', '(', 'lambda', '(', 'x', ')', '(', '*', 'x', 'x', ')', ')', ')']
```

The parser structures the tokens according to the program structure, producing a parse tree that record the structure of the input program. The parenthesis provide the program structure, so are removed from the parse tree. For the example, the resulting parse tree is:

```
['define',  
 'square',  
 [ 'lambda',  
   ['x'],  
   ['*', 'x', 'x']  
 ]  
 ]
```

The output parse structure is a list containing three elements, the first is the keyword 'define', the second is the name 'square', and the third is a list containing three elements, ['lambda', ['x'], ['*', 'x', 'x']], the third of which is itself a list containing three elements.

Here is the definition of *parse*:

```
def parse(s):
    def parsetokens(tokens, inner):
        res = []
        while len(tokens) > 0:
            current = tokens.pop(0)
            if current == '(':
                res.append(parsetokens(tokens, True))
            elif current == ')':
                if inner: return res
            else:
                error('Unmatched close paren: ' + s)
                return None
            else:
                res.append(current)

        if inner:
            error('Unmatched open paren: ' + s)
            return None
        else:
            return res

    return parsetokens(tokenize(s), False)
```

The input to *parse* is a string in the target language. The output is a list of the parenthesized-expressions in the input. Here are some examples:

```
>>> parse('150')
['150']
>>> parse('( + 1 2 )')
[['+', '1', '2']]
>>> parse('( + 1 ( * 2 3 ) )')
[['+', '1', ['*', '2', '3']]]
>>> parse('(define square (lambda (x) (* x x)))')
[['define', 'square', ['lambda', ['x'], ['*', 'x', 'x']]]]
>>> parse('( + 1 2 ) ( + 3 4 )')
[['+', '1', '2'], ['+', '3', '4']]
```

The parentheses are no longer included as tokens in the result, but their presence in the input string determines the structure of the result.

recursive descent The *parse* procedure implements what is known as a *recursive descent* parser. The main *parse* procedure defines the *parsetokens* helper procedure and returns the result of calling it with inputs that are the result of tokenizing the input string and the Boolean literal `False`: `return parsetokens(tokenize(s), False)`.

The *parsetokens* procedure takes two inputs: *tokens*, a list of tokens (that results from the *tokenize* procedure); and *inner*, a Boolean that indicates whether the parser is inside a parenthesized expression. The value of *inner* is *False* for the initial call since the parser starts outside a parenthesized expression. All of the recursive calls result from encountering a '(', so the value passed as *inner* is *True* for all the recursive calls.

The body of the *parsetokens* procedure initializes *res* to an empty list that will be used to store the result. Then, the **while** statement iterates as long as the token list contains at least one element. The first statement of the **while** statement block assigns *tokens.pop(0)* to *current*. The *pop* method of the list takes a parameter that selects an element from the list. The selected element is returned as the result. The *pop* method also mutates the list object by removing the selected element. So, *tokens.pop(0)* returns the first element of the *tokens* list and removes that element from the list. This is similar to (*cdr tokens*) with one big difference: the *tokens* object is modified by the call. This is essential to the parser making progress: every time the *tokens.pop(0)* expression is evaluated the number of elements in the token list is reduced by one.

If the *current* token is an open parenthesis, *parsetokens* is called recursively to parse the inner expression (that is, all the tokens until the matching close parenthesis). The result is a list of tokens, which is appended to the result. If the *current* token is a close parenthesis, the behavior depends on whether or not the parser is parsing an inner expression. If it is inside an expression (that is, an open parenthesis has been encountered with no matching close parenthesis yet), the close parenthesis closes the inner expression, and the result is returned. If it is not in an inner expression, the close parenthesis has no matching open parenthesis so a parse error is reported. The **else** clause deals with all other tokens by appending them to the list.

12.4 Evaluator

The evaluator takes a list representing a parsed program fragment in Charme and an environment, and outputs the result of evaluating the input code in the input environment. The evaluator implements the evaluation rules for the target language.

The core of the evaluator is the procedure *meval*:

```
def meval(expr, env):  
    if isPrimitive(expr): return evalPrimitive(expr)  
    elif isIf(expr): return evalIf(expr, env)  
    elif isDefinition(expr): evalDefinition(expr, env)
```

```

elif isName(expr): return evalName(expr, env)
elif isLambda(expr): return evalLambda(expr, env)
elif isApplication(expr): return evalApplication(expr, env)
else: error ('Unknown expression type: ' + str(expr))

```

The if statement matches the input expression with one of the expression types (or the definition) in the Charm language, and returns the result of applying the corresponding evaluation procedure (if the input is a definition, no value is returned since definitions do not produce an output value). We next consider each evaluation rule in turn.

12.4.1 Primitives

Charme supports two kinds of primitives: natural numbers and primitive procedures.

```

def isPrimitive(expr):
    return (isNumber(expr) or isPrimitiveProcedure(expr))

```

If the expression is a number, it is a string of digits. The *isNumber* procedure evaluates to True if and only if its input is a number:

```

def isNumber(expr):
    return isinstance(expr, str) and expr.isdigit()

```

Here, we use the built-in function *isinstance* to check if *expr* is of type *str*. The **and** expression in Python evaluates similarly to the Scheme **and** special form: the left operand is evaluated first; if it evaluates to a false value, the value of the and expression is that false value. If it evaluates to a true value, the right operand is evaluated, and the value of the and expression is the value of its right operand. This evaluation rule means it is safe to use *expr.isdigit()* in the right operand, since it is only evaluated if the left operand evaluated to a true value, which means *expr* is a string.

Primitive procedures are defined using Python procedures. Hence, the *isPrimitiveProcedure* procedure is defined using *callable*, a procedure that returns true only for objects that are callable (such as procedures and methods):

```

def isPrimitiveProcedure(expr):
    return callable(expr)

```

The evaluation rule for a primitive is identical to the Scheme rule:

Charme Evaluation Rule 1: Primitives. A primitive expression evaluates to its pre-defined value.

We need to implement the *pre-defined* values in our Charmé interpreter.

To evaluate a number primitive, we need to convert the string representation to a number of type *int*. The *int(s)* constructor takes a string as its input and outputs the corresponding integer:

```
def evalPrimitive(expr):
    if isNumber(expr): return int(expr)
    else: return expr
```

The **else** clause means that all other primitives (in Charmé, this is only primitive procedures and Boolean constants) self-evaluate: the value of evaluating a primitive is itself.

For the primitive procedures, we need to define Python procedures that implement the primitive procedure. For example, here is the *primitivePlus* procedure that is associated with the `+` primitive procedure:

```
def primitivePlus (operands):
    if (len(operands) == 0): return 0
    else: return operands[0] + primitivePlus (operands[1:])
```

The input is a list of operands. Since a procedure is applied only after all subexpressions are evaluated (according to the Scheme evaluation rule for an application expression), there is no need to evaluate the operands: they are already the evaluated values. For numbers, the values are Python integers, so we can use the Python `+` operator to add them. To provide the same behavior as the Scheme primitive `+` procedure, we define our Charmé primitive `+` procedure to evaluate to 0 when there are no operands, and otherwise, recursively add all of the operand values.

The other primitive procedures are defined similarly.

```
def primitiveTimes (operands):
    if (len(operands) == 0): return 1
    else: return operands[0] * primitiveTimes (operands[1:])

def primitiveMinus (operands):
    if (len(operands) == 1): return -1 * operands[0]
    elif len(operands) == 2: return operands[0] - operands[1]
    else:
        evalError('- expects 1 or 2 operands, given %s: %s' % (len(operands), str(operands)))

def primitiveEquals (operands):
    checkOperands (operands, 2, '=')
    return operands[0] == operands[1]
```

```

def primitiveLessThan (operands):
    checkOperands (operands, 2, '<')
    return operands[0] < operands[1]

```

The *checkOperands* procedure reports an error if a primitive procedure is applied to the wrong number of operands:

```

def checkOperands(operands, num, prim):
    if (len(operands) != num):
        evalError('Primitive %s expected %s operands, given %s: %s'
                  % (prim, num, len(operands), str(operands)))

```

12.4.2 If Expressions

Charme provides an if-expression special form with an evaluation rule identical to the Scheme if-expression.

The grammar rule for an if-expression is:

$$\begin{aligned}
 \textit{Expression} &::\Rightarrow \textit{IfExpression} \\
 \textit{IfExpression} &::\Rightarrow (\textit{if } \textit{Expression}_{\text{Predicate}} \\
 &\quad \textit{Expression}_{\text{Consequent}} \\
 &\quad \textit{Expression}_{\text{Alternate}})
 \end{aligned}$$

The expression object representing an if-expression should be a list containing three elements, with the first element matching the keyword *if*.

All special forms have this property: they are represented by lists where the first element is a keyword that identifies the special form. The *isSpecialForm* procedure takes an expression and a keyword and outputs a Boolean. The result is *True* if the expression is a special form matching the keyword:

```

def isSpecialForm(expr, keyword):
    return isinstance(expr, list) and len(expr) > 0 and expr[0] == keyword

```

We can use this to recognize different special forms by passing in different keywords. We recognize an if-expression by the *if* token at the beginning of the expression:

```

def isIf(expr):
    return isSpecialForm(expr, 'if')

```

The evaluation rule for an if-expression is:⁵

Charme Evaluation Rule 5: If. To evaluate an if-expression in the current environment, (a) evaluate the predicate expression in the current environment; then, (b) if the value of the predicate expression is a false value then the value of the if-expression is the value of the alternate expression in the current environment; otherwise, the value of the if-expression is the value of the consequent expression in the current environment.

The procedure *evalIf* implements this evaluation rule:

```
def evalIf(expr,env):  
    if meval(expr[1],env) != False: return meval(expr[2],env)  
    else: return meval(expr[3],env)
```

To program defensively, we also include some error checking in our *evalIf* procedure by adding these statements at the beginning of the procedure:

```
assert isIf(expr)  
if len(expr) != 4:  
    evalError ('Bad if expression: %s' % str(expr))
```

The first statement uses the Python **assert** statement to make an assertion. The **assert** keyword is followed by an expression. If the value of the expression is False the assertion produces an error message and terminates the execution. It is an error to apply *evalIf* to an expression that is not an if-expression.

The second statement is an if-expression that tests the length of the input expression. It should have four elements: the if keyword, the predicate expression, the consequence expression, and the alternate expression. If the input expression has more or less than four elements, *evalError* is used to report an error and terminate execution.

12.4.3 Definitions and Names

To evaluate definitions and names we need to represent environments. A definition adds a name to a frame, and a name expression evaluates to the value associated with a name.

⁵We number the Charme evaluation rules using the numbers we used for the analogous Scheme evaluation rules, but present them in a different order.

We will use a Python class to represent an environment. As in Chapter 11, a class packages state and procedures that manipulate that state. In Scheme, we needed to use a message-accepting procedure to do this. Python provides the class construct to support it directly. We define the *Environment* class for representing an environment. It has internal state for representing the parent (itself an *Environment* or *None*, Python's equivalent to *(cond CondClauseList)* for the global environment's parent), and for the frame.

The Python dictionary datatype provides a convenient way to implement a frame. The *__init__* procedure constructs a new object. It initializes the frame of the new environment to the empty dictionary using *self.frame = {}*.

The *addVariable* method either defines a new variable or updates the value associated with a variable. Using the dictionary datatype, we can do this with a simple assignment statement. The *lookupVariable* method first checks if the frame associated with this environment has a key associated with the input *name*. If it does, the value associated with that key is the value of the variable and that value is returned. Otherwise, if the environment has a parent, the value associated with the name is the value of looking up the variable in the parent environment. This directly follows from the stateful Scheme evaluation rule for name expressions. The **else** clause addresses the situation where the name is not found and there is no parent environment (since we have already reached the global environment) by reporting an evaluation error indicating an undefined name.

```
class Environment:
    def __init__(self, parent):
        self.parent = parent
        self.frame = {}
    def addVariable(self, name, value):
        self.frame[name] = value
    def lookupVariable(self, name):
        if self.frame.has_key(name): return self.frame[name]
        elif (self.parent): return self.parent.lookupVariable(name)
        else: evalError('Undefined name: %s' % (name))
```

Once the *Environment* class is defined, implementing the evaluation rules for definitions and name expressions is straightforward.

```
def isDefinition(expr):
    return isSpecialForm(expr, 'define')

def evalDefinition(expr, env):
    assert isDefinition(expr)
    if len(expr) != 3: evalError ('Bad definition: %s' % str(expr))
    name = expr[1]
```



```

if isinstance(name, str):
    value = meval(expr[2], env)
    env.addVariable(name, value)
else:
    evalError ('Bad definition: %s' % str(expr))

def isName(expr):
    return isinstance(expr, str)

def evalName(expr, env):
    assert isName(expr)
    return env.lookupVariable(expr)

```

12.4.4 Procedures

The result of evaluating a lambda-expression is a procedure. Hence, to define the evaluation rule for lambda-expressions we need to define a class for representing user-defined procedures. It needs to record the parameters, procedure body, and defining environment:

```

class Procedure:
    def __init__(self, params, body, env):
        self._params = params
        self._body = body
        self._env = env
    def __str__(self):
        return '<Procedure %s / %s>' % (str(self._params), str(self._body))

    def getParams(self): return self._params
    def getBody(self): return self._body
    def getEnvironment(self): return self._env

```

Using this, we can define the evaluation rule for lambda expressions to create a *Procedure* object:

```

def isLambda(expr):
    return isSpecialForm(expr, 'lambda')

def evalLambda(expr, env):
    assert isLambda(expr)
    if len(expr) != 3:
        evalError ('Bad lambda expression: %s' % str(expr))
    return Procedure(expr[1], expr[2], env)

```

12.4.5 Application

The evaluators circularity comes from the way evaluation and application are defined recursively. To perform an application, we need to evaluate all the subexpressions of the application expression, and then apply the result of evaluating the first subexpression to the values of the other subexpressions.

```
def isApplication(expr): # requires: all special forms checked first
    return isinstance(expr, list)

def evalApplication(expr, env):
    subexprs = expr
    subexprvals = map(lambda sexpr: meval(sexpr, env), subexprs)
    return mapapply(subexprvals[0], subexprvals[1:])
```

The *evalApplication* procedure uses the built-in *map* procedure, which is similar to (*Expression_{predicate} Expression_{consequent}*) from Chapter 5. The first parameter to *map* is a procedure constructed using a lambda expression (similar in meaning, but not in syntax, to Scheme's lambda expression); the second parameter is the list of subexpressions.

The *mapapply* procedure implements the application rules. If the procedure is a primitive, it “just does it”: it applies the primitive procedure to its operands. To apply a constructed procedure (represented by an object of the *Procedure* class) it follows the statefull application rule for applying constructed procedures: it creates a new environment, puts variables in that environment for each parameter and binds them to the corresponding operand values, and evaluates the procedure body in the new environment.

```
def mapapply(proc, operands):
    if (isPrimitiveProcedure(proc)): return proc(operands)
    elif isinstance(proc, Procedure):
        params = proc.getParams()
        newenv = Environment(proc.getEnvironment())
        if len(params) != len(operands):
            evalError('Parameter length mismatch: %s given operands %s'
                      % (str(proc), str(operands)))
        for i in range(0, len(params)):
            newenv.addVariable(params[i], operands[i])
        return meval(proc.getBody(), newenv)
    else:
        evalError('Application of non-procedure: %s' % (proc))
```

12.4.6 Finishing the Interpreter

To finish the interpreter, we define the *evalLoop* procedure that sets up the global environment and provides a simple user interface to the interpreter. To initialize the global environment, we need to create an environment with no parent and place variables in it corresponding to the primitives in Charmé:

```
def initializeGlobalEnvironment():
    global globalEnvironment
    globalEnvironment = Environment(None)
    globalEnvironment.addVariable('true', True)
    globalEnvironment.addVariable('false', False)
    globalEnvironment.addVariable('+', primitivePlus)
    globalEnvironment.addVariable('-', primitiveMinus)
    globalEnvironment.addVariable('*', primitiveTimes)
    globalEnvironment.addVariable('=', primitiveEquals)
    globalEnvironment.addVariable('<', primitiveLessThan)
```

The evaluation loop reads a string from the user using the Python built-in procedure *raw_input*. It uses *parse* to convert that string into a structured list representation. Then, it uses a for-expression to loop through the expressions. It evaluates each expression using *meval*, and prints out the result.

```
def evalLoop():
    initializeGlobalEnvironment()
    while True:
        inv = raw_input('Charmé> ')
        if inv == 'quit': break
        for expr in parse(inv):
            print str(meval(expr, globalEnvironment))
```

Here are some sample interactions with our Charmé interpreter:

```
>>> evalLoop()
Charmé> 150
150
Charmé> (+ 2 2)
4
Charmé> (define fibo (lambda (n)
                      (if (= n 1) 1
                          (if (= n 2) 1
                              (+ (fibo (- n 1)) (fibo (- n 2)))))))
None
Charmé> fibo
```

```
<Procedure ['n'] / ['if', ['=', 'n', '1'], '1', ['if', ['=', 'n', '2'], '1',  
    ['+', ['fibonacci', ['-', 'n', '1']], ['fibonacci', ['-', 'n', '2']]]]]>  
Charme> (fibonacci 10)  
55
```

12.5 Summary

Languages are tools for thinking, as well as means to express executable programs. A programming language is defined by its grammar and evaluation rules. To implement a language, we need to implement a parser that carries out the grammar rules and an evaluator that implements the evaluation rules.

Once we have an interpreter, we can change the meaning of our language by changing the evaluation rules. In the next chapter, we will see some examples that illustrate the value of being able to extend and change a language.