My G-CTMQC

Generated by Doxygen 1.9.1

1 Modules Index	1
1.1 Modules List	. 1
2 Module Documentation	3
2.1 analytical_potentials Module Reference	. 3
2.1.1 Detailed Description	4
2.1.2 Function/Subroutine Documentation	4
2.1.2.1 check_overlap()	4
2.1.2.2 diagonalize()	. 4
2.1.2.3 doublewell_potential()	. 5
2.1.2.4 ibr_potential()	. 5
2.1.2.5 nai_potential()	. 6
2.1.2.6 new_model_potentials()	. 6
2.1.2.7 non_adiabatic_couplings()	. 7
2.1.2.8 phenol_potential()	. 7
2.1.2.9 plot_potential()	. 8
2.1.2.10 subotnikjpca2019()	. 9
2.1.2.11 tully3()	. 9
2.2 atomic_masses Module Reference	. 9
2.2.1 Detailed Description	. 10
2.3 classical_evolution Module Reference	. 10
2.3.1 Detailed Description	10
2.3.2 Function/Subroutine Documentation	. 10
2.3.2.1 non_adiabatic_force()	. 11
2.3.2.2 update_position()	. 11
2.3.2.3 update_velocity()	. 12
2.4 coefficients_evolution Module Reference	. 12
2.4.1 Detailed Description	. 12
2.4.2 Function/Subroutine Documentation	. 12
2.4.2.1 cdot()	. 13
2.4.2.2 rk4_coeff()	. 13
2.5 coherence_corrections Module Reference	. 14
2.5.1 Detailed Description	. 14
2.5.2 Function/Subroutine Documentation	. 14
2.5.2.1 acc_force_ec()	. 14
2.5.2.2 accumulated_boforce()	. 15
2.5.2.3 quantum_momentum() [1/2]	. 15
2.5.2.4 quantum_momentum() [2/2]	. 17
2.6 electronic_problem Module Reference	. 18
2.6.1 Detailed Description	18
2.6.2 Function/Subroutine Documentation	18
2.6.2.1 boproblem()	. 18

2.6.2.2 check_nac_overlap()	19
2.7 kinds Module Reference	19
2.7.1 Detailed Description	19
2.8 output Module Reference	19
2.8.1 Detailed Description	20
2.8.2 Function/Subroutine Documentation	20
2.8.2.1 compute_energy()	20
2.8.2.2 initialize_output()	21
2.8.2.3 plot()	21
2.8.2.4 plot_coefficients()	22
2.8.2.5 plot_qmom()	22
2.8.2.6 plot_r_p_e()	23
2.8.2.7 plot_stc()	23
2.9 shopping Module Reference	24
2.9.1 Detailed Description	24
2.9.2 Function/Subroutine Documentation	24
<b>2.9.2.1 choose_bostate()</b> [1/2]	24
<b>2.9.2.2</b> choose_bostate() [2/2]	25
2.9.2.3 decoherence_coorection()	25
<b>2.9.2.4 hopping()</b> [1/2]	26
<b>2.9.2.5</b> hopping() [2/2]	27
<b>2.9.2.6</b> momentum_correction() [1/2]	27
<b>2.9.2.7 momentum_correction()</b> [2/2]	28
2.10 time_evolution Module Reference	28
2.10.1 Detailed Description	29
2.10.2 Function/Subroutine Documentation	29
2.10.2.1 evolution()	29
2.10.2.2 finalize_local_vars()	30
2.10.2.3 initialize_local_vars()	30
2.11 tools Module Reference	30
2.11.1 Detailed Description	31
2.11.2 Function/Subroutine Documentation	31
2.11.2.1 finalize()	31
2.11.2.2 generate_random_seed()	31
2.11.2.3 generate_random_seed_hop()	31
2.11.2.4 initialize_dynamics_vars()	33
2.11.2.5 initialize_trajectory_vars()	33
2.12 trajectories_selection Module Reference	33
2.12.1 Detailed Description	33
2.13 variables Module Reference	34
2.13.1 Detailed Description	37
2.14 wigner_distribution Module Reference	37

		III
	2.14.1 Detailed Description	38
	2.14.2 Function/Subroutine Documentation	
	2.14.2.1 gaussian_distribution()	38
	2.14.2.2 initial_conditions()	39
Index		41

# **Chapter 1**

# **Modules Index**

# 1.1 Modules List

Here is a list of all documented modules with brief descriptions:

analytical_potentials	
Diabatic low dimensional potentials	3
atomic_masses	
The module defines nuclear masses in atomic units	9
classical_evolution	
The module contains a collection of subroutines used in the classical evolution of the nuclei	10
coefficients_evolution	
Evolution of the electronic coefficients	12
coherence_corrections	
Calculations of quantities for decoherence corrections in CT-MQC	14
electronic_problem	
On-the-fly electronic-structure calculations	18
kinds	
Definiton of kinds	19
output	
Output subroutines that print: electronic populations and coherences as functions of time; elec-	
tronic coefficients as functions of positions at different time steps; positions, momenta and ener-	
gies at different time steps	19
shopping	
Surface hopping tools to compute the hop probability, the active state the energy rescaling after	0.4
the hop, and the energy decoherence correction	24
time_evolution	
Complete time evolution of Ntraj trajectories with Ehrenfest, surface hopping and CT-MQC, along with time initialization and finalization	20
tools	28
Numerical tools for initialization and finalization of the dynamically-allocated vectors, along with	
initialization of random numbers generators	30
trajectories selection	30
Subroutine under construction to "manually" select the coupled trajectories in CT-MQC	33
variables	00
The module defines all common variables	34
wigner distribution	04
Sampling of the initial conditions based on the harmonic Wigner distribution using the Box-Muller	
algorithm	37

2 Modules Index

# **Chapter 2**

# **Module Documentation**

# 2.1 analytical\_potentials Module Reference

Diabatic low dimensional potentials.

### **Functions/Subroutines**

• subroutine new model potentials (Hel, grad BO, NAC, Q)

Definition of electronic structure properties, ie, energies, gradients and derivative couplings on model potentials integrated in the G-CTMQC.

subroutine check\_overlap (eigenv1, eigenv2, factor)

Check that adjacent adiabatic states are continuous in nuclear space.

• subroutine diagonalize (matrix, eigenvalues, eigenvectors)

Diagonalization of a real symmetric matrix with the Lapac procedure dsyevd.

subroutine non\_adiabatic\_couplings (energy, gradients, eigenvectors, couplings)

Calculation of analytical non-adiabatic couplings.

• subroutine nai potential (H, R, grad H, R crossing)

Definition of the analytical model potentials for the diatomic molecule Nal following the work of Faist and Levine published in JCP (1976) DOI:10.1063/1.432555.

subroutine ibr\_potential (H, R, grad\_H, R\_crossing)

Definition of the analytical model potentials for the diatomic molecule Nal following the work of Guo published in JCP (1993) DOI:10.1063/1.465285.

subroutine doublewell\_potential (H, R, grad\_H, R\_crossing)

Definition of the analytical model potentials a double well.

• subroutine tully3 (H, R, grad H)

Definition of the analytical model potential Tully #3.

subroutine subotnikjpca2019 (H, R, grad\_H)

Definition of the analytical model potentials for parallel constant PESs.

• subroutine phenol\_potential (H, R, grad\_H, R\_crossing)

Definition of the analytical model potentials for the phenol molecule following the work of Faist and Levine published in JCP (1976) DOI:10.1063/1.432555.

• subroutine plot\_potential ()

Plot the adiabatic and diabatic analytical potentials.

### 2.1.1 Detailed Description

Diabatic low dimensional potentials.

### Author

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.1.2 Function/Subroutine Documentation

### 2.1.2.1 check\_overlap()

Check that adjacent adiabatic states are continuous in nuclear space.

### **Parameters**

in	eigenv1,eigenv2	eigenstates of the electronic Hamiltonian at adjecent points in nuclear space
in,out	factor	control factor for the phase relation between adjacent adiabatic states
	sum	scalar product between eigenv1 and eigenv2
	i,j	integer indices

#### Returns

The values of factor is returned: it is 1 if the two vectors are in phase or -1 if the two vectors are out of phase.

### 2.1.2.2 diagonalize()

Diagonalization of a real symmetric matrix with the Lapac procedure dsyevd.

in	matrix	to be diagonalized
in,out	eigenvalues	of the matrix
in,out	eigenvectors	of the matrix

#### **Parameters**

ioe	err	control variable for diagonalization errors
Iwo	ork	dimension of the array work
dir	n_work	temporary dimension of the array work
liw	rork	dimension of the array iwork
dir	n_iwork	temporary dimension of the array iwork
iwo	ork	integer array
wo	ork	double precision array

### Returns

The eigenvalues and eigenvectors of the matrix are returned.

### 2.1.2.3 doublewell\_potential()

Definition of the analytical model potentials a double well.

### **Parameters**

in,out	Н	electronic Hamiltonian in the diabatic basis
in,out	grad_H	gradient of the electronic Hamiltonian in the diabatic
		basis
in	R	nuclear position
	KX,DELTA,X1,X2,X3,GAMMA,ALPHA	parameters of the potentials: Note that the used units
		are atomic units

### Returns

The electronic Hamiltonian and its nuclear gradients are returned.

### 2.1.2.4 ibr\_potential()

Definition of the analytical model potentials for the diatomic molecule NaI following the work of Guo published in JCP (1993) DOI:10.1063/1.465285.

#### **Parameters**

in,out	Н	electronic Hamiltonian in the diabatic basis
in,out	grad_H	gradient of the electronic Hamiltonian in the
		diabatic basis
in	R	nuclear position
	A0,alpha0,r0,A1,alpha1,r1,D,A2,alpha2,B2,beta2	hparameters of the potentials: Note that the
		used units are atomic units

#### Returns

The electronic Hamiltonian and its nuclear gradients are returned.

### 2.1.2.5 nai\_potential()

Definition of the analytical model potentials for the diatomic molecule NaI following the work of Faist and Levine published in JCP (1976) DOI:10.1063/1.432555.

### **Parameters**

in,out	Н	electronic Hamiltonian in the diabatic basis
in,out	grad_H	gradient of the electronic Hamiltonian in the
		diabatic basis
in	R	nuclear position
	Acov,Bcov,rhocov,Ccov,Aion,Bion,rhoion,Cion,alp	hparameters of the potentials: Note that the
	Mp,alphaXm,Eth,A,rho	used units are electronvolts and and
		angstroms in the original definition

### Returns

The electronic Hamiltonian and its nuclear gradients are returned.

### 2.1.2.6 new\_model\_potentials()

Definition of electronic structure properties, ie, energies, gradients and derivative couplings on model potentials integrated in the G-CTMQC.

#### **Parameters**

in,out	Hel	electronic Hamiltonian at the trajectory position
in,out	grad_BO	gradient of the adiabatic energy at the trajectory position
in,out	NAC	non-adiabatic coupling vector at the trajectory position
in	Q	trajectory position
	Ebo	adiabatic energy at the trajectory position
	grad_Hel	gradient of the electronic Hamiltonian at the trajectory position
	U	transformation matrix from the diabatic to the adiabatic basis
	factor	control factor for the phase relation between adjacent adiabatic states
	delta	spatial increment to compute numerical derivatives
	i_dof	index running on the n_dof degrees of freedom
	ix,i	integer indices

### Returns

The values of the adiabatic energies are returned as the diagonal elements of Hel; the gradient of the adiabatic energies and the non-adiabatic couplings are returned in grad\_BO and NAC.

### 2.1.2.7 non\_adiabatic\_couplings()

Calculation of analytical non-adiabatic couplings.

### **Parameters**

in	energy	of the adiabatic states
in	gradients	of the adiabatic energies
in	eigenvectors	of the electronic Hamiltonian
in,out	couplings	matrix representing the non-adiabatic couplings
	i,j,k,l	integer indices

### Returns

The matrix of non-adiabatic couplings is returned.

### 2.1.2.8 phenol\_potential()

```
\label{eq:continuous} $$ \text{real(kind=dp), intent(in)} $$ R,$ \\ \text{real(kind=dp), dimension(nstates,nstates), intent(inout)} $$ grad_H,$ \\ \text{real(kind=dp), intent(inout), optional } $R\_crossing$ ) $$
```

Definition of the analytical model potentials for the phenol molecule following the work of Faist and Levine published in JCP (1976) DOI:10.1063/1.432555.

### **Parameters**

in,out	Н	electronic Hamiltonian in the diabatic basis
in,out	grad_H	gradient of the electronic Hamiltonian in the
		diabatic basis
in	R	nuclear position
	Acov,Bcov,rhocov,Ccov,Aion,Bion,rhoion,Cion,alp Mp,alphaXm,Eth,A,rho	used units are electronvolts and and
		angstroms in the original definition

### Returns

The electronic Hamiltonian and its nuclear gradients are returned.

### 2.1.2.9 plot\_potential()

```
subroutine analytical_potentials::plot_potential
```

Plot the adiabatic and diabatic analytical potentials.

Rmin,Rmax	limits of the domain to plot the potentials
V	values of the diabatic potentials
epsBO	values of the adiabatic potentials
nacv	values of the non-adiabatic couplings
grad_V	values of the gradients of the diabatic potentials
U	transformation matrix from the diabatic to the adiabatic basis at the current position
save_U	transformation matrix from the diabatic to the adiabatic basis at the previous position
factor	control factor for the phase relation between adjacent adiabatic states
npoints	number of grid points in nuclear space to plot the potentials
delta	spatial increment to compute numerical derivatives
R	
ground_states_density	initial nuclear density consistent with the distribution of classical initial positions and
	momenta
ios	control variable for output errors
ix,i	integer indices

### 2.1.2.10 subotnikjpca2019()

Definition of the analytical model potentials for parallel constant PESs.

#### **Parameters**

in,out	Н	electronic Hamiltonian in the diabatic basis
in,out	grad⊷	gradient of the electronic Hamiltonian in the diabatic basis
	_H	
in	R	nuclear position
	A,B	parameters of the potentials: Note that the used units are atomic units

#### Returns

The electronic Hamiltonian and its nuclear gradients are returned.

### 2.1.2.11 tully3()

Definition of the analytical model potential Tully #3.

### **Parameters**

-			
	in,out	Н	electronic Hamiltonian in the diabatic basis
	in,out	grad⊷ _H	gradient of the electronic Hamiltonian in the diabatic basis
	in	R	nuclear position
ſ		a,b,c	parameters of the potentials: Note that the used units are atomic units

### Returns

The electronic Hamiltonian and its nuclear gradients are returned.

# 2.2 atomic\_masses Module Reference

The module defines nuclear masses in atomic units.

### **Variables**

```
real(kind=dp), parameter m_hp = 1836.0_dp
```

Proton mass in atomic units.

real(kind=dp), parameter m\_na = 22.989769\_dp

Na mass in atomic mass units.

• real(kind=dp), parameter m\_i = 126.90447\_dp

I mass in atomic mass units.

• real(kind=dp), parameter m\_br = 79.9040\_dp

Br mass in atomic mass units.

real(kind=dp), parameter m\_h = 1.007825\_dp

H mass in atomic mass units.

real(kind=dp), parameter m\_o = 15.9994\_dp

O mass in atomic mass units.

### 2.2.1 Detailed Description

The module defines nuclear masses in atomic units.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.3 classical evolution Module Reference

The module contains a collection of subroutines used in the classical evolution of the nuclei.

### **Functions/Subroutines**

• subroutine update\_position (x, v)

Update of the classical positions according to the velocity Verlet algorithm.

subroutine update\_velocity (v, force)

Update of the classical velocities according to the velocity Verlet algorithm.

• subroutine non\_adiabatic\_force (coeff, force, acc\_force, k\_li, trajlabel)

Definition of the classical nuclear force depending on the type of calculation that is executed.

### 2.3.1 Detailed Description

The module contains a collection of subroutines used in the classical evolution of the nuclei.

Author

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.3.2 Function/Subroutine Documentation

### 2.3.2.1 non\_adiabatic\_force()

Definition of the classical nuclear force depending on the type of calculation that is executed.

#### **Parameters**

in	trajlabel	label indicating the trajectory number in the swarm	
in	coeff	coefficients of the expansion of the electronic time-dependent wavefunction in the basis used for the dynamics	
in	acc_force	gradient of the adiabatic or diabatic force accumulated over time along the trajectory trajlabel	
in	k_li	quantity related to the quantum momentum and responsible for decoherence; it is identically zero for Ehrenfest and surface hopping calculations	
in,out	force	classical force used to evolve the trajectory trajlabel	
	i,j	integer indices	
	i_dof	index running on the n_dof degrees of freedom	
	check	control variable for allocation errors	
	my_rho	temporary array of the electronic density matrix	

### Returns

The value of the classical force at the position of the trajectory is returned.

### 2.3.2.2 update\_position()

Update of the classical positions according to the velocity Verlet algorithm.

### **Parameters**

in,out	x	nuclear position
in	V	nuclear velocity
	my⊷ x	temporary nuclear position for internal calculations

#### Returns

The updated nuclear position is returned.

### 2.3.2.3 update velocity()

Update of the classical velocities according to the velocity Verlet algorithm.

#### **Parameters**

in	force	nuclear force
in,out	v	nuclear velocity
	my⊷	temporary nuclear velocity for internal calculations
	_ <i>v</i>	

#### Returns

The updated nuclear velocity is returned.

# 2.4 coefficients\_evolution Module Reference

Evolution of the electronic coefficients.

### **Functions/Subroutines**

- subroutine **evolve\_coeff** (v, coeff, k\_li, E\_old, NAC\_old, trajlabel)
- subroutine rk4\_coeff (v, coeff, k\_li, E, NAC, trajlabel)

Numerical integration of the non-linear differential equation describing the electronic evolution of the coefficients.

• complex(kind=qp) function cdot (state, kfunction, v, coeff, k\_li, E\_int, NAC\_int, trajlabel)

Total time derivative of the electronic coefficients as given in the Ehrenfest algorithm, surface hopping algorithm, and CT-MQC.

### 2.4.1 Detailed Description

Evolution of the electronic coefficients.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.4.2 Function/Subroutine Documentation

#### 2.4.2.1 cdot()

```
complex(kind=qp) function coefficients_evolution::cdot (
    integer, intent(in) state,
    complex(kind=qp), intent(in) kfunction,
    real(kind=dp), dimension(n_dof), intent(in) v,
    complex(kind=qp), dimension(nstates), intent(in) coeff,
    real(kind=dp), dimension(nstates,nstates), intent(in) k_li,
    real(kind=dp), dimension(nstates), intent(in) E_int,
    real(kind=dp), dimension(nstates,nstates,n_dof), intent(in) NAC_int,
    integer, intent(in) trajlabel)
```

Total time derivative of the electronic coefficients as given in the Ehrenfest algorithm, surface hopping algorithm, and CT-MQC.

#### **Parameters**

state	electronic state for which the time derivative of the coefficients is computer
trajlabel	label of the trajectory along which the equation is integrated
V	velocity of trajectory along which the time derivative of the coefficient is calculated
k_li	term accounting for decoherence effects in CT-MQC
coeff	electronic coefficientes
kfunction	function appearing in the expression of the time increment
cdot	time derivative of the coefficient
nonadiabatic_sum	off-diagonal contribution to the time derivative of the coefficients
my_coeff	local temporary values of the coefficients
i	integer index
my_gap	energy-gap threshold between the spin-diabatic states to tune the effect of the spin-orbit coupling
	trajlabel  v k_li coeff kfunction cdot nonadiabatic_sum my_coeff i

#### Returns

The values of the time derivative of the electronic coefficientes is returned.

### 2.4.2.2 rk4\_coeff()

Numerical integration of the non-linear differential equation describing the electronic evolution of the coefficients.

in	trajlabel	label of the trajectory along which the equation is integrated
in	V	velocity of trajectory along which the equation is integrated

#### **Parameters**

in	k_li	term accounting for decoherence effects in CT-MQC
in,out	coeff	electronic coefficientes
	i	integer index
	k1,k2,k3,k4	functions appearing in the expression of the time increment
	kfunction	function appearing in the expression of the time increment
	my_coeff	local temporary values of the coefficients
	normalization	norm of the electronic wavefunction after a time step

#### Returns

The values of the electronic coefficientes are returned after one step of dynamics.

## 2.5 coherence\_corrections Module Reference

Calculations of quantities for decoherence corrections in CT-MQC.

### **Functions/Subroutines**

- subroutine accumulated\_boforce (coeff, force, trajlabel)
  - The adiabatic (or spin-(a)diabatic) force is integrated in time along a trajectory.
- subroutine quantum\_momentum (Rcl, acc\_force, BOsigma, k\_li, qmom, qmom\_type)

Calculation of the quantum momentum by reconstructing the nuclear density as a sum of Gaussians centered at the positions of the trajectories.

- subroutine acc\_force\_ec (Vcl, coeff, acc\_force, acc\_force\_E)
  - The accumulated force is corrected to satisfy energy conservation.
- subroutine quantum\_momentum (Rcl, acc\_force, BOsigma, k\_li, qmom, qmom\_type)

Calculation of the quantum momentum by reconstructing the nuclear density as a sum of Gaussians centered at the positions of the trajectories.

### 2.5.1 Detailed Description

Calculations of quantities for decoherence corrections in CT-MQC.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.5.2 Function/Subroutine Documentation

### 2.5.2.1 acc\_force\_ec()

The accumulated force is corrected to satisfy energy conservation.

### **Parameters**

in	Vcl	classical velocities
in	coeff	electronic coefficientes
in	acc_force	accumulated force along the trajectories
in,out	acc_force⊷ E	new accumulated force
	i_dof	index running on the n_dof degrees of freedom
	i_traj	index running on the n_traj degrees number of trajectories
	istate	index running on the nstates of electronic states
	threshold	electronic population threshold to compute the acc forces
	R_threshold	velocity threshold to compute the new acc forces
	nvec	vector in the direction of the new acc force

### 2.5.2.2 accumulated\_boforce()

The adiabatic (or spin-(a)diabatic) force is integrated in time along a trajectory.

#### **Parameters**

in	trajlabel	label of the trajectory along which the equation is integrated
in	coeff	electronic coefficientes
in,out	force	integrated force along the trajectory
	i	integer index
	i_dof	index running on the n_dof degrees of freedom
	check	control variable for allocation errors
	threshold	electronic population threshold to accumate the force
	mean_force	average electronic force weighted by the electronic population

### Returns

The value of the adiabatic (or spin-(a)diabatic) force is returned if the electronic population of the corresponding state is larger than threshold and smaller that one minus the threshold.

### 2.5.2.3 quantum\_momentum() [1/2]

```
complex(kind=qp), dimension(ntraj,nstates,nstates), intent(in) BOsigma,
real(kind=dp), dimension(ntraj,nstates,nstates), intent(inout) k_li,
real(kind=dp), dimension(:,:,:), allocatable qmom,
integer, dimension(n_dof,ntraj,npairs), intent(inout) qmom_type)
```

Calculation of the quantum momentum by reconstructing the nuclear density as a sum of Gaussians centered at the positions of the trajectories.

#### **Parameters**

in	BOsigma	electronic density matrix
in	Rcl	positions of the trajectories
in	acc_force	force accumulated along the trajectory
in,out	k_li	term accounting for decoherence effects in CT-MQC
	itraj,jtraj	indices running on the Ntraj trajectories
	i_dof	index running on the n_dof degrees of freedom
	index_ij	index running on the pairs of electronic states
	istate,jstate	indices running on the electronic states
	gamma	variances of the Gaussians centered at the positions of the trajectories and used to reconstruct the nuclear density
	g_i	sum of Gaussians
	prod_g_i	product of one-dimensional Gaussians to construct a multi-dimensional Gaussian
	w_ij	see paper DOI:
	slope_i	slope of the quantum momentum when it is approximated as a linear function
	ratio	y-intercept when the quantum momentum is approximated as a linear function
	num_old	numerator in the expression of the y-intercept to approximate the quantum momentum as a linear function when the condition of no-population-transfer between two electronic states is imposed for zero values of the non-adiabatic couplings
	num_new	numerator in the analytical expression of the y-intercept to approximate the quantum momentum as a linear function
	num	numerator in the expression of the y-intercept of the linear quantum momentum
	denom	denominator in the expression of the y-intercept of the linear quantum momentum
	qmom	quantum momentum
	threshold	for the selection of the num_old or num_old (M_parameter * threshold is the applied distance criterion)

#### Returns

The value of k\_li is returned.

This is calculated each time; Consider saving them with a save varaiable

Sigma is standard deviation of wave function; not density, Thus, we need factor 2 in alpha (slope) and in the gauss later

Define alph (slope) for models/special cases

CALCULATE "gaus matrix" As above, the factor 2 is taken care of We take advantage of the symmetry for efficiency

### DENSITY AT EACH TRAJECTORY

standard intercept R\_ic Normal intercept, without respecting pop consersevation at NAC=0

fancy intercept R\_fi Intercept respecting pop consersevation at NAC=0

Periodicity part 1

Quantum momentum Start with 0 Priority: fancy intercept If too far away: normal intercept If still too far away it stays zero

double fancy intercept R\_fi Intercept respecting pop consersevation at NAC=0 only for same Carsten

Quantum momentum Start with 0, will stay 0 if Carsten is zero

Intercepts selected by Carsten of traj/state This may not work for older compilers

dont forget the slope! factor 0.5 from using the density insead of wavefunction in def of gmom

output k li

clean up crew, could be skipped I think

### 2.5.2.4 quantum\_momentum() [2/2]

Calculation of the quantum momentum by reconstructing the nuclear density as a sum of Gaussians centered at the positions of the trajectories.

in	BOsigma	electronic density matrix
in	Rcl	positions of the trajectories
in	acc_force	force accumulated along the trajectory
in,out	k_li	term accounting for decoherence effects in CT-MQC
	itraj,jtraj	indices running on the Ntraj trajectories
	i_dof	index running on the n_dof degrees of freedom
	index_ij	index running on the pairs of electronic states
	istate,jstate	indices running on the electronic states
	gamma	variances of the Gaussians centered at the positions of the trajectories and used to reconstruct the nuclear density
	g_i	sum of Gaussians
	prod_g_i	product of one-dimensional Gaussians to construct a multi-dimensional Gaussian
	w_ij	see paper DOI:
	slope_i	slope of the quantum momentum when it is approximated as a linear function
	ratio	y-intercept when the quantum momentum is approximated as a linear function
	num_old	numerator in the expression of the y-intercept to approximate the quantum momentum as a linear function when the condition of no-population-transfer between two electronic states is imposed for zero values of the non-adiabatic couplings
	num_new	numerator in the analytical expression of the y-intercept to approximate the
enerated by Dox	ygen	quantum momentum as a linear function
	num	numerator in the expression of the y-intercept of the linear quantum momentum
	denom	denominator in the expression of the y-intercept of the linear quantum momentum
	qmom	quantum momentum

### Returns

The value of k\_li is returned.

## 2.6 electronic\_problem Module Reference

On-the-fly electronic-structure calculations.

### **Functions/Subroutines**

• subroutine boproblem (Q, trajlabel)

Electronic energies (adiabatic or spin-(a)diabatic), forces and non-adiabatic couplings are compueted at the trajectory position.

subroutine check\_nac\_overlap (NACij, NACij\_old)

Arbitrary sign changes in the NACs due to the diagonalization are fixed.

### 2.6.1 Detailed Description

On-the-fly electronic-structure calculations.

#### **Author**

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.6.2 Function/Subroutine Documentation

### 2.6.2.1 boproblem()

Electronic energies (adiabatic or spin-(a)diabatic), forces and non-adiabatic couplings are compueted at the trajectory position.

in	trajlabel	label of the trajectory	
in	Q	position of the trajectory	
	istate	integer index running over the electronic states	
	V	array of (a)diabatic Hamiltonian	
	G	array of gradients of the (a)diabatic Hamiltonian	
	NAC	array of non-adiabatic couplings	
	NAC_old	array of non-adiabatic couplings at previous time step	
	initialize	logical to initialize the QMLLibrary potentials	

2.7 kinds Module Reference 19

#### Returns

Energies, forces and non-adiabatic couplings are stored in the arrays BOenergy, BOforce, coup.

### 2.6.2.2 check\_nac\_overlap()

Arbitrary sign changes in the NACs due to the diagonalization are fixed.

#### **Parameters**

in	NACij_old	NAC between two electronic states at time t
in,out	NACij	NAC between two electronic states at time t+dt param snac_old magnitude of NAC
		vector at time t param snac magnitude of NAC vector at time t+dt ovlp overlap
		between NAC_ij(t) and NAC_ij(t+dt) eps threshold for the overlap

### Returns

NAC at time t+dt with right sign respect to previous timestep

### 2.7 kinds Module Reference

Definiton of kinds.

### **Variables**

- integer, parameter dp =kind(0.0D0)

  Indicator for real double precision.
- integer, parameter qp =selected\_real\_kind(12)

  Indicator for real quadrupole precision.

### 2.7.1 Detailed Description

Definiton of kinds.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

# 2.8 output Module Reference

Output subroutines that print: electronic populations and coherences as functions of time; electronic coefficients as functions of positions at different time steps; positions, momenta and energies at different time steps.

### **Functions/Subroutines**

• subroutine plot (BOsigma, Rcl, Vcl, time)

Subroutine which writes electronic populations and coherences in output and calls additional output subroutines.

• subroutine plot\_coefficients (BOsigma, Rcl, time)

Subroutine which writes electronic coeffecients as functions of the trajectory positions at some selected time steps along the dynamics.

• subroutine plot\_r\_p\_e (Rcl, Vcl, time)

Subroutine which writes electronic coeffecients as functions of the trajectory positions at some selected time steps along the dynamics.

• subroutine plot\_qmom (Rcl, qmom, qmom\_type, time)

Subroutine which outputs information about the spurious transfer condition (STC), ie, sum\_traj Q(fl-fk)rho\_ll\*rho\_kk, and dE/dt.

• subroutine plot stc (k II, BOsigma, acc force E, Vcl, time)

Subroutine which outputs information about the spurious transfer condition (STC), ie, sum\_traj Q(fl-fk)rho\_ll\*rho\_kk, and dE/dt.

subroutine compute energy (my rho, e BO, trajlabel)

The subroutine computes the expectation value of the electronic Hamiltonian on the time-dependent electronic wavefunction, yielding the gauge-invariant part of the TDPES in CT-MQC or the mean Ehrenfest potential.

· subroutine initialize output

The files where electronic populations, coherences and the energy of the ensemble of trajectories are written are opened in this subroutine.

subroutine finalize\_output

The files where electronic populations, coherences and the energy of the ensemble of trajectories are written are closed in this subroutine.

### 2.8.1 Detailed Description

Output subroutines that print: electronic populations and coherences as functions of time; electronic coefficients as functions of positions at different time steps; positions, momenta and energies at different time steps.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

#### 2.8.2 Function/Subroutine Documentation

### 2.8.2.1 compute\_energy()

The subroutine computes the expectation value of the electronic Hamiltonian on the time-dependent electronic wavefunction, yielding the gauge-invariant part of the TDPES in CT-MQC or the mean Ehrenfest potential.

#### **Parameters**

in	trajlabel	label of the trajectory
in	my_rho	electronic density matrix
in	e_BO	adiabatic or spin-(a)diabatic energy
	i	integer index

### Returns

The value of the TDPES is returned, where "TDPES" means either the gauge-invariant part of the TDPES in CT-MQC or the mean Ehrenfest potential.

### 2.8.2.2 initialize\_output()

```
subroutine output::initialize_output
```

The files where electronic populations, coherences and the energy of the ensemble of trajectories are written are opened in this subroutine.

### **Parameters**

ios   control variable for output e	errors
-------------------------------------	--------

### 2.8.2.3 plot()

Subroutine which writes electronic populations and coherences in output and calls additional output subroutines.

_			
	in	time	time step
Ī	in	Rcl	positions of the trajectories
ſ	in	VcI	velocities of the trajectories
Ī	in	BOsigma	electronic density matrix
Ī		i,j	integer indices
Ī		itraj	integer index running over the Ntraj trajectories
Ī		index_ij	integer index running over the pairs of electronic states

#### Returns

Energies, forces and non-adiabatic couplings are stored in the arrays BOenergy, BOforce, coup.

### 2.8.2.4 plot\_coefficients()

Subroutine which writes electronic coeffecients as functions of the trajectory positions at some selected time steps along the dynamics.

#### **Parameters**

in	time	time step
in	Rcl	positions of the trajectories
in	BOsigma	electronic density matrix
	idx	index labelling the output files from 000 to 999
	filename	name of the output file
	itraj	integer index running over the Ntraj trajectories
	ios	control variable for output errors

### Returns

In the directory coeff the files coeff.XXX.dat are created, labelled from 000 to 999 (those indices label the time steps).

### 2.8.2.5 plot\_qmom()

Subroutine which outputs information about the spurious transfer condition (STC), ie, sum\_traj Q(fl-fk)rho\_ll\*rho\_kk, and dE/dt.

in	time	time step
----	------	-----------

### 2.8.2.6 plot\_r\_p\_e()

Subroutine which writes electronic coeffecients as functions of the trajectory positions at some selected time steps along the dynamics.

#### **Parameters**

in	time	time step
in	Rcl	positions of the trajectories
in	Vcl	velocities of the trajectories
	idx	index labelling the output files from 000 to 999
	filename	name of the output file
	itraj	integer index running over the Ntraj trajectories
	ios	control variable for output errors

#### Returns

In the directory trajectories the files RPE.XXX.dat are created, labelled from 000 to 999 (those indices label the time steps).

### 2.8.2.7 plot\_stc()

Subroutine which outputs information about the spurious transfer condition (STC), ie, sum\_traj Q(fl-fk)rho\_ll\*rho\_kk, and dE/dt.

### **Parameters**

i	n	time	time step
i	n	BOsigma	electronic density matrix
i	n	k_II	qmom*acc_force
		itraj	integer index running over the Ntraj trajectories
		ios	control variable for output errors

### Returns

In main directory STC.dat is created

### 2.9 shopping Module Reference

Surface hopping tools to compute the hop probability, the active state the energy rescaling after the hop, and the energy decoherence correction.

### **Functions/Subroutines**

• subroutine hopping (my\_rho, v, r, trajlabel, k\_li)

The hopping probability for the surface hopping procedure is computed according to the fewest switches procedure.

subroutine choose\_bostate (v, r, hop\_prob, trajlabel, k\_li, my\_rho)

According to the fewest switches algorithm, the new active state is selected.

• subroutine momentum\_correction (v, r, old\_occ\_state, trajlabel, k\_li, my\_rho)

Nuclear velocities are rescaled along the direction of the non-adiabatic couplings to impose energy conservation in case a hop to a new potential energy surface has occured.

• subroutine decoherence\_coorection (coeff, v, trajlabel)

Energy decoherence corrections are applied to surface hopping coefficients according to Granucci and Persico JCP 2007 DOI: 10.1063/1.2715585.

- subroutine xi\_for\_model\_system (dist, deltaE, xi, Rcl, Vcl, trajlabel)
- subroutine hopping (my rho, v, r, trajlabel)

The hopping probability for the surface hopping procedure is computed according to the fewest switches procedure.

• subroutine choose\_bostate (v, hop\_prob, trajlabel)

According to the fewest switches algorithm, the new active state is selected.

subroutine momentum correction (v, old occ state, trajlabel)

Nuclear velocities are rescaled along the direction of the non-adiabatic couplings to impose energy conservation in case a hop to a new potential energy surface has occured.

### 2.9.1 Detailed Description

Surface hopping tools to compute the hop probability, the active state the energy rescaling after the hop, and the energy decoherence correction.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.9.2 Function/Subroutine Documentation

### 2.9.2.1 choose\_bostate() [1/2]

According to the fewest switches algorithm, the new active state is selected.

#### **Parameters**

in	trajlabel	label of the trajectory
in,out	V	nuclear velocity
in,out	hop_prob	hopping probability for each electronic state
	myrand	random number
	prob_sum	cumulative hopping probability
	i_state,j_state	integer indices running over the nstates electronic states
	old_occ_state	previous active state

### Returns

The value of the hopping probability is returned, along with the new nuclear velocity in case a hop occurred.

### 2.9.2.2 choose\_bostate() [2/2]

```
subroutine shopping::choose_bostate (
    real(kind=dp), dimension(ntraj,n_dof), intent(inout) v,
    real(kind=dp), dimension(ntraj,n_dof), intent(in) r,
    real(kind=dp), dimension(nstates), intent(inout) hop_prob,
    integer, intent(in) trajlabel,
    real(kind=dp), dimension(nstates,nstates), intent(in), optional k_li,
    complex(kind=dp), dimension(nstates,nstates), intent(in), optional my_rho)
```

According to the fewest switches algorithm, the new active state is selected.

### **Parameters**

in	trajlabel	label of the trajectory
in,out	V	nuclear velocity
in,out	hop_prob	hopping probability for each electronic state
	myrand	random number
	prob_sum	cumulative hopping probability
	i_state,j_state	integer indices running over the nstates electronic states
	old_occ_state	previous active state

### Returns

The value of the hopping probability is returned, along with the new nuclear velocity in case a hop occurred.

### 2.9.2.3 decoherence\_coorection()

```
\label{eq:condition} real (kind=dp), \ dimension (n\_dof), \ intent (in) \ v, \\ integer \ trajlabel )
```

Energy decoherence corrections are applied to surface hopping coefficients according to Granucci and Persico JCP 2007 DOI: 10.1063/1.2715585.

### **Parameters**

in,out	coeff	electronic coefficients
in	v	nuclear velocity
	decay_time	characteristic time over which the electronic coeffecients of the non-activate states are exponentially damped
	deltaE	potential energy difference between the active states and the other electronic states
	kinetic_energy	nuclear kinetic energy along the trajectory
	sum_rho	sum of the populations of the non-active states
	i_dof	integer index running over the n_dof degrees of freedom
	i_state	integer index running over the nstates electronic states
	trajlabel	label of the trajectory

### Returns

The value of the new nuclear velocity is returned in case a hop occurred.

### 2.9.2.4 hopping() [1/2]

The hopping probability for the surface hopping procedure is computed according to the fewest switches procedure.

in	trajlabel	label of the trajectory
in	my_rho	electronic density matrix
in,out	V	nuclear velocity
	i_state	integer index running over the nstates electronic states
	i_dof	integer index running over the n_dof degrees of freedom
	scal2	scalar product beteween the nuclear velocity and the non-adiabatic coupling
	Re_rhoij	real part of the elements of the electronic density matrix
	rhojj	population of the electronic states
	hop_prob	hopping probability for each electronic state

#### Returns

The value of the nuclear velocity is returned, and it is modified to impose energy conservation if a hop occurred.

### 2.9.2.5 hopping() [2/2]

The hopping probability for the surface hopping procedure is computed according to the fewest switches procedure.

#### **Parameters**

in	trajlabel	label of the trajectory
in	my_rho	electronic density matrix
in,out	V	nuclear velocity
	i_state	integer index running over the nstates electronic states
	i_dof	integer index running over the n_dof degrees of freedom
	scal2	scalar product beteween the nuclear velocity and the non-adiabatic coupling
	Re_rhoij	real part of the elements of the electronic density matrix
	rhojj	population of the electronic states
	hop_prob	hopping probability for each electronic state

#### Returns

The value of the nuclear velocity is returned, and it is modified to impose energy conservation if a hop occurred.

### 2.9.2.6 momentum\_correction() [1/2]

Nuclear velocities are rescaled along the direction of the non-adiabatic couplings to impose energy conservation in case a hop to a new potential energy surface has occured.

in,out	V	nuclear velocity
in	trajlabel	label of the trajectory
in	old_occ_state	previous active state

#### **Parameters**

deltaE	potential energy difference between the old and the new electronic states
scal1	squared modulus of the non-adiabatic couplings divided by the nuclear mass
scal2	scalar product betweem the nuclear velocity and the non-adiabatic couplings
energy_check	criterion to identify the possibility of jump
scaling_factor	factor to rescal the velocities along the non-adiabatic couplings
i_dof	integer index running over the n_dof degrees of freedom

#### Returns

The value of the new nuclear velocity is returned in case a hop occurred.

### 2.9.2.7 momentum correction() [2/2]

Nuclear velocities are rescaled along the direction of the non-adiabatic couplings to impose energy conservation in case a hop to a new potential energy surface has occured.

#### **Parameters**

in,out	v	nuclear velocity
in	trajlabel	label of the trajectory
in	old_occ_state	previous active state
	deltaE	potential energy difference between the old and the new electronic states
	scal1	squared modulus of the non-adiabatic couplings divided by the nuclear mass
	scal2	scalar product betweem the nuclear velocity and the non-adiabatic couplings
	energy_check	criterion to identify the possibility of jump
	scaling_factor	factor to rescal the velocities along the non-adiabatic couplings
	i_dof	integer index running over the n_dof degrees of freedom

### Returns

The value of the new nuclear velocity is returned in case a hop occurred.

# 2.10 time\_evolution Module Reference

Complete time evolution of Ntraj trajectories with Ehrenfest, surface hopping and CT-MQC , along with time initialization and finalization.

### **Functions/Subroutines**

• subroutine evolution

Three algorithms are used to evolve classical nuclear trajectories along with the electronic coefficients: Ehrenfest dynamics, trajectory surface hopping and CT-MQC.

· subroutine input\_summary

Summary of the input is written on the terminal.

• subroutine initialize\_local\_vars

Variables used in the evolution subroutine are inizialized.

• subroutine finalize\_local\_vars

Variables used in the evolution subroutine are deallocated.

#### **Variables**

- real(kind=dp), dimension(:,:), allocatable rcl
- real(kind=dp), dimension(:,:), allocatable vcl
- real(kind=dp), dimension(:), allocatable classical\_force
- real(kind=dp), dimension(:,:,:), allocatable my\_force
- real(kind=dp), dimension(:,:,:), allocatable k li
- real(kind=dp), dimension(:,:), allocatable tdvp
- real(kind=dp), dimension(:), allocatable boenergy\_old
- real(kind=dp), dimension(:,:,:), allocatable coup\_old
- real(kind=dp), dimension(:,:,:), allocatable **qmom**
- integer, dimension(:,:,:), allocatable qmom type
- real(kind=dp), dimension(:,:,:), allocatable my\_force\_e
- complex(kind=qp), dimension(:,:,:), allocatable bosigma
- complex(kind=qp), dimension(:,:), allocatable bocoeff

### 2.10.1 Detailed Description

Complete time evolution of Ntraj trajectories with Ehrenfest, surface hopping and CT-MQC , along with time initialization and finalization.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

### 2.10.2 Function/Subroutine Documentation

### 2.10.2.1 evolution()

```
subroutine time_evolution::evolution
```

Three algorithms are used to evolve classical nuclear trajectories along with the electronic coefficients: Ehrenfest dynamics, trajectory surface hopping and CT-MQC.

#### **Parameters**

time	time step	
itraj	j integer index running over the Ntraj trajectories	
i,j integer indices		

### 2.10.2.2 finalize\_local\_vars()

```
subroutine time_evolution::finalize_local_vars
```

Variables used in the evolution subroutine are deallocated.

### **Parameters**

	check	control factor for deallocation errors	
--	-------	--	--

### 2.10.2.3 initialize\_local\_vars()

subroutine time\_evolution::initialize\_local\_vars

Variables used in the evolution subroutine are inizialized.

### **Parameters**

itraj	integer index running over the Ntraj trajectories	
i,j	integer indices	

### 2.11 tools Module Reference

Numerical tools for initialization and finalization of the dynamically-allocated vectors, along with initialization of random numbers generators.

### **Functions/Subroutines**

- subroutine initialize\_dynamics\_vars
  - Initialization of dynamics variables.
- subroutine initialize\_trajectory\_vars
  - Initialization of trajectory variables.
- · subroutine finalize
  - Deallocation of dynamically-allocayed arrays.
- subroutine generate\_random\_seed

Inizialization of random number generator for the initial conditions.

• subroutine generate\_random\_seed\_hop

Inizialization of random number generator for the trajectory hops.

# 2.11.1 Detailed Description

Numerical tools for initialization and finalization of the dynamically-allocated vectors, along with initialization of random numbers generators.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

# 2.11.2 Function/Subroutine Documentation

# 2.11.2.1 finalize()

subroutine tools::finalize

Deallocation of dynamically-allocayed arrays.

#### **Parameters**

check control factor for deallocation errors

#### 2.11.2.2 generate\_random\_seed()

subroutine tools::generate\_random\_seed

Inizialization of random number generator for the initial conditions.

#### **Parameters**

seed	seed for the random number generator
n,i	integer indices

# 2.11.2.3 generate\_random\_seed\_hop()

subroutine tools::generate\_random\_seed\_hop

Inizialization of random number generator for the trajectory hops.

#### **Parameters**

seed	seed for the random number generator
n,i	integer indices

# 2.11.2.4 initialize\_dynamics\_vars()

subroutine tools::initialize\_dynamics\_vars

Initialization of dynamics variables.

#### **Parameters**

# 2.11.2.5 initialize\_trajectory\_vars()

subroutine tools::initialize\_trajectory\_vars

Initialization of trajectory variables.

#### **Parameters**

ahaak	control factor for allocation errors
CHECK	control factor for allocation errors

# 2.12 trajectories\_selection Module Reference

Subroutine under construction to "manually" select the coupled trajectories in CT-MQC.

#### **Functions/Subroutines**

• subroutine select\_coupled\_trajectories

# 2.12.1 Detailed Description

Subroutine under construction to "manually" select the coupled trajectories in CT-MQC.

Author

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

#### 2.13 variables Module Reference

The module defines all common variables.

#### **Variables**

• real(kind=dp), parameter hbar = 1.0\_dp

Reduced Planck constant.

real(kind=dp), parameter zero = 0.0000000010\_dp

"Numerical" zero

real(kind=dp), parameter au\_to\_ang = 0.52917721067121\_dp

Conversion factor from bohr to angstrom.

real(kind=dp), parameter au\_to\_ev = 27.2114\_dp

Conversion factor from Hartree to electronvolts.

real(kind=dp), parameter amu\_to\_au = 1836.0\_dp

Conversion factor from atomic mass units to atomic units.

complex(kind=qp) im\_unit = (0.0\_dp, 1.0\_dp)

Imaginary unit.

real(kind=dp) pi = 3.14159265359 dp

p

• complex(kind=qp) cmp = CMPLX(0.0\_dp, 1.0\_dp, qp)

pi

character(len=5) typ cal = "EHREN"

Type of dynamics that is executed: EHREN for Ehrenfest dynamics, TSHLZ for surface hopping with Landau-Zener hopping probability, TSHFS for surface hopping with fewest-switches hopping probability, CTMQC for CT-MQC, read in input.

character(len=100) model\_potential = "unknown"

Name of the model potential as it is defined in QuantumModelLib, read in input.

• integer option = 1

Only used for Tully models and can be 1, 2, or 3, read in input.

logical new\_potential = .FALSE.

It is FALSE if the QuantumModelLib potential library is used; it is TRUE if the potentials in analytical\_potentials.f90 are used, read in input.

integer n\_dof = 1

Number of degrees of nuclear freedom, read in input.

• integer nstates = 2

Number of electronic states, read in input.

• integer npairs = 1

Number of pairs of electronic states.

• logical, dimension(100) periodic\_variable = .FALSE.

It is TRUE for each periodic nuclear coordinate, read in input.

real(kind=dp), dimension(100) periodicity = 0.0\_dp

Periodicity of the correspoding nuclear nuclear coordinate in unit of pi, read in input.

character(len=2) type\_deco = ""

Type of decoherence scheme applied on surface hooping: CT based on coupled trajectories and on quantum momentum, ED which is the energy-decoherence correction, read in input.

real(kind=dp) c\_parameter = 0.1\_dp

Value of the parameter C in the energy-decoherence correction used in surface hopping, read in input.

• integer jump seed = -100

Seed for the random number generator used for the probability jump is surface hopping, read in input.

integer initial\_condition\_seed = -100

Seed for the random number generator used for the selection of initial conditions, read in input.

real(kind=dp) adia\_nrg\_gap = 10000.0D0

Energy treshold to compute the non-adiabatic coupling vectors for the classical force or the Landau-Zener probability.

real(kind=dp) lz\_dist\_cutoff = 0.20D0

Distance cutoff from the crossing region to compute the Landau-Zener probability.

logical nrg\_check = .FALSE.

It is TRUE if the spin-orbit coupling is switched-off when the energy gap between spin-diabatic states is above a certain treshold, read in input.

real(kind=dp) nrg\_gap = 10000.0D0

Energy treshold to switch-off the spin-orbit coupling, read in input.

• logical spin\_dia = .FALSE.

It is TRUE when the spin-diabatic basis is used in CT-MQC, read in input.

• logical qmom\_force = .TRUE.

It is TRUE when quantum-momentum force is used in CT-MQC, read in input.

logical f correction = .FALSE.

It is TRUE when energy conserving acc\_force is used in CT-MQC (CTMQC-E), read in input.

real(kind=dp) r threshold = 0.001 dp

R\_threshold only used when f\_correction= TRUE to determine cut-off for computation of modified acc force in CTMQC-E.

real(kind=dp), dimension(100) m parameter = 100.0 dp

 $M_{parameter}$  is used only when  $cl_{qmom} = TRUE$  to determine "how far" each trajectory has to search to find its neighbours, read in input.

• integer rescaling\_type = 2

type of momentum rescaling after hop: 0 = isotropical, 2 = along NACV, 1 = along NACV, if frustrated isotropical

logical reflect\_frust = .FALSE.

It is TRUE if you want to invert the full velocity vector after frustrated hop.

• logical force hops = .FALSE.

Adds a threshold to force hops in CTTSH.

real(kind=dp) hop\_thr = 0.6

Above this threshold of population a trajectory is forced to hop.

• logical energy\_sharing = .FALSE.

Option to share energy for CCT TSH.

integer sharing\_type = 0

Types of energy sharing: 0 = equity based, 1 = overlap based, 2 = Qmom based.

• logical doubleintercept = .true.

If true then Qmom is calculated using double intercept.

real(kind=dp) dt = 0.1\_dp

Time step, read in input.

real(kind=dp) final\_time = 0.0\_dp

Length of the simulations, read in input.

real(kind=dp), dimension(100) r\_init

Mean positions to initialize nuclear positions, read in input.

real(kind=dp), dimension(100) k\_init

Mean momenta to initialize nuclear momenta, read in input.

real(kind=dp), dimension(100) mass input = 0.0 dp

Nuclear masses, read in input.

real(kind=dp), dimension(100) sigmar\_init

Position variances to initialize nuclear positions, read in input.

• real(kind=dp), dimension(100) sigmap\_init = -100.0\_dp

Momentum variances to initialize nuclear momenta, only necessary for non-Wigner sampling, read in input.

• integer ntraj = 100

Number of nuclear trajectories, read in input.

• integer nsteps = 100

Total number of dynamics time steps.

• integer nesteps = 20

Number of electronic time-steps per nuclear time-step.

integer dump = 1

Number of time steps after which the output is dumped, read in input.

integer n init bo = 1

Number of initially populated electronic state(s), read in input.

integer, dimension(100) init bostate = -1

Initial electronic state(s), read in input.

real(kind=dp), dimension(100) weight\_initbo = 1.0\_dp

Weight(s) of the initially populated electronic state(s), read in input.

real(kind=dp), dimension(100) phase initbo = 0.0 dp

Phase(s) of the initially populated electronic state(s), read in input.

• real(kind=dp), dimension(:), allocatable r0

Mean nuclear positions.

real(kind=dp), dimension(:), allocatable r02

Mean nuclear positions squared.

real(kind=dp), dimension(:), allocatable k0

Mean nuclear momenta.

• integer, dimension(:), allocatable initial bostate

BO states with non-zero initial occupation.

real(kind=dp), dimension(:), allocatable weight\_bostate

Occupation of the BO states with non-zero initial occupation.

real(kind=dp), dimension(:), allocatable phase\_bostate

Phases of the BO coefficients.

• real(kind=dp), dimension(:), allocatable period

Periodicity of the periodic nuclear nuclear coordinate in unit of pi.

logical, dimension(:), allocatable periodic\_in

It is TRUE for each periodic nuclear coordinate.

• real(kind=dp), dimension(:), allocatable mass

Nuclear masses.

• real(kind=dp), dimension(:), allocatable sigma

Position variances to initialize nuclear positions.

• real(kind=dp), dimension(:), allocatable var\_momentum

Momentum variances to initialize nuclear momenta.

• real(kind=dp), dimension(:,:,:), allocatable boforce

Gradients of the electronic energies, either adiabatic or spin-(a)diabatic.

real(kind=dp), dimension(:,:,:,:), allocatable coup

Non-adiabatic couplings.

complex(kind=qp), dimension(:,:,:), allocatable coup\_so

Spin-orbit coupling.

real(kind=dp), dimension(:,:), allocatable boenergy

Electronic energies, either adiabatic or spin-(a)diabatic.

real(kind=dp), dimension(:), allocatable bo\_pop

Populations of the electronic states computed from the electronic coefficients.

real(kind=dp), dimension(:), allocatable bo pop sh

Populations of the electronic states computed in surface hopping as the ratio of trajectories running in each state over the total number of trajectories.

• real(kind=dp), dimension(:), allocatable dia\_pop

diabatic Populations of the electronic states computed from the electronic coefficients

real(kind=dp), dimension(:), allocatable bo\_coh

Electronic coherences.

• real(kind=dp) ctmqc e

Trajectory-averaged CTMQC Energy.

real(kind=dp), dimension(:,:), allocatable initial positions

Initial nuclear positions.

real(kind=dp), dimension(:,:), allocatable initial\_momenta

Initial nuclear momenta.

· real(kind=dp), dimension(:), allocatable weight

Weight of each trajectory (usually it is equal to unity)

real(kind=dp), dimension(:), allocatable tdpes

Gauge invariant part of the TDPES in CT-MQC calculation and mean Ehrenfest potential in Ehrenfest dynamics.

· real(kind=dp), dimension(:), allocatable density

Nuclear density.

integer, dimension(:), allocatable occ\_state

Active or force state in surface hopping.

• integer, dimension(:), allocatable lz\_hop

Keeps track of jumps in Landau-Zener surface hopping.

integer count\_traj

Counts the trajectories that go through the avoided crossing.

integer, dimension(:), allocatable list\_coupled\_trajectories

List of coupled trajectories in CT-MQC (in the current version all trajectories are coupled)

real(kind=dp), dimension(:,:,:), allocatable vec0

NACV used to assure the Phase following from QmodelLib.

• real(kind=dp), dimension(:,:,:), allocatable previous\_eigenv

If NEW\_POTENTIAL == .TRUE. this variable is needed to check the phase of neighboring eigenvectors.

real(kind=dp), dimension(:,:,:,:), allocatable previous\_coup

Checks that the NACVs are continous along a trajectory.

- logical initial\_coup = .TRUE.
- character(len=400) positions\_file = ""

Path to the file here initial positions are listed in case they are generated by another program, read in input.

character(len=400) momenta\_file = ""

Path to the file here initial momenta are listed in case they are generated by another program, read in input.

• character(len=400) output folder = "./"

Path to the directory where the output is written, read in input; note that in such directory, two sub-directories (coeff and trajectories) have to be created.

# 2.13.1 Detailed Description

The module defines all common variables.

Author

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

# 2.14 wigner\_distribution Module Reference

Sampling of the initial conditions based on the harmonic Wigner distribution using the Box-Muller algorithm.

#### **Functions/Subroutines**

· subroutine initial\_conditions

If initial conditions are not provided, they are sampled according to Gaussian distributions.

• real(kind=dp) function, dimension(my\_nrand) gaussian\_distribution (xi, nrand, var, x0, my\_nrand)

Box-Muller transform to generate normally distributed random number starting with uniformly distributed random numbers between 0 and 1.

# 2.14.1 Detailed Description

Sampling of the initial conditions based on the harmonic Wigner distribution using the Box-Muller algorithm.

**Author** 

Federica Agostini, Institut de Chimie Physique, University Paris-Saclay.

#### 2.14.2 Function/Subroutine Documentation

#### 2.14.2.1 gaussian\_distribution()

```
real(kind=dp) function, dimension(my_nrand) wigner_distribution::gaussian_distribution ( real(kind=dp), dimension(nrand), intent(in) xi, integer, intent(in) nrand, real(kind=dp), intent(in) var, real(kind=dp), intent(in) x0, integer, intent(in) my_nrand)
```

Box-Muller transform to generate normally distributed random number starting with uniformly distributed random numbers between 0 and 1.

#### **Parameters**

in	nrand	amount of normally distributed random numbers to be generated
in	my_nrand	amount of normally distributed random numbers that are needed
in	xi	array of uniformly distributed random numbers
in	var	variance of the Gaussian distribution
in	x0	mean value of the Gaussian distribution
	y_tmp	normally distributed random numbers
	у	normally distributed random numbers that are returned by the function
	i,j	integer indices

#### Returns

Normally distributed random numbers are generated.

# 2.14.2.2 initial\_conditions()

 $\verb|subroutine| wigner_distribution:: initial_conditions|\\$ 

If initial conditions are not provided, they are sampled according to Gaussian distributions.

#### **Parameters**

xi	array of random numbers uniformally distributed
check	control factor allocation errors
nrand	integer index
i	integer index
ios	control factor output errors

# Returns

Initial positions and initial momenta are generated.

# Index

acc_force_ec coherence_corrections, 14	boproblem, 18 check_nac_overlap, 19
accumulated_boforce	evolution
coherence_corrections, 15	time_evolution, 29
analytical_potentials, 3	
check_overlap, 4	finalize
diagonalize, 4	tools, 31
doublewell_potential, 5	finalize_local_vars
ibr potential, 5	time_evolution, 30
nai_potential, 6	
new_model_potentials, 6	gaussian_distribution
non_adiabatic_couplings, 7	wigner_distribution, 38
phenol_potential, 7	generate_random_seed
plot_potential, 8	tools, 31
subotnikjpca2019, 8	generate_random_seed_hop
tully3, 9	tools, 31
atomic_masses, 9	
_	hopping
boproblem	shopping, 26, 27
electronic_problem, 18	ibr_potential
cdot	analytical_potentials, 5
coefficients_evolution, 12	initial_conditions
check_nac_overlap	wigner_distribution, 38
electronic_problem, 19	initialize_dynamics_vars
check_overlap	tools, 33
analytical_potentials, 4	initialize_local_vars
choose_bostate	time_evolution, 30
shopping, 24, 25	initialize_output
classical_evolution, 10	output, 21
non_adiabatic_force, 10	initialize_trajectory_vars
update_position, 11	tools, 33
update_velocity, 12	kinds, 19
coefficients_evolution, 12	Tallas, To
cdot, 12	momentum_correction
rk4_coeff, 13	shopping, 27, 28
coherence_corrections, 14	
acc_force_ec, 14	nai_potential
accumulated_boforce, 15	analytical_potentials, 6
quantum_momentum, 15, 17	new_model_potentials
compute_energy	analytical_potentials, 6
output, 20	non_adiabatic_couplings
decoherence coorection	analytical_potentials, 7
shopping, 25	non_adiabatic_force
diagonalize	classical_evolution, 10
analytical_potentials, 4	
doublewell_potential	output, 19
analytical potentials, 5	compute_energy, 20
a.a.j.toai_potortialo, o	initialize_output, 21
electronic problem, 18	plot, 21

42 INDEX

```
plot_coefficients, 22
     plot_qmom, 22
     plot_r_p_e, 22
     plot_stc, 23
phenol_potential
     analytical_potentials, 7
     output, 21
plot_coefficients
     output, 22
plot potential
     analytical_potentials, 8
plot_qmom
     output, 22
plot_r_p_e
     output, 22
plot_stc
     output, 23
quantum_momentum
     coherence corrections, 15, 17
rk4 coeff
     coefficients evolution, 13
shopping, 24
     choose_bostate, 24, 25
     decoherence_coorection, 25
     hopping, 26, 27
     momentum_correction, 27, 28
subotnikjpca2019
     analytical_potentials, 8
time_evolution, 28
     evolution, 29
     finalize_local_vars, 30
     initialize local vars, 30
tools, 30
     finalize, 31
     generate_random_seed, 31
     generate random seed hop, 31
     initialize_dynamics_vars, 33
     initialize_trajectory_vars, 33
trajectories_selection, 33
tully3
     analytical_potentials, 9
update_position
     classical_evolution, 11
update_velocity
     classical_evolution, 12
variables, 34
wigner_distribution, 37
     gaussian_distribution, 38
     initial conditions, 38
```