Table 1: Results

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $	ext{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|---|-----------------------------|---|---|-------------------------------------|--|---|-------------|
| pdb1ba5 320 | ClassicAll QuaternionAll | 16384 16384 | $\begin{array}{c} 3.5079 \times 10^{-2} \\ 3.5079 \times 10^{-2} \end{array}$ | 10070 10070 | $7.453 \times 10^{-7} 7.453 \times 10^{-7}$ | 5.5325 4.7959 | 15.359 |
| pdb1d1n 594 | ClassicAll QuaternionAll | 5376 5376 | $2.9766 \times 10^{-11} \\ 2.9311 \times 10^{-11}$ | 1707 1707 | $1.005 \times 10^{-11} 9.672 \times 10^{-12}$ | 1.0156×10^{1} 5.6835 | 78.694 |
| pdb1du1 122 | ClassicAll QuaternionAll | $\begin{array}{c} 212992 \\ 212992 \end{array}$ | $6.6600 \times 10^{-13} 1.6576 \times 10^{-12}$ | 45549 45549 | 8.225×10^{-13} 1.258×10^{-12} | 2.5062×10^{1} 2.5012×10^{1} | 0.201 |
| pdb1i2u 266 | ClassicAll QuaternionAll | 48 48 | 1.1301×10^{-3} 1.1301×10^{-3} | 22 22 | $5.676 \times 10^{-7} 5.676 \times 10^{-7}$ | $1.0456 \times 10^{-1} 5.2997 \times 10^{-2}$ | 97.300 |
| $\begin{array}{c} pdb1i2v \\ 266 \end{array}$ | ClassicAll QuaternionAll | 8 8 | $8.9125 \times 10^{-13} 8.8206 \times 10^{-13}$ | 5 5 | 2.422×10^{-13} 2.525×10^{-13} | $1.5406 \times 10^{-2} 7.3820 \times 10^{-3}$ | 108.701 |
| pdb1jlz 140 | ClassicAll QuaternionAll | 256 256 | $1.2003 \times 10^{-4} 1.2003 \times 10^{-4}$ | 73 73 | $3.238 \times 10^{-7} \\ 3.238 \times 10^{-7}$ | $3.0876 \times 10^{-2} 2.0054 \times 10^{-2}$ | 53.970 |
| pdb1k0v 440 | ClassicAll QuaternionAll | 8 8 | $8.3940 \times 10^{-5} 8.3940 \times 10^{-5}$ | 2 2 | $1.893 \times 10^{-13} 1.894 \times 10^{-13}$ | 4.1180×10^{-3} 2.5508×10^{-3} | 61.436 |
| pdb1k2h 1120 | ClassicAll QuaternionAll | 64 64 | 1.9334×10^{-4} 1.9334×10^{-4} | 6 6 | $4.671 \times 10^{-7} 4.671 \times 10^{-7}$ | $\begin{array}{c} 1.9235 \\ 8.8912 \times 10^{-1} \end{array}$ | 116.338 |
| pdb1k37 278 | ClassicAll QuaternionAll | 224 224 | $2.1407 \times 10^{-12} 2.0318 \times 10^{-12}$ | 30 30 | $4.711 \times 10^{-13} $ 4.988×10^{-13} | 2.9754×10^{1} 1.4785×10^{1} | 101.243 |
| pdb1kuw 62 | ClassicAll QuaternionAll | 16 16 | 1.8706×10^{-4} 1.8706×10^{-4} | 1 1 | $9.229 \times 10^{-14} 1.130 \times 10^{-13}$ | $1.1271 \times 10^{-3} 6.9661 \times 10^{-4}$ | 61.798 |
| pdb1kz0 98 | ClassicAll QuaternionAll | 16 16 | $6.7512 \times 10^{-13} 6.2568 \times 10^{-13}$ | 1 1 | $4.404 \times 10^{-14} 5.880 \times 10^{-14}$ | $9.1368 \times 10^{-4} \\ 6.4383 \times 10^{-4}$ | 41.913 |
| pdb1kz2 98 | ClassicAll QuaternionAll | 16 16 | $3.1076 \times 10^{-6} 3.1076 \times 10^{-6}$ | 5 5 | $2.119 \times 10^{-14} 2.886 \times 10^{-14}$ | $1.0205 \times 10^{-3} 7.0401 \times 10^{-4}$ | 44.959 |
| pdb1kz5 74 | ClassicAll QuaternionAll | 16 16 | $4.8094 \times 10^{-13} 5.2716 \times 10^{-13}$ | 1 1 | $4.081 \times 10^{-14} 4.738 \times 10^{-14}$ | $1.0049 \times 10^{-3} 6.4642 \times 10^{-4}$ | 55.449 |
| pdb1lvz 68 | ClassicAll QuaternionAll | 16 16 | 1.1842×10^{-3} 1.1842×10^{-3} | 1 1 | $6.483 \times 10^{-8} 6.483 \times 10^{-8}$ | $6.1571 \times 10^{-4} 4.4316 \times 10^{-4}$ | 38.938 |
| pdb1m4e 122 | ClassicAll QuaternionAll | 384 384 | $5.4966 \times 10^{-12} 5.5048 \times 10^{-12}$ | 25 25 | $5.949 \times 10^{-13} 5.972 \times 10^{-13}$ | $3.5242 \times 10^{-2} 2.3349 \times 10^{-2}$ | 50.933 |
| pdb1ma4 104 | ClassicAll QuaternionAll | 192 192 | $5.0392 \times 10^{-4} 5.0392 \times 10^{-4}$ | 54 54 | $7.441 \times 10^{-7} 7.441 \times 10^{-7}$ | 3.1803×10^{-2} 1.8756×10^{-2} | 69.565 |
| pdb1ma5 104 | ClassicAll QuaternionAll | 4608 4608 | $6.1895 \times 10^{-5} 6.1895 \times 10^{-5}$ | 1665 1665 | $7.863 \times 10^{-7} 7.863 \times 10^{-7}$ | 3.0799×10^{-1} 2.9139×10^{-1} | 5.694 |
| pdb1ma6 104 | ClassicAll QuaternionAll | $24576 \\ 24576$ | 1.2440×10^{-11} 1.4288×10^{-11} | 5094 5094 | $6.283 \times 10^{-13} \\ 8.487 \times 10^{-13}$ | 2.0697 2.3901 | -13.406 |
| pdb1nd9 296 | ClassicAll QuaternionAll | 512 512 | $1.0508 \times 10^{-12} 8.9082 \times 10^{-13}$ | 2 2 | 3.026×10^{-13} 3.845×10^{-13} | $8.4278 \times 10^{-1} 4.6467 \times 10^{-1}$ | 81.372 |
| pdb1nmj 170 | ClassicAll QuaternionAll | 8 8 | $2.3883 \times 10^{-13} $ 2.3832×10^{-13} | 7 7 | $1.236 \times 10^{-14} 1.422 \times 10^{-14}$ | $1.2173 \times 10^{-3} 7.6976 \times 10^{-4}$ | 58.144 |
| pdb1o53 92 | ClassicAll QuaternionAll | $\begin{array}{c} 294912 \\ 294912 \end{array}$ | $1.0887 \times 10^{-11} 1.1252 \times 10^{-11}$ | 69346 69346 | $3.999 \times 10^{-13} 4.527 \times 10^{-13}$ | $7.7107 \times 10^{1} $ 2.7689×10^{1} | 178.470 |
| pdb1oqp 580 | ClassicAll QuaternionAll | 8 8 | $2.9348 \times 10^{-3} 2.9348 \times 10^{-3}$ | 2 2 | $7.045 \times 10^{-14} \\ 8.314 \times 10^{-14}$ | 2.7797×10^{-2} 1.3325×10^{-2} | 108.609 |
| pdb1plw 32 | ClassicAll QuaternionAll | 64 64 | $\begin{array}{c} 3.0310 \times 10^{-13} \\ 3.2973 \times 10^{-13} \end{array}$ | 26 26 | $2.830 \times 10^{-14} \\ 3.112 \times 10^{-14}$ | $\begin{array}{c} 9.2563 \times 10^{-4} \\ 6.9320 \times 10^{-4} \end{array}$ | 33.530 |
| pdb1plx 32 | ClassicAll QuaternionAll | 256 256 | $1.8321 \times 10^{-4} 1.8321 \times 10^{-4}$ | 105 105 | $2.751 \times 10^{-6} $ 2.751×10^{-6} | $2.2670 \times 10^{-3} 2.0063 \times 10^{-3}$ | 12.992 |
| pdb1r57 614 | ClassicAll QuaternionAll | 64 64 | $4.1216 \times 10^{-3} 4.1216 \times 10^{-3}$ | 6 6 | 2.080×10^{-9} 2.080×10^{-9} | 5.1769×10^{-2} 3.0150×10^{-2} | 71.703 |
| pdb1s4h 80 | ClassicAll QuaternionAll | 393216 393216 | $3.7288 \times 10^{-6} 3.7288 \times 10^{-6}$ | 114246 114246 | $1.026 \times 10^{-6} 1.026 \times 10^{-6}$ | $1.4783 \times 10^2 \\ 1.2240 \times 10^2$ | 20.775 |
| pdb1s4j 80 | ClassicAll QuaternionAll | 512 512 | $5.8507 \times 10^{-12} 5.8479 \times 10^{-12}$ | 106 106 | $1.520 \times 10^{-13} 2.083 \times 10^{-13}$ | $1.4515 \times 10^{-2} 1.3990 \times 10^{-2}$ | 3.753 |
| pdb1sa8 | ClassicAll | 8 | 1.7170×10^{-3} | 1 | 9.340×10^{-13} | 2.4228×10^{-2} | |

Table 2: Results - continued

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $	ext{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|-----------------|-----------------------------|-----------------------|---|-------------------------------------|---|---|-------------|
| 638 | QuaternionAll | 8 | 1.7170×10^{-3} | 1 | 1.034×10^{-12} | 1.2110×10^{-2} | 100.076 |
| pdb1t2y 152 | ClassicAll QuaternionAll | 384 384 | $2.2800 \times 10^{-4} 2.2800 \times 10^{-4}$ | 169 169 | $5.096 \times 10^{-7} 5.096 \times 10^{-7}$ | $2.8234 \times 10^{-2} 2.1943 \times 10^{-2}$ | 28.667 |
| pdb1t5q 180 | ClassicAll QuaternionAll | 2 2 | $1.0265 \times 10^{-12} 1.0480 \times 10^{-12}$ | 1 1 | $3.877 \times 10^{-14} 5.093 \times 10^{-14}$ | $\begin{array}{c} 9.9171 \times 10^{-4} \\ 5.4202 \times 10^{-4} \end{array}$ | 82.966 |
| pdb1tot 314 | ClassicAll QuaternionAll | 8 8 | $\begin{array}{c} 3.4218 \times 10^{-3} \\ 3.4218 \times 10^{-3} \end{array}$ | 5 5 | $6.151 \times 10^{-14} 6.855 \times 10^{-14}$ | $2.3885 \times 10^{-3} 1.5272 \times 10^{-3}$ | 56.400 |
| pdb1v6r 128 | ClassicAll QuaternionAll | 448 448 | $7.3125 \times 10^{-5} \\ 7.3125 \times 10^{-5}$ | 122 122 | $\begin{array}{c} 1.648 \times 10^{-6} \\ 1.648 \times 10^{-6} \end{array}$ | $7.7798 \times 10^{-2} $ 4.7831×10^{-2} | 62.652 |
| pdb1v92 278 | ClassicAll QuaternionAll | $25600 \\ 25600$ | $\begin{array}{c} 2.3012 \times 10^{-5} \\ 2.3012 \times 10^{-5} \end{array}$ | 9449 9449 | $1.890 \times 10^{-6} 1.890 \times 10^{-6}$ | 6.3087 5.5854 | 12.949 |
| pdb1vpc 272 | ClassicAll QuaternionAll | 16 16 | $4.3482 \times 10^{-4} 4.3482 \times 10^{-4}$ | 14 14 | $8.510 \times 10^{-15} 1.002 \times 10^{-14}$ | $3.8676 \times 10^{-3} 2.4373 \times 10^{-3}$ | 58.683 |
| pdb1wnk 140 | ClassicAll QuaternionAll | $24576 \\ 24576$ | $\begin{array}{c} 2.2292 \times 10^{-10} \\ 2.2177 \times 10^{-10} \end{array}$ | $2433 \\ 2433$ | $4.112 \times 10^{-12} 4.632 \times 10^{-12}$ | 2.5894 2.3474 | 10.310 |
| pdb1wo4 152 | ClassicAll QuaternionAll | 62720 62720 | $\begin{array}{c} 1.0961 \times 10^{-5} \\ 1.0961 \times 10^{-5} \end{array}$ | 20998 20998 | $\begin{array}{c} 2.477 \times 10^{-6} \\ 2.477 \times 10^{-6} \end{array}$ | $\begin{array}{c} 1.3822 \times 10^{1} \\ 1.1665 \times 10^{1} \end{array}$ | 18.488 |
| pdb1y5c 68 | ClassicAll QuaternionAll | 8192 8192 | $8.7435 \times 10^{-13} \\ 8.2242 \times 10^{-13}$ | 2929 2929 | $7.693 \times 10^{-14} 9.383 \times 10^{-14}$ | 2.0069×10^{-1} 2.8012×10^{-1} | -28.353 |
| pdb2a4j 580 | ClassicAll QuaternionAll | 16 16 | $1.0516 \times 10^{-4} 1.0516 \times 10^{-4}$ | 2 2 | $2.085 \times 10^{-14} 2.727 \times 10^{-14}$ | $\begin{array}{c} 1.4460 \times 10^{-2} \\ 7.6298 \times 10^{-3} \end{array}$ | 89.524 |
| pdb2ajj 170 | ClassicAll QuaternionAll | 640 640 | $7.2549 \times 10^{-5} 7.2549 \times 10^{-5}$ | 121 121 | $\begin{array}{c} 1.229 \times 10^{-6} \\ 1.229 \times 10^{-6} \end{array}$ | $\begin{array}{c} 4.6544 \times 10^{-2} \\ 4.2916 \times 10^{-2} \end{array}$ | 8.453 |
| pdb2ajm 170 | ClassicAll QuaternionAll | 12288 12288 | $2.4063 \times 10^{-12} 2.7001 \times 10^{-12}$ | $1074 \\ 1074$ | $1.183 \times 10^{-13} \\ 1.555 \times 10^{-13}$ | 1.4240 1.3003 | 9.517 |
| pdb2ajn 170 | ClassicAll QuaternionAll | 53760 53760 | $3.7478 \times 10^{-4} \\ 3.7478 \times 10^{-4}$ | $\frac{15665}{15665}$ | 2.380×10^{-6} 2.380×10^{-6} | 9.4979 7.9646 | 19.252 |
| pdb2ajo 170 | ClassicAll QuaternionAll | $\frac{12288}{12288}$ | $2.4063 \times 10^{-12} \\ 2.7001 \times 10^{-12}$ | $1074 \\ 1074$ | $1.183 \times 10^{-13} \\ 1.555 \times 10^{-13}$ | 1.4322 1.3043 | 9.805 |
| pdb2akk 446 | ClassicAll QuaternionAll | 8 8 | 3.0416×10^{-3} 3.0416×10^{-3} | 2 2 | $1.289 \times 10^{-13} 1.279 \times 10^{-13}$ | $1.0365 \times 10^{-1} \\ 5.1613 \times 10^{-2}$ | 100.826 |
| pdb2bzb 748 | ClassicAll QuaternionAll | 32 32 | $4.6498 \times 10^{-13} \\ 6.0113 \times 10^{-13}$ | 29 29 | $9.361 \times 10^{-14} \\ 1.224 \times 10^{-13}$ | 3.2063×10^{-1} 1.5661×10^{-1} | 104.728 |
| pdb2c0s 386 | ClassicAll QuaternionAll | 8 8 | $\begin{array}{c} 1.0793 \times 10^{-2} \\ 1.0793 \times 10^{-2} \end{array}$ | 6 6 | 3.028×10^{-13} 3.380×10^{-13} | 3.8909×10^{-3} 2.3555×10^{-3} | 65.184 |
| pdb2dci 120 | ClassicAll QuaternionAll | 2 2 | $\begin{array}{c} 2.0907 \times 10^{-13} \\ 3.3732 \times 10^{-13} \end{array}$ | 1 1 | $2.366 \times 10^{-14} 2.950 \times 10^{-14}$ | $6.6909 \times 10^{-4} 3.7298 \times 10^{-4}$ | 79.389 |
| pdb2eem 206 | ClassicAll QuaternionAll | 128 128 | $\begin{array}{c} 9.5324 \times 10^{-12} \\ 9.5866 \times 10^{-12} \end{array}$ | 29 29 | $5.190 \times 10^{-13} 5.461 \times 10^{-13}$ | $\begin{array}{c} 4.5197 \times 10^{-1} \\ 2.3134 \times 10^{-1} \end{array}$ | 95.375 |
| pdb2fxz 80 | ClassicAll QuaternionAll | $41472 \\ 41472$ | $4.2293 \times 10^{-12} 5.3169 \times 10^{-12}$ | 13441 13441 | $1.489 \times 10^{-12} 1.749 \times 10^{-12}$ | 2.7845 2.7597 | 0.900 |
| pdb2g9j 848 | ClassicAll QuaternionAll | 16 16 | $5.8011 \times 10^{-4} 5.8011 \times 10^{-4}$ | 2 2 | $3.282 \times 10^{-12} 3.535 \times 10^{-12}$ | $8.6313 \times 10^{-1} 4.2753 \times 10^{-1}$ | 101.888 |
| pdb2g9l 224 | ClassicAll QuaternionAll | 8 8 | $1.0333 \times 10^{-4} 1.0333 \times 10^{-4}$ | $\frac{2}{2}$ | $6.365 \times 10^{-14} \\ 8.666 \times 10^{-14}$ | $\begin{array}{c} 1.6101 \times 10^{-3} \\ 1.0247 \times 10^{-3} \end{array}$ | 57.122 |
| pdb2h5m 614 | ClassicAll QuaternionAll | 128 128 | $1.2260 \times 10^{-3} 1.2260 \times 10^{-3}$ | 21 21 | $2.131 \times 10^{-7} \\ 2.131 \times 10^{-7}$ | $\begin{array}{c} 1.1055 \times 10^{-1} \\ 6.8655 \times 10^{-2} \end{array}$ | 61.026 |
| pdb2hep 252 | ClassicAll QuaternionAll | 676 676 | $2.1758 \times 10^{-11} 2.2038 \times 10^{-11}$ | 224 224 | $1.191 \times 10^{-12} 1.268 \times 10^{-12}$ | 3.2206 1.6251 | 98.178 |
| pdb2jmy 92 | ClassicAll QuaternionAll | 24 24 | $2.4695 \times 10^{-5} 2.4695 \times 10^{-5}$ | 9 9 | 3.958×10^{-6} 3.958×10^{-6} | $1.5905 \times 10^{-3} 1.0839 \times 10^{-3}$ | 46.738 |
| pdb2jn5 74 | ClassicAll QuaternionAll | 96 96 | $6.6339 \times 10^{-12} 2.0459 \times 10^{-11}$ | 45 45 | $1.104 \times 10^{-11} \\ 2.456 \times 10^{-11}$ | $3.1163 \times 10^{-3} \\ 2.3617 \times 10^{-3}$ | 31.954 |
| pdb2jpn 476 | ClassicAll QuaternionAll | 8 8 | $6.4192 \times 10^{-12} 6.5904 \times 10^{-12}$ | $\frac{2}{2}$ | $6.730 \times 10^{-14} \\ 6.984 \times 10^{-14}$ | 4.7008×10^{-3} 2.8260×10^{-3} | 66.341 |

Table 2: Results - continued

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $\mathrm{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|--|-----------------------------|---------------------|---|-------------------------------------|---|--|-------------|
| pdb2jvd 288 | ClassicAll QuaternionAll | 16 16 | 9.4244×10^{-13} 9.4969×10^{-13} | 6 6 | 3.339×10^{-14} 3.898×10^{-14} | $5.0341 \times 10^{-3} 3.0724 \times 10^{-3}$ | 63.848 |
| pdb2jxf 182 | ClassicAll QuaternionAll | 2048 2048 | $1.1644 \times 10^{-4} \\ 1.1644 \times 10^{-4}$ | 305 305 | $\begin{array}{c} 1.841 \times 10^{-6} \\ 1.841 \times 10^{-6} \end{array}$ | 1.2165×10^{-1} 1.2608×10^{-1} | -3.510 |
| pdb2jz5 548 | ClassicAll QuaternionAll | 64 64 | 1.7154×10^{-3} 1.7154×10^{-3} | 5 5 | $1.691 \times 10^{-7} \\ 1.691 \times 10^{-7}$ | 7.6168 3.6348 | 109.551 |
| pdb2k2a 422 | ClassicAll QuaternionAll | 8 8 | $4.7195 \times 10^{-3} 4.7195 \times 10^{-3}$ | 5 5 | 3.810×10^{-14} 5.148×10^{-14} | $4.2185 \times 10^{-3} 2.5402 \times 10^{-3}$ | 66.069 |
| pdb2k36 896 | ClassicAll QuaternionAll | 32 32 | $1.6972 \times 10^{-12} 1.6007 \times 10^{-12}$ | 13 13 | 1.922×10^{-13} 2.045×10^{-13} | $3.5895 \times 10^{-2} 2.2363 \times 10^{-2}$ | 60.512 |
| pdb2k37 356 | ClassicAll QuaternionAll | 192 192 | $3.7147 \times 10^{-12} 3.6176 \times 10^{-12}$ | 45 45 | 1.921×10^{-13} 2.525×10^{-13} | $3.2952 \times 10^{-2} 2.5747 \times 10^{-2}$ | 27.985 |
| pdb2k3i 656 | ClassicAll QuaternionAll | $1024 \\ 1024$ | $2.8710 \times 10^{-3} 2.8710 \times 10^{-3}$ | 393 393 | 6.869×10^{-7} 6.869×10^{-7} | $1.4346 \times 10^{1} \\ 6.7963$ | 111.093 |
| pdb2k6s 494 | ClassicAll QuaternionAll | $256 \\ 256$ | $8.2998 \times 10^{-12} 8.4519 \times 10^{-12}$ | 114 114 | $2.100 \times 10^{-13} 2.651 \times 10^{-13}$ | $\begin{array}{c} 1.1219 \\ 5.6482 \times 10^{-1} \end{array}$ | 98.633 |
| pdb2kdp 428 | ClassicAll QuaternionAll | 128 128 | 3.0283×10^{-12} 3.0741×10^{-12} | 5 5 | $2.621 \times 10^{-13} 2.865 \times 10^{-13}$ | $4.8129 \times 10^{-2} 3.0679 \times 10^{-2}$ | 56.876 |
| pdb2kdr 170 | ClassicAll QuaternionAll | 192 192 | 6.3024×10^{-5} 6.3024×10^{-5} | 86 86 | $6.618 \times 10^{-14} 8.490 \times 10^{-14}$ | $1.1125 \times 10^{-2} \\ 8.3046 \times 10^{-3}$ | 33.968 |
| pdb2kes 290 | ClassicAll QuaternionAll | 64 64 | $1.7403 \times 10^{-4} 1.7403 \times 10^{-4}$ | 43 43 | $1.149 \times 10^{-6} \\ 1.149 \times 10^{-6}$ | $1.1603 \times 10^{-2} \\ 6.8773 \times 10^{-3}$ | 68.711 |
| pdb2kjn 158 | ClassicAll QuaternionAll | $\frac{4608}{4608}$ | $1.9764 \times 10^{-12} 1.9265 \times 10^{-12}$ | 1194 1194 | $9.827 \times 10^{-14} \\ 1.174 \times 10^{-13}$ | $5.4626 \times 10^{-1} 4.8765 \times 10^{-1}$ | 12.019 |
| pdb2kjo 158 | ClassicAll QuaternionAll | $\frac{384}{384}$ | $1.2876 \times 10^{-11} 1.2921 \times 10^{-11}$ | 165 165 | 2.284×10^{-13} 2.421×10^{-13} | $2.4887 \times 10^{-2} 2.0677 \times 10^{-2}$ | 20.361 |
| pdb2kko 1300 | ClassicAll QuaternionAll | 32 32 | $6.9298 \times 10^{-4} $ 6.9298×10^{-4} | 10 10 | 1.852×10^{-7} 1.852×10^{-7} | 2.0477 1.0247 | 99.835 |
| pdb2kl5 662 | ClassicAll QuaternionAll | 96 96 | $2.4505 \times 10^{-12} 2.5206 \times 10^{-12}$ | 5 5 | $1.820 \times 10^{-13} 2.020 \times 10^{-13}$ | $6.3858 \times 10^{-2} 4.0071 \times 10^{-2}$ | 59.361 |
| $\begin{array}{c} \text{pdb2klz} \\ 276 \end{array}$ | ClassicAll QuaternionAll | $\frac{24}{24}$ | 3.9786×10^{-13} 3.7834×10^{-13} | 9 | 3.439×10^{-14} 4.443×10^{-14} | 6.3768×10^{-3} 3.9236×10^{-3} | 62.523 |
| pdb2ko1 1060 | ClassicAll QuaternionAll | 128 128 | $7.9853 \times 10^{-4} 7.9853 \times 10^{-4}$ | 46 46 | $7.782 \times 10^{-8} 7.782 \times 10^{-8}$ | 4.6840 2.2980 | 103.828 |
| $\begin{array}{c} \rm pdb2ksg\\ 290\end{array}$ | ClassicAll QuaternionAll | 8 8 | $9.2027 \times 10^{-13} 9.2208 \times 10^{-13}$ | 1 1 | $3.215 \times 10^{-14} 3.967 \times 10^{-14}$ | 1.9936×10^{-3} 1.2568×10^{-3} | 58.626 |
| pdb2kuh 404 | ClassicAll QuaternionAll | 8 8 | $1.1667 \times 10^{-3} $ 1.1667×10^{-3} | 6 6 | $2.015 \times 10^{-14} 2.491 \times 10^{-14}$ | $2.8811 \times 10^{-3} 1.8443 \times 10^{-3}$ | 56.215 |
| pdb2kwh 338 | ClassicAll QuaternionAll | 16 16 | $2.0587 \times 10^{-3} 2.0587 \times 10^{-3}$ | 6 6 | 1.408×10^{-13} 1.825×10^{-13} | 5.4492×10^{-3} 3.3426×10^{-3} | 63.020 |
| pdb2kxa 144 | ClassicAll QuaternionAll | 16 16 | $3.9712 \times 10^{-12} 3.7392 \times 10^{-12}$ | 8 8 | 1.325×10^{-12} 1.351×10^{-12} | $1.3758 \times 10^{-3} 9.7643 \times 10^{-4}$ | 40.899 |
| pdb2l3m 428 | ClassicAll QuaternionAll | 8 8 | 1.5178×10^{-3} 1.5178×10^{-3} | 1 1 | $1.028 \times 10^{-12} 9.340 \times 10^{-13}$ | 9.4920×10^{-3} 4.5640×10^{-3} | 107.977 |
| pdb2l3n 626 | ClassicAll QuaternionAll | 128 128 | $3.5629 \times 10^{-4} 3.5629 \times 10^{-4}$ | 109 109 | $2.376 \times 10^{-7} 2.376 \times 10^{-7}$ | $\begin{array}{c} 1.7057 \\ 8.2475 \times 10^{-1} \end{array}$ | 106.816 |
| pdb2l45 116 | ClassicAll QuaternionAll | 8 8 | $5.9466 \times 10^{-13} $ 6.7808×10^{-13} | 1 1 | $2.236 \times 10^{-14} 3.033 \times 10^{-14}$ | 9.4055×10^{-4} 5.8855×10^{-4} | 59.808 |
| pdb2l5r 138 | ClassicAll QuaternionAll | 2 2 | 3.0491×10^{-13} 3.0031×10^{-13} | 2 2 | 3.535×10^{-14} 4.436×10^{-14} | $7.5098 \times 10^{-4} 4.2098 \times 10^{-4}$ | 78.388 |
| pdb2l98 434 | ClassicAll QuaternionAll | 608 608 | $5.6413 \times 10^{-12} $ 6.2089×10^{-12} | 154 154 | 3.273×10^{-13} 3.637×10^{-13} | $\begin{array}{c} 1.0512 \\ 5.6327 \times 10^{-1} \end{array}$ | 86.629 |
| pdb2lci 806 | ClassicAll QuaternionAll | 128 128 | $1.2015 \times 10^{-12} 1.1830 \times 10^{-12}$ | 29 29 | $2.579 \times 10^{-13} 2.404 \times 10^{-13}$ | 1.1149×10^{-1} 7.1232×10^{-2} | 56.511 |

Table 2: Results - continued

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $\text{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|---|-----------------------------|-----------------|---|-------------------------------------|---|---|-------------|
| pdb2lde 152 | ClassicAll QuaternionAll | 32 32 | 6.0282×10^{-3} 6.0282×10^{-3} | 14 14 | 3.047×10^{-7} 3.047×10^{-7} | $2.6048 \times 10^{-3} $ 1.8393×10^{-3} | 41.618 |
| pdb2le2 676 | ClassicAll QuaternionAll | 16 16 | $\begin{array}{c} 1.5317 \times 10^{-12} \\ 1.4989 \times 10^{-12} \end{array}$ | $\frac{2}{2}$ | $\begin{array}{c} 2.064 \times 10^{-13} \\ 2.042 \times 10^{-13} \end{array}$ | $\begin{array}{c} 4.2776 \times 10^{-1} \\ 2.0895 \times 10^{-1} \end{array}$ | 104.716 |
| pdb2le7 122 | ClassicAll QuaternionAll | 8 8 | 8.8940×10^{-14} 1.1008×10^{-13} | 2 2 | $2.111 \times 10^{-14} 2.749 \times 10^{-14}$ | $7.9459 \times 10^{-4} 5.1307 \times 10^{-4}$ | 54.868 |
| pdb2ler 68 | ClassicAll QuaternionAll | 8 8 | $5.1096 \times 10^{-14} 6.2001 \times 10^{-14}$ | 2 2 | $1.314 \times 10^{-14} 1.532 \times 10^{-14}$ | $4.2740 \times 10^{-4} 2.7520 \times 10^{-4}$ | 55.305 |
| pdb2lgi 338 | ClassicAll QuaternionAll | 16 16 | $9.7255 \times 10^{-12} 9.6518 \times 10^{-12}$ | 6 6 | $1.068 \times 10^{-12} 1.052 \times 10^{-12}$ | $4.1270 \times 10^{-2} 2.1800 \times 10^{-2}$ | 89.307 |
| pdb2lhe 338 | ClassicAll QuaternionAll | 704 704 | $9.7862 \times 10^{-10} 9.7867 \times 10^{-10}$ | 54 54 | $4.963 \times 10^{-11} 4.967 \times 10^{-11}$ | $1.8045 \times 10^{1} \\ 8.6584$ | 108.405 |
| pdb2lhg 338 | ClassicAll QuaternionAll | 16 16 | 5.0995×10^{-13} 5.4683×10^{-13} | 14 14 | $6.485 \times 10^{-14} 7.343 \times 10^{-14}$ | 3.1087×10^{-3} 2.1955×10^{-3} | 41.590 |
| pdb2lix 162 | ClassicAll QuaternionAll | $\frac{2}{2}$ | $\begin{array}{c} 4.9988 \times 10^{-13} \\ 5.1517 \times 10^{-13} \end{array}$ | 1 1 | $4.842 \times 10^{-14} 5.614 \times 10^{-14}$ | $1.4134 \times 10^{-3} 7.7418 \times 10^{-4}$ | 82.565 |
| $\begin{array}{c} \text{pdb2lld} \\ 242 \end{array} \bigg $ | ClassicAll QuaternionAll | 16 16 | 3.3970×10^{-3} 3.3970×10^{-3} | 9 9 | $\begin{array}{c} 4.630 \times 10^{-7} \\ 4.630 \times 10^{-7} \end{array}$ | $4.5922 \times 10^{-3} 2.8003 \times 10^{-3}$ | 63.990 |
| pdb2lm9 578 | ClassicAll QuaternionAll | 8 8 | $\begin{array}{c} 2.2967 \times 10^{-3} \\ 2.2967 \times 10^{-3} \end{array}$ | 2 2 | $6.254 \times 10^{-14} 7.713 \times 10^{-14}$ | $4.0805 \times 10^{-3} $ 2.6141×10^{-3} | 56.093 |
| pdb2lmf 140 | ClassicAll QuaternionAll | 5376 5376 | $\begin{array}{c} 1.3912 \times 10^{-5} \\ 1.3912 \times 10^{-5} \end{array}$ | 1613 1613 | $2.554 \times 10^{-6} 2.554 \times 10^{-6}$ | $\begin{array}{c} 4.4378 \times 10^{-1} \\ 4.4877 \times 10^{-1} \end{array}$ | -1.112 |
| pdb2ln3 500 | ClassicAll QuaternionAll | 8 8 | $\begin{array}{c} 2.5821 \times 10^{-13} \\ 2.9987 \times 10^{-13} \end{array}$ | 1 1 | $1.292 \times 10^{-13} 1.359 \times 10^{-13}$ | $6.6050 \times 10^{-3} \\ 3.8591 \times 10^{-3}$ | 71.152 |
| pdb2lo2 230 | ClassicAll QuaternionAll | 64 64 | $\begin{array}{c} 1.4016 \times 10^{-2} \\ 1.4016 \times 10^{-2} \end{array}$ | 26 26 | $1.353 \times 10^{-7} \\ 1.353 \times 10^{-7}$ | $\begin{array}{c} 1.3196 \times 10^{-2} \\ 7.4255 \times 10^{-3} \end{array}$ | 77.715 |
| pdb2lqp 428 | ClassicAll QuaternionAll | 2304 2304 | $5.7598 \times 10^{-4} 5.7598 \times 10^{-4}$ | 222 222 | $\begin{array}{c} 8.247 \times 10^{-8} \\ 8.247 \times 10^{-8} \end{array}$ | $6.5259 \times 10^{-1} 5.9247 \times 10^{-1}$ | 10.149 |
| pdb2lr0 806 | ClassicAll QuaternionAll | 16 16 | $1.2202 \times 10^{-11} \\ 1.1747 \times 10^{-11}$ | 5 5 | 3.549×10^{-12} 3.440×10^{-12} | 3.2315×10^{-1} 1.6220×10^{-1} | 99.236 |
| pdb2lrh 806 | ClassicAll QuaternionAll | 384 384 | $\begin{array}{c} 2.9721 \times 10^{-12} \\ 2.9099 \times 10^{-12} \end{array}$ | 189 189 | $5.631 \times 10^{-13} \\ 6.564 \times 10^{-13}$ | 8.9441×10^{-1} 4.8708×10^{-1} | 83.629 |
| pdb2ls9 152 | ClassicAll QuaternionAll | 16 16 | $\begin{array}{c} 2.7045 \times 10^{-12} \\ 3.0425 \times 10^{-12} \end{array}$ | 5 5 | $\begin{array}{c} 1.122 \times 10^{-13} \\ 1.471 \times 10^{-13} \end{array}$ | $1.6481 \times 10^{-3} \\ 1.1036 \times 10^{-3}$ | 49.336 |
| pdb2lsa 140 | ClassicAll QuaternionAll | 8 8 | $2.5535 \times 10^{-3} 2.5535 \times 10^{-3}$ | $\frac{2}{2}$ | 5.235×10^{-14} 6.998×10^{-14} | 9.4580×10^{-4} 6.1781×10^{-4} | 53.090 |
| pdb2lss 422 | ClassicAll QuaternionAll | 8 8 | 1.2372×10^{-3} 1.2372×10^{-3} | 1 1 | $1.230 \times 10^{-13} 1.455 \times 10^{-13}$ | $5.1730 \times 10^{-3} 3.0589 \times 10^{-3}$ | 69.115 |
| pdb2lt3 680 | ClassicAll QuaternionAll | 8 8 | $9.6961 \times 10^{-13} \\ 1.0253 \times 10^{-12}$ | 6 6 | $7.245 \times 10^{-14} 7.760 \times 10^{-14}$ | 6.6260×10^{-3} 3.9988×10^{-3} | 65.699 |
| pdb2lu6 86 | ClassicAll QuaternionAll | 8 8 | $7.7550 \times 10^{-3} 7.7550 \times 10^{-3}$ | 1 1 | $5.356 \times 10^{-15} \\ 6.922 \times 10^{-15}$ | 5.3252×10^{-4} 3.4349×10^{-4} | 55.034 |
| pdb2lx0 194 | ClassicAll QuaternionAll | 24576 24576 | $7.4851 \times 10^{-12} $ 7.5304×10^{-12} | 3285 3285 | 3.569×10^{-13} 4.035×10^{-13} | 3.7916 3.4710 | 9.238 |
| pdb2lxb 892 | ClassicAll QuaternionAll | 16 16 | $9.0172 \times 10^{-13} \\ 8.6577 \times 10^{-13}$ | 5 5 | $1.542 \times 10^{-13} 1.585 \times 10^{-13}$ | $2.6833 \times 10^{-2} \\ 1.3296 \times 10^{-2}$ | 101.818 |
| pdb2lzf 820 | ClassicAll QuaternionAll | 8 8 | $5.9653 \times 10^{-4} $ 5.9653×10^{-4} | 2 2 | 3.217×10^{-14} 3.959×10^{-14} | $8.1541 \times 10^{-1} \\ 3.9900 \times 10^{-1}$ | 104.361 |
| pdb2m1a 158 | ClassicAll QuaternionAll | 8 | $9.1771 \times 10^{-14} 9.0451 \times 10^{-14}$ | 1 1 | $6.346 \times 10^{-15} $ 7.612×10^{-15} | $1.0487 \times 10^{-3} 6.7610 \times 10^{-4}$ | 55.111 |
| pdb2m1j 182 | ClassicAll QuaternionAll | 32 32 | 1.5890×10^{-13} 1.6894×10^{-13} | 10 10 | $1.865 \times 10^{-14} $ 2.212×10^{-14} | 4.6872×10^{-3} 3.0380×10^{-3} | 54.286 |
| pdb2m2y 110 | ClassicAll QuaternionAll | 8 8 | 1.8177×10^{-3} 1.8177×10^{-3} | 1 1 | 2.699×10^{-13} 2.808×10^{-13} | 9.8928×10^{-4} 6.0391×10^{-4} | 63.811 |

Table 2: Results - continued

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $\text{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|-----------------|-----------------------------|-----------------|---|-------------------------------------|---|---|-------------|
| pdb2m3f 134 | ClassicAll QuaternionAll | 16 16 | $9.5240 \times 10^{-14} $ 5.7597×10^{-14} | 5 5 | 3.629×10^{-14} 4.641×10^{-14} | $1.1373 \times 10^{-3} \\ 8.1308 \times 10^{-4}$ | 39.873 |
| pdb2m8m 170 | ClassicAll QuaternionAll | 8 8 | $6.9769 \times 10^{-3} 6.9769 \times 10^{-3}$ | 5 5 | $\begin{array}{c} 2.424 \times 10^{-14} \\ 3.058 \times 10^{-14} \end{array}$ | $\begin{array}{c} 1.1476 \times 10^{-3} \\ 7.3245 \times 10^{-4} \end{array}$ | 56.679 |
| pdb2m8o 170 | ClassicAll QuaternionAll | 16 16 | $4.6389 \times 10^{-3} 4.6389 \times 10^{-3}$ | 9 9 | $1.337 \times 10^{-7} \\ 1.337 \times 10^{-7}$ | 1.4163×10^{-3} 1.0138×10^{-3} | 39.702 |
| pdb2m97 416 | ClassicAll QuaternionAll | 8 8 | $2.4560 \times 10^{-12} 2.4592 \times 10^{-12}$ | 6 6 | $4.654 \times 10^{-14} 5.847 \times 10^{-14}$ | 2.9164×10^{-3} 1.8606×10^{-3} | 56.747 |
| pdb2m9g 1108 | ClassicAll QuaternionAll | 24 24 | $4.9692 \times 10^{-12} 4.9567 \times 10^{-12}$ | 9 9 | $2.939 \times 10^{-13} 3.170 \times 10^{-13}$ | $4.0916 \times 10^{-2} 2.4525 \times 10^{-2}$ | 66.833 |
| pdb2m9r 242 | ClassicAll QuaternionAll | 65536 65536 | $3.7505 \times 10^{-12} 3.6480 \times 10^{-12}$ | 7301 7301 | $3.537 \times 10^{-14} 4.406 \times 10^{-14}$ | 3.1853×10^{1} 2.3239×10^{1} | 37.069 |
| pdb2mdv 460 | ClassicAll QuaternionAll | 16 16 | $4.7210 \times 10^{-4} 4.7210 \times 10^{-4}$ | 6 6 | $3.178 \times 10^{-12} \\ 3.178 \times 10^{-12}$ | 2.7738×10^{-1} 1.3787×10^{-1} | 101.182 |
| pdb2me1 164 | ClassicAll QuaternionAll | 30720 30720 | $2.7384 \times 10^{-5} 2.7384 \times 10^{-5}$ | 14030 14030 | $1.477 \times 10^{-6} 1.477 \times 10^{-6}$ | 4.8603 4.4062 | 10.305 |
| pdb2me3 164 | ClassicAll QuaternionAll | 8192 8192 | 1.1059×10^{-5} 1.1059×10^{-5} | 2542 2542 | $2.347 \times 10^{-7} 2.347 \times 10^{-7}$ | 8.2984×10^{-1} 7.6690×10^{-1} | 8.206 |
| pdb2me4 164 | ClassicAll QuaternionAll | 32768 32768 | $\begin{array}{c} 2.9241 \times 10^{-5} \\ 2.9241 \times 10^{-5} \end{array}$ | 854 854 | $2.758 \times 10^{-7} $ 2.758×10^{-7} | 4.9982 4.2398 | 17.888 |
| pdb2mg1 164 | ClassicAll QuaternionAll | 8 8 | 4.4954×10^{-13} 5.4976×10^{-13} | 6 6 | $4.400 \times 10^{-14} 5.374 \times 10^{-14}$ | $1.1133 \times 10^{-3} 7.1597 \times 10^{-4}$ | 55.501 |
| pdb2mg2 170 | ClassicAll QuaternionAll | 16 16 | $\begin{array}{c} 1.0745 \times 10^{-3} \\ 1.0745 \times 10^{-3} \end{array}$ | 10 10 | $1.831 \times 10^{-14} 2.481 \times 10^{-14}$ | 1.5972×10^{-3} 1.1089×10^{-3} | 44.026 |
| pdb2mg3 170 | ClassicAll QuaternionAll | 16 16 | $6.2977 \times 10^{-13} 6.7812 \times 10^{-13}$ | 14 14 | 3.542×10^{-14} 4.459×10^{-14} | 1.9385×10^{-3} 1.2821×10^{-3} | 51.199 |
| pdb2mh8 338 | ClassicAll QuaternionAll | 40 40 | $4.2246 \times 10^{-12} 4.0208 \times 10^{-12}$ | 26 26 | $1.547 \times 10^{-13} 1.883 \times 10^{-13}$ | $5.3693 \times 10^{-3} $ 4.2367×10^{-3} | 26.731 |
| pdb2mhw 164 | ClassicAll QuaternionAll | 8 8 | $3.6932 \times 10^{-3} 3.6932 \times 10^{-3}$ | 2 2 | $6.229 \times 10^{-14} 7.130 \times 10^{-14}$ | $1.1186 \times 10^{-3} 7.2620 \times 10^{-4}$ | 54.037 |
| pdb2mij 224 | ClassicAll QuaternionAll | 16 16 | $1.2077 \times 10^{-12} 1.2294 \times 10^{-12}$ | 1 1 | 1.244×10^{-13} 1.522×10^{-13} | 5.3586×10^{-3} 3.1245×10^{-3} | 71.501 |
| pdb2mix 128 | ClassicAll QuaternionAll | 8 8 | 3.7545×10^{-13} 3.4098×10^{-13} | 1 1 | $4.816 \times 10^{-14} $ 4.684×10^{-14} | $1.4998 \times 10^{-3} 8.7949 \times 10^{-4}$ | 70.536 |
| pdb2mj1 110 | ClassicAll QuaternionAll | 168 168 | $8.6589 \times 10^{-4} 8.6589 \times 10^{-4}$ | 45 45 | $4.712 \times 10^{-7} 4.712 \times 10^{-7}$ | 7.9187×10^{-3} 6.1154×10^{-3} | 29.487 |
| pdb2mj2 218 | ClassicAll QuaternionAll | 32 32 | $3.7278 \times 10^{-3} 3.7278 \times 10^{-3}$ | 2 2 | $1.591 \times 10^{-7} \\ 1.591 \times 10^{-7}$ | $3.2246 \times 10^{-3} 2.3628 \times 10^{-3}$ | 36.475 |
| pdb2mjg 556 | ClassicAll QuaternionAll | $256 \\ 256$ | 1.4274×10^{-3} 1.4274×10^{-3} | 94 94 | 9.193×10^{-9} 9.193×10^{-9} | $7.6677 \times 10^{-1} 4.0430 \times 10^{-1}$ | 89.651 |
| pdb2mle 434 | ClassicAll QuaternionAll | 16 16 | 1.6719×10^{-3} 1.6719×10^{-3} | 6 6 | $1.491 \times 10^{-13} 1.535 \times 10^{-13}$ | $\begin{array}{c} 1.0910 \times 10^{-1} \\ 5.2413 \times 10^{-2} \end{array}$ | 108.158 |
| pdb2mlf 434 | ClassicAll QuaternionAll | 16 16 | $8.3036 \times 10^{-13} 8.8493 \times 10^{-13}$ | 6 6 | 9.918×10^{-14} 1.127×10^{-13} | $7.1563 \times 10^{-3} $ 4.3921×10^{-3} | 62.937 |
| pdb2mpu 554 | ClassicAll QuaternionAll | 8 8 | $2.5305 \times 10^{-12} 2.5592 \times 10^{-12}$ | 1 1 | $9.785 \times 10^{-14} 1.016 \times 10^{-13}$ | $1.7354 \times 10^{-2} 8.5980 \times 10^{-3}$ | 101.834 |
| pdb2mra 704 | ClassicAll QuaternionAll | 40 40 | $4.3616 \times 10^{-12} 4.3117 \times 10^{-12}$ | 9 9 | 2.632×10^{-13} 2.768×10^{-13} | $8.2104 \times 10^{-2} 4.3431 \times 10^{-2}$ | 89.047 |
| pdb2msu 122 | ClassicAll QuaternionAll | $1152 \\ 1152$ | $3.6237 \times 10^{-12} 3.6441 \times 10^{-12}$ | 29 29 | $7.813 \times 10^{-14} \\ 8.765 \times 10^{-14}$ | $7.9977 \times 10^{-2} 6.5515 \times 10^{-2}$ | 22.074 |
| pdb2mty 120 | ClassicAll QuaternionAll | 16 16 | 5.1232×10^{-12} 5.2129×10^{-12} | 16 16 | $1.848 \times 10^{-14} $ 2.363×10^{-14} | 1.7035×10^{-3} 1.0728×10^{-3} | 58.793 |
| pdb2muh 98 | ClassicAll QuaternionAll | 18432 18432 | $1.3995 \times 10^{-5} 1.3995 \times 10^{-5}$ | 5070 5070 | $4.190 \times 10^{-7} 4.190 \times 10^{-7}$ | $1.5133 \times 10^{1} \\ 8.1914$ | 84.741 |

Table 2: Results - continued

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $\text{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|-----------------|-----------------------------|------------------|---|-------------------------------------|---|---|-------------|
| pdb2mvj 156 | ClassicAll QuaternionAll | 64 64 | $6.1752 \times 10^{-12} $ 6.1858×10^{-12} | 3 3 | $1.534 \times 10^{-13} 1.647 \times 10^{-13}$ | $6.0424 \times 10^{-3} 4.1485 \times 10^{-3}$ | 45.652 |
| pdb2n00 572 | ClassicAll QuaternionAll | $1024 \\ 1024$ | $\begin{array}{c} 9.6419 \times 10^{-5} \\ 9.6419 \times 10^{-5} \end{array}$ | 342 342 | $\begin{array}{c} 3.910 \times 10^{-7} \\ 3.910 \times 10^{-7} \end{array}$ | $\begin{array}{c} 1.0703 \\ 7.0664 \times 10^{-1} \end{array}$ | 51.460 |
| pdb2n0b 60 | ClassicAll QuaternionAll | 573440 573440 | 1.0219×10^{-11} 1.0781×10^{-11} | 516662 516662 | $7.123 \times 10^{-13} 9.477 \times 10^{-13}$ | $1.3982 \times 10^2 \\ 1.1558 \times 10^2$ | 20.970 |
| pdb2n0c 60 | ClassicAll QuaternionAll | 409600 409600 | $1.0471 \times 10^{-12} 9.1394 \times 10^{-13}$ | 136912 136912 | 1.293×10^{-13} 1.682×10^{-13} | $8.1007 \times 10^{1} \\ 6.7311 \times 10^{1}$ | 20.347 |
| pdb2n0d 60 | ClassicAll QuaternionAll | 73728 73728 | $5.2061 \times 10^{-11} 5.7645 \times 10^{-11}$ | 61516 61516 | 3.639×10^{-12} 4.540×10^{-12} | 5.1307 4.5411 | 12.983 |
| pdb2n0e 60 | ClassicAll QuaternionAll | 448 448 | 1.1503×10^{-11} 1.8786×10^{-11} | 250 250 | 3.314×10^{-12} 4.286×10^{-12} | 2.2131×10^{-2} 1.2801×10^{-2} | 72.891 |
| pdb2n0f 60 | ClassicAll QuaternionAll | 24 24 | $2.2697 \times 10^{-12} 2.7490 \times 10^{-12}$ | 8 8 | 3.185×10^{-13} 4.023×10^{-13} | 2.3725×10^{-3} 1.3768×10^{-3} | 72.326 |
| pdb2n0g 60 | ClassicAll QuaternionAll | 2048 2048 | $1.4896 \times 10^{-11} \\ 1.4974 \times 10^{-11}$ | 1022 1022 | $8.315 \times 10^{-13} 9.618 \times 10^{-13}$ | $5.8145 \times 10^{-2} 5.7030 \times 10^{-2}$ | 1.955 |
| pdb2n0h 60 | ClassicAll QuaternionAll | 2048 2048 | $4.1935 \times 10^{-12} 4.1379 \times 10^{-12}$ | $2022 \\ 2022$ | $7.716 \times 10^{-13} \\ 8.755 \times 10^{-13}$ | $5.1485 \times 10^{-2} 5.4972 \times 10^{-2}$ | -6.344 |
| pdb2n35 314 | ClassicAll QuaternionAll | $256 \\ 256$ | $1.4234 \times 10^{-4} \\ 1.4234 \times 10^{-4}$ | 202 202 | $4.067 \times 10^{-8} 4.067 \times 10^{-8}$ | 3.9782×10^{-2} 2.9834×10^{-2} | 33.346 |
| pdb2n3a 574 | ClassicAll QuaternionAll | 64 64 | $\begin{array}{c} 2.1457 \times 10^{-3} \\ 2.1457 \times 10^{-3} \end{array}$ | 45 45 | $8.770 \times 10^{-14} 1.049 \times 10^{-13}$ | $6.4307 \times 10^{-1} \\ 3.1953 \times 10^{-1}$ | 101.256 |
| pdb2n41 638 | ClassicAll QuaternionAll | 384 384 | $\begin{array}{c} 3.6179 \times 10^{-3} \\ 3.6179 \times 10^{-3} \end{array}$ | $\frac{374}{374}$ | $\begin{array}{c} 1.067 \times 10^{-7} \\ 1.067 \times 10^{-7} \end{array}$ | $4.6591 \times 10^{-1} 2.6788 \times 10^{-1}$ | 73.925 |
| pdb2n4e 638 | ClassicAll QuaternionAll | 64 64 | $\begin{array}{c} 4.6757 \times 10^{-3} \\ 4.6757 \times 10^{-3} \end{array}$ | 18 18 | $\begin{array}{c} 1.081 \times 10^{-7} \\ 1.081 \times 10^{-7} \end{array}$ | $\begin{array}{c} 5.5445 \times 10^{-2} \\ 3.2210 \times 10^{-2} \end{array}$ | 72.139 |
| pdb2n67 566 | ClassicAll QuaternionAll | 16 16 | $2.0736 \times 10^{-12} 2.0936 \times 10^{-12}$ | 1 1 | $4.443 \times 10^{-13} 4.465 \times 10^{-13}$ | $7.6106 \times 10^{-3} $ 4.8955×10^{-3} | 55.460 |
| pdb2n7j 336 | ClassicAll QuaternionAll | 2 2 | $2.5110 \times 10^{-12} 2.6436 \times 10^{-12}$ | 1 1 | $5.969 \times 10^{-13} 6.094 \times 10^{-13}$ | 9.3849×10^{-2} 4.3939×10^{-2} | 113.589 |
| pdb2na9 266 | ClassicAll QuaternionAll | 96 96 | $\begin{array}{c} 2.3390 \times 10^{-12} \\ 2.3721 \times 10^{-12} \end{array}$ | 33 33 | 5.440×10^{-14} 6.690×10^{-14} | $\begin{array}{c} 2.0714 \times 10^{-2} \\ 1.2074 \times 10^{-2} \end{array}$ | 71.554 |
| pdb2ndc 110 | ClassicAll QuaternionAll | 8 8 | $\begin{array}{c} 3.1313 \times 10^{-3} \\ 3.1313 \times 10^{-3} \end{array}$ | $\frac{2}{2}$ | 3.365×10^{-14} 4.481×10^{-14} | $7.2414 \times 10^{-4} 4.7306 \times 10^{-4}$ | 53.077 |
| pdb2nde 110 | ClassicAll QuaternionAll | 8 8 | 8.5286×10^{-5} 8.5286×10^{-5} | 2 2 | 7.022×10^{-14} 8.855×10^{-14} | $7.2508 \times 10^{-4} 4.6803 \times 10^{-4}$ | 54.924 |
| pdb2nvj 152 | ClassicAll QuaternionAll | 8 8 | $6.7520 \times 10^{-3} 6.7520 \times 10^{-3}$ | 7 7 | 2.082×10^{-14} 2.293×10^{-14} | $1.0214 \times 10^{-3} \\ 6.6588 \times 10^{-4}$ | 53.387 |
| pdb2p6j 314 | ClassicAll QuaternionAll | 8 8 | 3.2640×10^{-13} 3.5480×10^{-13} | 1 1 | 4.795×10^{-14} 6.389×10^{-14} | $2.1989 \times 10^{-3} \\ 1.4052 \times 10^{-3}$ | 56.475 |
| pdb2rlg 108 | ClassicAll QuaternionAll | 8 8 | $\begin{array}{c} 4.8140 \times 10^{-13} \\ 5.3066 \times 10^{-13} \end{array}$ | $\frac{2}{2}$ | $5.501 \times 10^{-14} \\ 6.973 \times 10^{-14}$ | $\begin{array}{c} 2.2010 \times 10^{-3} \\ 1.2342 \times 10^{-3} \end{array}$ | 78.342 |
| pdb2rlh 108 | ClassicAll QuaternionAll | 8 8 | $1.0750 \times 10^{-12} 1.0423 \times 10^{-12}$ | 3 | $4.772 \times 10^{-14} 5.801 \times 10^{-14}$ | $1.5218 \times 10^{-3} \\ 8.8788 \times 10^{-4}$ | 71.391 |
| pdb2rmy 206 | ClassicAll QuaternionAll | 10240 10240 | $1.1655 \times 10^{-4} \\ 1.1655 \times 10^{-4}$ | 2805 2805 | $1.609 \times 10^{-7} 1.609 \times 10^{-7}$ | 1.5063 1.3421 | 12.235 |
| pdb2roo 260 | ClassicAll QuaternionAll | 16 16 | $3.0591 \times 10^{-4} 3.0591 \times 10^{-4}$ | 14 14 | 3.610×10^{-6} 3.610×10^{-6} | $4.2128 \times 10^{-2} 2.2029 \times 10^{-2}$ | 91.237 |
| pdb2rut 218 | ClassicAll QuaternionAll | 96 96 | $2.0579 \times 10^{-13} $ 4.0546×10^{-13} | 26 26 | 4.389×10^{-14} 5.013×10^{-14} | $1.9890 \times 10^{-2} 1.1147 \times 10^{-2}$ | 78.435 |
| pdb2ruv 224 | ClassicAll QuaternionAll | 32 32 | 5.4278×10^{-13} 6.5510×10^{-13} | 6 6 | $5.775 \times 10^{-14} 7.404 \times 10^{-14}$ | 4.8844×10^{-3} 3.2191×10^{-3} | 51.730 |
| pdb2rux 218 | ClassicAll QuaternionAll | 192 192 | 3.4373×10^{-3} 3.4373×10^{-3} | 49 49 | $3.717 \times 10^{-7} \\ 3.717 \times 10^{-7}$ | $2.7441 \times 10^{-2} 1.9435 \times 10^{-2}$ | 41.195 |
| | | | | | | | |

Table 2: Results - continued

| Problem Size | Method | $ \mathcal{X} $ | $\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$ | $i: \mathbf{x_i} \sim \mathbf{x}_o$ | $\text{MDE}(\mathbf{x}_i)$ | Time | Improv time |
|-----------------|-----------------------------|-----------------|---|-------------------------------------|---|--|-------------|
| pdb2ruy 224 | ClassicAll QuaternionAll | 384 384 | $4.1535 \times 10^{-13} \\ 3.5904 \times 10^{-13}$ | 17 17 | $1.968 \times 10^{-14} $ 2.387×10^{-14} | $2.8761 \times 10^{-2} 2.5472 \times 10^{-2}$ | 12.910 |
| pdb2rv3 218 | ClassicAll QuaternionAll | 16 16 | 3.0630×10^{-4} 3.0630×10^{-4} | 5 5 | $\begin{array}{c} 3.656 \times 10^{-14} \\ 4.118 \times 10^{-14} \end{array}$ | 3.3604×10^{-3} 2.0977×10^{-3} | 60.197 |
| pdb2rv5 212 | ClassicAll QuaternionAll | 192 192 | $7.5780 \times 10^{-4} 7.5780 \times 10^{-4}$ | 29 29 | $1.857 \times 10^{-7} 1.857 \times 10^{-7}$ | 3.7516×10^{-2} 2.3951×10^{-2} | 56.635 |