Consolidated Performance Tests

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Contents

1	Benchmark's tables	2
	1.1 Using BP-One versions	2
	1.2 Using BP-All versions	12
2	Visual analysis	22
	2.1 BP-One	22
	2.2 BP-All	2:

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1 Benchmark's tables

1.1 Using BP-One versions

Table 1: Results

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Problem Size	Method	MDE	RMSD	Time	Ratio
pdb1a57 698	Classic Quaternion	$2.096 \times 10^{-11} 2.092 \times 10^{-11}$	1.8861×10^{-12}	1.7078×10^{-3} 1.0276×10^{-3}	0.602
pdb1b4c 1108	Classic Quaternion	$5.070 \times 10^{-13} 5.498 \times 10^{-13}$	1.0757×10^{-12}	$3.5365 \times 10^{-3} 2.5634 \times 10^{-3}$	0.725
pdb1ba5 320	Classic Quaternion	$9.359 \times 10^{-13} 1.070 \times 10^{-12}$	4.1376×10^{-12}	$\begin{array}{c} 3.6012 \times 10^{-4} \\ 2.7669 \times 10^{-4} \end{array}$	0.768
pdb1d1n 594	Classic Quaternion	$1.005 \times 10^{-11} 9.672 \times 10^{-12}$	1.2689×10^{-12}	5.9682×10^{-4} 4.7694×10^{-4}	0.799
pdb1dp3 332	Classic Quaternion	7.704×10^{-13} 8.939×10^{-13}	1.4697×10^{-12}	2.9789×10^{-4} 2.3080×10^{-4}	0.775
pdb1du1 122	Classic Quaternion	$8.225 \times 10^{-13} \\ 1.258 \times 10^{-12}$	1.2376×10^{-12}	1.0246×10^{-4} 7.8000×10^{-5}	0.761
pdb1eii 806	Classic Quaternion	1.393×10^{-11} 1.365×10^{-11}	1.1331×10^{-11}	8.2178×10^{-4} 6.5466×10^{-4}	0.797
pdb1fcl 338	Classic Quaternion	4.542×10^{-12} 4.515×10^{-12}	8.0786×10^{-13}	$4.5137 \times 10^{-4} \\ 3.4246 \times 10^{-4}$	0.759
pdb1fd6 344	Classic Quaternion	3.182×10^{-12} 3.193×10^{-12}	3.3846×10^{-13}	3.4143×10^{-4} 2.6441×10^{-4}	0.774
pdb1hf9 496	Classic Quaternion	$1.157 \times 10^{-11} \\ 1.180 \times 10^{-11}$	3.9332×10^{-12}	9.6480×10^{-3} 6.1200×10^{-3}	0.634
pdb1i2u 266	Classic Quaternion	5.562×10^{-13} 5.607×10^{-13}	1.5136×10^{-13}	2.5459×10^{-4} 2.0184×10^{-4}	0.793
pdb1i2v 266	Classic Quaternion	$2.418 \times 10^{-13} 2.519 \times 10^{-13}$	6.9127×10^{-14}	2.7989×10^{-4} 2.2032×10^{-4}	0.787
pdb1ijc 380	Classic 1.408×10^{-11} Quaternion 1.426×10^{-11}		2.4877×10^{-12}	5.5728×10^{-4} 4.1998×10^{-4}	0.754
pdb1jlz 140	Classic Quaternion	5.594×10^{-13} 5.965×10^{-13}	1.3105×10^{-12}	$\begin{array}{c} 1.2392 \times 10^{-4} \\ 9.5602 \times 10^{-5} \end{array}$	0.771
pdb1jw3 842	Classic Quaternion	5.936×10^{-13} 5.897×10^{-13}	3.9013×10^{-13}	8.6446×10^{-4} 6.7580×10^{-4}	0.782
pdb1k0v 440	Classic Quaternion	1.893×10^{-13} 1.894×10^{-13}	1.3433×10^{-13}	$4.6703 \times 10^{-4} 3.5593 \times 10^{-4}$	0.762
pdb1k2h 1120	Classic Quaternion	5.491×10^{-13} 5.199×10^{-13}	2.2039×10^{-13}	2.9241×10^{-3} 1.9975×10^{-3}	0.683
pdb1k36 278	Classic Quaternion	8.820×10^{-12} 1.081×10^{-11}	2.8981×10^{-11}	2.6454×10^{-4} 1.9812×10^{-4}	0.749
pdb1k37 278	Classic Quaternion	$4.711 \times 10^{-13} 4.988 \times 10^{-13}$	1.5479×10^{-13}	3.8419×10^{-4} 2.7588×10^{-4}	0.718
pdb1kuw 62	Classic Quaternion	9.229×10^{-14} 1.130×10^{-13}	7.3457×10^{-14}	$5.8623 \times 10^{-5} 4.3799 \times 10^{-5}$	0.747
pdb1kz0 98	Classic Quaternion	4.404×10^{-14} 5.880×10^{-14}	2.4335×10^{-13}	9.2082×10^{-5} 6.9233×10^{-5}	0.752
pdb1kz2 98	Classic Quaternion	$2.119 \times 10^{-14} 2.886 \times 10^{-14}$	2.6112×10^{-14}	1.0225×10^{-4} 7.2798×10^{-5}	0.712
pdb1kz5 74	Classic Quaternion	4.081×10^{-14} 4.738×10^{-14}	4.8348×10^{-14}	$7.3916 \times 10^{-5} 5.2574 \times 10^{-5}$	0.711
pdb1lvz 68	Classic Quaternion	$6.336 \times 10^{-14} 7.315 \times 10^{-14}$	7.3919×10^{-14}	$6.5156 \times 10^{-5} 4.6871 \times 10^{-5}$	0.719
pdb1m4e 122	Classic Quaternion	5.949×10^{-13} 5.972×10^{-13}	1.1702×10^{-13}	$1.3874 \times 10^{-4} \\ 8.5423 \times 10^{-5}$	0.616

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb1ma2 104	Classic Quaternion	$8.695 \times 10^{-12} \\ 8.758 \times 10^{-12}$	4.7062×10^{-13}	2.3923×10^{-4} 1.0667×10^{-4}	0.446
pdb1ma4 104	Classic Quaternion	$7.247 \times 10^{-14} 7.981 \times 10^{-14}$	1.8851×10^{-13}	$4.1287 \times 10^{-4} \\ 1.7248 \times 10^{-4}$	0.418
pdb1ma5 104	Classic Quaternion	8.169×10^{-13} 9.044×10^{-13}	5.0234×10^{-13}	1.5005×10^{-4} 7.2148×10^{-5}	0.481
pdb1ma6 104	Classic Quaternion	$6.283 \times 10^{-13} \\ 8.522 \times 10^{-13}$	3.3052×10^{-12}	$1.4103 \times 10^{-4} 7.0075 \times 10^{-5}$	0.497
pdb1mpe 1352	Classic Quaternion	$2.617 \times 10^{-11} \\ 2.624 \times 10^{-11}$	7.1261×10^{-13}	8.1131×10^{-3} 3.4902×10^{-3}	0.430
pdb1nd9 296	Classic Quaternion	3.026×10^{-13} 3.845×10^{-13}	4.7137×10^{-13}	$4.5081 \times 10^{-4} $ 2.2590×10^{-4}	0.501
pdb1ne5 254	Classic Quaternion	1.214×10^{-12} 1.384×10^{-12}	7.5582×10^{-13}	3.6696×10^{-4} 1.8293×10^{-4}	0.498
pdb1nmj 170	Classic Quaternion	$1.237 \times 10^{-14} \\ 1.424 \times 10^{-14}$	1.3921×10^{-14}	2.6603×10^{-4} 1.3008×10^{-4}	0.489
pdb1o53 92	Classic Quaternion	3.999×10^{-13} 4.545×10^{-13}	6.5350×10^{-13}	1.4899×10^{-4} 6.9913×10^{-5}	0.469
pdb1oqp 580	Classic Quaternion	7.045×10^{-14} 8.315×10^{-14}	9.0066×10^{-14}	3.0062×10^{-3} 1.6903×10^{-3}	0.562
pdb1plw 32	Classic Quaternion	2.830×10^{-14} 3.122×10^{-14}	4.9118×10^{-14}	$4.5461 \times 10^{-5} \\ 2.2201 \times 10^{-5}$	0.488
pdb1plx 32	Classic Quaternion	$1.574 \times 10^{-13} 2.060 \times 10^{-13}$	1.7973×10^{-13}	$4.2650 \times 10^{-5} 2.0929 \times 10^{-5}$	0.491
pdb1pv0 278	Classic Quaternion	2.409×10^{-13} 2.723×10^{-13}	1.0662×10^{-13}	$4.4412 \times 10^{-4} \\ 2.0904 \times 10^{-4}$	0.471
pdb1pzr 724	Classic Quaternion	$5.644 \times 10^{-12} 5.871 \times 10^{-12}$	9.9935×10^{-12}	6.4490×10^{-3} 3.5690×10^{-3}	0.553
pdb1qlk 1108	Classic Quaternion	$9.019 \times 10^{-10} 9.019 \times 10^{-10}$	1.3287×10^{-12}	$1.0829 \times 10^{-2} 5.9579 \times 10^{-3}$	0.550
pdb1r57 614	Classic Quaternion	$1.847 \times 10^{-13} 2.054 \times 10^{-13}$	1.4866×10^{-13}	9.6998×10^{-4} 4.8680×10^{-4}	0.502
pdb1ry3 386	Classic Quaternion	4.938×10^{-13} 5.910×10^{-13}	4.7678×10^{-13}	$6.3087 \times 10^{-4} \\ 3.0993 \times 10^{-4}$	0.491
pdb1s4h 80	Classic Quaternion	4.300×10^{-9} 4.300×10^{-9}	1.1103×10^{-12}	$1.0674 \times 10^{-4} 5.3186 \times 10^{-5}$	0.498
pdb1s4j 80	Classic Quaternion	$1.520 \times 10^{-13} 2.230 \times 10^{-13}$	1.6407×10^{-13}	$1.2866 \times 10^{-4} \\ 6.7311 \times 10^{-5}$	0.523
pdb1s6j 524	Classic Quaternion	$6.073 \times 10^{-13} 7.660 \times 10^{-13}$	5.9201×10^{-13}	7.9899×10^{-4} 4.0640×10^{-4}	0.509
pdb1sa8 638	Classic Quaternion	$9.340 \times 10^{-13} \\ 1.034 \times 10^{-12}$	1.0370×10^{-12}	$9.9482 \times 10^{-4} \\ 5.2774 \times 10^{-4}$	0.530
$\begin{array}{c} pdb1t2y\\152\end{array}$	Classic Quaternion	$1.887 \times 10^{-13} 2.396 \times 10^{-13}$	2.3861×10^{-13}	$2.3413 \times 10^{-4} \\ 1.4533 \times 10^{-4}$	0.621
pdb1t5q 180	Classic Quaternion	3.877×10^{-14} 5.093×10^{-14}	5.3231×10^{-14}	2.5394×10^{-4} 1.3255×10^{-4}	0.522
pdb1tot 314	Classic Quaternion	$6.148 \times 10^{-14} 6.853 \times 10^{-14}$	2.8392×10^{-14}	$5.0126 \times 10^{-4} \\ 3.1670 \times 10^{-4}$	0.632
pdb1v6r 128	Classic Quaternion	$6.835 \times 10^{-13} 6.970 \times 10^{-13}$	3.1917×10^{-13}	1.9619×10^{-4} 1.1899×10^{-4}	0.607
pdb1v92 278	Classic Quaternion	$1.463 \times 10^{-13} 1.630 \times 10^{-13}$	5.6062×10^{-14}	$4.3360 \times 10^{-4} $ 2.6571×10^{-4}	0.613
pdb1vd7 140	Classic Quaternion	3.741×10^{-9} 3.741×10^{-9}	5.8433×10^{-13}	$2.0593 \times 10^{-4} 1.2499 \times 10^{-4}$	0.607
-		3.741×10^{-9}	5.8433×10^{-13}		0.607

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb1vd9 140	Classic Quaternion	$1.290 \times 10^{-12} \\ 1.554 \times 10^{-12}$	9.0327×10^{-13}	$2.4388 \times 10^{-4} \\ 1.4591 \times 10^{-4}$	0.598
pdb1vdb 140	Classic Quaternion	$9.108 \times 10^{-13} \\ 1.083 \times 10^{-12}$	3.8641×10^{-13}	$\begin{array}{c} 1.9946 \times 10^{-4} \\ 1.1987 \times 10^{-4} \end{array}$	0.601
$\begin{array}{c} \mathrm{pdb1vpc} \\ 272 \end{array}$	Classic Quaternion	$8.500 \times 10^{-15} 1.002 \times 10^{-14}$	8.5436×10^{-15}	$4.1694 \times 10^{-4} 2.6033 \times 10^{-4}$	0.624
pdb1wnk 140	Classic Quaternion	$4.112 \times 10^{-12} 4.632 \times 10^{-12}$	2.2335×10^{-11}	$2.0699 \times 10^{-4} 1.2347 \times 10^{-4}$	0.596
pdb1wo4 152	Classic Quaternion	$9.957 \times 10^{-13} 9.639 \times 10^{-13}$	2.3523×10^{-12}	$2.3205 \times 10^{-4} 1.4194 \times 10^{-4}$	0.612
pdb1wo5 152	Classic Quaternion	$5.257 \times 10^{-9} 5.258 \times 10^{-9}$	4.9063×10^{-12}	$2.3551 \times 10^{-4} 1.4405 \times 10^{-4}$	0.612
pdb1x60 476	Classic Quaternion	$1.076 \times 10^{-12} 1.179 \times 10^{-12}$	3.9684×10^{-13}	7.9397×10^{-4} 4.9474×10^{-4}	0.623
pdb1x9v 544	Classic Quaternion	$8.975 \times 10^{-13} 9.632 \times 10^{-13}$	1.3900×10^{-13}	$2.7541 \times 10^{-2} 1.4581 \times 10^{-2}$	0.529
pdb1y5c 68	Classic Quaternion	8.980×10^{-9} 8.980×10^{-9}	2.9085×10^{-13}	$9.7438 \times 10^{-5} 5.8897 \times 10^{-5}$	0.604
pdb1yx7 500	Classic Quaternion	$8.116 \times 10^{-10} \\ 8.125 \times 10^{-10}$	7.6614×10^{-12}	$1.1530 \times 10^{-3} 7.0746 \times 10^{-4}$	0.614
pdb1yx8 500	Classic Quaternion	$7.276 \times 10^{-12} \\ 8.217 \times 10^{-12}$	1.0819×10^{-11}	$\begin{array}{c} 9.4071 \times 10^{-4} \\ 5.8516 \times 10^{-4} \end{array}$	0.622
$\begin{array}{c} pdb1yxr\\ 464\end{array}$	Classic Quaternion	5.838×10^{-10} 5.839×10^{-10}	2.5240×10^{-13}	$6.7687 \times 10^{-4} 4.1626 \times 10^{-4}$	0.615
pdb2a2y 1072	Classic Quaternion	1.150×10^{-12} 1.151×10^{-12}	3.7416×10^{-13}	3.1010×10^{-2} 1.7439×10^{-2}	0.562
pdb2a4j 580	Classic Quaternion	$2.085 \times 10^{-14} $ 2.727×10^{-14}	1.4394×10^{-14}	$1.0563 \times 10^{-3} \\ 6.4214 \times 10^{-4}$	0.608
pdb2adl 868	Classic Quaternion	$1.752 \times 10^{-11} 1.787 \times 10^{-11}$	3.0093×10^{-12}	3.5641×10^{-2} 2.3248×10^{-2}	0.652
pdb2adn 868	Classic Quaternion	$6.693 \times 10^{-12} 6.465 \times 10^{-12}$	2.4957×10^{-12}	1.9119×10^{-3} 1.1481×10^{-3}	0.601
pdb2ajj 170	Classic Quaternion	$5.641 \times 10^{-14} \\ 6.584 \times 10^{-14}$	1.2744×10^{-13}	$2.5994 \times 10^{-4} 1.5702 \times 10^{-4}$	0.604
pdb2ajm 170	Classic Quaternion	1.183×10^{-13} 1.555×10^{-13}	8.9439×10^{-13}	2.7954×10^{-4} 1.6885×10^{-4}	0.604
pdb2ajn 170	Classic Quaternion	$1.076 \times 10^{-13} 1.217 \times 10^{-13}$	1.5981×10^{-13}	$2.7914 \times 10^{-4} 1.6719 \times 10^{-4}$	0.599
pdb2ajo 170	Classic Quaternion	1.183×10^{-13} 1.555×10^{-13}	8.9439×10^{-13}	2.7899×10^{-4} 1.6861×10^{-4}	0.604
pdb2akk 446	Classic Quaternion	1.288×10^{-13} 1.270×10^{-13}	1.1725×10^{-13}	$\begin{array}{c} 1.4448 \times 10^{-3} \\ 8.4721 \times 10^{-4} \end{array}$	0.586
pdb2bzb 748	Classic Quaternion	$9.365 \times 10^{-14} $ 1.224×10^{-13}	1.5097×10^{-13}	$1.4315 \times 10^{-2} 7.7992 \times 10^{-3}$	0.545
pdb2c0s 386	Classic Quaternion	$3.028 \times 10^{-13} 3.379 \times 10^{-13}$	7.2067×10^{-13}	6.2433×10^{-4} 3.8866×10^{-4}	0.623
pdb2dci 120	Classic Quaternion	$2.366 \times 10^{-14} 2.950 \times 10^{-14}$	1.3479×10^{-13}	$1.7238 \times 10^{-4} 1.0593 \times 10^{-4}$	0.615
pdb2eem 206	Classic Quaternion	5.190×10^{-13} 5.461×10^{-13}	4.0208×10^{-13}	$3.6143 \times 10^{-4} 2.1835 \times 10^{-4}$	0.604
pdb2fva 494	Classic Quaternion	1.047×10^{-12} 1.194×10^{-12}	1.5803×10^{-12}	$1.0303 \times 10^{-3} \\ 6.1618 \times 10^{-4}$	0.598
pdb2fvf 494	Classic Quaternion	$3.106 \times 10^{-13} \\ 3.445 \times 10^{-13}$	2.8750×10^{-13}	$7.4317 \times 10^{-4} 4.6101 \times 10^{-4}$	0.620

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2fxz 80	Classic Quaternion	1.489×10^{-12} 1.749×10^{-12}	2.0430×10^{-12}	1.2207×10^{-4} 7.5061×10^{-5}	0.615
pdb2g9j 848	Classic Quaternion	3.282×10^{-12} 3.535×10^{-12}	2.1668×10^{-12}	$4.9852 \times 10^{-2} 2.6562 \times 10^{-2}$	0.533
pdb2g9l 224	Classic Quaternion	$6.366 \times 10^{-14} \\ 8.672 \times 10^{-14}$	2.8081×10^{-13}	3.5082×10^{-4} 2.1658×10^{-4}	0.617
pdb2h5m 614	Classic Quaternion	$9.692 \times 10^{-13} \\ 1.032 \times 10^{-12}$	4.1376×10^{-12}	$9.9657 \times 10^{-4} \\ 6.2269 \times 10^{-4}$	0.625
pdb2hep 252	Classic Quaternion	$1.191 \times 10^{-12} \\ 1.268 \times 10^{-12}$	5.5848×10^{-13}	3.9601×10^{-4} 2.3695×10^{-4}	0.598
pdb2j0z 752	Classic Quaternion	3.192×10^{-10} 3.197×10^{-10}	4.5324×10^{-12}	2.3683×10^{-1} 1.4497×10^{-1}	0.612
pdb2j10 752	Classic Quaternion	5.870×10^{-10} 5.873×10^{-10}	9.5552×10^{-13}	$4.3767 \times 10^{-3} \\ 2.4477 \times 10^{-3}$	0.559
pdb2j11 752	Classic Quaternion	$7.191 \times 10^{-10} 7.194 \times 10^{-10}$	1.6970×10^{-12}	3.7834×10^{-3} 2.1799×10^{-3}	0.576
pdb2jmy 92	Classic Quaternion	9.834×10^{-13} 9.967×10^{-13}	5.0812×10^{-13}	$\begin{array}{c} 1.4579 \times 10^{-4} \\ 8.8216 \times 10^{-5} \end{array}$	0.605
pdb2jn5 74	Classic Quaternion	3.147×10^{-9} 3.160×10^{-9}	1.4394×10^{-11}	$\begin{array}{c} 1.0386 \times 10^{-4} \\ 6.2820 \times 10^{-5} \end{array}$	0.605
pdb2jnk 842	Classic Quaternion	$4.387 \times 10^{-10} 4.388 \times 10^{-10}$	3.9471×10^{-13}	$\begin{array}{c} 1.3640 \times 10^{-3} \\ 8.6217 \times 10^{-4} \end{array}$	0.632
pdb2jpn 476	Classic Quaternion	$6.730 \times 10^{-14} 6.983 \times 10^{-14}$	1.9605×10^{-13}	$1.1801 \times 10^{-3} \\ 6.8326 \times 10^{-4}$	0.579
pdb2jua 614	Classic Quaternion	$1.740 \times 10^{-11} \\ 1.882 \times 10^{-11}$	1.4391×10^{-11}	$1.0169 \times 10^{-3} \\ 6.2303 \times 10^{-4}$	0.613
pdb2jvd 288	Classic Quaternion	3.339×10^{-14} 3.898×10^{-14}	2.1712×10^{-14}	$4.7167 \times 10^{-4} $ 2.8141×10^{-4}	0.597
pdb2jwe 984	Classic Quaternion	$2.695 \times 10^{-11} 2.734 \times 10^{-11}$	1.0970×10^{-12}	$1.6909 \times 10^{-3} 1.0624 \times 10^{-3}$	0.628
pdb2jws 338	Classic Quaternion	$1.251 \times 10^{-13} 1.543 \times 10^{-13}$	2.8647×10^{-13}	5.6601×10^{-4} 3.4449×10^{-4}	0.609
pdb2jwu 338	Classic Quaternion	$\begin{array}{c} 4.421 \times 10^{-12} \\ 4.373 \times 10^{-12} \end{array}$	6.2322×10^{-13}	$7.6507 \times 10^{-4} 4.5845 \times 10^{-4}$	0.599
pdb2jxf 182	Classic Quaternion	$1.399 \times 10^{-13} 1.734 \times 10^{-13}$	5.8450×10^{-13}	2.8468×10^{-4} 1.6879×10^{-4}	0.593
pdb2jz5 548	Classic Quaternion	2.860×10^{-13} 2.854×10^{-13}	1.7635×10^{-13}	$1.0063 \times 10^{-3} \\ 6.1011 \times 10^{-4}$	0.606
pdb2k2a 422	Classic Quaternion	3.798×10^{-14} 5.134×10^{-14}	1.3435×10^{-13}	$7.2133 \times 10^{-4} 4.5278 \times 10^{-4}$	0.628
pdb2k2f 1268	Classic Quaternion	2.639×10^{-13} 2.818×10^{-13}	7.2949×10^{-14}	2.9933 1.5659	0.523
pdb2k36 896	Classic Quaternion	$1.922 \times 10^{-13} 2.045 \times 10^{-13}$	1.2563×10^{-13}	$\begin{array}{c} 1.4278 \times 10^{-3} \\ 8.9244 \times 10^{-4} \end{array}$	0.625
pdb2k37 356	Classic Quaternion	$1.921 \times 10^{-13} 2.525 \times 10^{-13}$	4.0204×10^{-13}	$5.7554 \times 10^{-4} 3.5444 \times 10^{-4}$	0.616
pdb2k3i 656	Classic Quaternion	3.810×10^{-13} 4.009×10^{-13}	2.4790×10^{-13}	$1.4433 \times 10^{-3} \\ 8.6964 \times 10^{-4}$	0.603
pdb2k6s 494	Classic Quaternion	2.100×10^{-13} 2.651×10^{-13}	4.8726×10^{-13}	$1.2378 \times 10^{-3} 7.1448 \times 10^{-4}$	0.577
pdb2k7o 1096	Classic Quaternion	1.279×10^{-13} 1.416×10^{-13}	4.6393×10^{-13}	$4.8228 \times 10^{-3} $ 2.7638×10^{-3}	0.573
pdb2kbm 1268	Classic Quaternion	$2.165 \times 10^{-13} $ 2.230×10^{-13}	2.6963×10^{-13}	$1.1020 \\ 6.7994 \times 10^{-1}$	0.617

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2kdh 434	Classic Quaternion	1.947×10^{-11} 2.228×10^{-11}	7.6317×10^{-11}	$7.8981 \times 10^{-4} 4.7942 \times 10^{-4}$	0.607
pdb2kdl 338	Classic Quaternion	$\begin{array}{c} 2.301 \times 10^{-13} \\ 2.927 \times 10^{-13} \end{array}$	3.1526×10^{-13}	5.4839×10^{-4} 3.3213×10^{-4}	0.606
pdb2kdm 338	Classic Quaternion	3.191×10^{-12} 3.284×10^{-12}	9.9439×10^{-13}	5.3480×10^{-4} 3.3159×10^{-4}	0.620
$\begin{array}{c} \mathrm{pdb2kdp} \\ 428 \end{array}$	Classic Quaternion	$2.621 \times 10^{-13} 2.865 \times 10^{-13}$	1.0772×10^{-13}	$6.8306 \times 10^{-4} 4.2205 \times 10^{-4}$	0.618
pdb2kdr 170	Classic Quaternion	$6.617 \times 10^{-14} \\ 8.490 \times 10^{-14}$	6.1679×10^{-14}	$2.7330 \times 10^{-4} 1.5899 \times 10^{-4}$	0.582
$\begin{array}{c} \text{pdb2kes} \\ 290 \end{array}$	Classic Quaternion	$4.468 \times 10^{-14} 5.425 \times 10^{-14}$	2.3286×10^{-14}	5.0386×10^{-4} 2.9163×10^{-4}	0.579
pdb2kib 352	Classic Quaternion	$2.533 \times 10^{-12} 2.539 \times 10^{-12}$	1.3388×10^{-12}	$6.0079 \times 10^{-3} \\ 3.2111 \times 10^{-3}$	0.534
pdb2kjn 158	Classic Quaternion	$1.125 \times 10^{-9} \\ 1.125 \times 10^{-9}$	1.3817×10^{-13}	$2.4788 \times 10^{-4} 1.4894 \times 10^{-4}$	0.601
pdb2kjo 158	Classic Quaternion	2.284×10^{-13} 2.421×10^{-13}	6.7185×10^{-14}	$2.3357 \times 10^{-4} 1.4172 \times 10^{-4}$	0.607
pdb2kjr 572	Classic Quaternion	3.247×10^{-12} 3.251×10^{-12}	4.0637×10^{-13}	$1.4415 \times 10^{-3} \\ 8.5930 \times 10^{-4}$	0.596
pdb <mark>2kko</mark> 1300	Classic Quaternion	1.191×10^{-13} 1.285×10^{-13}	2.9766×10^{-14}	$8.6106 \times 10^{-3} $ 4.8727×10^{-3}	0.566
pdb2kl5 662	Classic Quaternion	$1.820 \times 10^{-13} 2.020 \times 10^{-13}$	1.3796×10^{-13}	$1.0275 \times 10^{-3} \\ 6.4496 \times 10^{-4}$	0.628
$\begin{array}{c} \text{pdb2klz} \\ 276 \end{array}$	Classic Quaternion	3.439×10^{-14} 4.443×10^{-14}	6.4874×10^{-14}	4.7020×10^{-4} 2.7869×10^{-4}	0.593
pdb2ko1 1060	Classic Quaternion	1.150×10^{-12} 1.151×10^{-12}	7.8450×10^{-13}	$1.2485 \times 10^{-2} 7.0322 \times 10^{-3}$	0.563
pdb2koz 200	Classic Quaternion	$1.075 \times 10^{-9} 1.075 \times 10^{-9}$	8.8024×10^{-13}	3.0575×10^{-4} 1.9136×10^{-4}	0.626
pdb2kp0 200	Classic Quaternion	$4.893 \times 10^{-12} 5.588 \times 10^{-12}$	4.2756×10^{-12}	3.0698×10^{-4} 1.8959×10^{-4}	0.618
pdb2ksg 290	Classic Quaternion	3.215×10^{-14} 3.967×10^{-14}	2.4678×10^{-14}	$\begin{array}{c} 4.3551 \times 10^{-4} \\ 2.6495 \times 10^{-4} \end{array}$	0.608
pdb2kt8 458	Classic Quaternion	3.314×10^{-12} 3.535×10^{-12}	7.1394×10^{-13}	7.0930×10^{-4} 4.4313×10^{-4}	0.625
pdb2kuh 404	Classic Quaternion	$2.016 \times 10^{-14} 2.492 \times 10^{-14}$	4.0485×10^{-14}	$6.8106 \times 10^{-4} 4.3151 \times 10^{-4}$	0.634
pdb2kwh 338	Classic Quaternion	$1.408 \times 10^{-13} \\ 1.825 \times 10^{-13}$	2.9549×10^{-13}	5.2925×10^{-4} 3.1747×10^{-4}	0.600
pdb2kxa 144	Classic Quaternion	$\begin{array}{c} 1.325 \times 10^{-12} \\ 1.351 \times 10^{-12} \end{array}$	3.5240×10^{-13}	$\begin{array}{c} 2.1473 \times 10^{-4} \\ 1.3425 \times 10^{-4} \end{array}$	0.625
pdb2kyb 362	Classic Quaternion	$1.321 \times 10^{-11} \\ 1.373 \times 10^{-11}$	2.6755×10^{-12}	$\begin{array}{c} 1.6400 \times 10^{-3} \\ 9.2684 \times 10^{-4} \end{array}$	0.565
pdb2l3m 428	Classic Quaternion	$1.028 \times 10^{-12} 9.340 \times 10^{-13}$	6.9725×10^{-13}	$6.7557 \times 10^{-4} 4.1986 \times 10^{-4}$	0.621
pdb2l3n 626	Classic Quaternion	3.025×10^{-14} 3.634×10^{-14}	4.4517×10^{-14}	$4.0176 \times 10^{-3} $ 2.2465×10^{-3}	0.559
pdb2l45 116	Classic Quaternion	2.236×10^{-14} 3.033×10^{-14}	8.5325×10^{-14}	$1.8187 \times 10^{-4} \\ 1.1228 \times 10^{-4}$	0.617
pdb2l5r 138	Classic Quaternion	3.529×10^{-14} 4.432×10^{-14}	1.4398×10^{-14}	2.4104×10^{-4} 1.4613×10^{-4}	0.606
pdb2l6q 374	Classic Quaternion	$4.959 \times 10^{-9} \\ 6.131 \times 10^{-9}$	1.7792×10^{-8}	5.7492×10^{-4} 3.4945×10^{-4}	0.608

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2l6r 374	Classic Quaternion	$7.323 \times 10^{-10} 7.325 \times 10^{-10}$	2.4265×10^{-11}	$6.1184 \times 10^{-4} \\ 3.7345 \times 10^{-4}$	0.610
pdb2l98 434	Classic Quaternion	$\begin{array}{c} 3.273 \times 10^{-13} \\ 3.638 \times 10^{-13} \end{array}$	8.9102×10^{-13}	$6.8739 \times 10^{-4} 4.2127 \times 10^{-4}$	0.613
pdb2lci 806	Classic Quaternion	$2.579 \times 10^{-13} 2.404 \times 10^{-13}$	8.2767×10^{-14}	$\begin{array}{c} 1.3251 \times 10^{-3} \\ 8.1420 \times 10^{-4} \end{array}$	0.614
pdb2lde 152	Classic Quaternion	3.153×10^{-14} 3.762×10^{-14}	4.1691×10^{-14}	$2.2579 \times 10^{-4} 1.3643 \times 10^{-4}$	0.604
pdb2le2 676	Classic Quaternion	2.064×10^{-13} 2.042×10^{-13}	7.7661×10^{-14}	$1.2162 \times 10^{-2} \\ 6.8292 \times 10^{-3}$	0.562
pdb2le7 122	Classic Quaternion	$2.112 \times 10^{-14} 2.749 \times 10^{-14}$	3.9789×10^{-14}	1.8287×10^{-4} 1.1091×10^{-4}	0.606
pdb2ler 68	Classic Quaternion	$1.315 \times 10^{-14} 1.532 \times 10^{-14}$	2.1465×10^{-14}	$9.8364 \times 10^{-5} 5.9976 \times 10^{-5}$	0.610
pdb2lgi 338	Classic Quaternion	$1.068 \times 10^{-12} 1.052 \times 10^{-12}$	1.8917×10^{-13}	5.3405×10^{-4} 3.3074×10^{-4}	0.619
pdb2lhc 338	Classic Quaternion	$5.829 \times 10^{-10} 5.830 \times 10^{-10}$	2.1362×10^{-12}	5.7812×10^{-4} 3.4725×10^{-4}	0.601
pdb2lhd 338	Classic Quaternion	$1.930 \times 10^{-12} 2.033 \times 10^{-12}$	2.3902×10^{-12}	7.2693×10^{-4} 4.3294×10^{-4}	0.596
pdb2lhe 338	Classic Quaternion	$4.963 \times 10^{-11} 4.967 \times 10^{-11}$	4.8488×10^{-13}	$6.9959 \times 10^{-4} 4.2128 \times 10^{-4}$	0.602
pdb2lhg 338	Classic Quaternion	$6.459 \times 10^{-14} 7.322 \times 10^{-14}$	5.9754×10^{-14}	5.4166×10^{-4} 3.4252×10^{-4}	0.632
pdb2lix 162	Classic Quaternion	$4.842 \times 10^{-14} 5.614 \times 10^{-14}$	7.8975×10^{-14}	$2.5511 \times 10^{-4} 1.5798 \times 10^{-4}$	0.619
pdb2lld 242	Classic Quaternion	$1.937 \times 10^{-13} 2.214 \times 10^{-13}$	2.2642×10^{-13}	3.8603×10^{-4} 2.4657×10^{-4}	0.639
pdb2lm9 578	Classic Quaternion	$6.254 \times 10^{-14} 7.713 \times 10^{-14}$	1.5079×10^{-13}	$9.2867 \times 10^{-4} 5.5919 \times 10^{-4}$	0.602
pdb2lmf 140	Classic Quaternion	$1.282 \times 10^{-13} 1.462 \times 10^{-13}$	7.9808×10^{-14}	$\begin{array}{c} 2.0512 \times 10^{-4} \\ 1.2216 \times 10^{-4} \end{array}$	0.596
pdb2ln3 500	Classic Quaternion	$1.292 \times 10^{-13} 1.359 \times 10^{-13}$	8.4114×10^{-14}	$\begin{array}{c} 8.2481 \times 10^{-4} \\ 5.0672 \times 10^{-4} \end{array}$	0.614
pdb2lo2 230	Classic Quaternion	$2.068 \times 10^{-14} $ 2.571×10^{-14}	3.6944×10^{-14}	3.5286×10^{-4} 2.1708×10^{-4}	0.615
pdb2lqp 428	Classic Quaternion	2.950×10^{-13} 3.085×10^{-13}	4.7561×10^{-13}	$6.8026 \times 10^{-4} $ 4.1891×10^{-4}	0.616
pdb2lr0 806	Classic Quaternion	3.549×10^{-12} 3.440×10^{-12}	6.0485×10^{-13}	$1.3663 \times 10^{-3} \\ 8.4248 \times 10^{-4}$	0.617
pdb2lrh 806	Classic Quaternion	$5.631 \times 10^{-13} \\ 6.564 \times 10^{-13}$	3.2048×10^{-13}	$\begin{array}{c} 1.3271 \times 10^{-3} \\ 8.1453 \times 10^{-4} \end{array}$	0.614
pdb2ls9 152	Classic Quaternion	$1.122 \times 10^{-13} \\ 1.471 \times 10^{-13}$	3.7128×10^{-13}	$2.1166 \times 10^{-4} \\ 1.2974 \times 10^{-4}$	0.613
pdb2lsa 140	Classic Quaternion	$5.235 \times 10^{-14} 7.034 \times 10^{-14}$	1.5385×10^{-13}	2.0973×10^{-4} 1.3006×10^{-4}	0.620
$\begin{array}{c} \text{pdb2lss} \\ 422 \end{array}$	Classic Quaternion	$1.230 \times 10^{-13} 1.455 \times 10^{-13}$	1.6926×10^{-13}	$6.5717 \times 10^{-4} 4.1698 \times 10^{-4}$	0.635
pdb2lt3 680	Classic Quaternion	$7.245 \times 10^{-14} 7.760 \times 10^{-14}$	5.2634×10^{-14}	$\begin{array}{c} 1.0848 \times 10^{-3} \\ 6.8766 \times 10^{-4} \end{array}$	0.634
pdb2lu6 86	Classic Quaternion	$5.356 \times 10^{-15} \\ 6.922 \times 10^{-15}$	4.1890×10^{-15}	$\begin{array}{c} 1.3180 \times 10^{-4} \\ 7.8526 \times 10^{-5} \end{array}$	0.596
pdb2lwa 432	Classic Quaternion	$3.615 \times 10^{-13} 4.427 \times 10^{-13}$	9.3395×10^{-13}	$6.6402 \times 10^{-4} 4.1102 \times 10^{-4}$	0.619

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2lx0 194	Classic Quaternion	1.940×10^{-9} 1.940×10^{-9}	2.0923×10^{-13}	3.1226×10^{-4} 1.9112×10^{-4}	0.612
pdb2lxb 892	Classic Quaternion	$1.542 \times 10^{-13} \\ 1.585 \times 10^{-13}$	1.6837×10^{-13}	$1.8311 \times 10^{-3} \\ 1.1032 \times 10^{-3}$	0.602
pdb2lxy 404	Classic Quaternion	$9.313 \times 10^{-13} 1.025 \times 10^{-12}$	1.6618×10^{-12}	$8.0258 \times 10^{-4} $ 4.8297×10^{-4}	0.602
pdb2lxz 194	Classic Quaternion	$2.371 \times 10^{-12} 2.792 \times 10^{-12}$	1.9895×10^{-12}	$3.2047 \times 10^{-4} 1.9884 \times 10^{-4}$	0.620
pdb2lzf 820	Classic Quaternion	3.217×10^{-14} 3.957×10^{-14}	1.2991×10^{-13}	$3.6701 \times 10^{-2} 2.0489 \times 10^{-2}$	0.558
pdb2m1a 158	Classic Quaternion	$6.346 \times 10^{-15} 7.612 \times 10^{-15}$	6.5801×10^{-15}	$2.8770 \times 10^{-4} 1.6947 \times 10^{-4}$	0.589
pdb2m1j 182	Classic Quaternion	$1.865 \times 10^{-14} $ 2.212×10^{-14}	6.6915×10^{-14}	2.9298×10^{-4} 1.7721×10^{-4}	0.605
pdb2m2y 110	Classic Quaternion	2.699×10^{-13} 2.808×10^{-13}	1.4386×10^{-13}	$1.6766 \times 10^{-4} 1.0300 \times 10^{-4}$	0.614
pdb2m3f 134	Classic Quaternion	$3.629 \times 10^{-14} 4.641 \times 10^{-14}$	5.8107×10^{-14}	$1.9549 \times 10^{-4} 1.1839 \times 10^{-4}$	0.606
pdb2m4j 2178	Classic Quaternion	1.463×10^{-11} 1.455×10^{-11}	1.8385×10^{-13}	3.0899×10^{-2} 1.6683×10^{-2}	0.540
pdb2m8m 170	Classic Quaternion	$2.407 \times 10^{-14} 3.023 \times 10^{-14}$	1.1738×10^{-13}	$2.4356 \times 10^{-4} 1.5232 \times 10^{-4}$	0.625
pdb2m8o 170	Classic Quaternion	$1.672 \times 10^{-14} 2.039 \times 10^{-14}$	2.4755×10^{-14}	2.3852×10^{-4} 1.5126×10^{-4}	0.634
pdb2m97 416	Classic Quaternion	$4.646 \times 10^{-14} \\ 5.841 \times 10^{-14}$	2.0639×10^{-13}	$6.4149 \times 10^{-4} 4.0543 \times 10^{-4}$	0.632
pdb2m9g 1108	Classic Quaternion	$2.939 \times 10^{-13} 3.170 \times 10^{-13}$	5.8913×10^{-13}	$1.8543 \times 10^{-3} 1.1475 \times 10^{-3}$	0.619
pdb2m9r 242	Classic Quaternion	$3.537 \times 10^{-14} 4.406 \times 10^{-14}$	1.6694×10^{-13}	3.8746×10^{-4} 2.2436×10^{-4}	0.579
pdb2mdv 460	Classic Quaternion	$3.178 \times 10^{-12} 3.178 \times 10^{-12}$	3.0402×10^{-13}	1.7907×10^{-3} 1.0462×10^{-3}	0.584
pdb2me1 164	Classic Quaternion	1.886×10^{-13} 2.208×10^{-13}	1.6579×10^{-13}	2.4024×10^{-4} 1.4629×10^{-4}	0.609
pdb2me2 164	Classic Quaternion	$3.667 \times 10^{-13} 5.098 \times 10^{-13}$	1.1486×10^{-12}	$2.5397 \times 10^{-4} 1.5353 \times 10^{-4}$	0.605
pdb2me3 164	Classic Quaternion	$2.593 \times 10^{-9} 2.593 \times 10^{-9}$	9.2137×10^{-14}	$2.3516 \times 10^{-4} 1.4335 \times 10^{-4}$	0.610
pdb2me4 164	Classic Quaternion	$2.854 \times 10^{-9} 2.854 \times 10^{-9}$	9.9945×10^{-13}	$2.7671 \times 10^{-4} 1.6638 \times 10^{-4}$	0.601
pdb2mg1 164	Classic Quaternion	$4.398 \times 10^{-14} \\ 5.374 \times 10^{-14}$	1.5805×10^{-13}	$2.3575 \times 10^{-4} 1.4662 \times 10^{-4}$	0.622
pdb2mg2 170	Classic Quaternion	1.829×10^{-14} 2.480×10^{-14}	2.5921×10^{-14}	$2.4349 \times 10^{-4} 1.5351 \times 10^{-4}$	0.630
pdb2mg3 170	Classic Quaternion	$3.541 \times 10^{-14} 4.461 \times 10^{-14}$	2.4798×10^{-13}	$2.5354 \times 10^{-4} 1.5851 \times 10^{-4}$	0.625
pdb2mh8 338	Classic Quaternion	$1.547 \times 10^{-13} 1.883 \times 10^{-13}$	2.9903×10^{-13}	$5.5605 \times 10^{-4} 3.4429 \times 10^{-4}$	0.619
pdb2mhw 164	Classic Quaternion	$6.229 \times 10^{-14} 7.129 \times 10^{-14}$	4.9718×10^{-13}	$2.5108 \times 10^{-4} $ 1.5714×10^{-4}	0.626
pdb2mi1 84	Classic Quaternion	$1.827 \times 10^{-12} 2.052 \times 10^{-12}$	1.5687×10^{-12}	$1.3281 \times 10^{-4} \\ 8.2475 \times 10^{-5}$	0.621
pdb2mi7 404	Classic Quaternion	$6.022 \times 10^{-13} $ 6.817×10^{-13}	1.3690×10^{-12}	$5.8600 \times 10^{-4} 3.5786 \times 10^{-4}$	0.611

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2mij 224	Classic Quaternion	1.244×10^{-13} 1.522×10^{-13}	2.8681×10^{-13}	3.3831×10^{-4} 2.0663×10^{-4}	0.611
pdb2mix 128	Classic Quaternion	$\begin{array}{c} 4.816 \times 10^{-14} \\ 4.684 \times 10^{-14} \end{array}$	3.7348×10^{-14}	$\begin{array}{c} 1.9065 \times 10^{-4} \\ 1.1873 \times 10^{-4} \end{array}$	0.623
pdb2mj1 110	Classic Quaternion	1.309×10^{-13} 1.646×10^{-13}	2.3819×10^{-13}	$1.7651 \times 10^{-4} 1.0746 \times 10^{-4}$	0.609
pdb2mj2 218	Classic Quaternion	9.775×10^{-14} 1.196×10^{-13}	8.8713×10^{-14}	$3.4006 \times 10^{-4} 2.0304 \times 10^{-4}$	0.597
$\begin{array}{c} \rm pdb2mjg\\ 556 \end{array}$	Classic Quaternion	$5.503 \times 10^{-14} $ 6.580×10^{-14}	7.0670×10^{-14}	$2.1403 \times 10^{-3} 1.2087 \times 10^{-3}$	0.565
pdb2mji 788	Classic Quaternion	$3.207 \times 10^{-12} 3.247 \times 10^{-12}$	2.7336×10^{-13}	$1.2480 \times 10^{-3} 7.9502 \times 10^{-4}$	0.637
pdb2mle 434	Classic Quaternion	$1.491 \times 10^{-13} 1.535 \times 10^{-13}$	3.1271×10^{-13}	7.0584×10^{-4} 4.2886×10^{-4}	0.608
pdb2mlf 434	Classic Quaternion	9.918×10^{-14} 1.128×10^{-13}	9.2903×10^{-14}	7.0616×10^{-4} 4.3297×10^{-4}	0.613
pdb2mo5 854	Classic Quaternion	$2.527 \times 10^{-10} 2.527 \times 10^{-10}$	1.0204×10^{-12}	$1.3908 \times 10^{-3} \\ 8.7516 \times 10^{-4}$	0.629
pdb2mpu 554	Classic Quaternion	$9.785 \times 10^{-14} 1.016 \times 10^{-13}$	1.0352×10^{-13}	$8.9773 \times 10^{-4} 5.6068 \times 10^{-4}$	0.625
pdb2mra 704	Classic Quaternion	2.632×10^{-13} 2.768×10^{-13}	1.2867×10^{-13}	$1.4008 \times 10^{-3} \\ 8.4120 \times 10^{-4}$	0.601
pdb2msu 122	Classic Quaternion	$7.813 \times 10^{-14} \\ 8.765 \times 10^{-14}$	3.7025×10^{-14}	$2.0173 \times 10^{-4} $ 1.2208×10^{-4}	0.605
pdb2mty 120	Classic Quaternion	$1.849 \times 10^{-14} 2.364 \times 10^{-14}$	9.1457×10^{-14}	$2.1012 \times 10^{-4} 1.2629 \times 10^{-4}$	0.601
pdb2muh 98	Classic Quaternion	2.008×10^{-13} 2.251×10^{-13}	1.4292×10^{-13}	$1.4547 \times 10^{-4} \\ 8.7958 \times 10^{-5}$	0.605
pdb2mvj 156	Classic Quaternion	$1.534 \times 10^{-13} 1.647 \times 10^{-13}$	5.5998×10^{-14}	$2.4181 \times 10^{-4} 1.4392 \times 10^{-4}$	0.595
pdb2mvt 284	Classic Quaternion	$6.053 \times 10^{-12} 6.226 \times 10^{-12}$	3.1969×10^{-12}	$5.6681 \times 10^{-4} \\ 3.3934 \times 10^{-4}$	0.599
pdb2mvx 2360	Classic Quaternion	$4.728 \times 10^{-9} 4.729 \times 10^{-9}$	3.7181×10^{-11}	$2.1984 \times 10^{-2} 1.2119 \times 10^{-2}$	0.551
pdb2mz6 220	Classic Quaternion	$4.129 \times 10^{-8} 4.129 \times 10^{-8}$	4.4231×10^{-13}	$2.8851 \times 10^{-2} $ 1.5215×10^{-2}	0.527
pdb2n00 572	Classic Quaternion	$2.703 \times 10^{-13} 3.467 \times 10^{-13}$	7.3499×10^{-13}	$7.8567 \times 10^{-4} 4.9399 \times 10^{-4}$	0.629
pdb2n0b 60	Classic Quaternion	$7.104 \times 10^{-13} 9.458 \times 10^{-13}$	8.9441×10^{-13}	$9.1258 \times 10^{-5} 5.5481 \times 10^{-5}$	0.608
pdb2n0c 60	Classic Quaternion	1.293×10^{-13} 1.682×10^{-13}	2.8483×10^{-13}	8.9546×10^{-5} 5.3031×10^{-5}	0.592
pdb2n0d 60	Classic Quaternion	$1.925 \times 10^{-9} 1.926 \times 10^{-9}$	1.6149×10^{-11}	$8.7136 \times 10^{-5} 5.3740 \times 10^{-5}$	0.617
pdb2n0e 60	Classic Quaternion	$3.314 \times 10^{-12} 4.286 \times 10^{-12}$	8.3573×10^{-12}	$8.9640 \times 10^{-5} 5.5845 \times 10^{-5}$	0.623
pdb2n0f 60	Classic Quaternion	$8.103 \times 10^{-9} \\ 8.103 \times 10^{-9}$	5.8011×10^{-13}	$8.4756 \times 10^{-5} 5.1625 \times 10^{-5}$	0.609
pdb2n0g 60	Classic Quaternion	$8.315 \times 10^{-13} 9.618 \times 10^{-13}$	1.3124×10^{-13}	$1.0130 \times 10^{-4} 6.0317 \times 10^{-5}$	0.595
pdb2n0h 60	Classic Quaternion	$7.690 \times 10^{-13} \\ 8.730 \times 10^{-13}$	1.8191×10^{-13}	$9.3479 \times 10^{-5} 5.8237 \times 10^{-5}$	0.623
pdb2n35 314	Classic Quaternion	$3.541 \times 10^{-14} 4.466 \times 10^{-14}$	1.0752×10^{-13}	$4.9604 \times 10^{-4} \\ 3.0774 \times 10^{-4}$	0.620

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2n3a 574	Classic Quaternion	$8.761 \times 10^{-14} \\ 1.049 \times 10^{-13}$	1.0149×10^{-13}	$1.6767 \times 10^{-2} \\ 8.9551 \times 10^{-3}$	0.534
pdb2n41 638	Classic Quaternion	$\begin{array}{c} 1.812 \times 10^{-13} \\ 1.836 \times 10^{-13} \end{array}$	8.2539×10^{-14}	$\begin{array}{c} 1.0753 \times 10^{-3} \\ 6.5707 \times 10^{-4} \end{array}$	0.611
pdb2n4e 638	Classic Quaternion	$1.494 \times 10^{-13} 1.687 \times 10^{-13}$	1.8433×10^{-13}	$1.0563 \times 10^{-3} \\ 6.5324 \times 10^{-4}$	0.618
pdb2n5q 164	Classic Quaternion	$1.732 \times 10^{-12} 1.745 \times 10^{-12}$	1.7589×10^{-12}	$2.5502 \times 10^{-4} 1.6074 \times 10^{-4}$	0.630
pdb2n67 566	Classic Quaternion	$4.443 \times 10^{-13} 4.465 \times 10^{-13}$	6.3487×10^{-14}	$\begin{array}{c} 9.0517 \times 10^{-4} \\ 5.6303 \times 10^{-4} \end{array}$	0.622
pdb2n6n 192	Classic Quaternion	4.139×10^{-8} 4.139×10^{-8}	5.0670×10^{-13}	3.0612×10^{-4} 1.9266×10^{-4}	0.629
pdb2n7i 224	Classic Quaternion	9.212×10^{-13} 1.126×10^{-12}	3.0537×10^{-12}	$3.4800 \times 10^{-4} 2.1033 \times 10^{-4}$	0.604
pdb2n7j 336	Classic Quaternion	$5.969 \times 10^{-13} 6.094 \times 10^{-13}$	1.5144×10^{-13}	$5.5604 \times 10^{-4} \\ 3.3764 \times 10^{-4}$	0.607
pdb2n9b 832	Classic Quaternion	1.196×10^{-12} 1.238×10^{-12}	1.1231×10^{-12}	$7.5212 \times 10^{-3} 4.0541 \times 10^{-3}$	0.539
pdb2na9 266	Classic Quaternion	$5.440 \times 10^{-14} 6.690 \times 10^{-14}$	5.4544×10^{-14}	3.9985×10^{-4} 2.3943×10^{-4}	0.599
pdb2ndc 110	Classic Quaternion	3.365×10^{-14} 4.479×10^{-14}	5.1916×10^{-14}	$1.7449 \times 10^{-4} 1.0603 \times 10^{-4}$	0.608
pdb2nde 110	Classic Quaternion	7.022×10^{-14} 8.868×10^{-14}	2.5156×10^{-13}	$\begin{array}{c} 1.5498 \times 10^{-4} \\ 9.5265 \times 10^{-5} \end{array}$	0.615
pdb2ndk 290	Classic Quaternion	$5.022 \times 10^{-13} 6.279 \times 10^{-13}$	2.0516×10^{-12}	$4.3875 \times 10^{-4} 2.6635 \times 10^{-4}$	0.607
pdb2nvj 152	Classic Quaternion	$2.082 \times 10^{-14} 2.293 \times 10^{-14}$	1.4035×10^{-14}	$2.1106 \times 10^{-4} $ 1.3248×10^{-4}	0.628
pdb2p6j 314	Classic Quaternion	$4.795 \times 10^{-14} 6.389 \times 10^{-14}$	1.1404×10^{-13}	$4.9868 \times 10^{-4} \\ 3.0174 \times 10^{-4}$	0.605
pdb2p81 266	Classic Quaternion	$7.881 \times 10^{-13} \\ 8.250 \times 10^{-13}$	4.3715×10^{-13}	$4.0170 \times 10^{-4} 2.4128 \times 10^{-4}$	0.601
pdb2pqe 896	Classic Quaternion	$6.484 \times 10^{-10} 6.496 \times 10^{-10}$	8.5673×10^{-12}	$\begin{array}{c} 1.7464 \times 10^{-3} \\ 1.0742 \times 10^{-3} \end{array}$	0.615
pdb2rlg 108	Classic Quaternion	$5.501 \times 10^{-14} \\ 6.973 \times 10^{-14}$	6.8873×10^{-14}	$1.7141 \times 10^{-4} 1.0328 \times 10^{-4}$	0.603
pdb2rlh 108	Classic Quaternion	$4.772 \times 10^{-14} 5.801 \times 10^{-14}$	3.9131×10^{-14}	$1.8381 \times 10^{-4} 1.1035 \times 10^{-4}$	0.600
pdb2rmy 206	Classic Quaternion	$1.872 \times 10^{-13} 2.498 \times 10^{-13}$	3.6453×10^{-13}	3.2133×10^{-4} 1.9158×10^{-4}	0.596
pdb2rnd 206	Classic Quaternion	$\begin{array}{c} 2.626 \times 10^{-13} \\ 3.581 \times 10^{-13} \end{array}$	4.9979×10^{-13}	3.1245×10^{-4} 1.8852×10^{-4}	0.603
$\begin{array}{c} \mathrm{pdb2roo} \\ 260 \end{array}$	Classic Quaternion	$2.933 \times 10^{-12} 3.525 \times 10^{-12}$	3.5927×10^{-12}	9.2680×10^{-4} 5.2709×10^{-4}	0.569
pdb2rql 572	Classic Quaternion	$2.345 \times 10^{-12} 2.496 \times 10^{-12}$	8.7086×10^{-13}	$1.2692 \times 10^{-3} 7.5430 \times 10^{-4}$	0.594
$\begin{array}{c} \mathrm{pdb2rut} \\ 218 \end{array}$	Classic Quaternion	$4.389 \times 10^{-14} 5.014 \times 10^{-14}$	3.5338×10^{-13}	$3.3457 \times 10^{-4} 2.0440 \times 10^{-4}$	0.611
pdb2ruv 224	Classic Quaternion	$5.776 \times 10^{-14} 7.408 \times 10^{-14}$	1.2473×10^{-13}	$3.4892 \times 10^{-4} \\ 2.1174 \times 10^{-4}$	0.607
pdb2rux 218	Classic Quaternion	$2.671 \times 10^{-14} \\ 3.016 \times 10^{-14}$	6.2140×10^{-14}	$3.5268 \times 10^{-4} $ 2.1558×10^{-4}	0.611
pdb2ruy 224	Classic Quaternion	$1.968 \times 10^{-14} 2.387 \times 10^{-14}$	6.4254×10^{-14}	$3.5150 \times 10^{-4} 2.1187 \times 10^{-4}$	0.603

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2rv3 218	Classic Quaternion	3.656×10^{-14} 4.118×10^{-14}	6.3794×10^{-14}	3.5977×10^{-4} 2.1748×10^{-4}	0.605
pdb2rv5 212	Classic Quaternion	$1.145 \times 10^{-14} \\ 1.338 \times 10^{-14}$	1.6010×10^{-14}	3.3397×10^{-4} 2.0422×10^{-4}	0.611
pdb2y4q 476	Classic Quaternion	$1.410 \times 10^{-12} \\ 1.451 \times 10^{-12}$	2.0648×10^{-13}	$7.3303 \times 10^{-4} 4.5092 \times 10^{-4}$	0.615

log.txt

time_limit=120 seconds

 ${\tt function_of_central_tendency_meansure=median}$

function_of_improvement=#14

precision=1.0e-5

precision_virtual=1.0e-8

benchmark_seconds=300

benchmark_samples_limit=100000

all_solutions=False

list_of_problems=["pdb1a57", "pdb1b4c", "pdb1ba5", "pdb1d1n", "pdb1dp3", "pdb1du1", "pdb1eii", "pdb1fc1", "pdb1fd6", "pdb1start_time=2023-04-14T15:29:01.778

end_time=2023-04-15T13:10:15.373

Merge with

time_limit=120 seconds

 ${\tt function_of_central_tendency_meansure=median}$

 ${\tt function_of_improvement=\#16}$

precision=1.0e-5

precision_virtual=1.0e-8

benchmark_seconds=6000

benchmark_samples_limit=100000

all_solutions=False

list_of_problems=["pdb2k2f", "pdb2kbm", "pdb2j10", "pdb2j11", "pdb2lwa", "pdb2j0z", "pdb2adl", "pdb1pzr", "pdb2lzf", "pdb2lzf", "pdb2lzf", "pdb2lzf", "pdb2lwa", "pdb2j0z", "pdb2adl", "pdb1pzr", "pdb2lzf", "pdb2lzf", "pdb2lzf", "pdb2lwa", "pdb2j0z", "pdb2adl", "pdb2lzf", "pdb2lzf", "pdb2lzf", "pdb2lwa", "pdb2j0z", "pdb2adl", "pdb2lzf", "pdb2lzf", "pdb2lzf", "pdb2lwa", "pdb2lwa", "pdb2j0z", "pdb2lwa", "pdb

start_time=2023-04-25T10:34:45.483

end_time=2023-04-27T21:52:14.682

1.2 Using BP-All versions

Table 3: Results

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb1a57 698	ClassicAll QuaternionAll	8 8	3.1806×10^{-11} 3.3550×10^{-11}	5 5	2.096×10^{-11} 2.092×10^{-11}	3.8599×10^{-3} 3.0950×10^{-3}	0.802
pdb1b4c 1108	ClassicAll QuaternionAll	8 8	$2.6824 \times 10^{-12} \\ 3.4662 \times 10^{-12}$	5 5	$5.067 \times 10^{-13} 5.493 \times 10^{-13}$	1.0100×10^{-2} 7.3092×10^{-3}	0.724
pdb1ba5 320	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.5621 \times 10^{-2} \\ 3.5621 \times 10^{-2} \end{array}$	6 6	$9.363 \times 10^{-13} 1.069 \times 10^{-12}$	$1.2512 \times 10^{-3} 1.0356 \times 10^{-3}$	0.828
pdb1d1n 594	ClassicAll QuaternionAll	2 2	$2.9766 \times 10^{-11} 2.9311 \times 10^{-11}$	1 1	$1.005 \times 10^{-11} 9.672 \times 10^{-12}$	$1.7800 \times 10^{-3} 1.3701 \times 10^{-3}$	0.770
pdb1dp3 332	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.9981 \times 10^{-5} \\ 4.9981 \times 10^{-5} \end{array}$	2 2	7.704×10^{-13} 8.940×10^{-13}	$1.2596 \times 10^{-3} 1.0487 \times 10^{-3}$	0.833
pdb1du1 122	ClassicAll QuaternionAll	8 8	$6.6600 \times 10^{-13} 1.6577 \times 10^{-12}$	1 1	8.225×10^{-13} 1.258×10^{-12}	$4.3915 \times 10^{-4} 3.6638 \times 10^{-4}$	0.834
pdb1eii 806	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.9451 \times 10^{-10} \\ 1.8740 \times 10^{-10} \end{array}$	1 1	$1.393 \times 10^{-11} \\ 1.365 \times 10^{-11}$	$\begin{array}{c} 3.2821 \times 10^{-3} \\ 2.7601 \times 10^{-3} \end{array}$	0.841
pdb1fcl 338	ClassicAll QuaternionAll	8 8	$1.5447 \times 10^{-11} 1.5223 \times 10^{-11}$	2 2	$4.542 \times 10^{-12} 4.515 \times 10^{-12}$	1.3239×10^{-3} 1.1251×10^{-3}	0.850
pdb1fd6 344	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.0242 \times 10^{-5} \\ 2.0242 \times 10^{-5} \end{array}$	2 2	3.182×10^{-12} 3.193×10^{-12}	$1.3557 \times 10^{-3} 1.1437 \times 10^{-3}$	0.844
pdb1i2u 266	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.3842 \times 10^{-3} \\ 1.3842 \times 10^{-3} \end{array}$	$\frac{2}{2}$	$5.562 \times 10^{-13} 5.609 \times 10^{-13}$	$1.0550 \times 10^{-3} 9.0800 \times 10^{-4}$	0.861
pdb1i2v 266	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 8.9125 \times 10^{-13} \\ 8.8206 \times 10^{-13} \end{array}$	5 5	$\begin{array}{c} 2.422 \times 10^{-13} \\ 2.525 \times 10^{-13} \end{array}$	$\begin{array}{c} 1.0442 \times 10^{-3} \\ 8.9061 \times 10^{-4} \end{array}$	0.853
pdb1ijc 380	ClassicAll QuaternionAll	8 8	$9.1858 \times 10^{-11} 9.4110 \times 10^{-11}$	2 2	$1.408 \times 10^{-11} \\ 1.426 \times 10^{-11}$	$1.6215 \times 10^{-3} 1.3517 \times 10^{-3}$	0.834
pdb1jlz 140	ClassicAll QuaternionAll	8 8	$1.2304 \times 10^{-4} 1.2304 \times 10^{-4}$	1 1	$5.594 \times 10^{-13} 5.965 \times 10^{-13}$	$5.2092 \times 10^{-4} 4.4118 \times 10^{-4}$	0.847
pdb1jw3 842	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.9618 \times 10^{-12} \\ 1.8088 \times 10^{-12} \end{array}$	2 2	$5.936 \times 10^{-13} 5.897 \times 10^{-13}$	$\begin{array}{c} 3.4027 \times 10^{-3} \\ 2.8534 \times 10^{-3} \end{array}$	0.839
pdb1k0v 440	ClassicAll QuaternionAll	8 8	8.3940×10^{-5} 8.3940×10^{-5}	2 2	$1.893 \times 10^{-13} 1.894 \times 10^{-13}$	1.8110×10^{-3} 1.5550×10^{-3}	0.859
pdb1k2h 1120	ClassicAll QuaternionAll	8 8	$1.9788 \times 10^{-4} 1.9788 \times 10^{-4}$	$\frac{2}{2}$	5.490×10^{-13} 5.198×10^{-13}	$\begin{array}{c} 1.3499 \times 10^{-2} \\ 8.6254 \times 10^{-3} \end{array}$	0.639
pdb1k36 278	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.6100 \times 10^{-10} \\ 1.8077 \times 10^{-10} \end{array}$	1 1	$8.820 \times 10^{-12} \\ 1.081 \times 10^{-11}$	$\begin{array}{c} 1.0638 \times 10^{-3} \\ 8.9554 \times 10^{-4} \end{array}$	0.842
pdb1k37 278	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.1407 \times 10^{-12} \\ 2.0318 \times 10^{-12} \end{array}$	$\frac{2}{2}$	$4.711 \times 10^{-13} 4.988 \times 10^{-13}$	$\begin{array}{c} 1.0580 \times 10^{-3} \\ 8.9104 \times 10^{-4} \end{array}$	0.842
pdb1kuw 62	ClassicAll QuaternionAll	8 8	$1.8706 \times 10^{-4} 1.8706 \times 10^{-4}$	1 1	9.229×10^{-14} 1.130×10^{-13}	$2.1978 \times 10^{-4} 1.8539 \times 10^{-4}$	0.844
pdb1kz0 98	ClassicAll QuaternionAll	8 8	$6.7512 \times 10^{-13} 6.2568 \times 10^{-13}$	1 1	$4.404 \times 10^{-14} 5.880 \times 10^{-14}$	3.6097×10^{-4} 3.0833×10^{-4}	0.854
pdb1kz2 98	ClassicAll QuaternionAll	8 8	$3.1076 \times 10^{-6} \\ 3.1076 \times 10^{-6}$	1 1	$2.119 \times 10^{-14} 2.886 \times 10^{-14}$	3.6609×10^{-4} 3.1502×10^{-4}	0.861
pdb1kz5 74	ClassicAll QuaternionAll	8 8	4.8094×10^{-13} 5.2716×10^{-13}	1 1	$4.081 \times 10^{-14} 4.738 \times 10^{-14}$	$2.6746 \times 10^{-4} 2.2357 \times 10^{-4}$	0.836
pdb1lvz 68	ClassicAll QuaternionAll	8 8	1.4708×10^{-3} 1.4708×10^{-3}	1 1	$6.336 \times 10^{-14} 7.315 \times 10^{-14}$	$2.4405 \times 10^{-4} 2.0412 \times 10^{-4}$	0.836
pdb1m4e 122	ClassicAll QuaternionAll	8 8	5.4966×10^{-12} 5.5048×10^{-12}	1 1	$5.949 \times 10^{-13} 5.972 \times 10^{-13}$	4.5239×10^{-4} 3.8808×10^{-4}	0.858
pdb1ma2 104	ClassicAll QuaternionAll	8 8	$1.7458 \times 10^{-10} $ 1.7467×10^{-10}	2 2	$8.695 \times 10^{-12} \\ 8.757 \times 10^{-12}$	3.8223×10^{-4} 3.2459×10^{-4}	0.849
pdb1ma4 104	ClassicAll QuaternionAll	8 8	$5.4569 \times 10^{-4} 5.4569 \times 10^{-4}$	2 2	$7.247 \times 10^{-14} \\ 7.977 \times 10^{-14}$	$8.4468 \times 10^{-4} \\ 6.1590 \times 10^{-4}$	0.729

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb1ma5 104	ClassicAll QuaternionAll	8 8	$9.6358 \times 10^{-5} 9.6358 \times 10^{-5}$	1 1	$8.169 \times 10^{-13} 9.044 \times 10^{-13}$	3.8213×10^{-4} 3.2888×10^{-4}	0.861
pdb1ma6 104	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.2440 \times 10^{-11} \\ 1.4288 \times 10^{-11} \end{array}$	2 2	$6.283 \times 10^{-13} \\ 8.487 \times 10^{-13}$	3.8743×10^{-4} 3.2877×10^{-4}	0.849
pdb1mpe 1352	ClassicAll QuaternionAll	8 8	$5.1722 \times 10^{-10} 5.1751 \times 10^{-10}$	2 2	$2.617 \times 10^{-11} 2.624 \times 10^{-11}$	$6.2315 \times 10^{-3} 4.9641 \times 10^{-3}$	0.797
pdb1nd9 296	ClassicAll QuaternionAll	8 8	$1.0508 \times 10^{-12} 8.9082 \times 10^{-13}$	2 2	3.026×10^{-13} 3.845×10^{-13}	1.1832×10^{-3} 1.0109×10^{-3}	0.854
$\begin{array}{c} pdb1ne5 \\ 254 \end{array}$	ClassicAll QuaternionAll	128 128	$1.4845 \times 10^{-11} 1.5105 \times 10^{-11}$	33 33	$1.214 \times 10^{-12} 1.384 \times 10^{-12}$	$1.7300 \times 10^{-2} 1.2553 \times 10^{-2}$	0.726
pdb1nmj 170	ClassicAll QuaternionAll	8 8	$2.3883 \times 10^{-13} 2.3832 \times 10^{-13}$	7 7	1.236×10^{-14} 1.422×10^{-14}	$6.3754 \times 10^{-4} 5.4076 \times 10^{-4}$	0.848
pdb1o53 92	ClassicAll QuaternionAll	8 8	$1.0887 \times 10^{-11} 1.1252 \times 10^{-11}$	2 2	$3.999 \times 10^{-13} 4.527 \times 10^{-13}$	3.3240×10^{-4} 2.8384×10^{-4}	0.854
pdb1oqp 580	ClassicAll QuaternionAll	8 8	$2.9348 \times 10^{-3} 2.9348 \times 10^{-3}$	$\frac{2}{2}$	$7.045 \times 10^{-14} \\ 8.314 \times 10^{-14}$	$1.3065 \times 10^{-2} \\ 8.3320 \times 10^{-3}$	0.638
pdb1plw 32	ClassicAll QuaternionAll	8 8	3.0310×10^{-13} 3.2973×10^{-13}	2 2	$2.830 \times 10^{-14} 3.112 \times 10^{-14}$	$\begin{array}{c} 1.0674 \times 10^{-4} \\ 8.9316 \times 10^{-5} \end{array}$	0.837
$\begin{array}{c} \text{pdb1plx} \\ 32 \end{array}$	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.8525 \times 10^{-4} \\ 2.8525 \times 10^{-4} \end{array}$	1 1	$1.574 \times 10^{-13} 2.060 \times 10^{-13}$	$1.0578 \times 10^{-4} \\ 8.7475 \times 10^{-5}$	0.827
pdb1pv0 278	ClassicAll QuaternionAll	16 16	$1.3024 \times 10^{-11} \\ 1.3017 \times 10^{-11}$	1 1	$2.409 \times 10^{-13} 2.723 \times 10^{-13}$	2.0570×10^{-3} 1.7342×10^{-3}	0.843
pdb1qlk 1108	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.1378 \times 10^{-5} \\ 3.1378 \times 10^{-5} \end{array}$	5 5	$2.634 \times 10^{-13} \\ 2.870 \times 10^{-13}$	$1.7024 \times 10^{-2} 1.1102 \times 10^{-2}$	0.652
pdb1r57 614	ClassicAll QuaternionAll	8 8	$4.3330 \times 10^{-3} 4.3330 \times 10^{-3}$	$\frac{2}{2}$	$\begin{array}{c} 1.847 \times 10^{-13} \\ 2.054 \times 10^{-13} \end{array}$	$\begin{array}{c} 2.4096 \times 10^{-3} \\ 2.0315 \times 10^{-3} \end{array}$	0.843
pdb1ry3 386	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.1924 \times 10^{-12} \\ 9.4285 \times 10^{-12} \end{array}$	2 2	$4.938 \times 10^{-13} \\ 5.913 \times 10^{-13}$	$\begin{array}{c} 1.4750 \times 10^{-3} \\ 1.2437 \times 10^{-3} \end{array}$	0.843
pdb1s4h 80	ClassicAll QuaternionAll	8 8	$1.4643 \times 10^{-4} \\ 1.4643 \times 10^{-4}$	$\frac{2}{2}$	$4.696 \times 10^{-13} \\ 6.351 \times 10^{-13}$	$\begin{array}{c} 2.8387 \times 10^{-4} \\ 2.3661 \times 10^{-4} \end{array}$	0.834
pdb1s4j 80	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 5.8507 \times 10^{-12} \\ 5.8479 \times 10^{-12} \end{array}$	$\frac{2}{2}$	$1.520 \times 10^{-13} 2.083 \times 10^{-13}$	2.9100×10^{-4} 2.4847×10^{-4}	0.854
pdb1s6j 524	ClassicAll QuaternionAll	8 8	$6.0202 \times 10^{-5} \\ 6.0202 \times 10^{-5}$	1 1	$6.073 \times 10^{-13} 7.660 \times 10^{-13}$	$\begin{array}{c} 2.0402 \times 10^{-3} \\ 1.7324 \times 10^{-3} \end{array}$	0.849
pdb1sa8 638	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.7170 \times 10^{-3} \\ 1.7170 \times 10^{-3} \end{array}$	1 1	$9.340 \times 10^{-13} \\ 1.034 \times 10^{-12}$	2.5428×10^{-3} 2.1763×10^{-3}	0.856
pdb1t2y 152	ClassicAll QuaternionAll	8 8	$2.5460 \times 10^{-4} 2.5460 \times 10^{-4}$	1 1	$1.887 \times 10^{-13} 2.396 \times 10^{-13}$	$5.8265 \times 10^{-4} 5.0004 \times 10^{-4}$	0.858
pdb1t5q 180	ClassicAll QuaternionAll	2 2	$1.0265 \times 10^{-12} $ 1.0480×10^{-12}	1 1	3.877×10^{-14} 5.093×10^{-14}	$4.8571 \times 10^{-4} 3.5356 \times 10^{-4}$	0.728
pdb1tot 314	ClassicAll QuaternionAll	8 8	3.4218×10^{-3} 3.4218×10^{-3}	5 5	$6.151 \times 10^{-14} \\ 6.855 \times 10^{-14}$	$1.2434 \times 10^{-3} \\ 1.0616 \times 10^{-3}$	0.854
pdb1v6r 128	ClassicAll QuaternionAll	8 8	1.3650×10^{-4} 1.3650×10^{-4}	2 2	$6.835 \times 10^{-13} 6.971 \times 10^{-13}$	4.6433×10^{-4} 3.9778×10^{-4}	0.857
pdb1v92 278	ClassicAll QuaternionAll	8	3.1327×10^{-5} 3.1327×10^{-5}	1 1	$1.463 \times 10^{-13} \\ 1.630 \times 10^{-13}$	$1.0851 \times 10^{-3} 9.2523 \times 10^{-4}$	0.853
pdb1vd7 140	ClassicAll QuaternionAll	8 8	$7.8801 \times 10^{-12} $ 7.9022×10^{-12}	1 1	$6.342 \times 10^{-13} 7.439 \times 10^{-13}$	$5.1025 \times 10^{-4} 4.2899 \times 10^{-4}$	0.841
pdb1vd9 140	ClassicAll QuaternionAll	8 8	1.5514×10^{-11} 1.5541×10^{-11}	1 1	1.290×10^{-12} 1.554×10^{-12}	5.1829×10^{-4} 4.4015×10^{-4}	0.849
pdb1vdb 140	ClassicAll QuaternionAll	8 8	$8.5740 \times 10^{-12} \\ 8.5291 \times 10^{-12}$	2 2	9.108×10^{-13} 1.082×10^{-12}	5.1249×10^{-4} 4.2939×10^{-4}	0.838
pdb1vpc 272	ClassicAll QuaternionAll	8 8	$4.3482 \times 10^{-4} 4.3482 \times 10^{-4}$	6 6	$8.510 \times 10^{-15} \\ 1.002 \times 10^{-14}$	$1.0684 \times 10^{-3} \\ 8.8942 \times 10^{-4}$	0.832

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb1wnk 140	ClassicAll QuaternionAll	8 8	$2.2292 \times 10^{-10} 2.2177 \times 10^{-10}$	1 1	$4.112 \times 10^{-12} 4.632 \times 10^{-12}$	$5.1993 \times 10^{-4} 4.3235 \times 10^{-4}$	0.832
pdb1wo4 152	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.6193 \times 10^{-5} \\ 4.6193 \times 10^{-5} \end{array}$	2 2	$\begin{array}{c} 9.957 \times 10^{-13} \\ 9.634 \times 10^{-13} \end{array}$	$5.5877 \times 10^{-4} 4.7161 \times 10^{-4}$	0.844
pdb1wo5 152	ClassicAll QuaternionAll	8 8	$2.7147 \times 10^{-10} 2.7625 \times 10^{-10}$	1 1	$2.372 \times 10^{-12} 2.514 \times 10^{-12}$	$5.6296 \times 10^{-4} 4.7630 \times 10^{-4}$	0.846
pdb1x60 476	ClassicAll QuaternionAll	8 8	$6.7449 \times 10^{-12} 6.9447 \times 10^{-12}$	1 1	$1.076 \times 10^{-12} 1.179 \times 10^{-12}$	$1.8824 \times 10^{-3} 1.6151 \times 10^{-3}$	0.858
pdb1y5c 68	ClassicAll QuaternionAll	8 8	$8.7435 \times 10^{-13} \\ 8.2242 \times 10^{-13}$	1 1	$7.693 \times 10^{-14} 9.383 \times 10^{-14}$	$2.3392 \times 10^{-4} 1.9470 \times 10^{-4}$	0.832
pdb1yx7 500	ClassicAll QuaternionAll	8 8	$1.3647 \times 10^{-10} 1.4245 \times 10^{-10}$	5 5	3.509×10^{-12} 4.348×10^{-12}	$1.9625 \times 10^{-3} 1.6712 \times 10^{-3}$	0.852
pdb1yx8 500	ClassicAll QuaternionAll	8 8	$2.5841 \times 10^{-10} 2.6921 \times 10^{-10}$	6 6	$7.284 \times 10^{-12} \\ 8.217 \times 10^{-12}$	2.1905×10^{-3} 1.8202×10^{-3}	0.831
$\begin{array}{c} pdb1yxr\\ 464\end{array}$	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.3459 \times 10^{-4} \\ 9.3459 \times 10^{-4} \end{array}$	1 1	$6.979 \times 10^{-13} 7.989 \times 10^{-13}$	$1.7944 \times 10^{-3} 1.5091 \times 10^{-3}$	0.841
pdb2a4j 580	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.0516 \times 10^{-4} \\ 1.0516 \times 10^{-4} \end{array}$	$\frac{2}{2}$	$2.085 \times 10^{-14} \\ 2.727 \times 10^{-14}$	2.5605×10^{-3} 2.0942×10^{-3}	0.818
pdb2adn 868	ClassicAll QuaternionAll	8 8	2.3364×10^{-10} 2.3188×10^{-10}	1 1	$6.693 \times 10^{-12} 6.465 \times 10^{-12}$	5.5305×10^{-3} 4.1888×10^{-3}	0.757
pdb2ajj 170	ClassicAll QuaternionAll	8 8	$2.9810 \times 10^{-4} $ 2.9810×10^{-4}	1 1	$5.641 \times 10^{-14} \\ 6.584 \times 10^{-14}$	$6.2947 \times 10^{-4} 5.2547 \times 10^{-4}$	0.835
pdb2ajm 170	ClassicAll QuaternionAll	8 8	$2.4063 \times 10^{-12} \\ 2.7001 \times 10^{-12}$	2 2	1.183×10^{-13} 1.555×10^{-13}	6.3281×10^{-4} 5.3606×10^{-4}	0.847
pdb2ajn 170	ClassicAll QuaternionAll	8	4.3268×10^{-4} 4.3268×10^{-4}	1 1	$1.076 \times 10^{-13} \\ 1.217 \times 10^{-13}$	$6.2547 \times 10^{-4} 5.2149 \times 10^{-4}$	0.834
pdb2ajo 170	ClassicAll QuaternionAll	8 8	$2.4063 \times 10^{-12} \\ 2.7001 \times 10^{-12}$	2 2	1.183×10^{-13} 1.555×10^{-13}	$6.3214 \times 10^{-4} 5.3750 \times 10^{-4}$	0.850
pdb2akk 446	ClassicAll QuaternionAll	8 8	3.0416×10^{-3} 3.0416×10^{-3}	2 2	$1.289 \times 10^{-13} 1.279 \times 10^{-13}$	1.7725×10^{-3} 1.5298×10^{-3}	0.863
pdb2bzb 748	ClassicAll QuaternionAll	8 8	$4.6498 \times 10^{-13} \\ 6.0113 \times 10^{-13}$	5 5	$9.361 \times 10^{-14} \\ 1.224 \times 10^{-13}$	2.0879×10^{-2} 1.3608×10^{-2}	0.652
pdb2c0s 386	ClassicAll QuaternionAll	8	$1.0793 \times 10^{-2} \\ 1.0793 \times 10^{-2}$	6 6	3.028×10^{-13} 3.380×10^{-13}	1.5209×10^{-3} 1.2500×10^{-3}	0.822
pdb2dci 120	ClassicAll QuaternionAll	2 2	2.0907×10^{-13} 3.3732×10^{-13}	1 1	$2.366 \times 10^{-14} $ 2.950×10^{-14}	3.3281×10^{-4} 2.4895×10^{-4}	0.748
pdb2eem 206	ClassicAll QuaternionAll	8 8	$9.5324 \times 10^{-12} $ 9.5866×10^{-12}	1 1	5.190×10^{-13} 5.461×10^{-13}	$7.7216 \times 10^{-4} $ 6.5367×10^{-4}	0.847
pdb2fva 494	ClassicAll QuaternionAll	8 8	1.2680×10^{-11} 1.2689×10^{-11}	2 2	$1.047 \times 10^{-12} \\ 1.195 \times 10^{-12}$	1.9189×10^{-3} 1.6080×10^{-3}	0.838
pdb2fvf 494	ClassicAll QuaternionAll	8 8	3.5796×10^{-12} 3.3286×10^{-12}	1 1	3.106×10^{-13} 3.445×10^{-13}	1.9126×10^{-3} 1.6204×10^{-3}	0.847
pdb2fxz 80	ClassicAll QuaternionAll	8	4.2293×10^{-12} 5.3169×10^{-12}	1 1	$1.489 \times 10^{-12} \\ 1.749 \times 10^{-12}$	2.9810×10^{-4} 2.5266×10^{-4}	0.848
pdb2g9l 224	ClassicAll QuaternionAll	8	$1.0333 \times 10^{-4} \\ 1.0333 \times 10^{-4}$	2 2	$6.365 \times 10^{-14} \\ 8.666 \times 10^{-14}$	8.4774×10^{-4} 7.2563×10^{-4}	0.856
pdb2h5m 614	ClassicAll QuaternionAll	8 8	1.2267×10^{-3} 1.2267×10^{-3}	1 1	9.692×10^{-13} 1.032×10^{-12}	2.4098×10^{-3} 2.0340×10^{-3}	0.844
pdb2hep 252	ClassicAll QuaternionAll	2 2	2.1758×10^{-11} 2.2038×10^{-11}	1 1	1.191×10^{-12} 1.268×10^{-12}	$6.9652 \times 10^{-4} 5.1109 \times 10^{-4}$	0.734
pdb2jmy 92	ClassicAll QuaternionAll	8 8	7.0432×10^{-5} 7.0432×10^{-5}	1 1	9.834×10^{-13} 9.967×10^{-13}	3.4485×10^{-4} 2.9309×10^{-4}	0.850
pdb2jn5 74	ClassicAll QuaternionAll	8 8	$6.6339 \times 10^{-12} 2.0459 \times 10^{-11}$	1 1	1.104×10^{-11} 2.456×10^{-11}	$2.5907 \times 10^{-4} 2.1594 \times 10^{-4}$	0.834
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Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2jnk 842	ClassicAll QuaternionAll	8 8	3.4995×10^{-11} 3.4653×10^{-11}	1 1	$2.246 \times 10^{-12} 2.319 \times 10^{-12}$	3.4046×10^{-3} 2.8579×10^{-3}	0.839
pdb2jpn 476	ClassicAll QuaternionAll	8 8	$6.4192 \times 10^{-12} 6.5904 \times 10^{-12}$	2 2	$6.730 \times 10^{-14} 6.984 \times 10^{-14}$	$\begin{array}{c} 2.3805 \times 10^{-3} \\ 1.9077 \times 10^{-3} \end{array}$	0.801
pdb2jua 614	ClassicAll QuaternionAll	8 8	$1.8734 \times 10^{-4} 1.8734 \times 10^{-4}$	2 2	$1.740 \times 10^{-11} \\ 1.882 \times 10^{-11}$	$2.4657 \times 10^{-3} 2.0362 \times 10^{-3}$	0.826
pdb2jvd 288	ClassicAll QuaternionAll	2 2	$9.4244 \times 10^{-13} 9.4967 \times 10^{-13}$	1 1	3.339×10^{-14} 3.898×10^{-14}	$8.0214 \times 10^{-4} 5.8665 \times 10^{-4}$	0.731
pdb2jwe 984	ClassicAll QuaternionAll	$\frac{2}{2}$	$\begin{array}{c} 9.2597 \times 10^{-11} \\ 9.2052 \times 10^{-11} \end{array}$	1 1	$2.695 \times 10^{-11} 2.734 \times 10^{-11}$	$2.9579 \times 10^{-3} 2.2597 \times 10^{-3}$	0.764
pdb2jws 338	ClassicAll QuaternionAll	8 8	$4.5612 \times 10^{-4} 4.5612 \times 10^{-4}$	$\frac{2}{2}$	$1.251 \times 10^{-13} 1.543 \times 10^{-13}$	$\begin{array}{c} 1.3479 \times 10^{-3} \\ 1.1246 \times 10^{-3} \end{array}$	0.834
pdb2jwu 338	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.0876 \times 10^{-4} \\ 3.0876 \times 10^{-4} \end{array}$	1 1	$4.421 \times 10^{-12} 4.373 \times 10^{-12}$	$\begin{array}{c} 1.3171 \times 10^{-3} \\ 1.1127 \times 10^{-3} \end{array}$	0.845
pdb2jxf 182	ClassicAll QuaternionAll	8 8	$2.4000 \times 10^{-4} 2.4000 \times 10^{-4}$	1 1	$1.399 \times 10^{-13} 1.734 \times 10^{-13}$	$6.6977 \times 10^{-4} 5.5569 \times 10^{-4}$	0.830
pdb2jz5 548	ClassicAll QuaternionAll	8	$1.7460 \times 10^{-3} 1.7460 \times 10^{-3}$	1 1	2.860×10^{-13} 2.854×10^{-13}	$2.1161 \times 10^{-3} 1.7755 \times 10^{-3}$	0.839
pdb2k2a 422	ClassicAll QuaternionAll	8 8	$4.7195 \times 10^{-3} 4.7195 \times 10^{-3}$	5 5	3.810×10^{-14} 5.148×10^{-14}	$1.6369 \times 10^{-3} 1.3742 \times 10^{-3}$	0.839
pdb2k36 896	ClassicAll QuaternionAll	8 8	$1.6972 \times 10^{-12} 1.6007 \times 10^{-12}$	1 1	$1.922 \times 10^{-13} 2.045 \times 10^{-13}$	3.5800×10^{-3} 2.9607×10^{-3}	0.827
pdb2k37 356	ClassicAll QuaternionAll	8 8	3.7147×10^{-12} 3.6185×10^{-12}	1 1	$1.921 \times 10^{-13} 2.525 \times 10^{-13}$	$1.3935 \times 10^{-3} \\ 1.1781 \times 10^{-3}$	0.845
pdb2k3i 656	ClassicAll QuaternionAll	8 8	$4.6225 \times 10^{-3} 4.6225 \times 10^{-3}$	2 2	3.810×10^{-13} 4.009×10^{-13}	3.1944×10^{-3} 2.5603×10^{-3}	0.801
pdb2k6s 494	ClassicAll QuaternionAll	8	8.2998×10^{-12} 8.4519×10^{-12}	2 2	$2.100 \times 10^{-13} $ 2.651×10^{-13}	3.7623×10^{-3} 2.8028×10^{-3}	0.745
pdb2k7o 1096	ClassicAll QuaternionAll	8 8	1.8663×10^{-4} 1.8663×10^{-4}	1 1	$1.279 \times 10^{-13} \\ 1.416 \times 10^{-13}$	$2.4604 \times 10^{-2} \\ 1.6224 \times 10^{-2}$	0.659
pdb2kdh 434	ClassicAll QuaternionAll	8 8	$7.2209 \times 10^{-5} 7.2209 \times 10^{-5}$	2 2	$1.947 \times 10^{-11} \\ 2.228 \times 10^{-11}$	1.7165×10^{-3} 1.4424×10^{-3}	0.840
pdb2kdl 338	ClassicAll QuaternionAll	8 8	4.4591×10^{-12} 4.4513×10^{-12}	2 2	$2.301 \times 10^{-13} \\ 2.919 \times 10^{-13}$	1.2929×10^{-3} 1.0822×10^{-3}	0.837
pdb2kdm 338	ClassicAll QuaternionAll	8	2.1896×10^{-11} 2.1643×10^{-11}	1 1	3.191×10^{-12} 3.284×10^{-12}	1.3285×10^{-3} 1.1203×10^{-3}	0.843
pdb2kdp 428	ClassicAll QuaternionAll	8	$3.0283 \times 10^{-12} \\ 3.0741 \times 10^{-12}$	1 1	$2.621 \times 10^{-13} 2.865 \times 10^{-13}$	1.6703×10^{-3} 1.4010×10^{-3}	0.839
pdb2kdr 170	ClassicAll QuaternionAll	8 8	$6.3024 \times 10^{-5} \\ 6.3024 \times 10^{-5}$	2 2	$6.618 \times 10^{-14} \\ 8.490 \times 10^{-14}$	$6.2375 \times 10^{-4} 5.1064 \times 10^{-4}$	0.819
pdb2kes 290	ClassicAll QuaternionAll	8 8	1.8528×10^{-4} 1.8528×10^{-4}	7 7	$4.467 \times 10^{-14} \\ 5.425 \times 10^{-14}$	1.0859×10^{-3} 8.9171×10^{-4}	0.821
pdb2kib 352	ClassicAll QuaternionAll	8	2.9706×10^{-5} 2.9706×10^{-5}	1 1	$2.533 \times 10^{-12} \\ 2.539 \times 10^{-12}$	1.6764×10^{-2} 1.0720×10^{-2}	0.639
pdb2kjn 158	ClassicAll QuaternionAll	8 8	1.9764×10^{-12} 1.9265×10^{-12}	2 2	$9.827 \times 10^{-14} \\ 1.174 \times 10^{-13}$	5.8117×10^{-4} 4.8764×10^{-4}	0.839
pdb2kjo 158	ClassicAll QuaternionAll	8 8	1.2876×10^{-11} 1.2921×10^{-11}	1 1	2.284×10^{-13} 2.421×10^{-13}	5.8129×10^{-4} 4.8652×10^{-4}	0.837
pdb2kjr 572	ClassicAll QuaternionAll	8 8	5.1341×10^{-11} 5.1082×10^{-11}	2 2	3.247×10^{-12} 3.252×10^{-12}	2.2125×10^{-3} 1.8689×10^{-3}	0.845
pdb2kko 1300	ClassicAll QuaternionAll	8 8	6.9643×10^{-4} 6.9643×10^{-4}	2 2	$ \begin{array}{c} 1.191 \times 10^{-13} \\ 1.284 \times 10^{-13} \end{array} $	2.7542×10^{-2} 1.8252×10^{-2}	0.663
pdb2kl5 662	ClassicAll QuaternionAll	8 8	$2.4505 \times 10^{-12} $ 2.5206×10^{-12}	1 1	1.820×10^{-13} 2.020×10^{-13}	2.5879×10^{-3} 2.1747×10^{-3}	0.840
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Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2klz 276	ClassicAll QuaternionAll	2 2	3.9786×10^{-13} 3.7834×10^{-13}	1 1	3.439×10^{-14} 4.443×10^{-14}	$7.7529 \times 10^{-4} 5.6489 \times 10^{-4}$	0.729
pdb2koz 200	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.7204 \times 10^{-5} \\ 4.7204 \times 10^{-5} \end{array}$	2 2	$\begin{array}{c} 1.067 \times 10^{-12} \\ 1.151 \times 10^{-12} \end{array}$	$7.6838 \times 10^{-4} \\ 6.5712 \times 10^{-4}$	0.855
$\begin{array}{c} \mathrm{pdb2kp0} \\ 200 \end{array}$	ClassicAll QuaternionAll	8 8	$7.8392 \times 10^{-11} \\ 8.2404 \times 10^{-11}$	2 2	$4.894 \times 10^{-12} 5.595 \times 10^{-12}$	$7.5225 \times 10^{-4} 6.3851 \times 10^{-4}$	0.849
$\begin{array}{c} \rm pdb2ksg\\ 290\end{array}$	ClassicAll QuaternionAll	8 8	$9.2027 \times 10^{-13} 9.2208 \times 10^{-13}$	1 1	$3.215 \times 10^{-14} 3.967 \times 10^{-14}$	$1.1068 \times 10^{-3} 9.3448 \times 10^{-4}$	0.844
pdb2kt8 458	ClassicAll QuaternionAll	8 8	$4.1573 \times 10^{-4} 4.1573 \times 10^{-4}$	1 1	$3.314 \times 10^{-12} 3.535 \times 10^{-12}$	$1.7671 \times 10^{-3} 1.5006 \times 10^{-3}$	0.849
pdb2kuh 404	ClassicAll QuaternionAll	8 8	1.1667×10^{-3} 1.1667×10^{-3}	6 6	$2.015 \times 10^{-14} 2.491 \times 10^{-14}$	1.5882×10^{-3} 1.3470×10^{-3}	0.848
pdb2kwh 338	ClassicAll QuaternionAll	8 8	$2.0587 \times 10^{-3} 2.0587 \times 10^{-3}$	2 2	1.408×10^{-13} 1.825×10^{-13}	1.2962×10^{-3} 1.0811×10^{-3}	0.834
pdb2kxa 144	ClassicAll QuaternionAll	2 2	$3.9712 \times 10^{-12} 3.7392 \times 10^{-12}$	1 1	$1.325 \times 10^{-12} 1.351 \times 10^{-12}$	$4.0854 \times 10^{-4} 3.1275 \times 10^{-4}$	0.766
$pdb2kyb\\362$	ClassicAll QuaternionAll	8 8	$3.1200 \times 10^{-6} 3.1200 \times 10^{-6}$	2 2	$1.321 \times 10^{-11} \\ 1.373 \times 10^{-11}$	1.8390×10^{-3} 1.4801×10^{-3}	0.805
pdb2l3m 428	ClassicAll QuaternionAll	8 8	$1.5178 \times 10^{-3} 1.5178 \times 10^{-3}$	1 1	$1.028 \times 10^{-12} 9.340 \times 10^{-13}$	1.6830×10^{-3} 1.4266×10^{-3}	0.848
pdb2l3n 626	ClassicAll QuaternionAll	8 8	3.9987×10^{-4} 3.9987×10^{-4}	5 5	3.024×10^{-14} 3.632×10^{-14}	8.4304×10^{-3} 6.0881×10^{-3}	0.722
pdb2l45 116	ClassicAll QuaternionAll	8 8	$5.9466 \times 10^{-13} 6.7808 \times 10^{-13}$	1 1	$2.236 \times 10^{-14} 3.033 \times 10^{-14}$	$\begin{array}{c} 4.3100 \times 10^{-4} \\ 3.6853 \times 10^{-4} \end{array}$	0.855
pdb2l5r 138	ClassicAll QuaternionAll	$\frac{2}{2}$	$\begin{array}{c} 3.0491 \times 10^{-13} \\ 3.0031 \times 10^{-13} \end{array}$	$\frac{2}{2}$	3.535×10^{-14} 4.436×10^{-14}	3.7258×10^{-4} 2.7236×10^{-4}	0.731
pdb2l6q 374	ClassicAll QuaternionAll	4 4	$1.6115 \times 10^{-9} 1.6752 \times 10^{-9}$	1 1	$4.435 \times 10^{-11} 5.413 \times 10^{-11}$	$\begin{array}{c} 1.0503 \times 10^{-3} \\ 8.3213 \times 10^{-4} \end{array}$	0.792
pdb2l6r 374	ClassicAll QuaternionAll	8 8	$1.0970 \times 10^{-10} 9.8250 \times 10^{-11}$	2 2	$2.060 \times 10^{-12} \\ 2.174 \times 10^{-12}$	$1.4580 \times 10^{-3} 1.2105 \times 10^{-3}$	0.830
pdb2l98 434	ClassicAll QuaternionAll	8 8	$5.6413 \times 10^{-12} 6.2089 \times 10^{-12}$	$\frac{2}{2}$	3.273×10^{-13} 3.637×10^{-13}	$1.6730 \times 10^{-3} 1.4197 \times 10^{-3}$	0.849
pdb2lci 806	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.2015 \times 10^{-12} \\ 1.1830 \times 10^{-12} \end{array}$	1 1	$\begin{array}{c} 2.579 \times 10^{-13} \\ 2.404 \times 10^{-13} \end{array}$	$\begin{array}{c} 3.1674 \times 10^{-3} \\ 2.6221 \times 10^{-3} \end{array}$	0.828
pdb2lde 152	ClassicAll QuaternionAll	8 8	$6.0406 \times 10^{-3} 6.0406 \times 10^{-3}$	2 2	3.154×10^{-14} 3.766×10^{-14}	$5.5670 \times 10^{-4} 4.6551 \times 10^{-4}$	0.836
pdb2le7 122	ClassicAll QuaternionAll	8 8	8.8940×10^{-14} 1.1008×10^{-13}	2 2	$2.111 \times 10^{-14} 2.749 \times 10^{-14}$	$\begin{array}{c} 4.4383 \times 10^{-4} \\ 3.7371 \times 10^{-4} \end{array}$	0.842
pdb2ler 68	ClassicAll QuaternionAll	8 8	$5.1096 \times 10^{-14} 6.2001 \times 10^{-14}$	$\frac{2}{2}$	$1.314 \times 10^{-14} 1.532 \times 10^{-14}$	2.3841×10^{-4} 1.9906×10^{-4}	0.835
pdb2lgi 338	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.7255 \times 10^{-12} \\ 9.6518 \times 10^{-12} \end{array}$	$\frac{2}{2}$	$\begin{array}{c} 1.068 \times 10^{-12} \\ 1.052 \times 10^{-12} \end{array}$	$\begin{array}{c} 1.3304 \times 10^{-3} \\ 1.1234 \times 10^{-3} \end{array}$	0.844
pdb2lhc 338	ClassicAll QuaternionAll	8 8	3.8367×10^{-10} 3.8166×10^{-10}	1 1	$\begin{array}{c} 2.902 \times 10^{-12} \\ 2.997 \times 10^{-12} \end{array}$	$\begin{array}{c} 1.3470 \times 10^{-3} \\ 1.1146 \times 10^{-3} \end{array}$	0.828
pdb2lhd 338	ClassicAll QuaternionAll	8 8	$1.3048 \times 10^{-11} \\ 1.4592 \times 10^{-11}$	$\frac{2}{2}$	$1.930 \times 10^{-12} 2.033 \times 10^{-12}$	$\begin{array}{c} 1.3235 \times 10^{-3} \\ 1.1166 \times 10^{-3} \end{array}$	0.844
pdb2lhe 338	ClassicAll QuaternionAll	8 8	9.7862×10^{-10} 9.7867×10^{-10}	2 2	$4.963 \times 10^{-11} 4.967 \times 10^{-11}$	$1.4461 \times 10^{-3} \\ 1.1977 \times 10^{-3}$	0.828
pdb2lhg 338	ClassicAll QuaternionAll	8 8	5.0995×10^{-13} 5.4683×10^{-13}	6 6	$6.485 \times 10^{-14} 7.343 \times 10^{-14}$	1.3270×10^{-3} 1.1193×10^{-3}	0.843
pdb2lix 162	ClassicAll QuaternionAll	2 2	4.9988×10^{-13} 5.1517×10^{-13}	1 1	$4.842 \times 10^{-14} \\ 5.614 \times 10^{-14}$	$4.4755 \times 10^{-4} 3.4473 \times 10^{-4}$	0.770
pdb2lld 242	ClassicAll QuaternionAll	8 8	$3.3972 \times 10^{-3} 3.3972 \times 10^{-3}$	5 5	$1.938 \times 10^{-13} \\ 2.216 \times 10^{-13}$	$9.3708 \times 10^{-4} 7.9797 \times 10^{-4}$	0.852

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2lm9 578	ClassicAll QuaternionAll	8	2.2967×10^{-3} 2.2967×10^{-3}	2 2	$6.254 \times 10^{-14} 7.713 \times 10^{-14}$	2.2302×10^{-3} 1.8521×10^{-3}	0.830
pdb2lmf 140	ClassicAll QuaternionAll	8 8	$1.0942 \times 10^{-4} \\ 1.0942 \times 10^{-4}$	1 1	$1.282 \times 10^{-13} \\ 1.462 \times 10^{-13}$	$5.1406 \times 10^{-4} 4.2642 \times 10^{-4}$	0.829
pdb2ln3 500	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.5821 \times 10^{-13} \\ 2.9987 \times 10^{-13} \end{array}$	1 1	$1.292 \times 10^{-13} 1.359 \times 10^{-13}$	$\begin{array}{c} 1.9425 \times 10^{-3} \\ 1.6517 \times 10^{-3} \end{array}$	0.850
pdb2lo2 230	ClassicAll QuaternionAll	8 8	$1.4423 \times 10^{-2} \\ 1.4423 \times 10^{-2}$	2 2	$2.068 \times 10^{-14} 2.571 \times 10^{-14}$	8.7008×10^{-4} 7.3340×10^{-4}	0.843
$\begin{array}{c} pdb2lqp\\ 428\end{array}$	ClassicAll QuaternionAll	8 8	$5.7815 \times 10^{-4} 5.7815 \times 10^{-4}$	$\frac{2}{2}$	2.950×10^{-13} 3.085×10^{-13}	$1.6621 \times 10^{-3} 1.3941 \times 10^{-3}$	0.839
pdb2lr0 806	ClassicAll QuaternionAll	8 8	1.2202×10^{-11} 1.1747×10^{-11}	1 1	3.549×10^{-12} 3.440×10^{-12}	3.1919×10^{-3} 2.6561×10^{-3}	0.832
pdb2lrh 806	ClassicAll QuaternionAll	8 8	$2.9721 \times 10^{-12} 2.9099 \times 10^{-12}$	1 1	$5.631 \times 10^{-13} 6.564 \times 10^{-13}$	$3.1614 \times 10^{-3} 2.5993 \times 10^{-3}$	0.822
pdb2ls9 152	ClassicAll QuaternionAll	8 8	$2.7045 \times 10^{-12} 3.0425 \times 10^{-12}$	1 1	$1.122 \times 10^{-13} \\ 1.471 \times 10^{-13}$	$5.6596 \times 10^{-4} 4.7795 \times 10^{-4}$	0.844
pdb2lsa 140	ClassicAll QuaternionAll	8 8	$2.5535 \times 10^{-3} 2.5535 \times 10^{-3}$	2 2	$5.235 \times 10^{-14} 6.998 \times 10^{-14}$	$5.3541 \times 10^{-4} 4.5340 \times 10^{-4}$	0.847
pdb2lss 422	ClassicAll QuaternionAll	8 8	$1.2372 \times 10^{-3} 1.2372 \times 10^{-3}$	1 1	$1.230 \times 10^{-13} 1.455 \times 10^{-13}$	$1.6857 \times 10^{-3} 1.4477 \times 10^{-3}$	0.859
pdb2lt3 680	ClassicAll QuaternionAll	8 8	$9.6961 \times 10^{-13} 1.0253 \times 10^{-12}$	6 6	$7.245 \times 10^{-14} 7.760 \times 10^{-14}$	$2.6784 \times 10^{-3} 2.2363 \times 10^{-3}$	0.835
pdb2lu6 86	ClassicAll QuaternionAll	8 8	$7.7550 \times 10^{-3} 7.7550 \times 10^{-3}$	1 1	$5.356 \times 10^{-15} 6.922 \times 10^{-15}$	$\begin{array}{c} 2.9827 \times 10^{-4} \\ 2.4725 \times 10^{-4} \end{array}$	0.829
pdb2lx0 194	ClassicAll QuaternionAll	8 8	$7.4851 \times 10^{-12} 7.5304 \times 10^{-12}$	1 1	$3.569 \times 10^{-13} 4.035 \times 10^{-13}$	$7.4119 \times 10^{-4} 6.2838 \times 10^{-4}$	0.848
pdb2lxb 892	ClassicAll QuaternionAll	8 8	$9.0172 \times 10^{-13} 8.6577 \times 10^{-13}$	1 1	$1.542 \times 10^{-13} 1.585 \times 10^{-13}$	$7.5665 \times 10^{-3} $ 5.5068×10^{-3}	0.728
pdb2lxy 404	ClassicAll QuaternionAll	8 8	$1.1155 \times 10^{-10} 1.1215 \times 10^{-10}$	2 2	$9.313 \times 10^{-13} 1.025 \times 10^{-12}$	$1.5476 \times 10^{-3} 1.2882 \times 10^{-3}$	0.832
pdb2lxz 194	ClassicAll QuaternionAll	8 8	$1.1003 \times 10^{-4} 1.1003 \times 10^{-4}$	2 2	$2.371 \times 10^{-12} 2.792 \times 10^{-12}$	$7.3806 \times 10^{-4} $ 6.2722×10^{-4}	0.850
pdb2m1a 158	ClassicAll QuaternionAll	8 8	$9.1771 \times 10^{-14} 9.0451 \times 10^{-14}$	1 1	$6.346 \times 10^{-15} 7.612 \times 10^{-15}$	$5.8736 \times 10^{-4} 4.9317 \times 10^{-4}$	0.840
pdb2m1j 182	ClassicAll QuaternionAll	8 8	1.5890×10^{-13} 1.6894×10^{-13}	2 2	$1.865 \times 10^{-14} 2.212 \times 10^{-14}$	6.9896×10^{-4} 5.8122×10^{-4}	0.832
pdb2m2y 110	ClassicAll QuaternionAll	8 8	1.8177×10^{-3} 1.8177×10^{-3}	1 1	$2.699 \times 10^{-13} 2.808 \times 10^{-13}$	$4.0431 \times 10^{-4} 3.4517 \times 10^{-4}$	0.854
pdb2m3f 134	ClassicAll QuaternionAll	8	$9.5240 \times 10^{-14} \\ 5.7597 \times 10^{-14}$	1 1	$3.629 \times 10^{-14} 4.641 \times 10^{-14}$	$4.9469 \times 10^{-4} 4.1447 \times 10^{-4}$	0.838
pdb2m8m 170	ClassicAll QuaternionAll	8	$6.9769 \times 10^{-3} 6.9769 \times 10^{-3}$	5 5	$2.424 \times 10^{-14} 3.058 \times 10^{-14}$	$6.2808 \times 10^{-4} 5.2328 \times 10^{-4}$	0.833
pdb2m8o 170	ClassicAll QuaternionAll	8	$4.7097 \times 10^{-3} $ 4.7097×10^{-3}	5 5	$1.798 \times 10^{-14} 2.301 \times 10^{-14}$	$6.2951 \times 10^{-4} 5.2768 \times 10^{-4}$	0.838
pdb2m97 416	ClassicAll QuaternionAll	8	$2.4560 \times 10^{-12} 2.4592 \times 10^{-12}$	6 6	$4.654 \times 10^{-14} \\ 5.847 \times 10^{-14}$	$1.6020 \times 10^{-3} 1.3398 \times 10^{-3}$	0.836
pdb2m9g 1108	ClassicAll QuaternionAll	8	$4.9692 \times 10^{-12} $ 4.9567×10^{-12}	1 1	$2.939 \times 10^{-13} \\ 3.170 \times 10^{-13}$	$4.5639 \times 10^{-3} \\ 3.7324 \times 10^{-3}$	0.818
pdb2m9r 242	ClassicAll QuaternionAll	8	$3.7505 \times 10^{-12} 3.6480 \times 10^{-12}$	1 1	$3.537 \times 10^{-14} 4.406 \times 10^{-14}$	$8.6573 \times 10^{-4} $ 6.9560×10^{-4}	0.803
pdb2mdv 460	ClassicAll QuaternionAll	8	$4.7210 \times 10^{-4} 4.7210 \times 10^{-4}$	2 2	$3.178 \times 10^{-12} \\ 3.178 \times 10^{-12}$	$1.8237 \times 10^{-3} 1.5843 \times 10^{-3}$	0.869
pdb2me1 164	ClassicAll QuaternionAll	8 8	$1.4934 \times 10^{-4} 1.4934 \times 10^{-4}$	2 2	$1.886 \times 10^{-13} 2.202 \times 10^{-13}$	$6.0675 \times 10^{-4} 5.0964 \times 10^{-4}$	0.840

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2me2 164	ClassicAll QuaternionAll	8 8	$1.3863 \times 10^{-4} \\ 1.3863 \times 10^{-4}$	1 1	3.667×10^{-13} 5.098×10^{-13}	$6.3154 \times 10^{-4} 5.2472 \times 10^{-4}$	0.831
pdb2me3 164	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.4823 \times 10^{-5} \\ 3.4823 \times 10^{-5} \end{array}$	2 2	1.425×10^{-13} 1.590×10^{-13}	$6.0510 \times 10^{-4} 5.0923 \times 10^{-4}$	0.842
pdb2me4 164	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.9945 \times 10^{-5} \\ 2.9945 \times 10^{-5} \end{array}$	2 2	$5.547 \times 10^{-13} \\ 6.221 \times 10^{-13}$	$6.3064 \times 10^{-4} 5.2613 \times 10^{-4}$	0.834
pdb2mg1 164	ClassicAll QuaternionAll	8 8	4.4954×10^{-13} 5.4976×10^{-13}	6 6	$4.400 \times 10^{-14} 5.374 \times 10^{-14}$	$6.0826 \times 10^{-4} 5.0481 \times 10^{-4}$	0.830
pdb2mg2 170	ClassicAll QuaternionAll	8 8	$1.0745 \times 10^{-3} 1.0745 \times 10^{-3}$	6 6	$1.831 \times 10^{-14} 2.481 \times 10^{-14}$	$6.2908 \times 10^{-4} 5.2727 \times 10^{-4}$	0.838
pdb2mg3 170	ClassicAll QuaternionAll	8 8	$6.2977 \times 10^{-13} 6.7812 \times 10^{-13}$	6 6	$3.542 \times 10^{-14} 4.459 \times 10^{-14}$	$6.3373 \times 10^{-4} 5.3292 \times 10^{-4}$	0.841
pdb2mh8 338	ClassicAll QuaternionAll	8 8	$4.2246 \times 10^{-12} 4.0208 \times 10^{-12}$	6 6	$1.547 \times 10^{-13} 1.883 \times 10^{-13}$	1.3028×10^{-3} 1.0945×10^{-3}	0.840
pdb2mhw 164	ClassicAll QuaternionAll	8 8	3.6932×10^{-3} 3.6932×10^{-3}	2 2	$6.229 \times 10^{-14} 7.130 \times 10^{-14}$	$6.2718 \times 10^{-4} 5.4278 \times 10^{-4}$	0.865
pdb2mi1 84	ClassicAll QuaternionAll	4	$2.1485 \times 10^{-11} 2.2963 \times 10^{-11}$	4 4	$1.828 \times 10^{-12} 2.053 \times 10^{-12}$	$4.1151 \times 10^{-4} 3.1129 \times 10^{-4}$	0.756
pdb2mi7 404	ClassicAll QuaternionAll	8 8	$8.0637 \times 10^{-12} 8.8714 \times 10^{-12}$	2 2	6.022×10^{-13} 6.815×10^{-13}	1.5388×10^{-3} 1.2825×10^{-3}	0.833
pdb2mij 224	ClassicAll QuaternionAll	8 8	$1.2077 \times 10^{-12} 1.2294 \times 10^{-12}$	1 1	1.244×10^{-13} 1.522×10^{-13}	8.4790×10^{-4} 7.1736×10^{-4}	0.846
pdb2mix 128	ClassicAll QuaternionAll	8 8	3.7545×10^{-13} 3.4098×10^{-13}	1 1	$4.816 \times 10^{-14} 4.684 \times 10^{-14}$	$\begin{array}{c} 4.8126 \times 10^{-4} \\ 4.1297 \times 10^{-4} \end{array}$	0.858
pdb2mj1 110	ClassicAll QuaternionAll	8 8	$2.0809 \times 10^{-3} 2.0809 \times 10^{-3}$	1 1	$1.309 \times 10^{-13} 1.646 \times 10^{-13}$	$\begin{array}{c} 4.0562 \times 10^{-4} \\ 3.4807 \times 10^{-4} \end{array}$	0.858
pdb2mj2 218	ClassicAll QuaternionAll	8 8	$3.9018 \times 10^{-3} 3.9018 \times 10^{-3}$	2 2	9.775×10^{-14} 1.192×10^{-13}	$7.9935 \times 10^{-4} 6.6638 \times 10^{-4}$	0.834
pdb2mjg 556	ClassicAll QuaternionAll	8 8	$1.4497 \times 10^{-3} 1.4497 \times 10^{-3}$	2 2	$5.503 \times 10^{-14} 6.579 \times 10^{-14}$	9.8496×10^{-3} 6.9305×10^{-3}	0.704
pdb2mji 788	ClassicAll QuaternionAll	8 8	$1.3090 \times 10^{-11} 1.2949 \times 10^{-11}$	1 1	3.207×10^{-12} 3.247×10^{-12}	$3.1748 \times 10^{-3} 2.6796 \times 10^{-3}$	0.844
pdb2mle 434	ClassicAll QuaternionAll	8 8	1.6719×10^{-3} 1.6719×10^{-3}	2 2	1.491×10^{-13} 1.535×10^{-13}	1.6953×10^{-3} 1.4160×10^{-3}	0.835
pdb2mlf 434	ClassicAll QuaternionAll	8 8	$8.3036 \times 10^{-13} \\ 8.8493 \times 10^{-13}$	2 2	9.918×10^{-14} 1.127×10^{-13}	1.6903×10^{-3} 1.4173×10^{-3}	0.839
pdb2mo5 854	ClassicAll QuaternionAll	8 8	$1.9007 \times 10^{-11} 1.8458 \times 10^{-11}$	1 1	$1.394 \times 10^{-12} 1.403 \times 10^{-12}$	$3.3915 \times 10^{-3} 2.8453 \times 10^{-3}$	0.839
pdb2mpu 554	ClassicAll QuaternionAll	8 8	$2.5305 \times 10^{-12} 2.5592 \times 10^{-12}$	1 1	$9.785 \times 10^{-14} $ 1.016×10^{-13}	2.1776×10^{-3} 1.8563×10^{-3}	0.852
pdb2mra 704	ClassicAll QuaternionAll	8 8	$4.3616 \times 10^{-12} 4.3117 \times 10^{-12}$	1 1	2.632×10^{-13} 2.768×10^{-13}	3.1919×10^{-3} 2.5928×10^{-3}	0.812
pdb2msu 122	ClassicAll QuaternionAll	8 8	$3.6237 \times 10^{-12} 3.6441 \times 10^{-12}$	1 1	$7.813 \times 10^{-14} \\ 8.765 \times 10^{-14}$	$4.5303 \times 10^{-4} 3.8593 \times 10^{-4}$	0.852
pdb2mty 120	ClassicAll QuaternionAll	2 2	$5.1232 \times 10^{-12} 5.2129 \times 10^{-12}$	2 2	$1.848 \times 10^{-14} 2.363 \times 10^{-14}$	$3.4243 \times 10^{-4} 2.5241 \times 10^{-4}$	0.737
pdb2muh 98	ClassicAll QuaternionAll	8 8	$8.0615 \times 10^{-5} 8.0615 \times 10^{-5}$	2 2	$2.008 \times 10^{-13} 2.279 \times 10^{-13}$	$3.4633 \times 10^{-4} 2.9121 \times 10^{-4}$	0.841
pdb2mvj 156	ClassicAll QuaternionAll	2 2	$6.1752 \times 10^{-12} 6.1858 \times 10^{-12}$	1 1	$1.534 \times 10^{-13} 1.647 \times 10^{-13}$	$4.1678 \times 10^{-4} 3.0918 \times 10^{-4}$	0.742
pdb2mvt 284	ClassicAll QuaternionAll	8 8	$1.5441 \times 10^{-4} 1.5441 \times 10^{-4}$	2 2	$6.053 \times 10^{-12} 6.225 \times 10^{-12}$	$1.1137 \times 10^{-3} 9.4715 \times 10^{-4}$	0.850
pdb2n00 572	ClassicAll QuaternionAll	8 8	$1.2439 \times 10^{-4} 1.2439 \times 10^{-4}$	2 2	2.703×10^{-13} 3.466×10^{-13}	2.2232×10^{-3} 1.8588×10^{-3}	0.836

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2n0b 60	ClassicAll QuaternionAll	2 2	$1.0219 \times 10^{-11} 1.0781 \times 10^{-11}$	$\frac{2}{2}$	$7.123 \times 10^{-13} \\ 9.477 \times 10^{-13}$	$1.4871 \times 10^{-4} 1.0772 \times 10^{-4}$	0.724
pdb2n0c 60	ClassicAll QuaternionAll	2 2	$\begin{array}{c} 1.0471 \times 10^{-12} \\ 9.1394 \times 10^{-13} \end{array}$	1 1	$1.293 \times 10^{-13} 1.682 \times 10^{-13}$	$\begin{array}{c} 1.6022 \times 10^{-4} \\ 1.0615 \times 10^{-4} \end{array}$	0.663
pdb2n0d 60	ClassicAll QuaternionAll	2 2	$5.2061 \times 10^{-11} 5.7645 \times 10^{-11}$	2 2	$3.639 \times 10^{-12} 4.540 \times 10^{-12}$	$1.5071 \times 10^{-4} 1.1035 \times 10^{-4}$	0.732
pdb2n0e 60	ClassicAll QuaternionAll	2 2	$1.1503 \times 10^{-11} 1.8786 \times 10^{-11}$	2 2	$3.314 \times 10^{-12} 4.286 \times 10^{-12}$	$1.5451 \times 10^{-4} \\ 1.1311 \times 10^{-4}$	0.732
pdb2n0f 60	ClassicAll QuaternionAll	2 2	$2.2697 \times 10^{-12} 2.7490 \times 10^{-12}$	1 1	3.185×10^{-13} 4.023×10^{-13}	$1.5359 \times 10^{-4} 1.1102 \times 10^{-4}$	0.723
pdb2n0g 60	ClassicAll QuaternionAll	2 2	1.4896×10^{-11} 1.4974×10^{-11}	1 1	8.315×10^{-13} 9.618×10^{-13}	$1.5243 \times 10^{-4} 1.1061 \times 10^{-4}$	0.726
pdb2n0h 60	ClassicAll QuaternionAll	2 2	$4.1935 \times 10^{-12} 4.1379 \times 10^{-12}$	2 2	$7.716 \times 10^{-13} \\ 8.755 \times 10^{-13}$	$1.5238 \times 10^{-4} 1.1151 \times 10^{-4}$	0.732
pdb2n35 314	ClassicAll QuaternionAll	8 8	$1.4478 \times 10^{-4} 1.4478 \times 10^{-4}$	6 6	$3.658 \times 10^{-14} 4.617 \times 10^{-14}$	$1.2073 \times 10^{-3} 1.0074 \times 10^{-3}$	0.834
pdb2n41 638	ClassicAll QuaternionAll	8 8	$5.9366 \times 10^{-3} 5.9366 \times 10^{-3}$	2 2	$1.812 \times 10^{-13} 1.836 \times 10^{-13}$	$2.4828 \times 10^{-3} 2.0828 \times 10^{-3}$	0.839
pdb2n4e 638	ClassicAll QuaternionAll	8 8	5.1960×10^{-3} 5.1960×10^{-3}	2 2	1.494×10^{-13} 1.687×10^{-13}	$2.4771 \times 10^{-3} 2.0948 \times 10^{-3}$	0.846
pdb2n5q 164	ClassicAll QuaternionAll	8 8	$1.1051 \times 10^{-11} 9.3428 \times 10^{-12}$	1 1	$1.732 \times 10^{-12} 1.745 \times 10^{-12}$	6.3728×10^{-4} 5.4182×10^{-4}	0.850
pdb2n67 566	ClassicAll QuaternionAll	8 8	$2.0736 \times 10^{-12} 2.0936 \times 10^{-12}$	1 1	$4.443 \times 10^{-13} 4.465 \times 10^{-13}$	2.2113×10^{-3} 1.8823×10^{-3}	0.851
pdb2n6n 192	ClassicAll QuaternionAll	2 2	$1.6681 \times 10^{-12} 1.2630 \times 10^{-12}$	$\frac{2}{2}$	$6.557 \times 10^{-13} 7.492 \times 10^{-13}$	$6.0621 \times 10^{-4} 4.5330 \times 10^{-4}$	0.748
pdb2n7i 224	ClassicAll QuaternionAll	8 8	1.3998×10^{-4} 1.3998×10^{-4}	1 1	9.212×10^{-13} 1.126×10^{-12}	8.3429×10^{-4} 7.0047×10^{-4}	0.840
pdb2n7j 336	ClassicAll QuaternionAll	2 2	$2.5110 \times 10^{-12} 2.6436 \times 10^{-12}$	1 1	$5.969 \times 10^{-13} 6.094 \times 10^{-13}$	$9.5660 \times 10^{-4} 7.1828 \times 10^{-4}$	0.751
$\begin{array}{c} \mathrm{pdb2na9} \\ 266 \end{array}$	ClassicAll QuaternionAll	8 8	$2.3390 \times 10^{-12} 2.3721 \times 10^{-12}$	1 1	$5.440 \times 10^{-14} 6.690 \times 10^{-14}$	$1.0107 \times 10^{-3} \\ 8.4029 \times 10^{-4}$	0.831
pdb2ndc 110	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.1313 \times 10^{-3} \\ 3.1313 \times 10^{-3} \end{array}$	$\frac{2}{2}$	3.365×10^{-14} 4.481×10^{-14}	$4.0235 \times 10^{-4} 3.4737 \times 10^{-4}$	0.863
pdb2nde 110	ClassicAll QuaternionAll	8 8	$8.5286 \times 10^{-5} 8.5286 \times 10^{-5}$	2 2	$7.022 \times 10^{-14} \\ 8.855 \times 10^{-14}$	$3.9925 \times 10^{-4} 3.3781 \times 10^{-4}$	0.846
pdb2ndk 290	ClassicAll QuaternionAll	8 8	$9.0150 \times 10^{-5} 9.0150 \times 10^{-5}$	1 1	$5.022 \times 10^{-13} 6.279 \times 10^{-13}$	$1.1182 \times 10^{-3} 9.4276 \times 10^{-4}$	0.843
pdb2nvj 152	ClassicAll QuaternionAll	8 8	$6.7520 \times 10^{-3} 6.7520 \times 10^{-3}$	7 7	$2.082 \times 10^{-14} 2.293 \times 10^{-14}$	$5.8433 \times 10^{-4} 5.0024 \times 10^{-4}$	0.856
pdb2p6j 314	ClassicAll QuaternionAll	8 8	3.2640×10^{-13} 3.5480×10^{-13}	1 1	$4.795 \times 10^{-14} 6.389 \times 10^{-14}$	1.2092×10^{-3} 1.0133×10^{-3}	0.838
pdb2p81 266	ClassicAll QuaternionAll	8 8	6.8538×10^{-11} 6.8914×10^{-11}	2 2	$7.881 \times 10^{-13} \\ 8.226 \times 10^{-13}$	$1.0138 \times 10^{-3} \\ 8.4022 \times 10^{-4}$	0.829
pdb2pqe 896	ClassicAll QuaternionAll	8 8	$4.1258 \times 10^{-5} 4.1258 \times 10^{-5}$	2 2	$1.127 \times 10^{-11} 1.248 \times 10^{-11}$	$3.5834 \times 10^{-3} 3.0203 \times 10^{-3}$	0.843
pdb2rlg 108	ClassicAll QuaternionAll	2 2	$4.8140 \times 10^{-13} 5.3066 \times 10^{-13}$	1 1	$5.501 \times 10^{-14} \\ 6.973 \times 10^{-14}$	$2.8959 \times 10^{-4} 2.1489 \times 10^{-4}$	0.742
pdb2rlh 108	ClassicAll QuaternionAll	2 2	$1.0750 \times 10^{-12} 1.0423 \times 10^{-12}$	1 1	$4.772 \times 10^{-14} 5.801 \times 10^{-14}$	$2.9106 \times 10^{-4} 2.1763 \times 10^{-4}$	0.748
pdb2rmy 206	ClassicAll QuaternionAll	8 8	$1.2240 \times 10^{-4} 1.2240 \times 10^{-4}$	1 1	$1.872 \times 10^{-13} 2.498 \times 10^{-13}$	$7.6127 \times 10^{-4} 6.3412 \times 10^{-4}$	0.833
pdb2rnd 206	ClassicAll QuaternionAll	128 128	3.4031×10^{-12} 3.8842×10^{-12}	33 33	$2.626 \times 10^{-13} 3.569 \times 10^{-13}$	$\begin{array}{c} 1.2905 \times 10^{-2} \\ 9.0111 \times 10^{-3} \end{array}$	0.698

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2roo 260	ClassicAll QuaternionAll	8 8	3.3639×10^{-4} 3.3639×10^{-4}	6 6	2.933×10^{-12} 3.525×10^{-12}	$1.7042 \times 10^{-3} 1.2776 \times 10^{-3}$	0.750
pdb2rql 572	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.9510 \times 10^{-11} \\ 1.0013 \times 10^{-10} \end{array}$	1 1	$\begin{array}{c} 2.345 \times 10^{-12} \\ 2.496 \times 10^{-12} \end{array}$	$\begin{array}{c} 2.2341 \times 10^{-3} \\ 1.8932 \times 10^{-3} \end{array}$	0.847
pdb2rut 218	ClassicAll QuaternionAll	8 8	$2.0579 \times 10^{-13} 4.0527 \times 10^{-13}$	2 2	$4.389 \times 10^{-14} 5.013 \times 10^{-14}$	$8.1026 \times 10^{-4} \\ 6.8185 \times 10^{-4}$	0.842
pdb2ruv 224	ClassicAll QuaternionAll	8 8	$5.4278 \times 10^{-13} 6.5510 \times 10^{-13}$	$\frac{2}{2}$	$5.775 \times 10^{-14} 7.404 \times 10^{-14}$	8.2582×10^{-4} 6.9366×10^{-4}	0.840
pdb2rux 218	ClassicAll QuaternionAll	8 8	3.6084×10^{-3} 3.6084×10^{-3}	1 1	$\begin{array}{c} 2.671 \times 10^{-14} \\ 3.016 \times 10^{-14} \end{array}$	$\begin{array}{c} 8.1189 \times 10^{-4} \\ 6.8616 \times 10^{-4} \end{array}$	0.845
pdb2ruy 224	ClassicAll QuaternionAll	8 8	$4.1535 \times 10^{-13} 3.5981 \times 10^{-13}$	1 1	$1.968 \times 10^{-14} 2.387 \times 10^{-14}$	8.1713×10^{-4} 6.8694×10^{-4}	0.841
pdb2rv3 218	ClassicAll QuaternionAll	8 8	3.0630×10^{-4} 3.0630×10^{-4}	1 1	3.656×10^{-14} 4.118×10^{-14}	8.0680×10^{-4} 6.8179×10^{-4}	0.845
pdb2rv5 212	ClassicAll QuaternionAll	8 8	$8.6519 \times 10^{-4} \\ 8.6519 \times 10^{-4}$	1 1	$1.145 \times 10^{-14} \\ 1.338 \times 10^{-14}$	7.9030×10^{-4} 6.7668×10^{-4}	0.856
pdb2y4q 476	ClassicAll QuaternionAll	8 8	$4.6451 \times 10^{-11} $ 4.6324×10^{-11}	2 2	$1.410 \times 10^{-12} \\ 1.451 \times 10^{-12}$	$1.8369 \times 10^{-3} $ 1.5601×10^{-3}	0.849
pdb2k2f 1268	ClassicAll QuaternionAll	8	1.2926×10^{-11} 1.2956×10^{-11}	1 1	2.639×10^{-13} 2.818×10^{-13}	1.5687×10^{1} 9.5350	0.608
pdb2kbm 1268	ClassicAll QuaternionAll	8	1.5487×10^{-12} 1.6865×10^{-12}	2 2	$2.165 \times 10^{-13} 2.226 \times 10^{-13}$	1.2158×10^{1} 7.7655	0.639
pdb2j10 752	ClassicAll QuaternionAll	1024 1024	$2.9952 \times 10^{-5} $ 2.9952×10^{-5}	574 574	$9.196 \times 10^{-12} \\ 9.529 \times 10^{-12}$	$5.6669 \times 10^{-1} $ 4.7902×10^{-1}	0.845
pdb2j11 752	ClassicAll QuaternionAll	1024 1024	2.7803×10^{-11} 2.7661×10^{-11}	549 549	$5.256 \times 10^{-12} \\ 5.631 \times 10^{-12}$	5.6835×10^{-1} 4.8137×10^{-1}	0.847
pdb2lwa 432	ClassicAll QuaternionAll	2048 2048	4.9078×10^{-12} 4.0818×10^{-12}	449 449	3.616×10^{-13} 4.436×10^{-13}	$1.0042 \\ 7.4914 \times 10^{-1}$	0.746
pdb2j0z 752	ClassicAll QuaternionAll	8 8	1.3100×10^{-10} 1.3116×10^{-10}	6 6	4.392×10^{-12} 4.954×10^{-12}	$7.5375 \times 10^{-2} $ 4.9065×10^{-2}	0.651
pdb2adl 868	ClassicAll QuaternionAll	8 8	3.1161×10^{-11} 3.3255×10^{-11}	1 1	$1.752 \times 10^{-11} \\ 1.787 \times 10^{-11}$	7.5891×10^{-3} 5.4662×10^{-3}	0.720
pdb1pzr 724	ClassicAll QuaternionAll	8 8	3.9940×10^{-10} 3.9046×10^{-10}	1 1	$5.644 \times 10^{-12} \\ 5.871 \times 10^{-12}$	$6.0477 \times 10^{-2} 4.2970 \times 10^{-2}$	0.711
pdb2lzf 820	ClassicAll QuaternionAll	8 8	5.9653×10^{-4} 5.9653×10^{-4}	2 2	3.217×10^{-14} 3.959×10^{-14}	1.3270×10^{-1} 8.6061×10^{-2}	0.649
pdb2g9j 848	ClassicAll QuaternionAll	8 8	5.8011×10^{-4} 5.8011×10^{-4}	2 2	3.282×10^{-12} 3.535×10^{-12}	1.2568×10^{-1} 7.9801×10^{-2}	0.635
pdb2le2 676	ClassicAll QuaternionAll	8 8	1.5317×10^{-12} 1.4989×10^{-12}	2 2	2.064×10^{-13} 2.042×10^{-13}	1.0604×10^{-1} 7.1920×10^{-2}	0.678
pdb2mvx 2360	ClassicAll QuaternionAll	8 8	5.8655×10^{-5} 5.8655×10^{-5}	6 6	1.968×10^{-10} 1.971×10^{-10}	1.6123×10^{-2} 1.1023×10^{-2}	0.684
pdb2mz6 220	ClassicAll QuaternionAll	8 8	$2.3371 \times 10^{-10} $ 2.3374×10^{-10}	1 1	$2.141 \times 10^{-11} \\ 2.153 \times 10^{-11}$	2.2867×10^{-2} 1.4784×10^{-2}	0.647
pdb2a2y 1072	ClassicAll QuaternionAll	8 8	$8.1076 \times 10^{-5} \\ 8.1076 \times 10^{-5}$	2 2	1.150×10^{-12} 1.151×10^{-12}	1.0587×10^{-1} 6.5937×10^{-2}	0.623
pdb2n9b 832	ClassicAll QuaternionAll		4.0200×10^{-10} 4.0126×10^{-10}	1 1	$ \begin{array}{c} 1.196 \times 10^{-12} \\ 1.238 \times 10^{-12} \end{array} $	4.9956×10^{-2} 3.4607×10^{-2}	0.693
pdb1hf9 496	ClassicAll QuaternionAll	8 8	9.0139×10^{-10} 9.0282×10^{-10}	6 6	1.156×10^{-11} 1.180×10^{-11}	1.9801×10^{-2} 1.3024×10^{-2}	0.658
pdb2m4j 2178	ClassicAll QuaternionAll	8 8	5.2912×10^{-4} 5.2912×10^{-4}	1 1	1.463×10^{-11} 1.455×10^{-11}	3.2721×10^{-2} 2.4835×10^{-2}	0.759
pdb1x9v	ClassicAll	8 8	$ \begin{array}{c} 3.2912 \times 10^{-4} \\ 1.1547 \times 10^{-4} \\ 1.1547 \times 10^{-4} \end{array} $	6 6	8.968×10^{-13} 9.611×10^{-13}	$ \begin{array}{c} 2.4835 \times 10^{-2} \\ 1.9875 \times 10^{-2} \\ 1.2848 \times 10^{-2} \end{array} $	0.759
544	QuaternionAll	0	1.1047 X 10 -	U	3.011 X 10 -0	1.2040 X 1U 2	0.040

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Improv time
pdb2ko1 1060	ClassicAll QuaternionAll	8 8	$9.3273 \times 10^{-4} 9.3273 \times 10^{-4}$	$\frac{2}{2}$	1.150×10^{-12} 1.151×10^{-12}	3.7152×10^{-2} 2.7479×10^{-2}	0.740
pdb2n3a 574	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 2.1457 \times 10^{-3} \\ 2.1457 \times 10^{-3} \end{array}$	5 5	8.770×10^{-14} 1.049×10^{-13}	3.4809×10^{-2} 2.2580×10^{-2}	0.649

log.txt

 ${\tt time_limit=120~seconds}$

 ${\tt function_of_central_tendency_meansure=median}$

function_of_improvement=#18

precision=1.0e-6

precision_virtual=1.0e-8

benchmark_seconds=300

benchmark_samples_limit=100000

all_solutions=False

list_of_problems=["pdb1a57", "pdb1b4c", "pdb1ba5", "pdb1d1n", "pdb1dp3", "pdb1du1", "pdb1eii", "pdb1fc1", "pdb1fd6", "pdb

start_time=2023-05-03T16:03:05.590

end_time=2023-05-04T08:13:40.377

##########

 ${\tt time_limit=120~seconds}$

 ${\tt function_of_central_tendency_meansure=median}$

function_of_improvement=#20

precision=1.0e-6

precision_virtual=1.0e-8

benchmark_seconds=4000

benchmark_samples_limit=100000

all_solutions=False

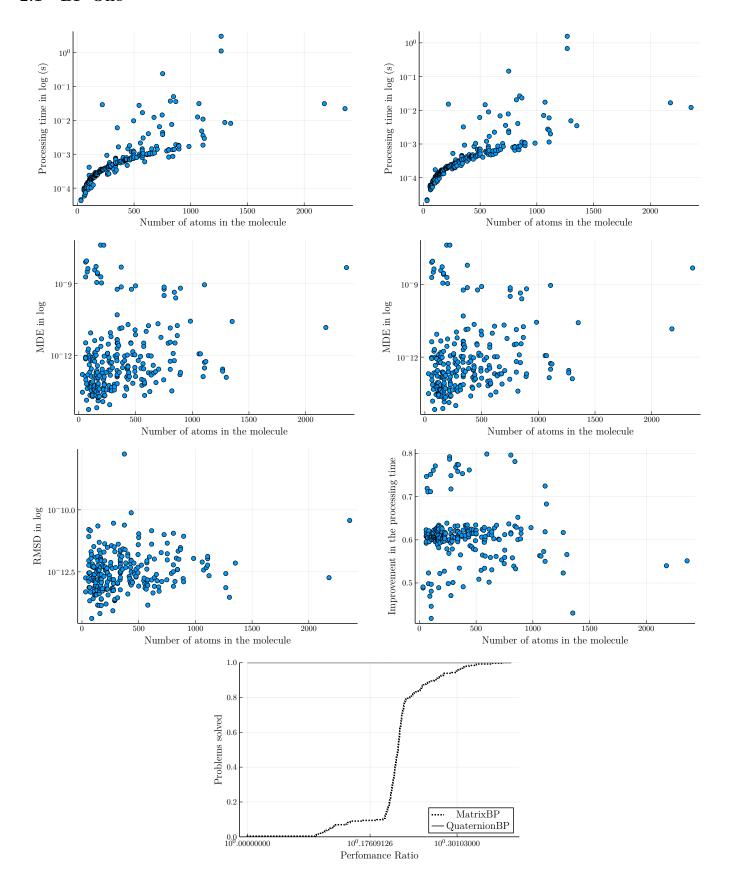
list_of_problems=["pdb2k2f", "pdb2kbm", "pdb2j10", "pdb2j11", "pdb2lwa", "pdb2j0z", "pdb2ad1", "pdb1pzr", "pdb2lzf", "pdb

start_time=2023-05-08T08:11:55.060

end_time=2023-05-09T19:45:47.272

2 Visual analysis

2.1 BP-One



2.2 BP-All

