Consolidated Performance Tests

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1 Benchmark's tables

1.1 Using BP-One versions

Table 1: Results

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb1a57 698	Classic Quaternion			73.561 01	
pdb1b4c 1108	Classic Quaternion	$1.203 \times 10^{-9} \\ 1.203 \times 10^{-9}$	1.0756×10^{-12}	$7.0285 \times 10^{-3} \\ 3.9253 \times 10^{-3}$	79.05440
pdb1ba5 320	Classic Quaternion	$9.359 \times 10^{-13} \\ 1.070 \times 10^{-12}$	4.1376×10^{-12}	$6.6698 \times 10^{-4} 3.9719 \times 10^{-4}$	67.92475
pdb1d1n 594	Classic Quaternion	$1.005 \times 10^{-11} 9.672 \times 10^{-12}$	1.2689×10^{-12}	$1.0563 \times 10^{-3} \\ 6.6521 \times 10^{-4}$	58.795 90
pdb1dp3 332	Classic Quaternion	$7.704 \times 10^{-13} \\ 8.939 \times 10^{-13}$	1.4697×10^{-12}	$5.4273 \times 10^{-4} 3.3159 \times 10^{-4}$	63.673 62
pdb1du1 122	Classic Quaternion	$8.225 \times 10^{-13} 1.258 \times 10^{-12}$	1.2376×10^{-12}	$1.8437 \times 10^{-4} 1.1232 \times 10^{-4}$	64.14752
pdb1eii 806	Classic Quaternion	$1.393 \times 10^{-11} \\ 1.365 \times 10^{-11}$	1.1331×10^{-11}	$\begin{array}{c} 1.4632 \times 10^{-3} \\ 9.2362 \times 10^{-4} \end{array}$	58.41953
pdb1fcl 338	Classic Quaternion	$4.542 \times 10^{-12} 4.515 \times 10^{-12}$	8.0786×10^{-13}	$1.0112 \times 10^{-3} 5.8997 \times 10^{-4}$	71.39196
pdb1fd6 344	Classic Quaternion	3.182×10^{-12} 3.193×10^{-12}	3.3846×10^{-13}	$6.1200 \times 10^{-4} 3.7254 \times 10^{-4}$	64.279 67
pdb1hf9 496	Classic Quaternion	1.157×10^{-11} 1.180×10^{-11}	3.9332×10^{-12}	$\begin{array}{c} 1.9207 \times 10^{-2} \\ 9.3737 \times 10^{-3} \end{array}$	104.90736
pdb1i2u 266	Classic Quaternion	$5.562 \times 10^{-13} 5.607 \times 10^{-13}$	1.5136×10^{-13}	$4.5520 \times 10^{-4} 2.8053 \times 10^{-4}$	62.26228
pdb1i2v 266	Classic Quaternion	2.418×10^{-13} 2.519×10^{-13}	6.9127×10^{-14}	$5.0893 \times 10^{-4} 3.1292 \times 10^{-4}$	62.640 03
pdb1ijc 380	Classic Quaternion	$1.408 \times 10^{-11} \\ 1.426 \times 10^{-11}$	2.4877×10^{-12}	$\begin{array}{c} 1.2551 \times 10^{-3} \\ 7.2816 \times 10^{-4} \end{array}$	72.36375
pdb1jlz 140	Classic Quaternion	5.594×10^{-13} 5.965×10^{-13}	1.3105×10^{-12}	$2.3048 \times 10^{-4} 1.3962 \times 10^{-4}$	65.073 90
pdb1jw3 842	Classic Quaternion	$5.936 \times 10^{-13} 5.897 \times 10^{-13}$	3.9013×10^{-13}	$\begin{array}{c} 1.5873 \times 10^{-3} \\ 9.8822 \times 10^{-4} \end{array}$	60.61759
pdb1k0v 440	Classic Quaternion	1.893×10^{-13} 1.894×10^{-13}	1.3433×10^{-13}	$8.4919 \times 10^{-4} 5.2530 \times 10^{-4}$	61.659 07
pdb1k2h 1120	Classic Quaternion	$5.491 \times 10^{-13} 5.199 \times 10^{-13}$	2.2039×10^{-13}	$5.4764 \times 10^{-3} 3.0636 \times 10^{-3}$	78.758 02
pdb1k36 278	Classic Quaternion	$8.820 \times 10^{-12} 1.081 \times 10^{-11}$	2.8981×10^{-11}	$\begin{array}{c} 4.8178 \times 10^{-4} \\ 2.8607 \times 10^{-4} \end{array}$	68.41411
pdb1k37 278	Classic Quaternion	$4.711 \times 10^{-13} 4.988 \times 10^{-13}$	1.5479×10^{-13}	$6.9144 \times 10^{-4} 4.0552 \times 10^{-4}$	70.505 95
pdb1kuw 62	Classic Quaternion	9.229×10^{-14} 1.130×10^{-13}	7.3457×10^{-14}	$1.0631 \times 10^{-4} \\ 6.4713 \times 10^{-5}$	64.281 52
pdb1kz0 98	Classic Quaternion	$\begin{array}{c} 4.404 \times 10^{-14} \\ 5.880 \times 10^{-14} \end{array}$	2.4335×10^{-13}	$\begin{array}{c} 1.6470 \times 10^{-4} \\ 9.9061 \times 10^{-5} \end{array}$	66.258 50
pdb1kz2 98	Classic Quaternion	$2.119 \times 10^{-14} \\ 2.886 \times 10^{-14}$	2.6112×10^{-14}	$\begin{array}{c} 1.7613 \times 10^{-4} \\ 1.0593 \times 10^{-4} \end{array}$	66.265 62
pdb1kz5 74	Classic Quaternion	$4.081 \times 10^{-14} 4.738 \times 10^{-14}$	4.8348×10^{-14}	$\begin{array}{c} 1.2806 \times 10^{-4} \\ 7.6891 \times 10^{-5} \end{array}$	66.54485
pdb1lvz 68	Classic Quaternion	$6.336 \times 10^{-14} 7.315 \times 10^{-14}$	7.3919×10^{-14}	$\begin{array}{c} 1.1210 \times 10^{-4} \\ 6.8546 \times 10^{-5} \end{array}$	63.541 27
pdb1m4e 122	Classic Quaternion	$5.949 \times 10^{-13} 5.972 \times 10^{-13}$	1.1702×10^{-13}	$2.0349 \times 10^{-4} 1.2380 \times 10^{-4}$	64.363 66

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb1ma2 104	Classic Quaternion	$8.695 \times 10^{-12} \\ 8.758 \times 10^{-12}$	4.7062×10^{-13}	3.2666×10^{-4} 1.8671×10^{-4}	74.95575
pdb1ma4 104	Classic Quaternion	$7.247 \times 10^{-14} 7.981 \times 10^{-14}$	1.8851×10^{-13}	$4.6898 \times 10^{-4} 2.5826 \times 10^{-4}$	81.59434
pdb1ma5 104	Classic Quaternion	$8.169 \times 10^{-13} 9.044 \times 10^{-13}$	5.0234×10^{-13}	$1.7470 \times 10^{-4} 1.0519 \times 10^{-4}$	66.07442
pdb1ma6 104	Classic Quaternion	$6.283 \times 10^{-13} 8.522 \times 10^{-13}$	3.3052×10^{-12}	$1.6156 \times 10^{-4} 9.8305 \times 10^{-5}$	64.35024
pdb1mpe 1352	Classic Quaternion	$2.617 \times 10^{-11} 2.624 \times 10^{-11}$	7.1261×10^{-13}	1.1304×10^{-2} 5.2556×10^{-3}	115.08839
pdb1nd9 296	Classic Quaternion	3.026×10^{-13} 3.845×10^{-13}	4.7137×10^{-13}	5.1913×10^{-4} 3.2185×10^{-4}	61.29357
$\begin{array}{c} \mathrm{pdb1ne5} \\ 254 \end{array}$	Classic Quaternion	$1.214 \times 10^{-12} 1.384 \times 10^{-12}$	7.5582×10^{-13}	$4.2127 \times 10^{-4} 2.5516 \times 10^{-4}$	65.10468
pdb1nmj 170	Classic Quaternion	$1.237 \times 10^{-14} 1.424 \times 10^{-14}$	1.3921×10^{-14}	3.0985×10^{-4} 1.8648×10^{-4}	66.153 75
pdb1o53 92	Classic Quaternion	3.999×10^{-13} 4.545×10^{-13}	6.5350×10^{-13}	$1.7000 \times 10^{-4} 1.0024 \times 10^{-4}$	69.583 22
pdb1oqp 580	Classic Quaternion	$7.045 \times 10^{-14} \\ 8.315 \times 10^{-14}$	9.0066×10^{-14}	3.4433×10^{-3} 1.9316×10^{-3}	78.264 56
pdb1plw 32	Classic Quaternion	2.830×10^{-14} 3.122×10^{-14}	4.9118×10^{-14}	$5.2547 \times 10^{-5} 3.2633 \times 10^{-5}$	61.02412
pdb1plx 32	Classic Quaternion	$1.574 \times 10^{-13} 2.060 \times 10^{-13}$	1.7973×10^{-13}	$\begin{array}{c} 4.9863 \times 10^{-5} \\ 3.0994 \times 10^{-5} \end{array}$	60.88212
pdb1pv0 278	Classic Quaternion	2.409×10^{-13} 2.723×10^{-13}	1.0662×10^{-13}	$5.0536 \times 10^{-4} 3.0395 \times 10^{-4}$	66.26441
$\begin{array}{c} \rm pdb1pzr \\ 724 \end{array}$	Classic Quaternion	$5.644 \times 10^{-12} \\ 5.871 \times 10^{-12}$	9.9935×10^{-12}	$7.4886 \times 10^{-3} 4.0800 \times 10^{-3}$	83.54421
pdb1qlk 1108	Classic Quaternion	9.019×10^{-10} 9.019×10^{-10}	1.3287×10^{-12}	$1.4160 \times 10^{-2} \\ 6.7812 \times 10^{-3}$	108.81176
pdb1r57 614	Classic Quaternion	$1.847 \times 10^{-13} 2.054 \times 10^{-13}$	1.4866×10^{-13}	$1.1509 \times 10^{-3} 7.1845 \times 10^{-4}$	60.19213
pdb1ry3 386	Classic Quaternion	2.023×10^{-9} 2.023×10^{-9}	6.0848×10^{-13}	$7.3868 \times 10^{-4} 4.3764 \times 10^{-4}$	68.78737
pdb1s4h 80	Classic Quaternion	4.300×10^{-9} 4.300×10^{-9}	1.1103×10^{-12}	$\begin{array}{c} 1.2121 \times 10^{-4} \\ 7.3903 \times 10^{-5} \end{array}$	64.01746
pdb1s4j 80	Classic Quaternion	$1.520 \times 10^{-13} 2.230 \times 10^{-13}$	1.6407×10^{-13}	$1.4646 \times 10^{-4} \\ 8.7409 \times 10^{-5}$	67.55712
pdb1s6j 524	Classic Quaternion	$6.073 \times 10^{-13} 7.660 \times 10^{-13}$	5.9201×10^{-13}	$\begin{array}{c} 9.8595 \times 10^{-4} \\ 6.0244 \times 10^{-4} \end{array}$	63.65882
pdb1sa8 638	Classic Quaternion	$9.340 \times 10^{-13} \\ 1.034 \times 10^{-12}$	1.0370×10^{-12}	$\begin{array}{c} 1.1605 \times 10^{-3} \\ 7.2310 \times 10^{-4} \end{array}$	60.48689
pdb1t2y 152	Classic Quaternion	$1.887 \times 10^{-13} 2.396 \times 10^{-13}$	2.3861×10^{-13}	$2.6701 \times 10^{-4} 1.6115 \times 10^{-4}$	65.68696
pdb1t5q 180	Classic Quaternion	3.877×10^{-14} 5.093×10^{-14}	5.3231×10^{-14}	$2.8653 \times 10^{-4} 1.7355 \times 10^{-4}$	65.10242
pdb1tot 314	Classic Quaternion	$6.148 \times 10^{-14} \\ 6.853 \times 10^{-14}$	2.8392×10^{-14}	$6.0050 \times 10^{-4} 3.6430 \times 10^{-4}$	64.83408
pdb1v6r 128	Classic Quaternion	$6.835 \times 10^{-13} 6.970 \times 10^{-13}$	3.1917×10^{-13}	2.2342×10^{-4} 1.3291×10^{-4}	68.095 19
pdb1v92 278	Classic Quaternion	1.463×10^{-13} 1.630×10^{-13}	5.6062×10^{-14}	$4.9476 \times 10^{-4} 2.9902 \times 10^{-4}$	65.461 84
pdb1vd7 140	Classic Quaternion	$\begin{array}{c} 3.741 \times 10^{-9} \\ 3.741 \times 10^{-9} \end{array}$	5.8433×10^{-13}	$2.3344 \times 10^{-4} 1.3950 \times 10^{-4}$	67.343 01

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb1vd9 140	Classic Quaternion	$1.290 \times 10^{-12} \\ 1.554 \times 10^{-12}$	9.0327×10^{-13}	$2.7679 \times 10^{-4} 1.6215 \times 10^{-4}$	70.70002
pdb1vdb 140	Classic Quaternion	9.108×10^{-13} 1.083×10^{-12}	3.8641×10^{-13}	$2.2516 \times 10^{-4} 1.3532 \times 10^{-4}$	66.395 08
$\begin{array}{c} \mathrm{pdb1vpc} \\ 272 \end{array}$	Classic Quaternion	$8.500 \times 10^{-15} 1.002 \times 10^{-14}$	8.5436×10^{-15}	$4.8303 \times 10^{-4} 2.9228 \times 10^{-4}$	65.26264
pdb1wnk 140	Classic Quaternion	$4.112 \times 10^{-12} 4.632 \times 10^{-12}$	2.2335×10^{-11}	$2.3185 \times 10^{-4} 1.3971 \times 10^{-4}$	65.94972
pdb1wo4 152	Classic Quaternion	$9.957 \times 10^{-13} 9.639 \times 10^{-13}$	2.3523×10^{-12}	2.6168×10^{-4} 1.5466×10^{-4}	69.19581
pdb1wo5 152	Classic Quaternion	$5.257 \times 10^{-9} 5.258 \times 10^{-9}$	4.9063×10^{-12}	2.6978×10^{-4} 1.6139×10^{-4}	67.161 64
pdb1x60 476	Classic Quaternion	$1.076 \times 10^{-12} 1.179 \times 10^{-12}$	3.9684×10^{-13}	$9.0043 \times 10^{-4} 5.6004 \times 10^{-4}$	60.779 66
pdb1x9v 544	Classic Quaternion	$8.975 \times 10^{-13} 9.632 \times 10^{-13}$	1.3900×10^{-13}	$3.4714 \times 10^{-2} 1.7086 \times 10^{-2}$	103.177 02
pdb1y5c 68	Classic Quaternion	$8.980 \times 10^{-9} 8.980 \times 10^{-9}$	2.9085×10^{-13}	$1.0994 \times 10^{-4} 6.6392 \times 10^{-5}$	65.58746
$\begin{array}{c} \text{pdb1yx7} \\ 500 \end{array}$	Classic Quaternion	$8.116 \times 10^{-10} \\ 8.125 \times 10^{-10}$	7.6614×10^{-12}	$1.3420 \times 10^{-3} \\ 8.1759 \times 10^{-4}$	64.13490
pdb1yx8 500	Classic Quaternion	$7.276 \times 10^{-12} \\ 8.217 \times 10^{-12}$	1.0819×10^{-11}	1.0980×10^{-3} 6.6669×10^{-4}	64.69641
$\begin{array}{c} \mathrm{pdb1yxr} \\ 464 \end{array}$	Classic Quaternion	$5.838 \times 10^{-10} 5.839 \times 10^{-10}$	2.5240×10^{-13}	$8.0441 \times 10^{-4} 4.8760 \times 10^{-4}$	64.973 95
$\begin{array}{c} \rm pdb2a2y \\ 1072 \end{array}$	Classic Quaternion	$1.150 \times 10^{-12} \\ 1.151 \times 10^{-12}$	3.7416×10^{-13}	$4.1882 \times 10^{-2} 1.9425 \times 10^{-2}$	115.608 11
pdb2a4j 580	Classic Quaternion	$2.085 \times 10^{-14} $ 2.727×10^{-14}	1.4394×10^{-14}	$1.2066 \times 10^{-3} 7.2504 \times 10^{-4}$	66.419 02
pdb2adl 868	Classic Quaternion	$1.752 \times 10^{-11} 1.787 \times 10^{-11}$	3.0093×10^{-12}	$8.2764 \times 10^{-2} 3.9669 \times 10^{-2}$	108.63660
pdb2adn 868	Classic Quaternion	$6.693 \times 10^{-12} 6.465 \times 10^{-12}$	2.4957×10^{-12}	2.2075×10^{-3} 1.3132×10^{-3}	68.10817
pdb2ajj 170	Classic Quaternion	$5.641 \times 10^{-14} \\ 6.584 \times 10^{-14}$	1.2744×10^{-13}	$\begin{array}{c} 2.9320 \times 10^{-4} \\ 1.7442 \times 10^{-4} \end{array}$	68.103 05
pdb2ajm 170	Classic Quaternion	1.183×10^{-13} 1.555×10^{-13}	8.9439×10^{-13}	3.1577×10^{-4} 1.8912×10^{-4}	66.97044
pdb2ajn 170	Classic Quaternion	$1.076 \times 10^{-13} 1.217 \times 10^{-13}$	1.5981×10^{-13}	$3.1551 \times 10^{-4} 1.8677 \times 10^{-4}$	68.936 10
pdb2ajo 170	Classic Quaternion	1.183×10^{-13} 1.555×10^{-13}	8.9439×10^{-13}	3.1799×10^{-4} 1.8869×10^{-4}	68.531 94
pdb2akk 446	Classic Quaternion	$1.288 \times 10^{-13} \\ 1.270 \times 10^{-13}$	1.1725×10^{-13}	$\begin{array}{c} 1.6540 \times 10^{-3} \\ 9.6115 \times 10^{-4} \end{array}$	72.08462
pdb2bzb 748	Classic Quaternion	$9.365 \times 10^{-14} \\ 1.224 \times 10^{-13}$	1.5097×10^{-13}	$1.8091 \times 10^{-2} 9.0010 \times 10^{-3}$	100.986 10
pdb2c0s 386	Classic Quaternion	3.028×10^{-13} 3.379×10^{-13}	7.2067×10^{-13}	7.4994×10^{-4} 4.5348×10^{-4}	65.375 60
pdb2dci 120	Classic Quaternion	$2.366 \times 10^{-14} 2.950 \times 10^{-14}$	1.3479×10^{-13}	$1.9331 \times 10^{-4} 1.1863 \times 10^{-4}$	62.946 92
pdb2eem 206	Classic Quaternion	5.190×10^{-13} 5.461×10^{-13}	4.0208×10^{-13}	4.1190×10^{-4} 2.4512×10^{-4}	68.04206
pdb2fva 494	Classic Quaternion	$1.047 \times 10^{-12} \\ 1.194 \times 10^{-12}$	1.5803×10^{-12}	$1.1865 \times 10^{-3} 7.0200 \times 10^{-4}$	69.024 18
pdb2fvf 494	Classic Quaternion	3.106×10^{-13} 3.445×10^{-13}	2.8750×10^{-13}	$8.6354 \times 10^{-4} 5.3257 \times 10^{-4}$	62.146 01

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2fxz 80	Classic Quaternion	$1.489 \times 10^{-12} 1.749 \times 10^{-12}$	2.0430×10^{-12}	1.3940×10^{-4} 8.4085×10^{-5}	65.78245
pdb2g9j 848	Classic Quaternion	3.282×10^{-12} 3.535×10^{-12}	2.1668×10^{-12}	6.9504×10^{-2} 3.3882×10^{-2}	105.13210
pdb2g9l 224	Classic Quaternion	$6.366 \times 10^{-14} \\ 8.672 \times 10^{-14}$	2.8081×10^{-13}	$4.0461 \times 10^{-4} 2.4340 \times 10^{-4}$	66.23213
pdb2h5m 614	Classic Quaternion	$9.692 \times 10^{-13} 1.032 \times 10^{-12}$	4.1376×10^{-12}	$1.1504 \times 10^{-3} 7.0370 \times 10^{-4}$	63.477 56
pdb2hep 252	Classic Quaternion	$1.191 \times 10^{-12} 1.268 \times 10^{-12}$	5.5848×10^{-13}	$4.5123 \times 10^{-4} 2.7064 \times 10^{-4}$	66.727 57
pdb2j0z 752	Classic Quaternion	3.192×10^{-10} 3.197×10^{-10}	4.5324×10^{-12}	$9.1775 \times 10^{-1} 4.6311 \times 10^{-1}$	98.16996
pdb2j10 752	Classic Quaternion	$5.870 \times 10^{-10} 5.873 \times 10^{-10}$	9.5552×10^{-13}	$1.0137 \times 10^{-2} $ 4.6567×10^{-3}	117.675 35
pdb2j11 752	Classic Quaternion	$7.191 \times 10^{-10} 7.194 \times 10^{-10}$	1.6970×10^{-12}	$5.4620 \times 10^{-3} 3.0397 \times 10^{-3}$	79.685 43
pdb2jmy 92	Classic Quaternion	9.834×10^{-13} 9.967×10^{-13}	5.0812×10^{-13}	$1.6556 \times 10^{-4} 1.0091 \times 10^{-4}$	64.065 33
pdb2jn5 74	Classic Quaternion	3.147×10^{-9} 3.160×10^{-9}	1.4394×10^{-11}	$1.1669 \times 10^{-4} 7.1694 \times 10^{-5}$	62.761 18
pdb2jnk 842	Classic Quaternion	$4.387 \times 10^{-10} 4.388 \times 10^{-10}$	3.9471×10^{-13}	$\begin{array}{c} 1.5665 \times 10^{-3} \\ 9.7952 \times 10^{-4} \end{array}$	59.92266
$\begin{array}{c} pdb2jpn \\ 476 \end{array}$	Classic Quaternion	$6.730 \times 10^{-14} 6.983 \times 10^{-14}$	1.9605×10^{-13}	$\begin{array}{c} 1.3840 \times 10^{-3} \\ 8.1097 \times 10^{-4} \end{array}$	70.66064
pdb2jua 614	Classic Quaternion	$1.740 \times 10^{-11} \\ 1.882 \times 10^{-11}$	1.4391×10^{-11}	$\begin{array}{c} 1.1647 \times 10^{-3} \\ 7.1516 \times 10^{-4} \end{array}$	62.85434
pdb2jvd 288	Classic Quaternion	3.339×10^{-14} 3.898×10^{-14}	2.1712×10^{-14}	$5.3906 \times 10^{-4} \\ 3.1791 \times 10^{-4}$	69.563 29
pdb2jwe 984	Classic Quaternion	$2.695 \times 10^{-11} 2.734 \times 10^{-11}$	1.0970×10^{-12}	$\begin{array}{c} 1.9257 \times 10^{-3} \\ 1.2000 \times 10^{-3} \end{array}$	60.481 48
pdb2jws 338	Classic Quaternion	$1.251 \times 10^{-13} 1.543 \times 10^{-13}$	2.8647×10^{-13}	$6.7057 \times 10^{-4} 3.9551 \times 10^{-4}$	69.545 36
pdb2jwu 338	Classic Quaternion	$\begin{array}{c} 4.421 \times 10^{-12} \\ 4.373 \times 10^{-12} \end{array}$	6.2322×10^{-13}	$\begin{array}{c} 9.5804 \times 10^{-4} \\ 5.5398 \times 10^{-4} \end{array}$	72.93662
pdb2jxf 182	Classic Quaternion	$1.399 \times 10^{-13} \\ 1.734 \times 10^{-13}$	5.8450×10^{-13}	3.2221×10^{-4} 1.9337×10^{-4}	66.62771
pdb2jz5 548	Classic Quaternion	2.860×10^{-13} 2.854×10^{-13}	1.7635×10^{-13}	$1.1449 \times 10^{-3} \\ 6.8794 \times 10^{-4}$	66.42672
pdb2k2a 422	Classic Quaternion	3.798×10^{-14} 5.134×10^{-14}	1.3435×10^{-13}	8.5947×10^{-4} 5.1708×10^{-4}	66.21780
pdb2k2f 1268	Classic Quaternion	$2.639 \times 10^{-13} \\ 2.818 \times 10^{-13}$	7.2949×10^{-14}	5.4893 2.7229	101.601 27
pdb2k36 896	Classic Quaternion	$1.922 \times 10^{-13} 2.045 \times 10^{-13}$	1.2563×10^{-13}	$1.6274 \times 10^{-3} 1.0185 \times 10^{-3}$	59.78318
pdb2k37 356	Classic Quaternion	$1.921 \times 10^{-13} 2.525 \times 10^{-13}$	4.0204×10^{-13}	$6.7390 \times 10^{-4} 4.0386 \times 10^{-4}$	66.86620
pdb2k3i 656	Classic Quaternion	3.810×10^{-13} 4.009×10^{-13}	2.4790×10^{-13}	$\begin{array}{c} 1.6771 \times 10^{-3} \\ 9.9328 \times 10^{-4} \end{array}$	68.842 45
pdb2k6s 494	Classic Quaternion	$2.100 \times 10^{-13} 2.651 \times 10^{-13}$	4.8726×10^{-13}	$1.4712 \times 10^{-3} \\ 8.5722 \times 10^{-4}$	71.61938
pdb2k7o 1096	Classic Quaternion	1.279×10^{-13} 1.416×10^{-13}	4.6393×10^{-13}	$5.6416 \times 10^{-3} \\ 3.1674 \times 10^{-3}$	78.11370
pdb2kbm 1268	Classic Quaternion	$2.165 \times 10^{-13} 2.230 \times 10^{-13}$	2.6963×10^{-13}	2.2556 1.1098	103.239 00

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2kdh 434	Classic Quaternion	$1.947 \times 10^{-11} \\ 2.228 \times 10^{-11}$	7.6317×10^{-11}	$1.0340 \times 10^{-3} \\ 6.0895 \times 10^{-4}$	69.80338
pdb2kdl 338	Classic Quaternion	$2.301 \times 10^{-13} 2.927 \times 10^{-13}$	3.1526×10^{-13}	$6.4298 \times 10^{-4} 3.8115 \times 10^{-4}$	68.69338
pdb2kdm 338	Classic Quaternion	3.191×10^{-12} 3.284×10^{-12}	9.9439×10^{-13}	$6.1470 \times 10^{-4} 3.6995 \times 10^{-4}$	66.155 79
pdb2kdp 428	Classic Quaternion	$2.621 \times 10^{-13} 2.865 \times 10^{-13}$	1.0772×10^{-13}	$7.9344 \times 10^{-4} 4.7257 \times 10^{-4}$	67.89987
pdb2kdr 170	Classic Quaternion	$6.617 \times 10^{-14} \\ 8.490 \times 10^{-14}$	6.1679×10^{-14}	$3.0345 \times 10^{-4} \\ 1.8116 \times 10^{-4}$	67.50405
pdb2kes 290	Classic Quaternion	$4.468 \times 10^{-14} 5.425 \times 10^{-14}$	2.3286×10^{-14}	$5.8000 \times 10^{-4} 3.3743 \times 10^{-4}$	71.88793
pdb2kib 352	Classic Quaternion	$2.533 \times 10^{-12} 2.539 \times 10^{-12}$	1.3388×10^{-12}	7.0185×10^{-3} 3.8145×10^{-3}	83.993 98
pdb2kjn 158	Classic Quaternion	$1.125 \times 10^{-9} 1.125 \times 10^{-9}$	1.3817×10^{-13}	$2.7560 \times 10^{-4} 1.6547 \times 10^{-4}$	66.548 92
pdb2kjo 158	Classic Quaternion	$2.284 \times 10^{-13} 2.421 \times 10^{-13}$	6.7185×10^{-14}	$2.6341 \times 10^{-4} 1.5811 \times 10^{-4}$	66.600 04
pdb2kjr 572	Classic Quaternion	$3.247 \times 10^{-12} 3.251 \times 10^{-12}$	4.0637×10^{-13}	$1.6612 \times 10^{-3} 9.6695 \times 10^{-4}$	71.79248
pdb2kko 1300	Classic Quaternion	1.191×10^{-13} 1.285×10^{-13}	2.9766×10^{-14}	$1.1580 \times 10^{-2} 5.3994 \times 10^{-3}$	114.476 59
pdb2kl5 662	Classic Quaternion	$1.820 \times 10^{-13} 2.020 \times 10^{-13}$	1.3796×10^{-13}	$1.1682 \times 10^{-3} 7.2738 \times 10^{-4}$	60.60902
$\begin{array}{c} \text{pdb2klz} \\ 276 \end{array}$	Classic Quaternion	3.439×10^{-14} 4.443×10^{-14}	6.4874×10^{-14}	$5.3462 \times 10^{-4} 3.1399 \times 10^{-4}$	70.26847
pdb2ko1 1060	Classic Quaternion	1.150×10^{-12} 1.151×10^{-12}	7.8450×10^{-13}	$1.6068 \times 10^{-2} 7.8097 \times 10^{-3}$	105.74497
pdb2koz 200	Classic Quaternion	$1.075 \times 10^{-9} 1.075 \times 10^{-9}$	8.8024×10^{-13}	$3.4678 \times 10^{-4} 2.1238 \times 10^{-4}$	63.283 12
pdb2kp0 200	Classic Quaternion	4.893×10^{-12} 5.588×10^{-12}	4.2756×10^{-12}	$3.7779 \times 10^{-4} 2.2317 \times 10^{-4}$	69.28340
pdb2ksg 290	Classic Quaternion	3.215×10^{-14} 3.967×10^{-14}	2.4678×10^{-14}	$\begin{array}{c} 4.9497 \times 10^{-4} \\ 2.9655 \times 10^{-4} \end{array}$	66.90811
pdb2kt8 458	Classic Quaternion	3.314×10^{-12} 3.535×10^{-12}	7.1394×10^{-13}	$8.1415 \times 10^{-4} 4.9532 \times 10^{-4}$	64.36676
pdb2kuh 404	Classic Quaternion	$2.016 \times 10^{-14} 2.492 \times 10^{-14}$	4.0485×10^{-14}	8.0609×10^{-4} 4.8916×10^{-4}	64.791 37
pdb2kwh 338	Classic Quaternion	$1.408 \times 10^{-13} 1.825 \times 10^{-13}$	2.9549×10^{-13}	5.9954×10^{-4} 3.5826×10^{-4}	67.347 03
pdb2kxa 144	Classic Quaternion	$\begin{array}{c} 1.325 \times 10^{-12} \\ 1.351 \times 10^{-12} \end{array}$	3.5240×10^{-13}	$\begin{array}{c} 2.4131 \times 10^{-4} \\ 1.4810 \times 10^{-4} \end{array}$	62.93424
$\begin{array}{c} \mathrm{pdb2kyb} \\ 362 \end{array}$	Classic Quaternion	$1.999 \times 10^{-8} 1.999 \times 10^{-8}$	2.6711×10^{-12}	$1.8346 \times 10^{-3} 1.0283 \times 10^{-3}$	78.415 08
pdb2l3m 428	Classic Quaternion	$1.028 \times 10^{-12} 9.340 \times 10^{-13}$	6.9725×10^{-13}	7.6538×10^{-4} 4.6736×10^{-4}	63.765 18
pdb2l3n 626	Classic Quaternion	3.025×10^{-14} 3.634×10^{-14}	4.4517×10^{-14}	$4.6289 \times 10^{-3} 2.5401 \times 10^{-3}$	82.23477
pdb2l45 116	Classic Quaternion	$2.236 \times 10^{-14} 3.033 \times 10^{-14}$	8.5325×10^{-14}	$2.0473 \times 10^{-4} 1.2174 \times 10^{-4}$	68.172 05
pdb2l5r 138	Classic Quaternion	3.529×10^{-14} 4.432×10^{-14}	1.4398×10^{-14}	2.7732×10^{-4} 1.6351×10^{-4}	69.60232
pdb2l6q 374	Classic Quaternion	$9.260 \times 10^{-9} \\ 1.043 \times 10^{-8}$	1.7792×10^{-8}	$6.5059 \times 10^{-4} 3.9752 \times 10^{-4}$	63.66393

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2l6r 374	Classic Quaternion			63.91045	
pdb2l98 434	Classic Quaternion	3.273×10^{-13} 3.638×10^{-13}	8.9102×10^{-13}	$8.3189 \times 10^{-4} 4.9565 \times 10^{-4}$	67.83843
pdb2lci 806	Classic Quaternion	$2.579 \times 10^{-13} 2.404 \times 10^{-13}$	8.2767×10^{-14}	$1.4953 \times 10^{-3} 9.1594 \times 10^{-4}$	63.258 27
pdb2lde 152	Classic Quaternion	3.153×10^{-14} 3.762×10^{-14}	4.1691×10^{-14}	$2.4935 \times 10^{-4} 1.5007 \times 10^{-4}$	66.157 56
pdb2le2 676	Classic Quaternion	$2.064 \times 10^{-13} 2.042 \times 10^{-13}$	7.7661×10^{-14}	$1.5828 \times 10^{-2} 7.6362 \times 10^{-3}$	107.271 58
pdb2le7 122	Classic Quaternion	$2.112 \times 10^{-14} 2.749 \times 10^{-14}$	3.9789×10^{-14}	2.0560×10^{-4} 1.2262×10^{-4}	67.66430
pdb2ler 68	Classic Quaternion	$1.315 \times 10^{-14} 1.532 \times 10^{-14}$	2.1465×10^{-14}	$1.1181 \times 10^{-4} \\ 6.7622 \times 10^{-5}$	65.346 08
pdb2lgi 338	Classic Quaternion	$1.068 \times 10^{-12} \\ 1.052 \times 10^{-12}$	1.8917×10^{-13}	$6.1011 \times 10^{-4} \\ 3.7216 \times 10^{-4}$	63.938 76
pdb2lhc 338	Classic Quaternion	5.829×10^{-10} 5.830×10^{-10}	2.1362×10^{-12}	$6.6728 \times 10^{-4} 3.9795 \times 10^{-4}$	67.68037
pdb2lhd 338	Classic Quaternion	$1.930 \times 10^{-12} 2.033 \times 10^{-12}$	2.3902×10^{-12}	8.2372×10^{-4} 4.8768×10^{-4}	68.90746
pdb2lhe 338	Classic Quaternion	4.963×10^{-11} 4.967×10^{-11}	4.8488×10^{-13}	7.9542×10^{-4} 4.7306×10^{-4}	68.14276
pdb2lhg 338	Classic Quaternion	$6.459 \times 10^{-14} 7.322 \times 10^{-14}$	5.9754×10^{-14}	$6.2955 \times 10^{-4} 3.8394 \times 10^{-4}$	63.972 53
pdb2lix 162	Classic Quaternion	4.842×10^{-14} 5.614×10^{-14}	7.8975×10^{-14}	2.8652×10^{-4} 1.7148×10^{-4}	67.08790
pdb2lld 242	Classic Quaternion	$\begin{array}{c} 1.937 \times 10^{-13} \\ 2.214 \times 10^{-13} \end{array}$	2.2642×10^{-13}	4.4840×10^{-4} 2.7615×10^{-4}	62.37681
pdb2lm9 578	Classic Quaternion	$6.254 \times 10^{-14} 7.713 \times 10^{-14}$	1.5079×10^{-13}	$1.0445 \times 10^{-3} \\ 6.3262 \times 10^{-4}$	65.10099
pdb2lmf 140	Classic Quaternion	$1.282 \times 10^{-13} \\ 1.462 \times 10^{-13}$	7.9808×10^{-14}	2.2760×10^{-4} 1.3654×10^{-4}	66.69267
pdb2ln3 500	Classic Quaternion	$\begin{array}{c} 1.292 \times 10^{-13} \\ 1.359 \times 10^{-13} \end{array}$	8.4114×10^{-14}	$\begin{array}{c} 9.2559 \times 10^{-4} \\ 5.6168 \times 10^{-4} \end{array}$	64.787 76
pdb2lo2 230	Classic Quaternion	$2.068 \times 10^{-14} $ 2.571×10^{-14}	3.6944×10^{-14}	3.9914×10^{-4} 2.4200×10^{-4}	64.931 22
pdb2lqp 428	Classic Quaternion	2.950×10^{-13} 3.085×10^{-13}	4.7561×10^{-13}	7.7204×10^{-4} 4.6975×10^{-4}	64.350 52
pdb2lr0 806	Classic Quaternion	3.549×10^{-12} 3.440×10^{-12}	6.0485×10^{-13}	$\begin{array}{c} 1.5240 \times 10^{-3} \\ 9.3151 \times 10^{-4} \end{array}$	63.610 15
pdb2lrh 806	Classic Quaternion	$\begin{array}{c} 5.631 \times 10^{-13} \\ 6.564 \times 10^{-13} \end{array}$	3.2048×10^{-13}	$\begin{array}{c} 1.4892 \times 10^{-3} \\ 9.1309 \times 10^{-4} \end{array}$	63.09709
pdb2ls9 152	Classic Quaternion	$1.122 \times 10^{-13} \\ 1.471 \times 10^{-13}$	3.7128×10^{-13}	2.3982×10^{-4} 1.4535×10^{-4}	64.98870
pdb2lsa 140	Classic Quaternion	$5.235 \times 10^{-14} 7.034 \times 10^{-14}$	1.5385×10^{-13}	2.3711×10^{-4} 1.4364×10^{-4}	65.065 25
$\begin{array}{c} \text{pdb2lss} \\ 422 \end{array}$	Classic Quaternion	$1.230 \times 10^{-13} \\ 1.455 \times 10^{-13}$	1.6926×10^{-13}	$7.6212 \times 10^{-4} 4.7620 \times 10^{-4}$	60.039 98
pdb2lt3 680	Classic Quaternion	$7.245 \times 10^{-14} 7.760 \times 10^{-14}$	5.2634×10^{-14}	$1.2642 \times 10^{-3} 7.8956 \times 10^{-4}$	60.11423
pdb2lu6 86	Classic Quaternion	$5.356 \times 10^{-15} \\ 6.922 \times 10^{-15}$	4.1890×10^{-15}	$1.4840 \times 10^{-4} \\ 8.7935 \times 10^{-5}$	68.75988
pdb2lwa 432	Classic Quaternion	$\begin{array}{c} 3.615 \times 10^{-13} \\ 4.427 \times 10^{-13} \end{array}$	9.3395×10^{-13}	$7.6963 \times 10^{-4} 4.6916 \times 10^{-4}$	64.04462

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2lx0 194	Classic 1.940×10^{-9} 3.5120×10^{-4} Quaternion 1.940×10^{-9} 2.0923×10^{-13} 2.1099×10^{-4}		66.45686		
pdb2lxb 892	Classic Quaternion	$1.542 \times 10^{-13} 1.585 \times 10^{-13}$	1.6837×10^{-13}	2.0736×10^{-3} 1.2389×10^{-3}	67.368 73
$\begin{array}{c} \text{pdb2lxy} \\ 404 \end{array}$	Classic Quaternion	$9.313 \times 10^{-13} 1.025 \times 10^{-12}$	1.6618×10^{-12}	$9.4891 \times 10^{-4} 5.5823 \times 10^{-4}$	69.986 27
pdb2lxz 194	Classic Quaternion	$2.371 \times 10^{-12} 2.792 \times 10^{-12}$	1.9895×10^{-12}	$3.6233 \times 10^{-4} 2.1837 \times 10^{-4}$	65.928 01
pdb2lzf 820	Classic Quaternion	$3.217 \times 10^{-14} 3.957 \times 10^{-14}$	1.2991×10^{-13}	$5.1196 \times 10^{-2} 2.4720 \times 10^{-2}$	107.10568
pdb2m1a 158	Classic Quaternion	$6.346 \times 10^{-15} 7.612 \times 10^{-15}$	6.5801×10^{-15}	$3.2338 \times 10^{-4} $ 1.9137×10^{-4}	68.978 54
pdb2m1j 182	Classic Quaternion	$1.865 \times 10^{-14} $ 2.212×10^{-14}	6.6915×10^{-14}	3.3130×10^{-4} 1.9828×10^{-4}	67.08484
pdb2m2y 110	Classic Quaternion	$2.699 \times 10^{-13} 2.808 \times 10^{-13}$	1.4386×10^{-13}	$1.8685 \times 10^{-4} 1.1245 \times 10^{-4}$	66.16688
pdb2m3f 134	Classic Quaternion	$3.629 \times 10^{-14} 4.641 \times 10^{-14}$	5.8107×10^{-14}	$2.1466 \times 10^{-4} 1.3036 \times 10^{-4}$	64.66922
pdb2m4j 2178	Classic Quaternion	1.463×10^{-11} 1.455×10^{-11}	1.8385×10^{-13}	4.0158×10^{-2} 1.9961×10^{-2}	101.181 51
pdb2m8m 170	Classic Quaternion	$2.407 \times 10^{-14} 3.023 \times 10^{-14}$	1.1738×10^{-13}	2.8258×10^{-4} 1.7129×10^{-4}	64.973 13
pdb2m8o 170	Classic Quaternion	$1.672 \times 10^{-14} 2.039 \times 10^{-14}$	2.4755×10^{-14}	2.7663×10^{-4} 1.6880×10^{-4}	63.88076
pdb2m97 416	Classic Quaternion	$4.646 \times 10^{-14} \\ 5.841 \times 10^{-14}$	2.0639×10^{-13}	$7.6201 \times 10^{-4} 4.7284 \times 10^{-4}$	61.15389
pdb2m9g 1108	Classic Quaternion	$2.939 \times 10^{-13} 3.170 \times 10^{-13}$	5.8913×10^{-13}	2.0976×10^{-3} 1.2856×10^{-3}	63.16189
pdb2m9r 242	Classic Quaternion	$3.537 \times 10^{-14} 4.406 \times 10^{-14}$	1.6694×10^{-13}	$4.3800 \times 10^{-4} 2.5305 \times 10^{-4}$	73.088 18
$\begin{array}{c} \rm pdb2mdv\\ 460\end{array}$	Classic Quaternion	$3.178 \times 10^{-12} 3.178 \times 10^{-12}$	3.0402×10^{-13}	2.1264×10^{-3} 1.2079×10^{-3}	76.04640
pdb2me1 164	Classic Quaternion	1.886×10^{-13} 2.208×10^{-13}	1.6579×10^{-13}	$2.7337 \times 10^{-4} 1.6513 \times 10^{-4}$	65.54894
pdb2me2 164	Classic Quaternion	$3.667 \times 10^{-13} 5.098 \times 10^{-13}$	1.1486×10^{-12}	2.9177×10^{-4} 1.7359×10^{-4}	68.082 58
pdb2me3 164	Classic Quaternion	$2.593 \times 10^{-9} 2.593 \times 10^{-9}$	9.2137×10^{-14}	$2.6801 \times 10^{-4} 1.6247 \times 10^{-4}$	64.96376
pdb2me4 164	Classic Quaternion	$2.854 \times 10^{-9} 2.854 \times 10^{-9}$	9.9945×10^{-13}	3.1285×10^{-4} 1.8609×10^{-4}	68.12227
pdb2mg1 164	Classic Quaternion	$\begin{array}{c} 4.398 \times 10^{-14} \\ 5.374 \times 10^{-14} \end{array}$	1.5805×10^{-13}	$\begin{array}{c} 2.7477 \times 10^{-4} \\ 1.6842 \times 10^{-4} \end{array}$	63.153 22
pdb2mg2 170	Classic Quaternion	$1.829 \times 10^{-14} 2.480 \times 10^{-14}$	2.5921×10^{-14}	$2.8189 \times 10^{-4} 1.7237 \times 10^{-4}$	63.538 77
pdb2mg3 170	Classic Quaternion	3.541×10^{-14} 4.461×10^{-14}	2.4798×10^{-13}	$2.9087 \times 10^{-4} 1.7847 \times 10^{-4}$	62.97889
pdb2mh8 338	Classic Quaternion	$1.547 \times 10^{-13} \\ 1.883 \times 10^{-13}$	2.9903×10^{-13}	6.4620×10^{-4} 3.8846×10^{-4}	66.35020
pdb2mhw 164	Classic Quaternion	$6.229 \times 10^{-14} 7.129 \times 10^{-14}$	4.9718×10^{-13}	$2.8046 \times 10^{-4} $ 1.7330×10^{-4}	61.83457
pdb2mi1 84	Classic Quaternion	$1.827 \times 10^{-12} 2.052 \times 10^{-12}$	1.5687×10^{-12}	$\begin{array}{c} 1.5245 \times 10^{-4} \\ 9.2051 \times 10^{-5} \end{array}$	65.61743
pdb2mi7 404	Classic Quaternion	$6.022 \times 10^{-13} \\ 6.817 \times 10^{-13}$	1.3690×10^{-12}	$6.6253 \times 10^{-4} 4.0685 \times 10^{-4}$	62.84471

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2mij 224	Classic Quaternion	1.244×10^{-13} 1.522×10^{-13}	2.8681×10^{-13}	$3.8008 \times 10^{-4} $ 2.2922×10^{-4}	65.81037
pdb2mix 128	Classic Quaternion	$4.816 \times 10^{-14} 4.684 \times 10^{-14}$	3.7348×10^{-14}	$2.1355 \times 10^{-4} 1.3050 \times 10^{-4}$	63.633 44
pdb2mj1 110	Classic Quaternion	1.309×10^{-13} 1.646×10^{-13}	2.3819×10^{-13}	1.9866×10^{-4} 1.1766×10^{-4}	68.84296
pdb2mj2 218	Classic Quaternion	9.775×10^{-14} 1.196×10^{-13}	8.8713×10^{-14}	$3.8096 \times 10^{-4} 2.2764 \times 10^{-4}$	67.35497
$\begin{array}{c} \rm pdb2mjg \\ 556 \end{array}$	Classic Quaternion	$5.503 \times 10^{-14} $ 6.580×10^{-14}	7.0670×10^{-14}	$2.4548 \times 10^{-3} 1.3970 \times 10^{-3}$	75.71910
pdb2mji 788	Classic Quaternion	3.207×10^{-12} 3.247×10^{-12}	2.7336×10^{-13}	$1.4144 \times 10^{-3} \\ 8.8363 \times 10^{-4}$	60.06735
pdb2mle 434	Classic Quaternion	$1.491 \times 10^{-13} 1.535 \times 10^{-13}$	3.1271×10^{-13}	$8.0971 \times 10^{-4} 4.8857 \times 10^{-4}$	65.72887
pdb2mlf 434	Classic Quaternion	9.918×10^{-14} 1.128×10^{-13}	9.2903×10^{-14}	$8.0349 \times 10^{-4} 4.8419 \times 10^{-4}$	65.946 59
pdb2mo5 854	Classic Quaternion	$2.527 \times 10^{-10} 2.527 \times 10^{-10}$	1.0204×10^{-12}	$1.5646 \times 10^{-3} 9.7189 \times 10^{-4}$	60.981 08
pdb2mpu 554	Classic Quaternion	$9.785 \times 10^{-14} $ 1.016×10^{-13}	1.0352×10^{-13}	1.0274×10^{-3} 6.3650×10^{-4}	61.421 28
pdb2mra 704	Classic Quaternion	2.632×10^{-13} 2.768×10^{-13}	1.2867×10^{-13}	$1.6134 \times 10^{-3} 9.6953 \times 10^{-4}$	66.41381
pdb2msu 122	Classic Quaternion	$7.813 \times 10^{-14} \\ 8.765 \times 10^{-14}$	3.7025×10^{-14}	$2.2473 \times 10^{-4} 1.3344 \times 10^{-4}$	68.41932
pdb2mty 120	Classic Quaternion	$1.849 \times 10^{-14} 2.364 \times 10^{-14}$	9.1457×10^{-14}	$2.4184 \times 10^{-4} 1.4186 \times 10^{-4}$	70.478 04
pdb2muh 98	Classic Quaternion	2.008×10^{-13} 2.251×10^{-13}	1.4292×10^{-13}	$\begin{array}{c} 1.6587 \times 10^{-4} \\ 9.9743 \times 10^{-5} \end{array}$	66.29972
pdb2mvj 156	Classic Quaternion	$1.534 \times 10^{-13} 1.647 \times 10^{-13}$	5.5998×10^{-14}	$2.6945 \times 10^{-4} 1.6377 \times 10^{-4}$	64.52874
pdb2mvt 284	Classic Quaternion	$6.053 \times 10^{-12} 6.226 \times 10^{-12}$	3.1969×10^{-12}	$6.4266 \times 10^{-4} 3.7860 \times 10^{-4}$	69.74934
pdb2mvx 2360	Classic Quaternion	$\begin{array}{c} 4.728 \times 10^{-9} \\ 4.729 \times 10^{-9} \end{array}$	3.7181×10^{-11}	3.7186×10^{-2} 1.8636×10^{-2}	99.533 19
pdb2mz6 220	Classic Quaternion	$4.129 \times 10^{-8} 4.129 \times 10^{-8}$	4.4231×10^{-13}	$9.7662 \times 10^{-2} $ 4.7517×10^{-2}	105.533 00
pdb2n00 572	Classic Quaternion	2.703×10^{-13} 3.467×10^{-13}	7.3499×10^{-13}	$8.9193 \times 10^{-4} 5.6154 \times 10^{-4}$	58.83733
pdb2n0b 60	Classic Quaternion	$7.104 \times 10^{-13} 9.458 \times 10^{-13}$	8.9441×10^{-13}	$1.0532 \times 10^{-4} \\ 6.4478 \times 10^{-5}$	63.339 43
pdb2n0c 60	Classic Quaternion	$\begin{array}{c} 1.293 \times 10^{-13} \\ 1.682 \times 10^{-13} \end{array}$	2.8483×10^{-13}	$\begin{array}{c} 9.9088 \times 10^{-5} \\ 5.9963 \times 10^{-5} \end{array}$	65.249 95
pdb2n0d 60	Classic Quaternion	$1.925 \times 10^{-9} 1.926 \times 10^{-9}$	1.6149×10^{-11}	$9.9021 \times 10^{-5} 6.0649 \times 10^{-5}$	63.269 50
pdb2n0e 60	Classic Quaternion	3.314×10^{-12} 4.286×10^{-12}	8.3573×10^{-12}	$1.0405 \times 10^{-4} \\ 6.3836 \times 10^{-5}$	63.000 01
pdb2n0f 60	Classic Quaternion	$8.103 \times 10^{-9} \\ 8.103 \times 10^{-9}$	5.8011×10^{-13}	9.4798×10^{-5} 5.8399×10^{-5}	62.328 66
pdb2n0g 60	Classic Quaternion	$8.315 \times 10^{-13} 9.618 \times 10^{-13}$	1.3124×10^{-13}	$\begin{array}{c} 1.1269 \times 10^{-4} \\ 6.7681 \times 10^{-5} \end{array}$	66.50463
pdb2n0h 60	Classic Quaternion	7.690×10^{-13} 8.730×10^{-13}	1.8191×10^{-13}	$1.0649 \times 10^{-4} \\ 6.5592 \times 10^{-5}$	62.35774
pdb2n35 314	Classic Quaternion	3.541×10^{-14} 4.466×10^{-14}	1.0752×10^{-13}	$5.7583 \times 10^{-4} 3.4850 \times 10^{-4}$	65.229 90

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2n3a 574	Classic Quaternion	$8.761 \times 10^{-14} 1.049 \times 10^{-13}$	1.0149×10^{-13}	2.1136×10^{-2} 1.0581×10^{-2}	99.75447
pdb2n41 638	Classic Quaternion	1.812×10^{-13} 1.836×10^{-13}	8.2539×10^{-14}	$\begin{array}{c} 1.2214 \times 10^{-3} \\ 7.5387 \times 10^{-4} \end{array}$	62.020 24
pdb2n4e 638	Classic Quaternion	1.494×10^{-13} 1.687×10^{-13}	1.8433×10^{-13}	$1.2005 \times 10^{-3} 7.4403 \times 10^{-4}$	61.35593
pdb2n5q 164	Classic Quaternion	$1.732 \times 10^{-12} 1.745 \times 10^{-12}$	1.7589×10^{-12}	$2.8586 \times 10^{-4} $ 1.7326×10^{-4}	64.988 36
pdb2n67 566	Classic Quaternion	$4.443 \times 10^{-13} 4.465 \times 10^{-13}$	6.3487×10^{-14}	$1.0705 \times 10^{-3} 6.5889 \times 10^{-4}$	62.466 17
pdb2n6n 192	Classic Quaternion	$4.139 \times 10^{-8} 4.139 \times 10^{-8}$	5.0670×10^{-13}	$3.5018 \times 10^{-4} $ 2.1213×10^{-4}	65.076 79
pdb2n7i 224	Classic Quaternion	9.212×10^{-13} 1.126×10^{-12}	3.0537×10^{-12}	$3.9039 \times 10^{-4} 2.3389 \times 10^{-4}$	66.911 44
pdb2n7j 336	Classic Quaternion	$5.969 \times 10^{-13} 6.094 \times 10^{-13}$	1.5144×10^{-13}	$6.2452 \times 10^{-4} 3.7466 \times 10^{-4}$	66.69233
pdb2n9b 832	Classic Quaternion	1.196×10^{-12} 1.238×10^{-12}	1.1231×10^{-12}	$1.0415 \times 10^{-2} 4.6876 \times 10^{-3}$	122.17414
pdb2na9 266	Classic Quaternion	$5.440 \times 10^{-14} 6.690 \times 10^{-14}$	5.4544×10^{-14}	$4.5118 \times 10^{-4} 2.6866 \times 10^{-4}$	67.933 62
pdb2ndc 110	Classic Quaternion	3.365×10^{-14} 4.479×10^{-14}	5.1916×10^{-14}	$1.9645 \times 10^{-4} 1.1711 \times 10^{-4}$	67.751 29
pdb2nde 110	Classic Quaternion	7.022×10^{-14} 8.868×10^{-14}	2.5156×10^{-13}	$1.7381 \times 10^{-4} 1.0512 \times 10^{-4}$	65.34687
pdb2ndk 290	Classic Quaternion	$5.022 \times 10^{-13} 6.279 \times 10^{-13}$	2.0516×10^{-12}	4.9350×10^{-4} 3.0069×10^{-4}	64.12092
pdb2nvj 152	Classic Quaternion	$2.082 \times 10^{-14} 2.293 \times 10^{-14}$	1.4035×10^{-14}	$2.3645 \times 10^{-4} 1.4631 \times 10^{-4}$	61.61223
pdb2p6j 314	Classic Quaternion	$4.795 \times 10^{-14} 6.389 \times 10^{-14}$	1.1404×10^{-13}	$5.6452 \times 10^{-4} 3.4004 \times 10^{-4}$	66.01640
pdb2p81 266	Classic Quaternion	$7.881 \times 10^{-13} \\ 8.250 \times 10^{-13}$	4.3715×10^{-13}	$4.5289 \times 10^{-4} 2.7048 \times 10^{-4}$	67.435 54
pdb2pqe 896	Classic Quaternion	$6.484 \times 10^{-10} \\ 6.496 \times 10^{-10}$	8.5673×10^{-12}	2.0028×10^{-3} 1.2182×10^{-3}	64.40425
pdb2rlg 108	Classic Quaternion	$5.501 \times 10^{-14} \\ 6.973 \times 10^{-14}$	6.8873×10^{-14}	$\begin{array}{c} 1.9145 \times 10^{-4} \\ 1.1444 \times 10^{-4} \end{array}$	67.28663
pdb2rlh 108	Classic Quaternion	$4.772 \times 10^{-14} 5.801 \times 10^{-14}$	3.9131×10^{-14}	$2.0634 \times 10^{-4} 1.2294 \times 10^{-4}$	67.845 06
pdb2rmy 206	Classic Quaternion	$1.872 \times 10^{-13} 2.498 \times 10^{-13}$	3.6453×10^{-13}	3.6036×10^{-4} 2.1423×10^{-4}	68.21464
pdb2rnd 206	Classic Quaternion	$\begin{array}{c} 2.626 \times 10^{-13} \\ 3.581 \times 10^{-13} \end{array}$	4.9979×10^{-13}	3.4764×10^{-4} 2.0993×10^{-4}	65.595 44
pdb2roo 260	Classic Quaternion	$2.933 \times 10^{-12} 3.525 \times 10^{-12}$	3.5927×10^{-12}	$1.0899 \times 10^{-3} \\ 6.1599 \times 10^{-4}$	76.93892
$\begin{array}{c} pdb2rql\\ 572\end{array}$	Classic Quaternion	2.345×10^{-12} 2.496×10^{-12}	8.7086×10^{-13}	$\begin{array}{c} 1.4716 \times 10^{-3} \\ 8.7885 \times 10^{-4} \end{array}$	67.44257
pdb2rut 218	Classic Quaternion	$4.389 \times 10^{-14} \\ 5.014 \times 10^{-14}$	3.5338×10^{-13}	3.7874×10^{-4} 2.2736×10^{-4}	66.579 51
pdb2ruv 224	Classic Quaternion	$5.776 \times 10^{-14} 7.408 \times 10^{-14}$	1.2473×10^{-13}	3.9526×10^{-4} 2.3560×10^{-4}	67.767 96
pdb2rux 218	Classic Quaternion	$2.671 \times 10^{-14} \\ 3.016 \times 10^{-14}$	6.2140×10^{-14}	3.9808×10^{-4} 2.3731×10^{-4}	67.745 85
pdb2ruy 224	Classic Quaternion	$1.968 \times 10^{-14} 2.387 \times 10^{-14}$	6.4254×10^{-14}	3.9089×10^{-4} 2.3568×10^{-4}	65.85413

Table 2: Results - continued

Problem Size	Method	LDE	RMSD	Time	Improv time
pdb2rv3 218	Classic Quaternion	3.656×10^{-14} 4.118×10^{-14}	6.3794×10^{-14}	4.0489×10^{-4} 2.4209×10^{-4}	67.248 33
$pdb2rv5 \\ 212$			1.6010×10^{-14}	3.7540×10^{-4} 2.2636×10^{-4}	65.841 45
pdb2y4q 476	Classic Quaternion	$1.410 \times 10^{-12} \\ 1.451 \times 10^{-12}$	2.0648×10^{-13}	8.2759×10^{-4} 5.0510×10^{-4}	63.847 03

1.2 Using BP-All versions

Table 3: Results

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb1a57 698	ClassicAll QuaternionAll	8 8	3.1806×10^{-11} 3.3550×10^{-11}	5 5	$2.096 \times 10^{-11} 2.092 \times 10^{-11}$	$7.2168 \times 10^{-3} $ 4.4005×10^{-3}	63.999
pdb1b4c 1108	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.6824 \times 10^{-12} \\ 3.4662 \times 10^{-12} \end{array}$	5 5	$5.067 \times 10^{-13} 5.493 \times 10^{-13}$	$2.1307 \times 10^{-2} \\ 1.1153 \times 10^{-2}$	91.045
pdb1ba5 320	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.5621 \times 10^{-2} \\ 3.5621 \times 10^{-2} \end{array}$	6 6	$9.363 \times 10^{-13} 1.069 \times 10^{-12}$	$\begin{array}{c} 2.2181 \times 10^{-3} \\ 1.4090 \times 10^{-3} \end{array}$	57.428
pdb1d1n 594	ClassicAll QuaternionAll	$\frac{2}{2}$	$2.9766 \times 10^{-11} 2.9311 \times 10^{-11}$	1 1	$1.005 \times 10^{-11} 9.672 \times 10^{-12}$	3.4262×10^{-3} 1.9654×10^{-3}	74.331
pdb1dp3 332	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.9981 \times 10^{-5} \\ 4.9981 \times 10^{-5} \end{array}$	$\frac{2}{2}$	7.704×10^{-13} 8.940×10^{-13}	$2.2527 \times 10^{-3} 1.4370 \times 10^{-3}$	56.765
pdb1du1 122	ClassicAll QuaternionAll	8 8	$6.6600 \times 10^{-13} $ 1.6577×10^{-12}	1 1	8.225×10^{-13} 1.258×10^{-12}	$7.7204 \times 10^{-4} 5.0114 \times 10^{-4}$	54.055
pdb1eii 806	ClassicAll QuaternionAll	8 8	1.9451×10^{-10} 1.8740×10^{-10}	1 1	1.393×10^{-11} 1.365×10^{-11}	$5.7653 \times 10^{-3} 3.7502 \times 10^{-3}$	53.735
pdb1fcl 338	ClassicAll QuaternionAll	8 8	1.5447×10^{-11} 1.5223×10^{-11}	2 2	$4.542 \times 10^{-12} 4.515 \times 10^{-12}$	2.3463×10^{-3} 1.5115×10^{-3}	55.228
pdb1fd6 344	ClassicAll QuaternionAll	8 8	$2.0242 \times 10^{-5} 2.0242 \times 10^{-5}$	2 2	3.182×10^{-12} 3.193×10^{-12}	$2.4067 \times 10^{-3} 1.5457 \times 10^{-3}$	55.707
pdb1hf9 496	ClassicAll QuaternionAll	8 8	9.0139×10^{-10} 9.0282×10^{-10}	6 6	1.156×10^{-11} 1.180×10^{-11}	4.1394×10^{-2} 2.1486×10^{-2}	92.651
pdb1i2u 266	ClassicAll QuaternionAll	8 8	1.3842×10^{-3} 1.3842×10^{-3}	2 2	5.562×10^{-13} 5.609×10^{-13}	1.8649×10^{-3} 1.2106×10^{-3}	54.043
pdb1i2v 266	ClassicAll QuaternionAll	8	8.9125×10^{-13} 8.8206×10^{-13}	5 5	2.422×10^{-13} 2.525×10^{-13}	1.8297×10^{-3} 1.1844×10^{-3}	54.479
pdb1ijc 380	ClassicAll QuaternionAll	8 8	9.1858×10^{-11} 9.4110×10^{-11}	2 2	1.408×10^{-11} 1.426×10^{-11}	2.9060×10^{-3} 1.8500×10^{-3}	57.083
pdb1jlz 140	ClassicAll QuaternionAll	8 8	$1.2304 \times 10^{-4} \\ 1.2304 \times 10^{-4}$	1 1	5.594×10^{-13} 5.965×10^{-13}	9.1346×10^{-4} 5.9424×10^{-4}	53.718
pdb1jw3 842	ClassicAll QuaternionAll	8	1.9618×10^{-12} 1.8088×10^{-12}	2 2	5.936×10^{-13} 5.897×10^{-13}	5.9916×10^{-3} 3.8800×10^{-3}	54.421
pdb1k0v 440	ClassicAll QuaternionAll	8	8.3940×10^{-5} 8.3940×10^{-5}	2 2	1.893×10^{-13} 1.894×10^{-13}	3.2384×10^{-3} 2.0929×10^{-3}	54.728
pdb1k2h 1120	ClassicAll QuaternionAll	8 8	1.9788×10^{-4} 1.9788×10^{-4}	2 2	5.490×10^{-13} 5.198×10^{-13}	2.6758×10^{-2} 1.3144×10^{-2}	103.577
pdb1k36 278	ClassicAll QuaternionAll	8 8	1.6100×10^{-10} 1.8077×10^{-10}	1 1	8.820×10^{-12} 1.081×10^{-11}	$1.8692 \times 10^{-3} \\ 1.1901 \times 10^{-3}$	57.060
pdb1k37 278	ClassicAll QuaternionAll	8	$2.1407 \times 10^{-12} $ 2.0318×10^{-12}	2 2	$4.711 \times 10^{-13} $ 4.988×10^{-13}	1.8674×10^{-3} 1.1885×10^{-3}	57.126
pdb1kuw	ClassicAll QuaternionAll	8 8	1.8706×10^{-4} 1.8706×10^{-4}	1 1	9.229×10^{-14} 1.130×10^{-13}	3.9029×10^{-4} 2.5891×10^{-4}	50.741
pdb1kz0 98	ClassicAll QuaternionAll	8 8	6.7512×10^{-13} 6.2568×10^{-13}	1 1	4.404×10^{-14} 5.880×10^{-14}	$6.3022 \times 10^{-4} 4.0976 \times 10^{-4}$	53.803
pdb1kz2 98	ClassicAll QuaternionAll	8 8	3.1076×10^{-6} 3.1076×10^{-6}	1 1	$2.119 \times 10^{-14} 2.886 \times 10^{-14}$	$6.4018 \times 10^{-4} 4.1913 \times 10^{-4}$	52.740
pdb1kz5 74	ClassicAll QuaternionAll	8 8	4.8094×10^{-13} 5.2716×10^{-13}	1 1	$4.081 \times 10^{-14} 4.738 \times 10^{-14}$	4.7184×10^{-4} 3.0708×10^{-4}	53.651
pdb1lvz 68	ClassicAll QuaternionAll	8 8	1.4708×10^{-3} 1.4708×10^{-3} 1.4708×10^{-3}	1 1	$6.336 \times 10^{-14} 7.315 \times 10^{-14}$	4.2873×10^{-4} 2.8144×10^{-4}	52.337
pdb1m4e 122	ClassicAll QuaternionAll	8 8	5.4966×10^{-12} 5.5048×10^{-12}	1 1	$5.949 \times 10^{-13} 5.972 \times 10^{-13}$	$7.9497 \times 10^{-4} 5.2298 \times 10^{-4}$	52.008
pdb1ma2	ClassicAll	8	1.7458×10^{-10}	2	8.695×10^{-12}	6.6260×10^{-4}	

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb1ma4 104	ClassicAll QuaternionAll	8 8	$5.4569 \times 10^{-4} 5.4569 \times 10^{-4}$	$\frac{2}{2}$	$7.247 \times 10^{-14} 7.977 \times 10^{-14}$	$1.6390 \times 10^{-3} 9.2800 \times 10^{-4}$	76.615
pdb1ma5 104	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.6358 \times 10^{-5} \\ 9.6358 \times 10^{-5} \end{array}$	1 1	$\begin{array}{c} 8.169 \times 10^{-13} \\ 9.044 \times 10^{-13} \end{array}$	$6.7216 \times 10^{-4} 4.3986 \times 10^{-4}$	52.813
pdb1ma6 104	ClassicAll QuaternionAll	8 8	$1.2440 \times 10^{-11} 1.4288 \times 10^{-11}$	2 2	$6.283 \times 10^{-13} \\ 8.487 \times 10^{-13}$	$6.7314 \times 10^{-4} 4.4000 \times 10^{-4}$	52.988
pdb1mpe 1352	ClassicAll QuaternionAll	8 8	$5.1722 \times 10^{-10} 5.1751 \times 10^{-10}$	$\frac{2}{2}$	$2.617 \times 10^{-11} 2.624 \times 10^{-11}$	$\begin{array}{c} 1.2925 \times 10^{-2} \\ 7.1170 \times 10^{-3} \end{array}$	81.604
pdb1nd9 296	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.0508 \times 10^{-12} \\ 8.9082 \times 10^{-13} \end{array}$	$\frac{2}{2}$	3.026×10^{-13} 3.845×10^{-13}	$2.0602 \times 10^{-3} \\ 1.3414 \times 10^{-3}$	53.589
$\begin{array}{c} \text{pdb1ne5} \\ 254 \end{array}$	ClassicAll QuaternionAll	128 128	$1.4845 \times 10^{-11} 1.5105 \times 10^{-11}$	33 33	$1.214 \times 10^{-12} \\ 1.384 \times 10^{-12}$	$\begin{array}{c} 3.1537 \times 10^{-2} \\ 1.9559 \times 10^{-2} \end{array}$	61.239
pdb1nmj 170	ClassicAll QuaternionAll	8 8	$2.3883 \times 10^{-13} 2.3832 \times 10^{-13}$	7 7	$1.236 \times 10^{-14} 1.422 \times 10^{-14}$	$\begin{array}{c} 1.1175 \times 10^{-3} \\ 7.2169 \times 10^{-4} \end{array}$	54.843
pdb1o53 92	ClassicAll QuaternionAll	8 8	$1.0887 \times 10^{-11} \\ 1.1252 \times 10^{-11}$	$\frac{2}{2}$	3.999×10^{-13} 4.527×10^{-13}	$\begin{array}{c} 5.8817 \times 10^{-4} \\ 3.8500 \times 10^{-4} \end{array}$	52.771
pdb1oqp 580	ClassicAll QuaternionAll	8 8	$2.9348 \times 10^{-3} $ 2.9348×10^{-3}	2 2	$7.045 \times 10^{-14} \\ 8.314 \times 10^{-14}$	2.6452×10^{-2} 1.2882×10^{-2}	105.339
pdb1plw 32	ClassicAll QuaternionAll	8	3.0310×10^{-13} 3.2973×10^{-13}	2 2	2.830×10^{-14} 3.112×10^{-14}	$1.8013 \times 10^{-4} 1.2037 \times 10^{-4}$	49.647
pdb1plx 32	ClassicAll QuaternionAll	8	$2.8525 \times 10^{-4} $ 2.8525×10^{-4}	1 1	$1.574 \times 10^{-13} $ 2.060×10^{-13}	$1.8123 \times 10^{-4} \\ 1.2033 \times 10^{-4}$	50.613
pdb1pv0 278	ClassicAll QuaternionAll	16 16	1.3024×10^{-11} 1.3017×10^{-11}	1 1	$2.409 \times 10^{-13} 2.723 \times 10^{-13}$	3.6764×10^{-3} 2.3561×10^{-3}	56.037
pdb1pzr 724	ClassicAll QuaternionAll	8 8	3.9940×10^{-10} 3.9046×10^{-10}	1 1	$5.644 \times 10^{-12} \\ 5.871 \times 10^{-12}$	1.3472×10^{-1} 6.3919×10^{-2}	110.770
pdb1qlk 1108	ClassicAll QuaternionAll	8 8	3.1378×10^{-5} 3.1378×10^{-5}	5 5	$2.634 \times 10^{-13} \\ 2.870 \times 10^{-13}$	3.4224×10^{-2} 1.8366×10^{-2}	86.341
pdb1r57 614	ClassicAll QuaternionAll	8	4.3330×10^{-3} 4.3330×10^{-3}	2 2	$1.847 \times 10^{-13} 2.054 \times 10^{-13}$	4.3587×10^{-3} 2.8209×10^{-3}	54.518
pdb1ry3 386	ClassicAll QuaternionAll	8	$9.1924 \times 10^{-12} 9.4285 \times 10^{-12}$	2 2	4.938×10^{-13} 5.913×10^{-13}	2.6880×10^{-3} 1.6985×10^{-3}	58.256
pdb1s4h 80	ClassicAll QuaternionAll	8 8	1.4643×10^{-4} 1.4643×10^{-4}	2 2	4.696×10^{-13} 6.351×10^{-13}	5.0040×10^{-4} 3.2503×10^{-4}	53.952
pdb1s4j 80	ClassicAll QuaternionAll	8 8	5.8507×10^{-12} 5.8479×10^{-12}	2 2	$1.520 \times 10^{-13} $ 2.083×10^{-13}	5.1183×10^{-4} 3.3630×10^{-4}	52.193
pdb1s6j 524	ClassicAll QuaternionAll	8 8	6.0202×10^{-5} 6.0202×10^{-5}	1 1	6.073×10^{-13} 7.660×10^{-13}	3.7005×10^{-3} 2.3304×10^{-3}	58.796
pdb1sa8 638	ClassicAll QuaternionAll	8 8	1.7170×10^{-3} 1.7170×10^{-3}	1 1	9.340×10^{-13} 1.034×10^{-12}	4.5346×10^{-3} 3.0039×10^{-3}	50.957
pdb1t2y 152	ClassicAll QuaternionAll	8 8	$2.5460 \times 10^{-4} $ 2.5460×10^{-4}	1 1	$1.887 \times 10^{-13} $ 2.396×10^{-13}	1.0142×10^{-3} 6.6476×10^{-4}	52.562
pdb1t5q 180	ClassicAll QuaternionAll	2 2	1.0265×10^{-12} 1.0480×10^{-12}	1 1	$3.877 \times 10^{-14} 5.093 \times 10^{-14}$	9.4120×10^{-4} 5.2552×10^{-4}	79.096
pdb1tot 314	ClassicAll QuaternionAll	8 8	3.4218×10^{-3} 3.4218×10^{-3}	5 5	$6.151 \times 10^{-14} 6.855 \times 10^{-14}$	2.2365×10^{-3} 1.4438×10^{-3}	54.902
pdb1v6r 128	ClassicAll QuaternionAll	8 8	1.3650×10^{-4} 1.3650×10^{-4} 1.3650×10^{-4}	2 2	6.835×10^{-13} 6.835×10^{-13} 6.971×10^{-13}	$8.2447 \times 10^{-4} 5.3590 \times 10^{-4}$	53.848
pdb1v92 278	ClassicAll QuaternionAll	8 8	3.1327×10^{-5} 3.1327×10^{-5}	1 1	$ \begin{array}{c} 1.463 \times 10^{-13} \\ 1.630 \times 10^{-13} \end{array} $	1.9226×10^{-3} 1.2375×10^{-3}	55.364
pdb1vd7 140	ClassicAll QuaternionAll	8 8	$7.8801 \times 10^{-12} $ 7.9022×10^{-12}	1 1 1	6.342×10^{-13} 7.439×10^{-13}	9.0575×10^{-4} 5.9296×10^{-4}	52.750
pdb1vd9 140	ClassicAll QuaternionAll	8 8	$ \begin{array}{r} 1.5514 \times 10^{-11} \\ 1.5541 \times 10^{-11} \end{array} $	1 1 1	1.290×10^{-12} 1.554×10^{-12}	$\begin{array}{c} 3.9296 \times 10 \\ \hline 9.0526 \times 10^{-4} \\ 5.8499 \times 10^{-4} \end{array}$	54.747
140	QuatermonAll	•	1.0041 X 10	1	1.554 X 10 -2	0.0499 X 1U	04.141

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb1vdb 140	ClassicAll QuaternionAll	8 8	$8.5740 \times 10^{-12} \\ 8.5291 \times 10^{-12}$	2 2	9.108×10^{-13} 1.082×10^{-12}	9.0390×10^{-4} 5.8446×10^{-4}	54.655
pdb1vpc 272	ClassicAll QuaternionAll	8 8	$4.3482 \times 10^{-4} 4.3482 \times 10^{-4}$	6 6	$8.510 \times 10^{-15} 1.002 \times 10^{-14}$	$1.8807 \times 10^{-3} 1.1963 \times 10^{-3}$	57.209
pdb1wnk 140	ClassicAll QuaternionAll	8 8	$2.2292 \times 10^{-10} 2.2177 \times 10^{-10}$	1 1	$4.112 \times 10^{-12} 4.632 \times 10^{-12}$	$9.0852 \times 10^{-4} 5.8888 \times 10^{-4}$	54.279
pdb1wo4 152	ClassicAll QuaternionAll	8 8	$4.6193 \times 10^{-5} 4.6193 \times 10^{-5}$	2 2	$9.957 \times 10^{-13} 9.634 \times 10^{-13}$	$9.9077 \times 10^{-4} 6.3894 \times 10^{-4}$	55.065
pdb1wo5 152	ClassicAll QuaternionAll	8 8	$2.7147 \times 10^{-10} 2.7625 \times 10^{-10}$	1 1	$2.372 \times 10^{-12} 2.514 \times 10^{-12}$	$9.9623 \times 10^{-4} \\ 6.4531 \times 10^{-4}$	54.380
pdb1x60 476	ClassicAll QuaternionAll	8 8	$6.7449 \times 10^{-12} 6.9447 \times 10^{-12}$	1 1	1.076×10^{-12} 1.179×10^{-12}	3.3136×10^{-3} 2.1603×10^{-3}	53.386
pdb1x9v 544	ClassicAll QuaternionAll	8 8	$1.1547 \times 10^{-4} 1.1547 \times 10^{-4}$	6 6	8.968×10^{-13} 9.611×10^{-13}	$4.1615 \times 10^{-2} 2.1452 \times 10^{-2}$	93.994
pdb1y5c 68	ClassicAll QuaternionAll	8 8	$8.7435 \times 10^{-13} \\ 8.2242 \times 10^{-13}$	1 1	$7.693 \times 10^{-14} 9.383 \times 10^{-14}$	$\begin{array}{c} 4.2161 \times 10^{-4} \\ 2.7276 \times 10^{-4} \end{array}$	54.570
pdb1yx7 500	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.3647 \times 10^{-10} \\ 1.4245 \times 10^{-10} \end{array}$	5 5	3.509×10^{-12} 4.348×10^{-12}	$3.5138 \times 10^{-3} 2.2682 \times 10^{-3}$	54.917
pdb1yx8 500	ClassicAll QuaternionAll	8 8	$2.5841 \times 10^{-10} 2.6921 \times 10^{-10}$	6 6	$7.284 \times 10^{-12} \\ 8.217 \times 10^{-12}$	3.9642×10^{-3} 2.5052×10^{-3}	58.237
pdb1yxr 464	ClassicAll QuaternionAll	8	9.3459×10^{-4} 9.3459×10^{-4}	1 1	$6.979 \times 10^{-13} 7.989 \times 10^{-13}$	3.2919×10^{-3} 2.1481×10^{-3}	53.244
pdb2a2y 1072	ClassicAll QuaternionAll	8 8	8.1076×10^{-5} 8.1076×10^{-5}	$\frac{2}{2}$	$1.150 \times 10^{-12} \\ 1.151 \times 10^{-12}$	2.0710×10^{-1} 9.7691×10^{-2}	111.993
pdb2a4j 580	ClassicAll QuaternionAll	8 8	$1.0516 \times 10^{-4} \\ 1.0516 \times 10^{-4}$	2 2	$2.085 \times 10^{-14} 2.727 \times 10^{-14}$	$4.8461 \times 10^{-3} \\ 3.0597 \times 10^{-3}$	58.387
pdb2adl 868	ClassicAll QuaternionAll	8	3.1161×10^{-11} 3.3255×10^{-11}	1 1	$1.752 \times 10^{-11} 1.787 \times 10^{-11}$	$1.6403 \times 10^{-2} \\ 8.4920 \times 10^{-3}$	93.158
pdb2adn 868	ClassicAll QuaternionAll	8 8	$2.3364 \times 10^{-10} 2.3188 \times 10^{-10}$	1 1	$6.693 \times 10^{-12} 6.465 \times 10^{-12}$	$\begin{array}{c} 1.2112 \times 10^{-2} \\ 6.3753 \times 10^{-3} \end{array}$	89.982
pdb2ajj 170	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.9810 \times 10^{-4} \\ 2.9810 \times 10^{-4} \end{array}$	1 1	$5.641 \times 10^{-14} \\ 6.584 \times 10^{-14}$	$\begin{array}{c} 1.1115 \times 10^{-3} \\ 7.1627 \times 10^{-4} \end{array}$	55.172
pdb2ajm 170	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.4063 \times 10^{-12} \\ 2.7001 \times 10^{-12} \end{array}$	2 2	$\begin{array}{c} 1.183 \times 10^{-13} \\ 1.555 \times 10^{-13} \end{array}$	$\begin{array}{c} 1.1195 \times 10^{-3} \\ 7.2295 \times 10^{-4} \end{array}$	54.857
pdb2ajn 170	ClassicAll QuaternionAll	8 8	$4.3268 \times 10^{-4} 4.3268 \times 10^{-4}$	1 1	$\begin{array}{c} 1.076 \times 10^{-13} \\ 1.217 \times 10^{-13} \end{array}$	$\begin{array}{c} 1.1117 \times 10^{-3} \\ 7.1301 \times 10^{-4} \end{array}$	55.920
pdb2ajo 170	ClassicAll QuaternionAll	8 8	$2.4063 \times 10^{-12} 2.7001 \times 10^{-12}$	2 2	$1.183 \times 10^{-13} 1.555 \times 10^{-13}$	$\begin{array}{c} 1.1267 \times 10^{-3} \\ 7.3113 \times 10^{-4} \end{array}$	54.105
pdb2akk 446	ClassicAll QuaternionAll	8 8	3.0416×10^{-3} 3.0416×10^{-3}	2 2	$1.289 \times 10^{-13} 1.279 \times 10^{-13}$	3.1293×10^{-3} 2.0386×10^{-3}	53.502
pdb2bzb 748	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.6498 \times 10^{-13} \\ 6.0113 \times 10^{-13} \end{array}$	5 5	$9.361 \times 10^{-14} \\ 1.224 \times 10^{-13}$	$\begin{array}{c} 4.3490 \times 10^{-2} \\ 2.2541 \times 10^{-2} \end{array}$	92.941
pdb2c0s 386	ClassicAll QuaternionAll	8 8	$1.0793 \times 10^{-2} 1.0793 \times 10^{-2}$	6 6	3.028×10^{-13} 3.380×10^{-13}	$2.7425 \times 10^{-3} 1.7394 \times 10^{-3}$	57.670
pdb2dci 120	ClassicAll QuaternionAll	$\frac{2}{2}$	$2.0907 \times 10^{-13} \\ 3.3732 \times 10^{-13}$	1 1	$2.366 \times 10^{-14} 2.950 \times 10^{-14}$	$6.3428 \times 10^{-4} \\ 3.6157 \times 10^{-4}$	75.424
pdb2eem 206	ClassicAll QuaternionAll	8 8	$9.5324 \times 10^{-12} 9.5866 \times 10^{-12}$	1 1	5.190×10^{-13} 5.461×10^{-13}	$1.3738 \times 10^{-3} \\ 8.8063 \times 10^{-4}$	56.002
pdb2fva 494	ClassicAll QuaternionAll	8 8	1.2680×10^{-11} 1.2689×10^{-11}	2 2	$1.047 \times 10^{-12} \\ 1.195 \times 10^{-12}$	3.4355×10^{-3} 2.1902×10^{-3}	56.856
pdb2fvf 494	ClassicAll QuaternionAll	8	3.5796×10^{-12} 3.3286×10^{-12}	1 1	3.106×10^{-13} 3.445×10^{-13}	3.4452×10^{-3} 2.2127×10^{-3}	55.699
pdb2fxz 80	ClassicAll QuaternionAll	8 8	$4.2293 \times 10^{-12} 5.3169 \times 10^{-12}$	1 1	$1.489 \times 10^{-12} 1.749 \times 10^{-12}$	$5.1456 \times 10^{-4} \\ 3.3937 \times 10^{-4}$	51.622

Table 4: Results - continued

Pelbage ClassicAll S	Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
224 QuaternionAll 8								102.051
Page						0.0000		55.102
Pub2 252 QuaternionAll 2 2.2038 × 10 ⁻¹¹ 1 1.268 × 10 ⁻¹² 7.5315 × 10 ⁻⁴ 82.177								55.110
Poblic P								82.177
Post	- "							108.703
Part								23.678
Pub2	- "							22.844
Page								50.662
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	- "							53.793
Public P	- "							54.384
Pub Pub								65.366
Pdb2jvd ClassicAll 2 9.4244 × 10^{-13} 1 3.339 × 10^{-14} 1.5850 × 10^{-3} 82.264 Pdb2jwe ClassicAll 2 9.2597 × 10^{-11} 1 2.695 × 10^{-11} 5.7134 × 10^{-3} 76.233 Pdb2jwe ClassicAll 2 9.2597 × 10^{-11} 1 2.695 × 10^{-11} 3.2419 × 10^{-3} 76.233 Pdb2jwe ClassicAll 8 4.5612 × 10^{-4} 2 1.251 × 10^{-13} 2.4140 × 10^{-3} 338 Pdb2jwe ClassicAll 8 4.5612 × 10^{-4} 2 1.543 × 10^{-13} 2.4140 × 10^{-3} 56.376 Pdb2jwe ClassicAll 8 4.5612 × 10^{-4} 2 1.543 × 10^{-13} 2.4140 × 10^{-3} 56.376 Pdb2jwe ClassicAll 8 3.0876 × 10^{-4} 1 4.421 × 10^{-12} 2.3899 × 10^{-3} 56.376 Pdb2jwe ClassicAll 8 3.0876 × 10^{-4} 1 4.421 × 10^{-12} 2.3899 × 10^{-3} 56.376 Pdb2jxf ClassicAll 8 2.4000 × 10^{-4} 1 1.399 × 10^{-13} 1.2131 × 10^{-3} 1.5437 × 10^{-3} 55.782 Pdb2jxf ClassicAll 8 2.4000 × 10^{-4} 1 1.399 × 10^{-13} 1.2131 × 10^{-3} 1.5437 × 10^{-4} 55.782 Pdb2jzf ClassicAll 8 1.7460 × 10^{-3} 1 2.860 × 10^{-13} 3.7907 × 10^{-3} 56.177 Pdb2k2a ClassicAll 8 4.7195 × 10^{-3} 5 3.810 × 10^{-14} 2.9808 × 10^{-3} 56.177 Pdb2k2a ClassicAll 8 4.7195 × 10^{-3} 5 3.810 × 10^{-14} 2.9968 × 10^{-3} 56.839 Pdb2k2f ClassicAll 8 1.2926 × 10^{-11} 1 2.639 × 10^{-13} 2.9746 × 10^{1} 115.049 Pdb2k3f ClassicAll 8 1.6972 × 10^{-12} 1 1.922 × 10^{-13} 6.4707 × 10^{-3} 6.4615 Pdb2k3f ClassicAll 8 1.6972 × 10^{-12} 1 1.922 × 10^{-13} 5.5621 Pdb2k3f ClassicAll 8 3.7147 × 10^{-12} 1 1.922 × 10^{-13} 5.967 × 10^{-3} 56.576 Pdb2k3f ClassicAll 8 4.6225 × 10^{-3} 2 3.810 × 10^{-13} 3.5884 × 10^{-3} 56.576 Pdb2k3f ClassicAll 8 8.4598 × 10^{-12} 2 2.100 × 10^{-13} 3.5884 × 10^{-3} 56.576 Pdb2k3f ClassicAll 8 8.4598 × 10^{-12} 2 2.2058 × 10^{-13} 3.5000 × 10^{-3} 75.280 Pdb2k4b ClassicAll 8 1.8663 × 10^								57.461
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	- "			9.4244×10^{-13}				82.264
Pdb2 ws ClassicAll 8								76.233
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	- "							56.376
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								54.854
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		ClassicAll		2.4000×10^{-4}		1.399×10^{-13}	1.2131×10^{-3}	55.782
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		ClassicAll						56.177
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				4.7195×10^{-3}	5	3.810×10^{-14}	2.9808×10^{-3}	56.839
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		ClassicAll	8	1.2926×10^{-11}	1		2.9746×10^{1}	
$\begin{array}{ c c c c c c c c c } \hline pdb2k37 & ClassicAll & 8 & 3.7147 \times 10^{-12} & 1 & 1.921 \times 10^{-13} & 2.5637 \times 10^{-3} \\ 356 & QuaternionAll & 8 & 3.6185 \times 10^{-12} & 1 & 2.525 \times 10^{-13} & 1.6373 \times 10^{-3} & 56.576 \\ \hline pdb2k3i & ClassicAll & 8 & 4.6225 \times 10^{-3} & 2 & 3.810 \times 10^{-13} & 5.9071 \times 10^{-3} \\ 656 & QuaternionAll & 8 & 4.6225 \times 10^{-3} & 2 & 4.009 \times 10^{-13} & 3.5884 \times 10^{-3} & 64.615 \\ \hline pdb2k6s & ClassicAll & 8 & 8.2998 \times 10^{-12} & 2 & 2.100 \times 10^{-13} & 7.3740 \times 10^{-3} \\ 494 & QuaternionAll & 8 & 8.4519 \times 10^{-12} & 2 & 2.651 \times 10^{-13} & 4.2070 \times 10^{-3} & 75.280 \\ \hline pdb2k7o & ClassicAll & 8 & 1.8663 \times 10^{-4} & 1 & 1.279 \times 10^{-13} & 5.1186 \times 10^{-2} \\ 1096 & QuaternionAll & 8 & 1.8663 \times 10^{-4} & 1 & 1.416 \times 10^{-13} & 2.6689 \times 10^{-2} & 91.784 \\ \hline pdb2kbm & ClassicAll & 8 & 1.5487 \times 10^{-12} & 2 & 2.165 \times 10^{-13} & 2.5000 \times 10^{1} \\ 1268 & QuaternionAll & 8 & 1.6865 \times 10^{-12} & 2 & 2.226 \times 10^{-13} & 1.1776 \times 10^{1} & 112.296 \\ \hline pdb2kdh & ClassicAll & 8 & 7.2209 \times 10^{-5} & 2 & 1.947 \times 10^{-11} & 3.0999 \times 10^{-3} \\ \hline \end{array}$	pdb2k36	ClassicAll	8	1.6972×10^{-12}	1			55.621
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-	ClassicAll	8	3.7147×10^{-12}	1		2.5637×10^{-3}	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	pdb2k3i	ClassicAll	8	4.6225×10^{-3}	2	3.810×10^{-13}	5.9071×10^{-3}	
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	pdb2k6s	ClassicAll	8	8.2998×10^{-12}	2	2.100×10^{-13}	7.3740×10^{-3}	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	pdb2k7o	ClassicAll	8	1.8663×10^{-4}	1	1.279×10^{-13}	5.1186×10^{-2}	
pdb2kdh ClassicAll 8 7.2209×10^{-5} 2 1.947×10^{-11} 3.0999×10^{-3}	pdb2kbm	ClassicAll	8	1.5487×10^{-12}	2	2.165×10^{-13}	2.5000×10^{1}	
434 QuaternionAll 8 7.2209×10^{-5} 2 2.228×10^{-11} 1.9917×10^{-3} 55.644	pdb2kdh	ClassicAll	8	7.2209×10^{-5}	2	1.947×10^{-11}	3.0999×10^{-3}	

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2kdl 338	ClassicAll QuaternionAll	8 8	$4.4591 \times 10^{-12} 4.4513 \times 10^{-12}$	2 2	2.301×10^{-13} 2.919×10^{-13}	$2.3135 \times 10^{-3} \\ 1.4812 \times 10^{-3}$	56.185
pdb2kdm 338	ClassicAll QuaternionAll	8 8	$2.1896 \times 10^{-11} 2.1643 \times 10^{-11}$	1 1	$\begin{array}{c} 3.191 \times 10^{-12} \\ 3.284 \times 10^{-12} \end{array}$	$2.3738 \times 10^{-3} 1.5183 \times 10^{-3}$	56.347
$\begin{array}{c} \rm pdb2kdp\\ 428\end{array}$	ClassicAll QuaternionAll	8 8	$3.0283 \times 10^{-12} 3.0741 \times 10^{-12}$	1 1	$2.621 \times 10^{-13} 2.865 \times 10^{-13}$	3.0102×10^{-3} 1.9209×10^{-3}	56.709
pdb2kdr 170	ClassicAll QuaternionAll	8 8	$6.3024 \times 10^{-5} 6.3024 \times 10^{-5}$	2 2	$6.618 \times 10^{-14} \\ 8.490 \times 10^{-14}$	$\begin{array}{c} 1.1171 \times 10^{-3} \\ 7.1496 \times 10^{-4} \end{array}$	56.243
pdb2kes 290	ClassicAll QuaternionAll	8 8	$1.8528 \times 10^{-4} 1.8528 \times 10^{-4}$	7 7	$\begin{array}{c} 4.467 \times 10^{-14} \\ 5.425 \times 10^{-14} \end{array}$	$1.9606 \times 10^{-3} 1.2466 \times 10^{-3}$	57.266
pdb2kib 352	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.9706 \times 10^{-5} \\ 2.9706 \times 10^{-5} \end{array}$	1 1	$2.533 \times 10^{-12} 2.539 \times 10^{-12}$	$3.5759 \times 10^{-2} 1.7861 \times 10^{-2}$	100.203
pdb2kjn 158	ClassicAll QuaternionAll	8 8	$1.9764 \times 10^{-12} 1.9265 \times 10^{-12}$	2 2	$9.827 \times 10^{-14} \\ 1.174 \times 10^{-13}$	$\begin{array}{c} 1.0281 \times 10^{-3} \\ 6.6463 \times 10^{-4} \end{array}$	54.686
pdb2kjo 158	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.2876 \times 10^{-11} \\ 1.2921 \times 10^{-11} \end{array}$	1 1	$2.284 \times 10^{-13} \\ 2.421 \times 10^{-13}$	$1.0360 \times 10^{-3} \\ 6.6731 \times 10^{-4}$	55.247
pdb2kjr 572	ClassicAll QuaternionAll	8 8	$5.1341 \times 10^{-11} 5.1082 \times 10^{-11}$	$\frac{2}{2}$	3.247×10^{-12} 3.252×10^{-12}	3.9453×10^{-3} 2.5296×10^{-3}	55.966
pdb2kko 1300	ClassicAll QuaternionAll	8 8	$6.9643 \times 10^{-4} $ 6.9643×10^{-4}	2 2	1.191×10^{-13} 1.284×10^{-13}	$5.7810 \times 10^{-2} 2.9904 \times 10^{-2}$	93.315
pdb2kl5 662	ClassicAll QuaternionAll	8 8	$2.4505 \times 10^{-12} 2.5206 \times 10^{-12}$	1 1	$1.820 \times 10^{-13} 2.020 \times 10^{-13}$	$4.6640 \times 10^{-3} 2.9957 \times 10^{-3}$	55.690
pdb2klz 276	ClassicAll QuaternionAll	2 2	3.9786×10^{-13} 3.7834×10^{-13}	1 1	3.439×10^{-14} 4.443×10^{-14}	$1.5068 \times 10^{-3} \\ 8.2650 \times 10^{-4}$	82.307
pdb2ko1 1060	ClassicAll QuaternionAll	8 8	$9.3273 \times 10^{-4} \\ 9.3273 \times 10^{-4}$	2 2	$1.150 \times 10^{-12} \\ 1.151 \times 10^{-12}$	8.1329×10^{-2} 3.8494×10^{-2}	111.278
pdb2koz 200	ClassicAll QuaternionAll	8	4.7204×10^{-5} 4.7204×10^{-5}	2 2	1.067×10^{-12} 1.151×10^{-12}	1.3638×10^{-3} 8.8530×10^{-4}	54.047
pdb2kp0 200	ClassicAll QuaternionAll	8 8	$7.8392 \times 10^{-11} \\ 8.2404 \times 10^{-11}$	2 2	$4.894 \times 10^{-12} 5.595 \times 10^{-12}$	$1.3497 \times 10^{-3} \\ 8.7224 \times 10^{-4}$	54.739
pdb2ksg 290	ClassicAll QuaternionAll	8 8	$9.2027 \times 10^{-13} $ 9.2208×10^{-13}	1 1	3.215×10^{-14} 3.967×10^{-14}	1.9883×10^{-3} 1.2800×10^{-3}	55.337
pdb2kt8 458	ClassicAll QuaternionAll	8 8	$4.1573 \times 10^{-4} 4.1573 \times 10^{-4}$	1 1	3.314×10^{-12} 3.535×10^{-12}	3.1420×10^{-3} 2.0305×10^{-3}	54.738
pdb2kuh 404	ClassicAll QuaternionAll	8	1.1667×10^{-3} 1.1667×10^{-3}	6 6	$2.015 \times 10^{-14} $ 2.491×10^{-14}	2.8482×10^{-3} 1.8381×10^{-3}	54.954
pdb2kwh 338	ClassicAll QuaternionAll	8	$2.0587 \times 10^{-3} $ 2.0587×10^{-3}	2 2	1.408×10^{-13} 1.825×10^{-13}	2.3177×10^{-3} 1.4781×10^{-3}	56.804
pdb2kxa 144	ClassicAll QuaternionAll	2 2	3.9712×10^{-12} 3.7392×10^{-12}	1 1	$1.325 \times 10^{-12} \\ 1.351 \times 10^{-12}$	7.8119×10^{-4} 4.4945×10^{-4}	73.810
pdb2kyb 362	ClassicAll QuaternionAll	8	3.1200×10^{-6} 3.1200×10^{-6}	2 2	$1.321 \times 10^{-11} \\ 1.373 \times 10^{-11}$	3.4027×10^{-3} 2.0755×10^{-3}	63.943
pdb2l3m 428	ClassicAll QuaternionAll	8	1.5178×10^{-3} 1.5178×10^{-3}	1 1	$1.028 \times 10^{-12} \\ 9.340 \times 10^{-13}$	2.9766×10^{-3} 1.9217×10^{-3}	54.897
pdb2l3n 626	ClassicAll QuaternionAll	8 8	3.9987×10^{-4} 3.9987×10^{-4}	5 5	3.024×10^{-14} 3.632×10^{-14}	1.8277×10^{-2} 9.2061×10^{-3}	98.537
pdb2l45 116	ClassicAll QuaternionAll	8 8	5.9466×10^{-13} 6.7808×10^{-13}	1 1	2.236×10^{-14} 3.033×10^{-14}	$7.6098 \times 10^{-4} $ 4.9929×10^{-4}	52.412
pdb2l5r 138	ClassicAll QuaternionAll	2 2	3.0491×10^{-13} 3.0031×10^{-13}	2 2	$3.535 \times 10^{-14} $ 4.436×10^{-14}	$7.1230 \times 10^{-4} $ 4.0015×10^{-4}	78.007
pdb2l6q 374	ClassicAll QuaternionAll	4 4	1.6115×10^{-9} 1.6752×10^{-9}	1 1	4.435×10^{-11} 5.413×10^{-11}	1.9704×10^{-3} 1.1738×10^{-3}	67.872
pdb2l6r 374	ClassicAll QuaternionAll	8 8	1.0970×10^{-10} 9.8250×10^{-11}	2 2	2.060×10^{-12} 2.174×10^{-12}	2.6361×10^{-3} 1.6745×10^{-3}	57.422
	<u> </u>						

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2l98 434	ClassicAll QuaternionAll	8 8	$5.6413 \times 10^{-12} $ 6.2089×10^{-12}	$\frac{2}{2}$	3.273×10^{-13} 3.637×10^{-13}	3.0147×10^{-3} 1.9279×10^{-3}	56.372
pdb2lci 806	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.2015 \times 10^{-12} \\ 1.1830 \times 10^{-12} \end{array}$	1 1	$\begin{array}{c} 2.579 \times 10^{-13} \\ 2.404 \times 10^{-13} \end{array}$	$\begin{array}{c} 5.6616 \times 10^{-3} \\ 3.6360 \times 10^{-3} \end{array}$	55.707
pdb2lde 152	ClassicAll QuaternionAll	8 8	$6.0406 \times 10^{-3} 6.0406 \times 10^{-3}$	2 2	3.154×10^{-14} 3.766×10^{-14}	$9.8617 \times 10^{-4} \\ 6.3873 \times 10^{-4}$	54.396
pdb2le2 676	ClassicAll QuaternionAll	8 8	$1.5317 \times 10^{-12} 1.4989 \times 10^{-12}$	2 2	$2.064 \times 10^{-13} 2.042 \times 10^{-13}$	$2.2512 \times 10^{-1} 1.0961 \times 10^{-1}$	105.376
pdb2le7 122	ClassicAll QuaternionAll	8 8	$8.8940 \times 10^{-14} 1.1008 \times 10^{-13}$	2 2	$2.111 \times 10^{-14} 2.749 \times 10^{-14}$	$7.8547 \times 10^{-4} 5.1159 \times 10^{-4}$	53.534
pdb2ler 68	ClassicAll QuaternionAll	8 8	$5.1096 \times 10^{-14} 6.2001 \times 10^{-14}$	2 2	$1.314 \times 10^{-14} 1.532 \times 10^{-14}$	$4.2376 \times 10^{-4} 2.7519 \times 10^{-4}$	53.992
pdb2lgi 338	ClassicAll QuaternionAll	8 8	$9.7255 \times 10^{-12} 9.6518 \times 10^{-12}$	2 2	$1.068 \times 10^{-12} 1.052 \times 10^{-12}$	2.3776×10^{-3} 1.5301×10^{-3}	55.393
pdb2lhc 338	ClassicAll QuaternionAll	8 8	3.8367×10^{-10} 3.8166×10^{-10}	1 1	$2.902 \times 10^{-12} 2.997 \times 10^{-12}$	$2.4365 \times 10^{-3} 1.5379 \times 10^{-3}$	58.426
pdb2lhd 338	ClassicAll QuaternionAll	8 8	$1.3048 \times 10^{-11} 1.4592 \times 10^{-11}$	2 2	$1.930 \times 10^{-12} 2.033 \times 10^{-12}$	2.3559×10^{-3} 1.5150×10^{-3}	55.502
pdb2lhe 338	ClassicAll QuaternionAll	8 8	$9.7862 \times 10^{-10} 9.7867 \times 10^{-10}$	$\frac{2}{2}$	$\begin{array}{c} 4.963 \times 10^{-11} \\ 4.967 \times 10^{-11} \end{array}$	$2.5781 \times 10^{-3} 1.6370 \times 10^{-3}$	57.493
pdb2lhg 338	ClassicAll QuaternionAll	8 8	$5.0995 \times 10^{-13} 5.4683 \times 10^{-13}$	6 6	$6.485 \times 10^{-14} 7.343 \times 10^{-14}$	$2.3862 \times 10^{-3} 1.5279 \times 10^{-3}$	56.176
pdb2lix 162	ClassicAll QuaternionAll	$\frac{2}{2}$	$\begin{array}{c} 4.9988 \times 10^{-13} \\ 5.1517 \times 10^{-13} \end{array}$	1 1	$\begin{array}{c} 4.842 \times 10^{-14} \\ 5.614 \times 10^{-14} \end{array}$	8.5831×10^{-4} 4.8839×10^{-4}	75.743
pdb2lld 242	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.3972 \times 10^{-3} \\ 3.3972 \times 10^{-3} \end{array}$	5 5	$\begin{array}{c} 1.938 \times 10^{-13} \\ 2.216 \times 10^{-13} \end{array}$	$1.6492 \times 10^{-3} 1.0697 \times 10^{-3}$	54.176
pdb2lm9 578	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.2967 \times 10^{-3} \\ 2.2967 \times 10^{-3} \end{array}$	$\frac{2}{2}$	$6.254 \times 10^{-14} 7.713 \times 10^{-14}$	$4.0365 \times 10^{-3} $ 2.5617×10^{-3}	57.571
pdb2lmf 140	ClassicAll QuaternionAll	8 8	$1.0942 \times 10^{-4} 1.0942 \times 10^{-4}$	1 1	$1.282 \times 10^{-13} 1.462 \times 10^{-13}$	$9.1035 \times 10^{-4} 5.8702 \times 10^{-4}$	55.081
$pdb2ln3 \\ 500$	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.5821 \times 10^{-13} \\ 2.9987 \times 10^{-13} \end{array}$	1 1	$1.292 \times 10^{-13} 1.359 \times 10^{-13}$	3.4688×10^{-3} 2.2326×10^{-3}	55.367
pdb2lo2 230	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.4423 \times 10^{-2} \\ 1.4423 \times 10^{-2} \end{array}$	2 2	$2.068 \times 10^{-14} \\ 2.571 \times 10^{-14}$	$\begin{array}{c} 1.5525 \times 10^{-3} \\ 1.0000 \times 10^{-3} \end{array}$	55.244
pdb2lqp 428	ClassicAll QuaternionAll	8 8	$5.7815 \times 10^{-4} 5.7815 \times 10^{-4}$	2 2	$2.950 \times 10^{-13} 3.085 \times 10^{-13}$	2.9691×10^{-3} 1.9058×10^{-3}	55.794
pdb2lr0 806	ClassicAll QuaternionAll	8 8	$1.2202 \times 10^{-11} 1.1747 \times 10^{-11}$	1 1	3.549×10^{-12} 3.440×10^{-12}	$5.6876 \times 10^{-3} \\ 3.6523 \times 10^{-3}$	55.724
pdb2lrh 806	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.9721 \times 10^{-12} \\ 2.9099 \times 10^{-12} \end{array}$	1 1	$5.631 \times 10^{-13} \\ 6.564 \times 10^{-13}$	$5.6939 \times 10^{-3} 3.6372 \times 10^{-3}$	56.546
pdb2ls9 152	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.7045 \times 10^{-12} \\ 3.0425 \times 10^{-12} \end{array}$	1 1	$\begin{array}{c} 1.122 \times 10^{-13} \\ 1.471 \times 10^{-13} \end{array}$	$\begin{array}{c} 1.0102 \times 10^{-3} \\ 6.5577 \times 10^{-4} \end{array}$	54.050
pdb2lsa 140	ClassicAll QuaternionAll	8 8	$2.5535 \times 10^{-3} 2.5535 \times 10^{-3}$	2 2	$5.235 \times 10^{-14} 6.998 \times 10^{-14}$	9.2737×10^{-4} 6.0696×10^{-4}	52.790
pdb2lss 422	ClassicAll QuaternionAll	8 8	$1.2372 \times 10^{-3} 1.2372 \times 10^{-3}$	1 1	$1.230 \times 10^{-13} 1.455 \times 10^{-13}$	3.0024×10^{-3} 1.9476×10^{-3}	54.157
pdb2lt3 680	ClassicAll QuaternionAll	8 8	$9.6961 \times 10^{-13} \\ 1.0253 \times 10^{-12}$	6 6	$7.245 \times 10^{-14} 7.760 \times 10^{-14}$	4.7925×10^{-3} 3.0730×10^{-3}	55.954
pdb2lu6 86	ClassicAll QuaternionAll	8 8	$7.7550 \times 10^{-3} 7.7550 \times 10^{-3}$	1 1	$5.356 \times 10^{-15} \\ 6.922 \times 10^{-15}$	5.3249×10^{-4} 3.4442×10^{-4}	54.604
pdb2lwa 432	ClassicAll QuaternionAll	2048 2048	$4.9078 \times 10^{-12} 4.0818 \times 10^{-12}$	449 449	$3.616 \times 10^{-13} 4.436 \times 10^{-13}$	$\begin{array}{c} 1.2911 \\ 9.2788 \times 10^{-1} \end{array}$	39.145
pdb2lx0 194	ClassicAll QuaternionAll	8 8	$7.4851 \times 10^{-12} 7.5304 \times 10^{-12}$	1 1	3.569×10^{-13} 4.035×10^{-13}	$\begin{array}{c} 1.3161 \times 10^{-3} \\ 8.5217 \times 10^{-4} \end{array}$	54.440

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2lxb 892	ClassicAll QuaternionAll	8 8	$9.0172 \times 10^{-13} \\ 8.6577 \times 10^{-13}$	1 1	$1.542 \times 10^{-13} 1.585 \times 10^{-13}$	$1.6539 \times 10^{-2} \\ 8.5426 \times 10^{-3}$	93.606
$\begin{array}{c} \text{pdb2lxy} \\ 404 \end{array}$	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.1155 \times 10^{-10} \\ 1.1215 \times 10^{-10} \end{array}$	2 2	$\begin{array}{c} 9.313 \times 10^{-13} \\ 1.025 \times 10^{-12} \end{array}$	$\begin{array}{c} 2.8074 \times 10^{-3} \\ 1.7838 \times 10^{-3} \end{array}$	57.383
pdb2lxz 194	ClassicAll QuaternionAll	8 8	$1.1003 \times 10^{-4} \\ 1.1003 \times 10^{-4}$	2 2	$2.371 \times 10^{-12} 2.792 \times 10^{-12}$	$\begin{array}{c} 1.3136 \times 10^{-3} \\ 8.4998 \times 10^{-4} \end{array}$	54.545
$\begin{array}{c} \text{pdb2lzf} \\ 820 \end{array}$	ClassicAll QuaternionAll	8 8	$5.9653 \times 10^{-4} 5.9653 \times 10^{-4}$	2 2	3.217×10^{-14} 3.959×10^{-14}	$2.6541 \times 10^{-1} \\ 1.2717 \times 10^{-1}$	108.709
pdb2m1a 158	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.1771 \times 10^{-14} \\ 9.0451 \times 10^{-14} \end{array}$	1 1	$6.346 \times 10^{-15} 7.612 \times 10^{-15}$	$\begin{array}{c} 1.0358 \times 10^{-3} \\ 6.6637 \times 10^{-4} \end{array}$	55.437
pdb2m1j 182	ClassicAll QuaternionAll	8 8	$1.5890 \times 10^{-13} 1.6894 \times 10^{-13}$	$\frac{2}{2}$	$1.865 \times 10^{-14} 2.212 \times 10^{-14}$	$\begin{array}{c} 1.2810 \times 10^{-3} \\ 8.1920 \times 10^{-4} \end{array}$	56.375
pdb2m2y 110	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.8177 \times 10^{-3} \\ 1.8177 \times 10^{-3} \end{array}$	1 1	$2.699 \times 10^{-13} 2.808 \times 10^{-13}$	$7.1505 \times 10^{-4} 4.6500 \times 10^{-4}$	53.774
pdb2m3f 134	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.5240 \times 10^{-14} \\ 5.7597 \times 10^{-14} \end{array}$	1 1	3.629×10^{-14} 4.641×10^{-14}	$8.6816 \times 10^{-4} 5.6331 \times 10^{-4}$	54.117
pdb2m4j 2178	ClassicAll QuaternionAll	8 8	$5.2912 \times 10^{-4} 5.2912 \times 10^{-4}$	1 1	$1.463 \times 10^{-11} \\ 1.455 \times 10^{-11}$	$7.0056 \times 10^{-2} 3.5973 \times 10^{-2}$	94.747
pdb2m8m 170	ClassicAll QuaternionAll	8 8	6.9769×10^{-3} 6.9769×10^{-3}	5 5	2.424×10^{-14} 3.058×10^{-14}	1.1181×10^{-3} 7.1566×10^{-4}	56.229
pdb2m8o 170	ClassicAll QuaternionAll	8	$4.7097 \times 10^{-3} 4.7097 \times 10^{-3}$	5 5	$1.798 \times 10^{-14} $ 2.301×10^{-14}	$1.1217 \times 10^{-3} 7.2157 \times 10^{-4}$	55.446
pdb2m97 416	ClassicAll QuaternionAll	8 8	$2.4560 \times 10^{-12} $ 2.4592×10^{-12}	6 6	$4.654 \times 10^{-14} \\ 5.847 \times 10^{-14}$	2.9099×10^{-3} 1.8594×10^{-3}	56.502
pdb2m9g 1108	ClassicAll QuaternionAll	8 8	$4.9692 \times 10^{-12} $ 4.9567×10^{-12}	1 1	2.939×10^{-13} 3.170×10^{-13}	$1.0016 \times 10^{-2} 5.2963 \times 10^{-3}$	89.107
pdb2m9r 242	ClassicAll QuaternionAll	8 8	3.7505×10^{-12} 3.6480×10^{-12}	1 1	3.537×10^{-14} 4.406×10^{-14}	1.6064×10^{-3} 9.8646×10^{-4}	62.840
pdb2mdv 460	ClassicAll QuaternionAll	8 8	$4.7210 \times 10^{-4} 4.7210 \times 10^{-4}$	2 2	$3.178 \times 10^{-12} \\ 3.178 \times 10^{-12}$	3.3404×10^{-3} 2.1592×10^{-3}	54.706
pdb2me1 164	ClassicAll QuaternionAll	8 8	$1.4934 \times 10^{-4} \\ 1.4934 \times 10^{-4}$	2 2	$1.886 \times 10^{-13} 2.202 \times 10^{-13}$	$1.0737 \times 10^{-3} \\ 6.8778 \times 10^{-4}$	56.114
pdb2me2 164	ClassicAll QuaternionAll	8 8	1.3863×10^{-4} 1.3863×10^{-4}	1 1	3.667×10^{-13} 5.098×10^{-13}	$1.1361 \times 10^{-3} \\ 7.1731 \times 10^{-4}$	58.383
pdb2me3 164	ClassicAll QuaternionAll	8	3.4823×10^{-5} 3.4823×10^{-5}	2 2	1.425×10^{-13} 1.590×10^{-13}	1.0830×10^{-3} 6.9159×10^{-4}	56.590
pdb2me4 164	ClassicAll QuaternionAll	8 8	2.9945×10^{-5} 2.9945×10^{-5}	2 2	$5.547 \times 10^{-13} \\ 6.221 \times 10^{-13}$	$1.1386 \times 10^{-3} 7.2300 \times 10^{-4}$	57.477
pdb2mg1 164	ClassicAll QuaternionAll	8 8	4.4954×10^{-13} 5.4976×10^{-13}	6 6	$4.400 \times 10^{-14} \\ 5.374 \times 10^{-14}$	1.0749×10^{-3} 6.8859×10^{-4}	56.100
pdb2mg2 170	ClassicAll QuaternionAll	8 8	$1.0745 \times 10^{-3} 1.0745 \times 10^{-3}$	6 6	$1.831 \times 10^{-14} \\ 2.481 \times 10^{-14}$	1.1148×10^{-3} 7.1821×10^{-4}	55.223
pdb2mg3 170	ClassicAll QuaternionAll	8	$6.2977 \times 10^{-13} $ 6.7812×10^{-13}	6 6	3.542×10^{-14} 4.459×10^{-14}	1.1292×10^{-3} 7.2254×10^{-4}	56.277
pdb2mh8 338	ClassicAll QuaternionAll	8 8	$4.2246 \times 10^{-12} $ 4.0208×10^{-12}	6 6	$1.547 \times 10^{-13} \\ 1.883 \times 10^{-13}$	$2.3125 \times 10^{-3} \\ 1.4856 \times 10^{-3}$	55.656
pdb2mhw 164	ClassicAll QuaternionAll	8 8	3.6932×10^{-3} 3.6932×10^{-3}	2 2	$6.229 \times 10^{-14} 7.130 \times 10^{-14}$	1.1199×10^{-3} 7.2828×10^{-4}	53.778
pdb2mi1 84	ClassicAll QuaternionAll	4 4	2.1485×10^{-11} 2.2963×10^{-11}	4 4	$1.828 \times 10^{-12} $ 2.053×10^{-12}	7.9150×10^{-4} 4.4975×10^{-4}	75.987
pdb2mi7 404	ClassicAll QuaternionAll	8 8	$8.0637 \times 10^{-12} \\ 8.8714 \times 10^{-12}$	2 2	6.022×10^{-13} 6.815×10^{-13}	2.7539×10^{-3} 1.7510×10^{-3}	57.280
pdb2mij 224	ClassicAll QuaternionAll	8 8	$1.2077 \times 10^{-12} $ 1.2294×10^{-12}	1 1	1.244×10^{-13} 1.522×10^{-13}	$1.5043 \times 10^{-3} 9.6447 \times 10^{-4}$	55.973

Table 4: Results - continued

Problem	Method	$ \mathcal{X} $	min RMSD(\mathbf{x}, \mathbf{x}_o)	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$ ext{MDE}(\mathbf{x}_i)$	Time	Improv time
Size	Wethod	111	$\mathbf{x} \in \mathcal{X}$	ι . Λ ₁ / • Λ ₀	$MDE(\mathbf{x}_i)$	Time	Improv time
pdb2mix 128	ClassicAll QuaternionAll	8 8	3.7545×10^{-13} 3.4098×10^{-13}	1 1	4.816×10^{-14} 4.684×10^{-14}	8.4472×10^{-4} 5.5285×10^{-4}	52.794
pdb2mj1	ClassicAll	8	2.0809×10^{-3}	1	1.309×10^{-13}	7.1806×10^{-4}	92.194
110	QuaternionAll	8	2.0809×10^{-3} 2.0809×10^{-3}	1	1.646×10^{-13}	4.6531×10^{-4}	54.318
pdb2mj2	ClassicAll	8	3.9018×10^{-3}	2	9.775×10^{-14}	1.4385×10^{-3}	
218	QuaternionAll	8	3.9018×10^{-3}	2	1.192×10^{-13}	9.1651×10^{-4}	56.956
pdb2mjg 556	ClassicAll QuaternionAll	8 8	$1.4497 \times 10^{-3} 1.4497 \times 10^{-3}$	$\frac{2}{2}$	$5.503 \times 10^{-14} $ 6.579×10^{-14}	2.1163×10^{-2} 1.0643×10^{-2}	98.846
pdb2mji	ClassicAll	8	1.3090×10^{-11}	1	3.207×10^{-12}	5.6582×10^{-3}	
788	QuaternionAll	8	1.2949×10^{-11}	1	3.247×10^{-12}	3.6855×10^{-3}	53.528
pdb2mle	ClassicAll	8	1.6719×10^{-3}	2	1.491×10^{-13}	3.0881×10^{-3}	F. 0. 170 F
434	QuaternionAll	8	1.6719×10^{-3}	2	1.535×10^{-13}	1.9706×10^{-3}	56.705
pdb2mlf 434	ClassicAll QuaternionAll	8 8	8.3036×10^{-13} 8.8493×10^{-13}	$\frac{2}{2}$	9.918×10^{-14} 1.127×10^{-13}	3.0447×10^{-3} 1.9552×10^{-3}	55.724
pdb2mo5	ClassicAll	8	1.9007×10^{-11}	1	1.394×10^{-12}	6.1861×10^{-3}	
854	QuaternionAll	8	1.8458×10^{-11}	1	1.403×10^{-12}	3.9989×10^{-3}	54.695
pdb2mpu	ClassicAll	8	2.5305×10^{-12}	1	9.785×10^{-14}	3.9406×10^{-3}	
554	QuaternionAll	8	2.5592×10^{-12}	1	1.016×10^{-13}	2.5394×10^{-3}	55.178
pdb2mra 704	ClassicAll QuaternionAll	8 8	$4.3616 \times 10^{-12} $ 4.3117×10^{-12}	1 1	2.632×10^{-13} 2.768×10^{-13}	5.9738×10^{-3} 3.7144×10^{-3}	60.829
pdb2msu	ClassicAll	8	3.6237×10^{-12}	1	7.813×10^{-14}	7.9014×10^{-4}	
122	QuaternionAll	8	3.6441×10^{-12}	1	8.765×10^{-14}	5.1566×10^{-4}	53.229
pdb2mty	ClassicAll	2	5.1232×10^{-12}	2	1.848×10^{-14}	6.7409×10^{-4}	
120	QuaternionAll	2	5.2129×10^{-12}	2	2.363×10^{-14}	3.7637×10^{-4}	79.103
pdb2muh 98	ClassicAll QuaternionAll	8 8	8.0615×10^{-5} 8.0615×10^{-5}	$\frac{2}{2}$	2.008×10^{-13} 2.279×10^{-13}	6.2151×10^{-4} 3.9926×10^{-4}	55.666
pdb2mvj	ClassicAll	2	6.1752×10^{-12}	1	1.534×10^{-13}	8.1384×10^{-4}	
156	QuaternionAll	2	6.1858×10^{-12}	1	1.647×10^{-13}	4.5906×10^{-4}	77.282
pdb2mvt	ClassicAll	8	1.5441×10^{-4}	2	6.053×10^{-12}	1.9649×10^{-3}	
284	QuaternionAll	8	1.5441×10^{-4}	2	6.225×10^{-12}	1.2743×10^{-3}	54.200
pdb2mvx 2360	ClassicAll QuaternionAll	8 8	5.8655×10^{-5} 5.8655×10^{-5}	6 6	1.968×10^{-10} 1.971×10^{-10}	3.1667×10^{-2} 1.7955×10^{-2}	76.369
pdb2mz6	ClassicAll	8	2.3371×10^{-10}	1	2.141×10^{-11}	4.7695×10^{-2}	
220	QuaternionAll	8	2.3374×10^{-10}	1	2.153×10^{-11}	2.4584×10^{-2}	94.004
pdb2n00	ClassicAll	8	1.2439×10^{-4}	2	2.703×10^{-13}	4.0558×10^{-3}	
572	QuaternionAll	8	1.2439×10^{-4}	2	3.466×10^{-13}	2.6001×10^{-3}	55.986
pdb2n0b 60	ClassicAll QuaternionAll	$\frac{2}{2}$	$1.0219 \times 10^{-11} 1.0781 \times 10^{-11}$	$\frac{2}{2}$	$7.123 \times 10^{-13} 9.477 \times 10^{-13}$	2.9131×10^{-4} 1.6266×10^{-4}	79.095
pdb2n0c	ClassicAll	2	1.0471×10^{-12}	1	1.293×10^{-13}	2.8892×10^{-4}	
60	QuaternionAll	2	9.1394×10^{-13}	1	1.682×10^{-13}	1.6213×10^{-4}	78.206
pdb2n0d	ClassicAll	2	5.2061×10^{-11}	2	3.639×10^{-12}	2.9353×10^{-4}	
60	QuaternionAll	2	5.7645×10^{-11}	2	4.540×10^{-12}	1.6380×10^{-4}	79.201
pdb2n0e 60	ClassicAll QuaternionAll	$\frac{2}{2}$	$1.1503 \times 10^{-11} 1.8786 \times 10^{-11}$	$\frac{2}{2}$	3.314×10^{-12} 4.286×10^{-12}	2.9862×10^{-4} 1.7032×10^{-4}	75.335
pdb2n0f	ClassicAll	2	2.2697×10^{-12}	1	3.185×10^{-13}	2.9557×10^{-4}	, 0.000
60	QuaternionAll	2	2.7490×10^{-12}	1	4.023×10^{-13}	1.6613×10^{-4}	77.919
pdb2n0g	ClassicAll	2	1.4896×10^{-11}	1	8.315×10^{-13}	2.9465×10^{-4}	<u>.</u>
60	QuaternionAll	2	1.4974×10^{-11}	1	9.618×10^{-13}	1.6859×10^{-4}	74.774
pdb2n0h 60	ClassicAll QuaternionAll	$\frac{2}{2}$	$4.1935 \times 10^{-12} 4.1379 \times 10^{-12}$	$rac{2}{2}$	$7.716 \times 10^{-13} \\ 8.755 \times 10^{-13}$	2.9523×10^{-4} 1.6501×10^{-4}	78.920
pdb2n35	ClassicAll	8	1.4478×10^{-4}	6	3.658×10^{-14}	2.1553×10^{-3}	,
314	QuaternionAll	8	1.4478×10^{-4} 1.4478×10^{-4}	6	4.617×10^{-14}	1.3703×10^{-3}	57.290
pdb2n3a	ClassicAll	8	2.1457×10^{-3}	5	8.770×10^{-14}	7.4548×10^{-2}	
574	QuaternionAll	8	2.1457×10^{-3}	5	1.049×10^{-13}	3.7047×10^{-2}	101.227

Table 4: Results - continued

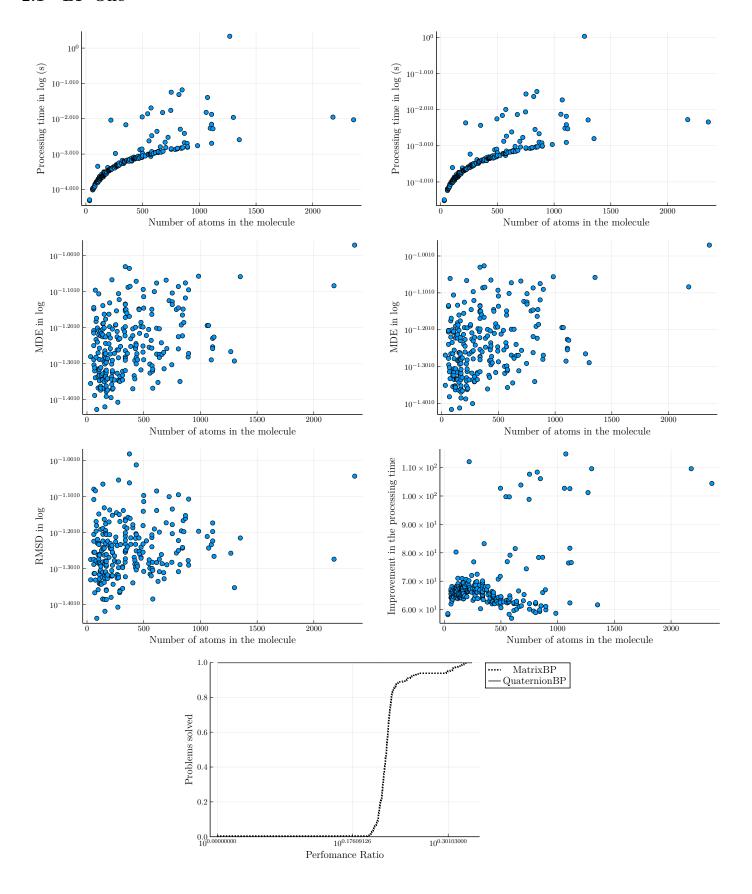
Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2n41 638	ClassicAll QuaternionAll	8 8	5.9366×10^{-3} 5.9366×10^{-3}	$\frac{2}{2}$	1.812×10^{-13} 1.836×10^{-13}	$4.5500 \times 10^{-3} 2.8766 \times 10^{-3}$	58.176
pdb2n4e 638	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 5.1960 \times 10^{-3} \\ 5.1960 \times 10^{-3} \end{array}$	$\frac{2}{2}$	$\begin{array}{c} 1.494 \times 10^{-13} \\ 1.687 \times 10^{-13} \end{array}$	$\begin{array}{c} 4.4792 \times 10^{-3} \\ 2.9218 \times 10^{-3} \end{array}$	53.305
pdb2n5q 164	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.1051 \times 10^{-11} \\ 9.3428 \times 10^{-12} \end{array}$	1 1	$1.732 \times 10^{-12} 1.745 \times 10^{-12}$	$1.1036 \times 10^{-3} 7.1961 \times 10^{-4}$	53.367
pdb2n67 566	ClassicAll QuaternionAll	8 8	$2.0736 \times 10^{-12} 2.0936 \times 10^{-12}$	1 1	$4.443 \times 10^{-13} 4.465 \times 10^{-13}$	$4.0023 \times 10^{-3} 2.5811 \times 10^{-3}$	55.062
pdb2n6n 192	ClassicAll QuaternionAll	2 2	$1.6681 \times 10^{-12} 1.2630 \times 10^{-12}$	$\frac{2}{2}$	$6.557 \times 10^{-13} 7.492 \times 10^{-13}$	$1.1880 \times 10^{-3} \\ 6.6004 \times 10^{-4}$	79.991
pdb2n7i 224	ClassicAll QuaternionAll	8 8	$1.3998 \times 10^{-4} 1.3998 \times 10^{-4}$	1 1	9.212×10^{-13} 1.126×10^{-12}	$1.5001 \times 10^{-3} 9.5671 \times 10^{-4}$	56.801
pdb2n7j 336	ClassicAll QuaternionAll	2 2	$2.5110 \times 10^{-12} 2.6436 \times 10^{-12}$	1 1	$5.969 \times 10^{-13} 6.094 \times 10^{-13}$	$1.8835 \times 10^{-3} 1.0410 \times 10^{-3}$	80.945
pdb2n9b 832	ClassicAll QuaternionAll	8 8	4.0200×10^{-10} 4.0126×10^{-10}	1 1	$1.196 \times 10^{-12} \\ 1.238 \times 10^{-12}$	$\begin{array}{c} 1.1441 \times 10^{-1} \\ 5.3057 \times 10^{-2} \end{array}$	115.633
pdb2na9 266	ClassicAll QuaternionAll	8 8	$2.3390 \times 10^{-12} \\ 2.3721 \times 10^{-12}$	1 1	$5.440 \times 10^{-14} \\ 6.690 \times 10^{-14}$	$1.8226 \times 10^{-3} 1.1543 \times 10^{-3}$	57.894
pdb2ndc 110	ClassicAll QuaternionAll	8 8	3.1313×10^{-3} 3.1313×10^{-3}	2 2	3.365×10^{-14} 4.481×10^{-14}	$7.1114 \times 10^{-4} $ 4.6542×10^{-4}	52.796
pdb2nde 110	ClassicAll QuaternionAll	8 8	8.5286×10^{-5} 8.5286×10^{-5}	2 2	7.022×10^{-14} 8.855×10^{-14}	$7.0378 \times 10^{-4} 4.5662 \times 10^{-4}$	54.126
pdb2ndk 290	ClassicAll QuaternionAll	8 8	$9.0150 \times 10^{-5} $ 9.0150×10^{-5}	1 1	$5.022 \times 10^{-13} \\ 6.279 \times 10^{-13}$	$1.9955 \times 10^{-3} 1.2676 \times 10^{-3}$	57.420
pdb2nvj 152	ClassicAll QuaternionAll	8	$6.7520 \times 10^{-3} $ 6.7520×10^{-3}	7 7	$2.082 \times 10^{-14} $ 2.293×10^{-14}	$1.0271 \times 10^{-3} \\ 6.7479 \times 10^{-4}$	52.215
pdb2p6j 314	ClassicAll QuaternionAll	8	3.2640×10^{-13} 3.5480×10^{-13}	1 1	4.795×10^{-14} 6.389×10^{-14}	2.1604×10^{-3} 1.3869×10^{-3}	55.769
pdb2p81 266	ClassicAll QuaternionAll	8	$6.8538 \times 10^{-11} $ 6.8914×10^{-11}	2 2	$7.881 \times 10^{-13} \\ 8.226 \times 10^{-13}$	1.8154×10^{-3} 1.1458×10^{-3}	58.435
pdb2pqe 896	ClassicAll QuaternionAll	8 8	$4.1258 \times 10^{-5} $ 4.1258×10^{-5}	2 2	$1.127 \times 10^{-11} \\ 1.248 \times 10^{-11}$	$6.4705 \times 10^{-3} 4.1703 \times 10^{-3}$	55.156
pdb2rlg 108	ClassicAll QuaternionAll	2 2	4.8140×10^{-13} 5.3066×10^{-13}	1 1	$5.501 \times 10^{-14} \\ 6.973 \times 10^{-14}$	5.5687×10^{-4} 3.1140×10^{-4}	78.828
pdb2rlh 108	ClassicAll QuaternionAll	2 2	1.0750×10^{-12} 1.0423×10^{-12}	1 1	$4.772 \times 10^{-14} \\ 5.801 \times 10^{-14}$	5.6031×10^{-4} 3.1601×10^{-4}	77.306
pdb2rmy 206	ClassicAll QuaternionAll	8 8	$1.2240 \times 10^{-4} \\ 1.2240 \times 10^{-4}$	1 1	$1.872 \times 10^{-13} $ 2.498×10^{-13}	$1.3607 \times 10^{-3} \\ 8.7649 \times 10^{-4}$	55.244
pdb2rnd 206	ClassicAll QuaternionAll	128 128	3.4031×10^{-12} 3.8842×10^{-12}	33 33	$2.626 \times 10^{-13} \\ 3.569 \times 10^{-13}$	2.2644×10^{-2} 1.2864×10^{-2}	76.027
pdb2roo 260	ClassicAll QuaternionAll	8 8	3.3639×10^{-4} 3.3639×10^{-4}	6 6	$2.933 \times 10^{-12} \\ 3.525 \times 10^{-12}$	3.1899×10^{-3} 1.8971×10^{-3}	68.144
pdb2rql 572	ClassicAll QuaternionAll	8	9.9510×10^{-11} 1.0013×10^{-10}	1 1	$2.345 \times 10^{-12} 2.496 \times 10^{-12}$	3.9594×10^{-3} 2.5420×10^{-3}	55.758
pdb2rut 218	ClassicAll QuaternionAll	8 8	$2.0579 \times 10^{-13} $ 4.0527×10^{-13}	2 2	4.389×10^{-14} 5.013×10^{-14}	$1.4384 \times 10^{-3} 9.2275 \times 10^{-4}$	55.878
pdb2ruv 224	ClassicAll QuaternionAll	8 8	5.4278×10^{-13} 6.5510×10^{-13}	2 2	5.775×10^{-14} 7.404×10^{-14}	1.5078×10^{-3} 9.5680×10^{-4}	57.593
pdb2rux 218	ClassicAll QuaternionAll	8 8	3.6084×10^{-3} 3.6084×10^{-3}	1 1	$2.671 \times 10^{-14} 3.016 \times 10^{-14}$	$1.4544 \times 10^{-3} 9.3587 \times 10^{-4}$	55.411
pdb2ruy 224	ClassicAll QuaternionAll	8 8	$4.1535 \times 10^{-13} \\ 3.5981 \times 10^{-13}$	1 1	$ \begin{array}{r} 1.968 \times 10^{-14} \\ 2.387 \times 10^{-14} \end{array} $	1.4661×10^{-3} 9.3448×10^{-4}	56.889
pdb2rv3 218	ClassicAll QuaternionAll		3.0630×10^{-4} 3.0630×10^{-4} 3.0630×10^{-4}	1 1	$3.656 \times 10^{-14} $ 4.118×10^{-14}	$ \begin{array}{c} 1.4407 \times 10^{-3} \\ 9.2552 \times 10^{-4} \end{array} $	55.664
2.10	~			-	2 = 0		20.004

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2rv5 212	ClassicAll QuaternionAll	8 8	$8.6519 \times 10^{-4} \\ 8.6519 \times 10^{-4}$	1 1	$1.145 \times 10^{-14} \\ 1.338 \times 10^{-14}$	$1.4125 \times 10^{-3} 9.0624 \times 10^{-4}$	55.864
pdb2y4q 476	ClassicAll QuaternionAll	8 8	$4.6451 \times 10^{-11} $ 4.6324×10^{-11}	2 2	1.410×10^{-12} 1.451×10^{-12}	3.3001×10^{-3} 2.1201×10^{-3}	55.657

2 Visual analysis

2.1 BP-One



2.2 BP-All

