Consolidated Performance Tests

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1 Benchmark's tables

1.1 Using BP-One versions

Table 1: Results

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Problem Size	Method	MDE	RMSD	Time	Ratio
pdb1a57 698	Classic Quaternion	$2.096 \times 10^{-11} 2.092 \times 10^{-11}$	1.8861×10^{-12}	1.7078×10^{-3} 1.0276×10^{-3}	0.602
pdb1b4c 1108	Classic Quaternion	$5.070 \times 10^{-13} 5.498 \times 10^{-13}$	1.0757×10^{-12}	$3.5365 \times 10^{-3} 2.5634 \times 10^{-3}$	0.725
pdb1ba5 320	Classic Quaternion	$9.359 \times 10^{-13} 1.070 \times 10^{-12}$	4.1376×10^{-12}	$\begin{array}{c} 3.6012 \times 10^{-4} \\ 2.7669 \times 10^{-4} \end{array}$	0.768
pdb1d1n 594	Classic Quaternion	$1.005 \times 10^{-11} 9.672 \times 10^{-12}$	1.2689×10^{-12}	$5.9682 \times 10^{-4} 4.7694 \times 10^{-4}$	0.799
pdb1dp3 332	Classic Quaternion	7.704×10^{-13} 8.939×10^{-13}	1.4697×10^{-12}	2.9789×10^{-4} 2.3080×10^{-4}	0.775
pdb1du1 122	Classic Quaternion	$8.225 \times 10^{-13} \\ 1.258 \times 10^{-12}$	1.2376×10^{-12}	1.0246×10^{-4} 7.8000×10^{-5}	0.761
pdb1eii 806	Classic Quaternion	1.393×10^{-11} 1.365×10^{-11}	1.1331×10^{-11}	8.2178×10^{-4} 6.5466×10^{-4}	0.797
pdb1fcl 338	Classic Quaternion	4.542×10^{-12} 4.515×10^{-12}	8.0786×10^{-13}	$4.5137 \times 10^{-4} \\ 3.4246 \times 10^{-4}$	0.759
pdb1fd6 344	Classic Quaternion	3.182×10^{-12} 3.193×10^{-12}	3.3846×10^{-13}	3.4143×10^{-4} 2.6441×10^{-4}	0.774
pdb1hf9 496	Classic Quaternion	$1.157 \times 10^{-11} \\ 1.180 \times 10^{-11}$	3.9332×10^{-12}	9.6480×10^{-3} 6.1200×10^{-3}	0.634
pdb1i2u 266	Classic Quaternion	5.562×10^{-13} 5.607×10^{-13}	1.5136×10^{-13}	2.5459×10^{-4} 2.0184×10^{-4}	0.793
pdb1i2v 266	Classic Quaternion	$2.418 \times 10^{-13} 2.519 \times 10^{-13}$	6.9127×10^{-14}	2.7989×10^{-4} 2.2032×10^{-4}	0.787
pdb1ijc 380	Classic Quaternion	$1.408 \times 10^{-11} \\ 1.426 \times 10^{-11}$	2.4877×10^{-12}	5.5728×10^{-4} 4.1998×10^{-4}	0.754
pdb1jlz 140	Classic Quaternion	5.594×10^{-13} 5.965×10^{-13}	1.3105×10^{-12}	$\begin{array}{c} 1.2392 \times 10^{-4} \\ 9.5602 \times 10^{-5} \end{array}$	0.771
pdb1jw3 842	Classic Quaternion	5.936×10^{-13} 5.897×10^{-13}	3.9013×10^{-13}	8.6446×10^{-4} 6.7580×10^{-4}	0.782
pdb1k0v 440	Classic Quaternion	1.893×10^{-13} 1.894×10^{-13}	1.3433×10^{-13}	$4.6703 \times 10^{-4} 3.5593 \times 10^{-4}$	0.762
pdb1k2h 1120	Classic Quaternion	5.491×10^{-13} 5.199×10^{-13}	2.2039×10^{-13}	2.9241×10^{-3} 1.9975×10^{-3}	0.683
pdb1k36 278	Classic Quaternion	8.820×10^{-12} 1.081×10^{-11}	2.8981×10^{-11}	2.6454×10^{-4} 1.9812×10^{-4}	0.749
pdb1k37 278	Classic Quaternion	$4.711 \times 10^{-13} 4.988 \times 10^{-13}$	1.5479×10^{-13}	3.8419×10^{-4} 2.7588×10^{-4}	0.718
pdb1kuw 62	Classic Quaternion	9.229×10^{-14} 1.130×10^{-13}	7.3457×10^{-14}	$5.8623 \times 10^{-5} 4.3799 \times 10^{-5}$	0.747
pdb1kz0 98	Classic Quaternion	4.404×10^{-14} 5.880×10^{-14}	2.4335×10^{-13}	9.2082×10^{-5} 6.9233×10^{-5}	0.752
pdb1kz2 98	Classic Quaternion	$2.119 \times 10^{-14} 2.886 \times 10^{-14}$	2.6112×10^{-14}	1.0225×10^{-4} 7.2798×10^{-5}	0.712
pdb1kz5 74	Classic Quaternion	4.081×10^{-14} 4.738×10^{-14}	4.8348×10^{-14}	$7.3916 \times 10^{-5} 5.2574 \times 10^{-5}$	0.711
pdb1lvz 68	Classic Quaternion	$6.336 \times 10^{-14} 7.315 \times 10^{-14}$	7.3919×10^{-14}	$6.5156 \times 10^{-5} 4.6871 \times 10^{-5}$	0.719
pdb1m4e 122	Classic Quaternion	5.949×10^{-13} 5.972×10^{-13}	1.1702×10^{-13}	$1.3874 \times 10^{-4} \\ 8.5423 \times 10^{-5}$	0.616

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb1ma2 104	Classic Quaternion	$8.695 \times 10^{-12} \\ 8.758 \times 10^{-12}$	4.7062×10^{-13}	2.3923×10^{-4} 1.0667×10^{-4}	0.446
pdb1ma4 104	Classic Quaternion	$7.247 \times 10^{-14} 7.981 \times 10^{-14}$	1.8851×10^{-13}	$4.1287 \times 10^{-4} \\ 1.7248 \times 10^{-4}$	0.418
pdb1ma5 104	Classic Quaternion	8.169×10^{-13} 9.044×10^{-13}	5.0234×10^{-13}	1.5005×10^{-4} 7.2148×10^{-5}	0.481
pdb1ma6 104	Classic Quaternion	$6.283 \times 10^{-13} \\ 8.522 \times 10^{-13}$	3.3052×10^{-12}	$1.4103 \times 10^{-4} 7.0075 \times 10^{-5}$	0.497
pdb1mpe 1352	Classic Quaternion	$2.617 \times 10^{-11} \\ 2.624 \times 10^{-11}$	7.1261×10^{-13}	8.1131×10^{-3} 3.4902×10^{-3}	0.430
pdb1nd9 296	Classic Quaternion	3.026×10^{-13} 3.845×10^{-13}	4.7137×10^{-13}	$4.5081 \times 10^{-4} $ 2.2590×10^{-4}	0.501
pdb1ne5 254	Classic Quaternion	1.214×10^{-12} 1.384×10^{-12}	7.5582×10^{-13}	3.6696×10^{-4} 1.8293×10^{-4}	0.498
pdb1nmj 170	Classic Quaternion	$1.237 \times 10^{-14} \\ 1.424 \times 10^{-14}$	1.3921×10^{-14}	2.6603×10^{-4} 1.3008×10^{-4}	0.489
pdb1o53 92	Classic Quaternion	3.999×10^{-13} 4.545×10^{-13}	6.5350×10^{-13}	1.4899×10^{-4} 6.9913×10^{-5}	0.469
pdb1oqp 580	Classic Quaternion	7.045×10^{-14} 8.315×10^{-14}	9.0066×10^{-14}	3.0062×10^{-3} 1.6903×10^{-3}	0.562
pdb1plw 32	Classic Quaternion	2.830×10^{-14} 3.122×10^{-14}	4.9118×10^{-14}	$4.5461 \times 10^{-5} \\ 2.2201 \times 10^{-5}$	0.488
pdb1plx 32	Classic Quaternion	$1.574 \times 10^{-13} 2.060 \times 10^{-13}$	1.7973×10^{-13}	$4.2650 \times 10^{-5} $ 2.0929×10^{-5}	0.491
pdb1pv0 278	Classic Quaternion	2.409×10^{-13} 2.723×10^{-13}	1.0662×10^{-13}	$4.4412 \times 10^{-4} \\ 2.0904 \times 10^{-4}$	0.471
pdb1pzr 724	Classic Quaternion	$5.644 \times 10^{-12} 5.871 \times 10^{-12}$	9.9935×10^{-12}	6.4490×10^{-3} 3.5690×10^{-3}	0.553
pdb1qlk 1108	Classic Quaternion	$9.019 \times 10^{-10} 9.019 \times 10^{-10}$	1.3287×10^{-12}	$1.0829 \times 10^{-2} 5.9579 \times 10^{-3}$	0.550
pdb1r57 614	Classic Quaternion	$1.847 \times 10^{-13} 2.054 \times 10^{-13}$	1.4866×10^{-13}	9.6998×10^{-4} 4.8680×10^{-4}	0.502
pdb1ry3 386	Classic Quaternion	4.938×10^{-13} 5.910×10^{-13}	4.7678×10^{-13}	$6.3087 \times 10^{-4} \\ 3.0993 \times 10^{-4}$	0.491
pdb1s4h 80	Classic Quaternion	4.300×10^{-9} 4.300×10^{-9}	1.1103×10^{-12}	$1.0674 \times 10^{-4} 5.3186 \times 10^{-5}$	0.498
pdb1s4j 80	Classic Quaternion	1.520×10^{-13} 2.230×10^{-13}	1.6407×10^{-13}	$1.2866 \times 10^{-4} \\ 6.7311 \times 10^{-5}$	0.523
pdb1s6j 524	Classic Quaternion	$6.073 \times 10^{-13} 7.660 \times 10^{-13}$	5.9201×10^{-13}	7.9899×10^{-4} 4.0640×10^{-4}	0.509
pdb1sa8 638	Classic Quaternion	$9.340 \times 10^{-13} \\ 1.034 \times 10^{-12}$	1.0370×10^{-12}	$9.9482 \times 10^{-4} \\ 5.2774 \times 10^{-4}$	0.530
$\begin{array}{c} pdb1t2y\\152\end{array}$	Classic Quaternion	$1.887 \times 10^{-13} 2.396 \times 10^{-13}$	2.3861×10^{-13}	$2.3413 \times 10^{-4} \\ 1.4533 \times 10^{-4}$	0.621
pdb1t5q 180	Classic Quaternion	3.877×10^{-14} 5.093×10^{-14}	5.3231×10^{-14}	2.5394×10^{-4} 1.3255×10^{-4}	0.522
pdb1tot 314	Classic Quaternion	$6.148 \times 10^{-14} \\ 6.853 \times 10^{-14}$	2.8392×10^{-14}	$5.0126 \times 10^{-4} \\ 3.1670 \times 10^{-4}$	0.632
pdb1v6r 128	Classic Quaternion	$6.835 \times 10^{-13} 6.970 \times 10^{-13}$	3.1917×10^{-13}	1.9619×10^{-4} 1.1899×10^{-4}	0.607
pdb1v92 278	Classic Quaternion	$1.463 \times 10^{-13} \\ 1.630 \times 10^{-13}$	5.6062×10^{-14}	$4.3360 \times 10^{-4} $ 2.6571×10^{-4}	0.613
pdb1vd7 140	Classic Quaternion	3.741×10^{-9} 3.741×10^{-9}	5.8433×10^{-13}	$2.0593 \times 10^{-4} 1.2499 \times 10^{-4}$	0.607
-		3.741×10^{-9}	5.8433×10^{-13}		0.607

Table 2: Results - continued

Problem Size	Method MDE RMSD Time		Ratio		
pdb1vd9 140	Classic Quaternion	$1.290 \times 10^{-12} \\ 1.554 \times 10^{-12}$	9.0327×10^{-13}	$2.4388 \times 10^{-4} \\ 1.4591 \times 10^{-4}$	0.598
pdb1vdb 140	Classic Quaternion	$9.108 \times 10^{-13} \\ 1.083 \times 10^{-12}$	3.8641×10^{-13}	$\begin{array}{c} 1.9946 \times 10^{-4} \\ 1.1987 \times 10^{-4} \end{array}$	0.601
$\begin{array}{c} \mathrm{pdb1vpc} \\ 272 \end{array}$	Classic Quaternion	$8.500 \times 10^{-15} 1.002 \times 10^{-14}$	8.5436×10^{-15}	$4.1694 \times 10^{-4} 2.6033 \times 10^{-4}$	0.624
pdb1wnk 140	Classic Quaternion	$4.112 \times 10^{-12} 4.632 \times 10^{-12}$	2.2335×10^{-11}	$2.0699 \times 10^{-4} 1.2347 \times 10^{-4}$	0.596
pdb1wo4 152	Classic Quaternion	$9.957 \times 10^{-13} 9.639 \times 10^{-13}$	2.3523×10^{-12}	$2.3205 \times 10^{-4} 1.4194 \times 10^{-4}$	0.612
pdb1wo5 152	Classic Quaternion	$5.257 \times 10^{-9} 5.258 \times 10^{-9}$	4.9063×10^{-12}	$2.3551 \times 10^{-4} 1.4405 \times 10^{-4}$	0.612
pdb1x60 476	Classic Quaternion	$1.076 \times 10^{-12} 1.179 \times 10^{-12}$	3.9684×10^{-13}	7.9397×10^{-4} 4.9474×10^{-4}	0.623
pdb1x9v 544	Classic Quaternion	$8.975 \times 10^{-13} 9.632 \times 10^{-13}$	1.3900×10^{-13}	$2.7541 \times 10^{-2} 1.4581 \times 10^{-2}$	0.529
pdb1y5c 68	Classic Quaternion	8.980×10^{-9} 8.980×10^{-9}	2.9085×10^{-13}	$9.7438 \times 10^{-5} 5.8897 \times 10^{-5}$	0.604
pdb1yx7 500	Classic Quaternion	$8.116 \times 10^{-10} \\ 8.125 \times 10^{-10}$	7.6614×10^{-12}	$1.1530 \times 10^{-3} 7.0746 \times 10^{-4}$	0.614
pdb1yx8 500	Classic Quaternion	$7.276 \times 10^{-12} \\ 8.217 \times 10^{-12}$	1.0819×10^{-11}	$\begin{array}{c} 9.4071 \times 10^{-4} \\ 5.8516 \times 10^{-4} \end{array}$	0.622
$\begin{array}{c} pdb1yxr\\ 464\end{array}$	Classic Quaternion	5.838×10^{-10} 5.839×10^{-10}	2.5240×10^{-13}	$6.7687 \times 10^{-4} 4.1626 \times 10^{-4}$	0.615
pdb2a2y 1072	Classic Quaternion	1.150×10^{-12} 1.151×10^{-12}	3.7416×10^{-13}	3.1010×10^{-2} 1.7439×10^{-2}	0.562
pdb2a4j 580	Classic Quaternion	$2.085 \times 10^{-14} $ 2.727×10^{-14}	1.4394×10^{-14}	$1.0563 \times 10^{-3} \\ 6.4214 \times 10^{-4}$	0.608
pdb2adl 868	Classic Quaternion	$1.752 \times 10^{-11} 1.787 \times 10^{-11}$	3.0093×10^{-12}	3.5641×10^{-2} 2.3248×10^{-2}	0.652
pdb2adn 868	Classic Quaternion	$6.693 \times 10^{-12} 6.465 \times 10^{-12}$	2.4957×10^{-12}	1.9119×10^{-3} 1.1481×10^{-3}	0.601
pdb2ajj 170	Classic Quaternion	$5.641 \times 10^{-14} \\ 6.584 \times 10^{-14}$	1.2744×10^{-13}	2.5994×10^{-4} 1.5702×10^{-4}	0.604
pdb2ajm 170	Classic Quaternion	1.183×10^{-13} 1.555×10^{-13}	8.9439×10^{-13}	2.7954×10^{-4} 1.6885×10^{-4}	0.604
pdb2ajn 170	Classic Quaternion	$1.076 \times 10^{-13} 1.217 \times 10^{-13}$	1.5981×10^{-13}	$2.7914 \times 10^{-4} 1.6719 \times 10^{-4}$	0.599
pdb2ajo 170	Classic Quaternion	1.183×10^{-13} 1.555×10^{-13}	8.9439×10^{-13}	2.7899×10^{-4} 1.6861×10^{-4}	0.604
pdb2akk 446	Classic Quaternion	1.288×10^{-13} 1.270×10^{-13}	1.1725×10^{-13}	$\begin{array}{c} 1.4448 \times 10^{-3} \\ 8.4721 \times 10^{-4} \end{array}$	0.586
pdb2bzb 748	Classic Quaternion	$9.365 \times 10^{-14} $ 1.224×10^{-13}	1.5097×10^{-13}	$1.4315 \times 10^{-2} 7.7992 \times 10^{-3}$	0.545
pdb2c0s 386	Classic Quaternion	$3.028 \times 10^{-13} 3.379 \times 10^{-13}$	7.2067×10^{-13}	6.2433×10^{-4} 3.8866×10^{-4}	0.623
pdb2dci 120	Classic Quaternion	$2.366 \times 10^{-14} 2.950 \times 10^{-14}$	1.3479×10^{-13}	$1.7238 \times 10^{-4} 1.0593 \times 10^{-4}$	0.615
pdb2eem 206	Classic Quaternion	5.190×10^{-13} 5.461×10^{-13}	4.0208×10^{-13}	$3.6143 \times 10^{-4} 2.1835 \times 10^{-4}$	0.604
pdb2fva 494	Classic Quaternion	1.047×10^{-12} 1.194×10^{-12}	1.5803×10^{-12}	$1.0303 \times 10^{-3} \\ 6.1618 \times 10^{-4}$	0.598
pdb2fvf 494	Classic Quaternion	$3.106 \times 10^{-13} \\ 3.445 \times 10^{-13}$	2.8750×10^{-13}	$7.4317 \times 10^{-4} 4.6101 \times 10^{-4}$	0.620

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2fxz 80	Classic Quaternion	1.489×10^{-12} 1.749×10^{-12}	2.0430×10^{-12}	1.2207×10^{-4} 7.5061×10^{-5}	0.615
pdb2g9j 848	Classic Quaternion	3.282×10^{-12} 3.535×10^{-12}	2.1668×10^{-12}	$4.9852 \times 10^{-2} 2.6562 \times 10^{-2}$	0.533
pdb2g9l 224	Classic Quaternion	$6.366 \times 10^{-14} \\ 8.672 \times 10^{-14}$	2.8081×10^{-13}	3.5082×10^{-4} 2.1658×10^{-4}	0.617
pdb2h5m 614	Classic Quaternion	$9.692 \times 10^{-13} \\ 1.032 \times 10^{-12}$	4.1376×10^{-12}	$9.9657 \times 10^{-4} \\ 6.2269 \times 10^{-4}$	0.625
pdb2hep 252	Classic Quaternion	$1.191 \times 10^{-12} \\ 1.268 \times 10^{-12}$	5.5848×10^{-13}	3.9601×10^{-4} 2.3695×10^{-4}	0.598
pdb2j0z 752	Classic Quaternion	3.192×10^{-10} 3.197×10^{-10}	4.5324×10^{-12}	2.3683×10^{-1} 1.4497×10^{-1}	0.612
pdb2j10 752	Classic Quaternion	5.870×10^{-10} 5.873×10^{-10}	9.5552×10^{-13}	$4.3767 \times 10^{-3} \\ 2.4477 \times 10^{-3}$	0.559
pdb2j11 752	Classic Quaternion	$7.191 \times 10^{-10} 7.194 \times 10^{-10}$	1.6970×10^{-12}	3.7834×10^{-3} 2.1799×10^{-3}	0.576
pdb2jmy 92	Classic Quaternion	9.834×10^{-13} 9.967×10^{-13}	5.0812×10^{-13}	$\begin{array}{c} 1.4579 \times 10^{-4} \\ 8.8216 \times 10^{-5} \end{array}$	0.605
pdb2jn5 74	Classic Quaternion	3.147×10^{-9} 3.160×10^{-9}	1.4394×10^{-11}	$\begin{array}{c} 1.0386 \times 10^{-4} \\ 6.2820 \times 10^{-5} \end{array}$	0.605
pdb2jnk 842	Classic Quaternion	$4.387 \times 10^{-10} 4.388 \times 10^{-10}$	3.9471×10^{-13}	$\begin{array}{c} 1.3640 \times 10^{-3} \\ 8.6217 \times 10^{-4} \end{array}$	0.632
pdb2jpn 476	Classic Quaternion	$6.730 \times 10^{-14} 6.983 \times 10^{-14}$	1.9605×10^{-13}	$1.1801 \times 10^{-3} \\ 6.8326 \times 10^{-4}$	0.579
pdb2jua 614	Classic Quaternion	$1.740 \times 10^{-11} \\ 1.882 \times 10^{-11}$	1.4391×10^{-11}	$1.0169 \times 10^{-3} \\ 6.2303 \times 10^{-4}$	0.613
pdb2jvd 288	Classic Quaternion	3.339×10^{-14} 3.898×10^{-14}	2.1712×10^{-14}	$4.7167 \times 10^{-4} $ 2.8141×10^{-4}	0.597
pdb2jwe 984	Classic Quaternion	$2.695 \times 10^{-11} 2.734 \times 10^{-11}$	1.0970×10^{-12}	$1.6909 \times 10^{-3} 1.0624 \times 10^{-3}$	0.628
$\begin{array}{c} \text{pdb2jws} \\ 338 \end{array}$	Classic Quaternion	$1.251 \times 10^{-13} 1.543 \times 10^{-13}$	2.8647×10^{-13}	5.6601×10^{-4} 3.4449×10^{-4}	0.609
pdb2jwu 338	Classic Quaternion	$\begin{array}{c} 4.421 \times 10^{-12} \\ 4.373 \times 10^{-12} \end{array}$	6.2322×10^{-13}	$7.6507 \times 10^{-4} 4.5845 \times 10^{-4}$	0.599
pdb2jxf 182	Classic Quaternion	$1.399 \times 10^{-13} 1.734 \times 10^{-13}$	5.8450×10^{-13}	2.8468×10^{-4} 1.6879×10^{-4}	0.593
pdb2jz5 548	Classic Quaternion	2.860×10^{-13} 2.854×10^{-13}	1.7635×10^{-13}	$1.0063 \times 10^{-3} \\ 6.1011 \times 10^{-4}$	0.606
pdb2k2a 422	Classic Quaternion	3.798×10^{-14} 5.134×10^{-14}	1.3435×10^{-13}	$7.2133 \times 10^{-4} 4.5278 \times 10^{-4}$	0.628
pdb2k2f 1268	Classic Quaternion	2.639×10^{-13} 2.818×10^{-13}	7.2949×10^{-14}	2.9933 1.5659	0.523
pdb2k36 896	Classic Quaternion	$1.922 \times 10^{-13} 2.045 \times 10^{-13}$	1.2563×10^{-13}	$\begin{array}{c} 1.4278 \times 10^{-3} \\ 8.9244 \times 10^{-4} \end{array}$	0.625
pdb2k37 356	Classic Quaternion	$1.921 \times 10^{-13} 2.525 \times 10^{-13}$	4.0204×10^{-13}	$5.7554 \times 10^{-4} 3.5444 \times 10^{-4}$	0.616
pdb2k3i 656	Classic Quaternion	3.810×10^{-13} 4.009×10^{-13}	2.4790×10^{-13}	$1.4433 \times 10^{-3} \\ 8.6964 \times 10^{-4}$	0.603
pdb2k6s 494	Classic Quaternion	2.100×10^{-13} 2.651×10^{-13}	4.8726×10^{-13}	$1.2378 \times 10^{-3} 7.1448 \times 10^{-4}$	0.577
pdb2k7o 1096	Classic Quaternion	1.279×10^{-13} 1.416×10^{-13}	4.6393×10^{-13}	$4.8228 \times 10^{-3} $ 2.7638×10^{-3}	0.573
pdb2kbm 1268	Classic Quaternion	$2.165 \times 10^{-13} $ 2.230×10^{-13}	2.6963×10^{-13}	$1.1020 \\ 6.7994 \times 10^{-1}$	0.617

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2kdh 434	Classic Quaternion	1.947×10^{-11} 2.228×10^{-11}	7.6317×10^{-11}	$7.8981 \times 10^{-4} 4.7942 \times 10^{-4}$	0.607
pdb2kdl 338	Classic Quaternion	$\begin{array}{c} 2.301 \times 10^{-13} \\ 2.927 \times 10^{-13} \end{array}$	3.1526×10^{-13}	5.4839×10^{-4} 3.3213×10^{-4}	0.606
pdb2kdm 338	Classic Quaternion	3.191×10^{-12} 3.284×10^{-12}	9.9439×10^{-13}	5.3480×10^{-4} 3.3159×10^{-4}	0.620
$\begin{array}{c} \mathrm{pdb2kdp} \\ 428 \end{array}$	Classic Quaternion	$2.621 \times 10^{-13} 2.865 \times 10^{-13}$	1.0772×10^{-13}	$6.8306 \times 10^{-4} 4.2205 \times 10^{-4}$	0.618
pdb2kdr 170	Classic Quaternion	$6.617 \times 10^{-14} \\ 8.490 \times 10^{-14}$	6.1679×10^{-14}	$2.7330 \times 10^{-4} 1.5899 \times 10^{-4}$	0.582
$\begin{array}{c} \text{pdb2kes} \\ 290 \end{array}$	Classic Quaternion	$4.468 \times 10^{-14} 5.425 \times 10^{-14}$	2.3286×10^{-14}	5.0386×10^{-4} 2.9163×10^{-4}	0.579
pdb2kib 352	Classic Quaternion	$2.533 \times 10^{-12} 2.539 \times 10^{-12}$	1.3388×10^{-12}	6.0079×10^{-3} 3.2111×10^{-3}	0.534
pdb2kjn 158	Classic Quaternion	$1.125 \times 10^{-9} \\ 1.125 \times 10^{-9}$	1.3817×10^{-13}	$2.4788 \times 10^{-4} 1.4894 \times 10^{-4}$	0.601
pdb2kjo 158	Classic Quaternion	2.284×10^{-13} 2.421×10^{-13}	6.7185×10^{-14}	$2.3357 \times 10^{-4} 1.4172 \times 10^{-4}$	0.607
pdb2kjr 572	Classic Quaternion	$3.247 \times 10^{-12} 3.251 \times 10^{-12}$	4.0637×10^{-13}	$1.4415 \times 10^{-3} \\ 8.5930 \times 10^{-4}$	0.596
pdb <mark>2kko</mark> 1300	Classic Quaternion	1.191×10^{-13} 1.285×10^{-13}	2.9766×10^{-14}	$8.6106 \times 10^{-3} $ 4.8727×10^{-3}	0.566
pdb2kl5 662	Classic Quaternion	$1.820 \times 10^{-13} 2.020 \times 10^{-13}$	1.3796×10^{-13}	$1.0275 \times 10^{-3} \\ 6.4496 \times 10^{-4}$	0.628
$\begin{array}{c} \text{pdb2klz} \\ 276 \end{array}$	Classic Quaternion	3.439×10^{-14} 4.443×10^{-14}	6.4874×10^{-14}	4.7020×10^{-4} 2.7869×10^{-4}	0.593
pdb2ko1 1060	Classic Quaternion	1.150×10^{-12} 1.151×10^{-12}	7.8450×10^{-13}	$1.2485 \times 10^{-2} 7.0322 \times 10^{-3}$	0.563
pdb2koz 200	Classic Quaternion	$1.075 \times 10^{-9} 1.075 \times 10^{-9}$	8.8024×10^{-13}	3.0575×10^{-4} 1.9136×10^{-4}	0.626
pdb2kp0 200	Classic Quaternion	$4.893 \times 10^{-12} 5.588 \times 10^{-12}$	4.2756×10^{-12}	3.0698×10^{-4} 1.8959×10^{-4}	0.618
pdb2ksg 290	Classic Quaternion	3.215×10^{-14} 3.967×10^{-14}	2.4678×10^{-14}	$\begin{array}{c} 4.3551 \times 10^{-4} \\ 2.6495 \times 10^{-4} \end{array}$	0.608
pdb2kt8 458	Classic Quaternion	3.314×10^{-12} 3.535×10^{-12}	7.1394×10^{-13}	7.0930×10^{-4} 4.4313×10^{-4}	0.625
pdb2kuh 404	Classic Quaternion	$2.016 \times 10^{-14} 2.492 \times 10^{-14}$	4.0485×10^{-14}	$6.8106 \times 10^{-4} 4.3151 \times 10^{-4}$	0.634
pdb2kwh 338	Classic Quaternion	$1.408 \times 10^{-13} \\ 1.825 \times 10^{-13}$	2.9549×10^{-13}	5.2925×10^{-4} 3.1747×10^{-4}	0.600
pdb2kxa 144	Classic Quaternion	$\begin{array}{c} 1.325 \times 10^{-12} \\ 1.351 \times 10^{-12} \end{array}$	3.5240×10^{-13}	$\begin{array}{c} 2.1473 \times 10^{-4} \\ 1.3425 \times 10^{-4} \end{array}$	0.625
pdb2kyb 362	Classic Quaternion	$1.321 \times 10^{-11} \\ 1.373 \times 10^{-11}$	2.6755×10^{-12}	$\begin{array}{c} 1.6400 \times 10^{-3} \\ 9.2684 \times 10^{-4} \end{array}$	0.565
pdb2l3m 428	Classic Quaternion	$1.028 \times 10^{-12} 9.340 \times 10^{-13}$	6.9725×10^{-13}	$6.7557 \times 10^{-4} 4.1986 \times 10^{-4}$	0.621
pdb2l3n 626	Classic Quaternion	3.025×10^{-14} 3.634×10^{-14}	4.4517×10^{-14}	$4.0176 \times 10^{-3} $ 2.2465×10^{-3}	0.559
pdb2l45 116	Classic Quaternion	2.236×10^{-14} 3.033×10^{-14}	8.5325×10^{-14}	$1.8187 \times 10^{-4} \\ 1.1228 \times 10^{-4}$	0.617
pdb2l5r 138	Classic Quaternion	3.529×10^{-14} 4.432×10^{-14}	1.4398×10^{-14}	2.4104×10^{-4} 1.4613×10^{-4}	0.606
pdb2l6q 374	Classic Quaternion	$4.959 \times 10^{-9} \\ 6.131 \times 10^{-9}$	1.7792×10^{-8}	5.7492×10^{-4} 3.4945×10^{-4}	0.608

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2l6r 374	Classic Quaternion	$7.323 \times 10^{-10} 7.325 \times 10^{-10}$	2.4265×10^{-11}	$6.1184 \times 10^{-4} \\ 3.7345 \times 10^{-4}$	0.610
pdb2l98 434	Classic Quaternion	$\begin{array}{c} 3.273 \times 10^{-13} \\ 3.638 \times 10^{-13} \end{array}$	8.9102×10^{-13}	$6.8739 \times 10^{-4} 4.2127 \times 10^{-4}$	0.613
pdb2lci 806	Classic Quaternion	$2.579 \times 10^{-13} 2.404 \times 10^{-13}$	8.2767×10^{-14}	$\begin{array}{c} 1.3251 \times 10^{-3} \\ 8.1420 \times 10^{-4} \end{array}$	0.614
pdb2lde 152	Classic Quaternion	3.153×10^{-14} 3.762×10^{-14}	4.1691×10^{-14}	$2.2579 \times 10^{-4} 1.3643 \times 10^{-4}$	0.604
pdb2le2 676	Classic Quaternion	2.064×10^{-13} 2.042×10^{-13}	7.7661×10^{-14}	$1.2162 \times 10^{-2} \\ 6.8292 \times 10^{-3}$	0.562
pdb2le7 122	Classic Quaternion	$2.112 \times 10^{-14} 2.749 \times 10^{-14}$	3.9789×10^{-14}	1.8287×10^{-4} 1.1091×10^{-4}	0.606
pdb2ler 68	Classic Quaternion	1.315×10^{-14} 1.532×10^{-14}	2.1465×10^{-14}	$9.8364 \times 10^{-5} 5.9976 \times 10^{-5}$	0.610
pdb2lgi 338	Classic Quaternion	$1.068 \times 10^{-12} 1.052 \times 10^{-12}$	1.8917×10^{-13}	5.3405×10^{-4} 3.3074×10^{-4}	0.619
pdb2lhc 338	Classic Quaternion	$5.829 \times 10^{-10} 5.830 \times 10^{-10}$	2.1362×10^{-12}	5.7812×10^{-4} 3.4725×10^{-4}	0.601
pdb2lhd 338	Classic Quaternion	$1.930 \times 10^{-12} 2.033 \times 10^{-12}$	2.3902×10^{-12}	7.2693×10^{-4} 4.3294×10^{-4}	0.596
pdb2lhe 338	Classic Quaternion	$4.963 \times 10^{-11} 4.967 \times 10^{-11}$	4.8488×10^{-13}	$6.9959 \times 10^{-4} 4.2128 \times 10^{-4}$	0.602
pdb2lhg 338	Classic Quaternion	$6.459 \times 10^{-14} 7.322 \times 10^{-14}$	5.9754×10^{-14}	5.4166×10^{-4} 3.4252×10^{-4}	0.632
pdb2lix 162	Classic Quaternion	$4.842 \times 10^{-14} 5.614 \times 10^{-14}$	7.8975×10^{-14}	$2.5511 \times 10^{-4} 1.5798 \times 10^{-4}$	0.619
pdb2lld 242	Classic Quaternion	$1.937 \times 10^{-13} 2.214 \times 10^{-13}$	2.2642×10^{-13}	3.8603×10^{-4} 2.4657×10^{-4}	0.639
pdb2lm9 578	Classic Quaternion	$6.254 \times 10^{-14} 7.713 \times 10^{-14}$	1.5079×10^{-13}	$9.2867 \times 10^{-4} 5.5919 \times 10^{-4}$	0.602
pdb2lmf 140	Classic Quaternion	$1.282 \times 10^{-13} 1.462 \times 10^{-13}$	7.9808×10^{-14}	$\begin{array}{c} 2.0512 \times 10^{-4} \\ 1.2216 \times 10^{-4} \end{array}$	0.596
pdb2ln3 500	Classic Quaternion	$1.292 \times 10^{-13} \\ 1.359 \times 10^{-13}$	8.4114×10^{-14}	$\begin{array}{c} 8.2481 \times 10^{-4} \\ 5.0672 \times 10^{-4} \end{array}$	0.614
pdb2lo2 230	Classic Quaternion	$2.068 \times 10^{-14} $ 2.571×10^{-14}	3.6944×10^{-14}	3.5286×10^{-4} 2.1708×10^{-4}	0.615
pdb2lqp 428	Classic Quaternion	2.950×10^{-13} 3.085×10^{-13}	4.7561×10^{-13}	$6.8026 \times 10^{-4} $ 4.1891×10^{-4}	0.616
pdb2lr0 806	Classic Quaternion	3.549×10^{-12} 3.440×10^{-12}	6.0485×10^{-13}	$1.3663 \times 10^{-3} \\ 8.4248 \times 10^{-4}$	0.617
pdb2lrh 806	Classic Quaternion	$5.631 \times 10^{-13} \\ 6.564 \times 10^{-13}$	3.2048×10^{-13}	$\begin{array}{c} 1.3271 \times 10^{-3} \\ 8.1453 \times 10^{-4} \end{array}$	0.614
pdb2ls9 152	Classic Quaternion	$1.122 \times 10^{-13} \\ 1.471 \times 10^{-13}$	3.7128×10^{-13}	$2.1166 \times 10^{-4} \\ 1.2974 \times 10^{-4}$	0.613
pdb2lsa 140	Classic Quaternion	$5.235 \times 10^{-14} 7.034 \times 10^{-14}$	1.5385×10^{-13}	2.0973×10^{-4} 1.3006×10^{-4}	0.620
$\begin{array}{c} \text{pdb2lss} \\ 422 \end{array}$	Classic Quaternion	$1.230 \times 10^{-13} 1.455 \times 10^{-13}$	1.6926×10^{-13}	$6.5717 \times 10^{-4} 4.1698 \times 10^{-4}$	0.635
pdb2lt3 680	Classic Quaternion	$7.245 \times 10^{-14} 7.760 \times 10^{-14}$	5.2634×10^{-14}	$\begin{array}{c} 1.0848 \times 10^{-3} \\ 6.8766 \times 10^{-4} \end{array}$	0.634
pdb2lu6 86	Classic Quaternion	$5.356 \times 10^{-15} \\ 6.922 \times 10^{-15}$	4.1890×10^{-15}	$\begin{array}{c} 1.3180 \times 10^{-4} \\ 7.8526 \times 10^{-5} \end{array}$	0.596
pdb2lwa 432	Classic Quaternion	$3.615 \times 10^{-13} 4.427 \times 10^{-13}$	9.3395×10^{-13}	$6.6402 \times 10^{-4} 4.1102 \times 10^{-4}$	0.619

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2lx0 194	Classic Quaternion	1.940×10^{-9} 1.940×10^{-9}	2.0923×10^{-13}	3.1226×10^{-4} 1.9112×10^{-4}	0.612
pdb2lxb 892	Classic Quaternion	$1.542 \times 10^{-13} \\ 1.585 \times 10^{-13}$	1.6837×10^{-13}	$1.8311 \times 10^{-3} \\ 1.1032 \times 10^{-3}$	0.602
pdb2lxy 404	Classic Quaternion	$9.313 \times 10^{-13} 1.025 \times 10^{-12}$	1.6618×10^{-12}	$8.0258 \times 10^{-4} $ 4.8297×10^{-4}	0.602
pdb2lxz 194	Classic Quaternion	$2.371 \times 10^{-12} 2.792 \times 10^{-12}$	1.9895×10^{-12}	$3.2047 \times 10^{-4} 1.9884 \times 10^{-4}$	0.620
pdb2lzf 820	Classic Quaternion	3.217×10^{-14} 3.957×10^{-14}	1.2991×10^{-13}	$3.6701 \times 10^{-2} 2.0489 \times 10^{-2}$	0.558
pdb2m1a 158	Classic Quaternion	$6.346 \times 10^{-15} 7.612 \times 10^{-15}$	6.5801×10^{-15}	$2.8770 \times 10^{-4} 1.6947 \times 10^{-4}$	0.589
pdb2m1j 182	Classic Quaternion	$1.865 \times 10^{-14} $ 2.212×10^{-14}	6.6915×10^{-14}	$2.9298 \times 10^{-4} 1.7721 \times 10^{-4}$	0.605
pdb2m2y 110	Classic Quaternion	2.699×10^{-13} 2.808×10^{-13}	1.4386×10^{-13}	$1.6766 \times 10^{-4} 1.0300 \times 10^{-4}$	0.614
pdb2m3f 134	Classic Quaternion	$3.629 \times 10^{-14} 4.641 \times 10^{-14}$	5.8107×10^{-14}	$1.9549 \times 10^{-4} 1.1839 \times 10^{-4}$	0.606
pdb2m4j 2178	Classic Quaternion	1.463×10^{-11} 1.455×10^{-11}	1.8385×10^{-13}	3.0899×10^{-2} 1.6683×10^{-2}	0.540
pdb2m8m 170	Classic Quaternion	$2.407 \times 10^{-14} 3.023 \times 10^{-14}$	1.1738×10^{-13}	$2.4356 \times 10^{-4} 1.5232 \times 10^{-4}$	0.625
pdb2m8o 170	Classic Quaternion	$1.672 \times 10^{-14} 2.039 \times 10^{-14}$	2.4755×10^{-14}	$2.3852 \times 10^{-4} 1.5126 \times 10^{-4}$	0.634
pdb2m97 416	Classic Quaternion	$4.646 \times 10^{-14} \\ 5.841 \times 10^{-14}$	2.0639×10^{-13}	$6.4149 \times 10^{-4} 4.0543 \times 10^{-4}$	0.632
pdb2m9g 1108	Classic Quaternion	$2.939 \times 10^{-13} 3.170 \times 10^{-13}$	5.8913×10^{-13}	$1.8543 \times 10^{-3} 1.1475 \times 10^{-3}$	0.619
pdb2m9r 242	Classic Quaternion	$3.537 \times 10^{-14} 4.406 \times 10^{-14}$	1.6694×10^{-13}	3.8746×10^{-4} 2.2436×10^{-4}	0.579
pdb2mdv 460	Classic Quaternion	$3.178 \times 10^{-12} 3.178 \times 10^{-12}$	3.0402×10^{-13}	1.7907×10^{-3} 1.0462×10^{-3}	0.584
pdb2me1 164	Classic Quaternion	1.886×10^{-13} 2.208×10^{-13}	1.6579×10^{-13}	2.4024×10^{-4} 1.4629×10^{-4}	0.609
pdb2me2 164	Classic Quaternion	$3.667 \times 10^{-13} 5.098 \times 10^{-13}$	1.1486×10^{-12}	$2.5397 \times 10^{-4} 1.5353 \times 10^{-4}$	0.605
pdb2me3 164	Classic Quaternion	$2.593 \times 10^{-9} 2.593 \times 10^{-9}$	9.2137×10^{-14}	$2.3516 \times 10^{-4} 1.4335 \times 10^{-4}$	0.610
pdb2me4 164	Classic Quaternion	$2.854 \times 10^{-9} 2.854 \times 10^{-9}$	9.9945×10^{-13}	$2.7671 \times 10^{-4} 1.6638 \times 10^{-4}$	0.601
pdb2mg1 164	Classic Quaternion	$4.398 \times 10^{-14} \\ 5.374 \times 10^{-14}$	1.5805×10^{-13}	$\begin{array}{c} 2.3575 \times 10^{-4} \\ 1.4662 \times 10^{-4} \end{array}$	0.622
pdb2mg2 170	Classic Quaternion	1.829×10^{-14} 2.480×10^{-14}	2.5921×10^{-14}	$2.4349 \times 10^{-4} 1.5351 \times 10^{-4}$	0.630
pdb2mg3 170	Classic Quaternion	$3.541 \times 10^{-14} 4.461 \times 10^{-14}$	2.4798×10^{-13}	$2.5354 \times 10^{-4} 1.5851 \times 10^{-4}$	0.625
pdb2mh8 338	Classic Quaternion	$1.547 \times 10^{-13} 1.883 \times 10^{-13}$	2.9903×10^{-13}	$5.5605 \times 10^{-4} 3.4429 \times 10^{-4}$	0.619
pdb2mhw 164	Classic Quaternion	$6.229 \times 10^{-14} 7.129 \times 10^{-14}$	4.9718×10^{-13}	$2.5108 \times 10^{-4} $ 1.5714×10^{-4}	0.626
pdb2mi1 84	Classic Quaternion	$1.827 \times 10^{-12} 2.052 \times 10^{-12}$	1.5687×10^{-12}	$1.3281 \times 10^{-4} \\ 8.2475 \times 10^{-5}$	0.621
pdb2mi7 404	Classic Quaternion	$6.022 \times 10^{-13} $ 6.817×10^{-13}	1.3690×10^{-12}	$5.8600 \times 10^{-4} 3.5786 \times 10^{-4}$	0.611

Table 2: Results - continued

Problem Size	Method	MDE	RMSD	Time	Ratio
pdb2mij 224	Classic Quaternion	1.244×10^{-13} 1.522×10^{-13}	2.8681×10^{-13}	3.3831×10^{-4} 2.0663×10^{-4}	0.611
pdb2mix 128	Classic Quaternion	$\begin{array}{c} 4.816 \times 10^{-14} \\ 4.684 \times 10^{-14} \end{array}$	3.7348×10^{-14}	$\begin{array}{c} 1.9065 \times 10^{-4} \\ 1.1873 \times 10^{-4} \end{array}$	0.623
pdb2mj1 110	Classic Quaternion	1.309×10^{-13} 1.646×10^{-13}	2.3819×10^{-13}	$1.7651 \times 10^{-4} 1.0746 \times 10^{-4}$	0.609
pdb2mj2 218	Classic Quaternion	9.775×10^{-14} 1.196×10^{-13}	8.8713×10^{-14}	$3.4006 \times 10^{-4} 2.0304 \times 10^{-4}$	0.597
$\begin{array}{c} \rm pdb2mjg\\ 556 \end{array}$	Classic Quaternion	$5.503 \times 10^{-14} $ 6.580×10^{-14}	7.0670×10^{-14}	$2.1403 \times 10^{-3} 1.2087 \times 10^{-3}$	0.565
pdb2mji 788	Classic Quaternion	$3.207 \times 10^{-12} 3.247 \times 10^{-12}$	2.7336×10^{-13}	$1.2480 \times 10^{-3} 7.9502 \times 10^{-4}$	0.637
pdb2mle 434	Classic Quaternion	$1.491 \times 10^{-13} 1.535 \times 10^{-13}$	3.1271×10^{-13}	7.0584×10^{-4} 4.2886×10^{-4}	0.608
pdb2mlf 434	Classic Quaternion	9.918×10^{-14} 1.128×10^{-13}	9.2903×10^{-14}	7.0616×10^{-4} 4.3297×10^{-4}	0.613
pdb2mo5 854	Classic Quaternion	$2.527 \times 10^{-10} 2.527 \times 10^{-10}$	1.0204×10^{-12}	$1.3908 \times 10^{-3} \\ 8.7516 \times 10^{-4}$	0.629
pdb2mpu 554	Classic Quaternion	$9.785 \times 10^{-14} 1.016 \times 10^{-13}$	1.0352×10^{-13}	$8.9773 \times 10^{-4} 5.6068 \times 10^{-4}$	0.625
pdb2mra 704	Classic Quaternion	2.632×10^{-13} 2.768×10^{-13}	1.2867×10^{-13}	$1.4008 \times 10^{-3} \\ 8.4120 \times 10^{-4}$	0.601
pdb2msu 122	Classic Quaternion	$7.813 \times 10^{-14} \\ 8.765 \times 10^{-14}$	3.7025×10^{-14}	2.0173×10^{-4} 1.2208×10^{-4}	0.605
pdb2mty 120	Classic Quaternion	$1.849 \times 10^{-14} 2.364 \times 10^{-14}$	9.1457×10^{-14}	$2.1012 \times 10^{-4} 1.2629 \times 10^{-4}$	0.601
pdb2muh 98	Classic Quaternion	2.008×10^{-13} 2.251×10^{-13}	1.4292×10^{-13}	$1.4547 \times 10^{-4} \\ 8.7958 \times 10^{-5}$	0.605
pdb2mvj 156	Classic Quaternion	$1.534 \times 10^{-13} 1.647 \times 10^{-13}$	5.5998×10^{-14}	$2.4181 \times 10^{-4} 1.4392 \times 10^{-4}$	0.595
pdb2mvt 284	Classic Quaternion	$6.053 \times 10^{-12} 6.226 \times 10^{-12}$	3.1969×10^{-12}	$5.6681 \times 10^{-4} \\ 3.3934 \times 10^{-4}$	0.599
pdb2mvx 2360	Classic Quaternion	$4.728 \times 10^{-9} 4.729 \times 10^{-9}$	3.7181×10^{-11}	$2.1984 \times 10^{-2} 1.2119 \times 10^{-2}$	0.551
pdb2mz6 220	Classic Quaternion	$4.129 \times 10^{-8} 4.129 \times 10^{-8}$	4.4231×10^{-13}	$2.8851 \times 10^{-2} $ 1.5215×10^{-2}	0.527
pdb2n00 572	Classic Quaternion	$2.703 \times 10^{-13} 3.467 \times 10^{-13}$	7.3499×10^{-13}	$7.8567 \times 10^{-4} 4.9399 \times 10^{-4}$	0.629
pdb2n0b 60	Classic Quaternion	$7.104 \times 10^{-13} 9.458 \times 10^{-13}$	8.9441×10^{-13}	$9.1258 \times 10^{-5} 5.5481 \times 10^{-5}$	0.608
pdb2n0c 60	Classic Quaternion	1.293×10^{-13} 1.682×10^{-13}	2.8483×10^{-13}	8.9546×10^{-5} 5.3031×10^{-5}	0.592
pdb2n0d 60	Classic Quaternion	$1.925 \times 10^{-9} 1.926 \times 10^{-9}$	1.6149×10^{-11}	$8.7136 \times 10^{-5} 5.3740 \times 10^{-5}$	0.617
pdb2n0e 60	Classic Quaternion	$3.314 \times 10^{-12} 4.286 \times 10^{-12}$	8.3573×10^{-12}	$8.9640 \times 10^{-5} 5.5845 \times 10^{-5}$	0.623
pdb2n0f 60	Classic Quaternion	$8.103 \times 10^{-9} \\ 8.103 \times 10^{-9}$	5.8011×10^{-13}	$8.4756 \times 10^{-5} 5.1625 \times 10^{-5}$	0.609
pdb2n0g 60	Classic Quaternion	8.315×10^{-13} 9.618×10^{-13}	1.3124×10^{-13}	$1.0130 \times 10^{-4} 6.0317 \times 10^{-5}$	0.595
pdb2n0h 60	Classic Quaternion	$7.690 \times 10^{-13} 8.730 \times 10^{-13}$	1.8191×10^{-13}	$9.3479 \times 10^{-5} 5.8237 \times 10^{-5}$	0.623
pdb2n35 314	Classic Quaternion	$3.541 \times 10^{-14} 4.466 \times 10^{-14}$	1.0752×10^{-13}	$4.9604 \times 10^{-4} \\ 3.0774 \times 10^{-4}$	0.620

Table 2: Results - continued

Problem Size	Method MDE RMSD Time		Ratio		
pdb2n3a 574	Classic Quaternion	$8.761 \times 10^{-14} \\ 1.049 \times 10^{-13}$	1.0149×10^{-13}	$1.6767 \times 10^{-2} \\ 8.9551 \times 10^{-3}$	0.534
pdb2n41 638	Classic Quaternion	$\begin{array}{c} 1.812 \times 10^{-13} \\ 1.836 \times 10^{-13} \end{array}$	8.2539×10^{-14}	$\begin{array}{c} 1.0753 \times 10^{-3} \\ 6.5707 \times 10^{-4} \end{array}$	0.611
pdb2n4e 638	Classic Quaternion	$1.494 \times 10^{-13} 1.687 \times 10^{-13}$	1.8433×10^{-13}	$1.0563 \times 10^{-3} \\ 6.5324 \times 10^{-4}$	0.618
pdb2n5q 164	Classic Quaternion	$1.732 \times 10^{-12} 1.745 \times 10^{-12}$	1.7589×10^{-12}	$2.5502 \times 10^{-4} 1.6074 \times 10^{-4}$	0.630
pdb2n67 566	Classic Quaternion	$4.443 \times 10^{-13} 4.465 \times 10^{-13}$	6.3487×10^{-14}	$\begin{array}{c} 9.0517 \times 10^{-4} \\ 5.6303 \times 10^{-4} \end{array}$	0.622
pdb2n6n 192	Classic Quaternion	4.139×10^{-8} 4.139×10^{-8}	5.0670×10^{-13}	3.0612×10^{-4} 1.9266×10^{-4}	0.629
pdb2n7i 224	Classic Quaternion	9.212×10^{-13} 1.126×10^{-12}	3.0537×10^{-12}	$3.4800 \times 10^{-4} 2.1033 \times 10^{-4}$	0.604
pdb2n7j 336	Classic Quaternion	$5.969 \times 10^{-13} 6.094 \times 10^{-13}$	1.5144×10^{-13}	$5.5604 \times 10^{-4} \\ 3.3764 \times 10^{-4}$	0.607
pdb2n9b 832	Classic Quaternion	1.196×10^{-12} 1.238×10^{-12}	1.1231×10^{-12}	$7.5212 \times 10^{-3} 4.0541 \times 10^{-3}$	0.539
pdb2na9 266	Classic Quaternion	$5.440 \times 10^{-14} 6.690 \times 10^{-14}$	5.4544×10^{-14}	3.9985×10^{-4} 2.3943×10^{-4}	0.599
pdb2ndc 110	Classic Quaternion	3.365×10^{-14} 4.479×10^{-14}	5.1916×10^{-14}	$1.7449 \times 10^{-4} 1.0603 \times 10^{-4}$	0.608
pdb2nde 110	Classic Quaternion	7.022×10^{-14} 8.868×10^{-14}	2.5156×10^{-13}	$\begin{array}{c} 1.5498 \times 10^{-4} \\ 9.5265 \times 10^{-5} \end{array}$	0.615
pdb2ndk 290	Classic Quaternion	$5.022 \times 10^{-13} 6.279 \times 10^{-13}$	2.0516×10^{-12}	$4.3875 \times 10^{-4} 2.6635 \times 10^{-4}$	0.607
pdb2nvj 152	Classic Quaternion	$2.082 \times 10^{-14} 2.293 \times 10^{-14}$	1.4035×10^{-14}	$2.1106 \times 10^{-4} $ 1.3248×10^{-4}	0.628
pdb2p6j 314	Classic Quaternion	$4.795 \times 10^{-14} 6.389 \times 10^{-14}$	1.1404×10^{-13}	$4.9868 \times 10^{-4} \\ 3.0174 \times 10^{-4}$	0.605
pdb2p81 266	Classic Quaternion	$7.881 \times 10^{-13} \\ 8.250 \times 10^{-13}$	4.3715×10^{-13}	$4.0170 \times 10^{-4} 2.4128 \times 10^{-4}$	0.601
pdb2pqe 896	Classic Quaternion	$6.484 \times 10^{-10} 6.496 \times 10^{-10}$	8.5673×10^{-12}	$\begin{array}{c} 1.7464 \times 10^{-3} \\ 1.0742 \times 10^{-3} \end{array}$	0.615
pdb2rlg 108	Classic Quaternion	$5.501 \times 10^{-14} \\ 6.973 \times 10^{-14}$	6.8873×10^{-14}	$1.7141 \times 10^{-4} 1.0328 \times 10^{-4}$	0.603
pdb2rlh 108	Classic Quaternion	$4.772 \times 10^{-14} 5.801 \times 10^{-14}$	3.9131×10^{-14}	$1.8381 \times 10^{-4} 1.1035 \times 10^{-4}$	0.600
pdb2rmy 206	Classic Quaternion	$1.872 \times 10^{-13} 2.498 \times 10^{-13}$	3.6453×10^{-13}	3.2133×10^{-4} 1.9158×10^{-4}	0.596
pdb2rnd 206	Classic Quaternion	$\begin{array}{c} 2.626 \times 10^{-13} \\ 3.581 \times 10^{-13} \end{array}$	4.9979×10^{-13}	3.1245×10^{-4} 1.8852×10^{-4}	0.603
$\begin{array}{c} pdb2roo\\ 260\end{array}$	Classic Quaternion	$2.933 \times 10^{-12} 3.525 \times 10^{-12}$	3.5927×10^{-12}	9.2680×10^{-4} 5.2709×10^{-4}	0.569
pdb2rql 572	Classic Quaternion	$2.345 \times 10^{-12} 2.496 \times 10^{-12}$	8.7086×10^{-13}	$1.2692 \times 10^{-3} 7.5430 \times 10^{-4}$	0.594
$\begin{array}{c} \mathrm{pdb2rut} \\ 218 \end{array}$	Classic Quaternion	$4.389 \times 10^{-14} 5.014 \times 10^{-14}$	3.5338×10^{-13}	$3.3457 \times 10^{-4} 2.0440 \times 10^{-4}$	0.611
pdb2ruv 224	Classic Quaternion	$5.776 \times 10^{-14} 7.408 \times 10^{-14}$	1.2473×10^{-13}	$3.4892 \times 10^{-4} \\ 2.1174 \times 10^{-4}$	0.607
pdb2rux 218	Classic Quaternion	$2.671 \times 10^{-14} \\ 3.016 \times 10^{-14}$	6.2140×10^{-14}	$3.5268 \times 10^{-4} $ 2.1558×10^{-4}	0.611
pdb2ruy 224	Classic Quaternion	$1.968 \times 10^{-14} 2.387 \times 10^{-14}$	6.4254×10^{-14}	$3.5150 \times 10^{-4} 2.1187 \times 10^{-4}$	0.603

Table 2: Results - continued

Problem Size	Method	MDE RMSD		Time	Ratio
pdb2rv3 218	Classic Quaternion	3.656×10^{-14} 4.118×10^{-14}	6.3794×10^{-14}	3.5977×10^{-4} 2.1748×10^{-4}	0.605
pdb2rv5 212	Classic Quaternion	$1.145 \times 10^{-14} \\ 1.338 \times 10^{-14}$	1.6010×10^{-14}	$\begin{array}{c} 3.3397 \times 10^{-4} \\ 2.0422 \times 10^{-4} \end{array}$	0.611
pdb2y4q 476	Classic Quaternion	1.410×10^{-12} 1.451×10^{-12}	2.0648×10^{-13}	7.3303×10^{-4} 4.5092×10^{-4}	0.615

1.2 Using BP-All versions

Table 3: Results

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb1a57 698	ClassicAll QuaternionAll	8 8	$3.1806 \times 10^{-11} \\ 3.3550 \times 10^{-11}$	5 5	$2.096 \times 10^{-11} 2.092 \times 10^{-11}$	$6.9182 \times 10^{-3} 5.0382 \times 10^{-3}$	0.728
pdb1b4c 1108	ClassicAll QuaternionAll	8 8	$2.6824 \times 10^{-12} 3.4662 \times 10^{-12}$	5 5	$5.067 \times 10^{-13} 5.493 \times 10^{-13}$	$\begin{array}{c} 1.2052 \times 10^{-2} \\ 7.2075 \times 10^{-3} \end{array}$	0.598
pdb1ba5 320	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 3.5621 \times 10^{-2} \\ 3.5621 \times 10^{-2} \end{array}$	6 6	$9.363 \times 10^{-13} 1.069 \times 10^{-12}$	$1.2507 \times 10^{-3} 1.0149 \times 10^{-3}$	0.811
pdb1d1n 594	ClassicAll QuaternionAll	2 2	$2.9766 \times 10^{-11} 2.9311 \times 10^{-11}$	1 1	$1.005 \times 10^{-11} 9.672 \times 10^{-12}$	2.2555×10^{-3} 1.5438×10^{-3}	0.684
pdb1dp3 332	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.9981 \times 10^{-5} \\ 4.9981 \times 10^{-5} \end{array}$	2 2	$7.704 \times 10^{-13} \\ 8.940 \times 10^{-13}$	$1.3026 \times 10^{-3} 1.0477 \times 10^{-3}$	0.804
pdb1du1 122	ClassicAll QuaternionAll	16 16	$6.6600 \times 10^{-13} 1.6577 \times 10^{-12}$	1 1	$8.225 \times 10^{-13} 1.258 \times 10^{-12}$	$5.9706 \times 10^{-4} 5.3243 \times 10^{-4}$	0.892
pdb1eii 806	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.9451 \times 10^{-10} \\ 1.8740 \times 10^{-10} \end{array}$	1 1	$\begin{array}{c} 1.393 \times 10^{-11} \\ 1.365 \times 10^{-11} \end{array}$	$\begin{array}{c} 3.3491 \times 10^{-3} \\ 2.7209 \times 10^{-3} \end{array}$	0.812
pdb1fcl 338	ClassicAll QuaternionAll	8 8	$1.5447 \times 10^{-11} \\ 1.5223 \times 10^{-11}$	2 2	$\begin{array}{c} 4.542 \times 10^{-12} \\ 4.515 \times 10^{-12} \end{array}$	$2.3501 \times 10^{-3} 1.2523 \times 10^{-3}$	0.533
pdb1fd6 344	ClassicAll QuaternionAll	8 8	$2.0242 \times 10^{-5} 2.0242 \times 10^{-5}$	$\frac{2}{2}$	3.182×10^{-12} 3.193×10^{-12}	$2.0331 \times 10^{-3} 1.1489 \times 10^{-3}$	0.565
pdb1hf9 496	ClassicAll QuaternionAll	8 8	$9.0139 \times 10^{-10} 9.0282 \times 10^{-10}$	6 6	$1.156 \times 10^{-11} \\ 1.180 \times 10^{-11}$	3.3232×10^{-2} 2.1811×10^{-2}	0.656
pdb1i2u 266	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.3842 \times 10^{-3} \\ 1.3842 \times 10^{-3} \end{array}$	$\frac{2}{2}$	$5.562 \times 10^{-13} 5.609 \times 10^{-13}$	1.5846×10^{-3} 1.0920×10^{-3}	0.689
pdb1i2v 266	ClassicAll QuaternionAll	8 8	8.9125×10^{-13} 8.8206×10^{-13}	5 5	$2.422 \times 10^{-13} 2.525 \times 10^{-13}$	$1.5690 \times 10^{-3} 1.0743 \times 10^{-3}$	0.685
pdb1ijc 380	ClassicAll QuaternionAll	8 8	$9.1858 \times 10^{-11} 9.4110 \times 10^{-11}$	$\frac{2}{2}$	$1.408 \times 10^{-11} \\ 1.426 \times 10^{-11}$	$\begin{array}{c} 3.1831 \times 10^{-3} \\ 2.0327 \times 10^{-3} \end{array}$	0.639
pdb1jlz 140	ClassicAll QuaternionAll	8 8	$1.2304 \times 10^{-4} \\ 1.2304 \times 10^{-4}$	1 1	$5.594 \times 10^{-13} 5.965 \times 10^{-13}$	$\begin{array}{c} 8.1780 \times 10^{-4} \\ 5.5375 \times 10^{-4} \end{array}$	0.677
pdb1jw3 842	ClassicAll QuaternionAll	8 8	$1.9618 \times 10^{-12} 1.8088 \times 10^{-12}$	2 2	$5.936 \times 10^{-13} 5.897 \times 10^{-13}$	$\begin{array}{c} 5.2284 \times 10^{-3} \\ 3.5114 \times 10^{-3} \end{array}$	0.672
pdb1k0v 440	ClassicAll QuaternionAll	8 8	8.3940×10^{-5} 8.3940×10^{-5}	$\frac{2}{2}$	$1.893 \times 10^{-13} 1.894 \times 10^{-13}$	$\begin{array}{c} 2.7266 \times 10^{-3} \\ 1.8617 \times 10^{-3} \end{array}$	0.683
pdb1k2h 1120	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 1.9788 \times 10^{-4} \\ 1.9788 \times 10^{-4} \end{array}$	$\frac{2}{2}$	5.490×10^{-13} 5.198×10^{-13}	$2.0608 \times 10^{-2} 1.1749 \times 10^{-2}$	0.570
pdb1k36 278	ClassicAll QuaternionAll	8 8	1.6100×10^{-10} 1.8077×10^{-10}	1 1	$8.820 \times 10^{-12} \\ 1.081 \times 10^{-11}$	1.8790×10^{-3} 1.2348×10^{-3}	0.657
pdb1k37 278	ClassicAll QuaternionAll	8 8	$2.1407 \times 10^{-12} 2.0318 \times 10^{-12}$	$\frac{2}{2}$	$4.711 \times 10^{-13} 4.988 \times 10^{-13}$	2.6549×10^{-3} 1.6523×10^{-3}	0.622
pdb1kuw 62	ClassicAll QuaternionAll	8 8	$1.8706 \times 10^{-4} $ 1.8706×10^{-4}	1 1	$9.229 \times 10^{-14} \\ 1.130 \times 10^{-13}$	3.4102×10^{-4} 2.3265×10^{-4}	0.682
pdb1kz0 98	ClassicAll QuaternionAll	8 8	$6.7512 \times 10^{-13} $ 6.2568×10^{-13}	1 1	$4.404 \times 10^{-14} 5.880 \times 10^{-14}$	$5.5536 \times 10^{-4} 3.7998 \times 10^{-4}$	0.684
pdb1kz2 98	ClassicAll QuaternionAll	8 8	3.1076×10^{-6} 3.1076×10^{-6}	1 1	$2.119 \times 10^{-14} 2.886 \times 10^{-14}$	$5.6129 \times 10^{-4} 3.8757 \times 10^{-4}$	0.690
pdb1kz5 74	ClassicAll QuaternionAll	8 8	4.8094×10^{-13} 5.2716×10^{-13}	1 1	$4.081 \times 10^{-14} 4.738 \times 10^{-14}$	$4.1086 \times 10^{-4} 2.7979 \times 10^{-4}$	0.681
pdb1lvz 68	ClassicAll QuaternionAll	8 8	1.4708×10^{-3} 1.4708×10^{-3}	1 1	$6.336 \times 10^{-14} 7.315 \times 10^{-14}$	3.7435×10^{-4} 2.5337×10^{-4}	0.677
pdb1m4e 122	ClassicAll QuaternionAll	8	$5.4966 \times 10^{-12} $ 5.5048×10^{-12}	1 1	5.949×10^{-13} 5.972×10^{-13}	$6.9394 \times 10^{-4} 4.7876 \times 10^{-4}$	0.690
pdb1ma2 104	ClassicAll QuaternionAll	8 8	1.7458×10^{-10} 1.7467×10^{-10}	2 2	$8.695 \times 10^{-12} \\ 8.757 \times 10^{-12}$	8.2408×10^{-4} 5.2271×10^{-4}	0.634

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb1ma4 104	ClassicAll QuaternionAll	8 8	$5.4569 \times 10^{-4} 5.4569 \times 10^{-4}$	$\frac{2}{2}$	$7.247 \times 10^{-14} 7.977 \times 10^{-14}$	$1.4405 \times 10^{-3} \\ 8.2199 \times 10^{-4}$	0.571
pdb1ma5 104	ClassicAll QuaternionAll	8 8	$9.6358 \times 10^{-5} 9.6358 \times 10^{-5}$	1 1	8.169×10^{-13} 9.044×10^{-13}	$5.9293 \times 10^{-4} 4.0681 \times 10^{-4}$	0.686
pdb1ma6 104	ClassicAll QuaternionAll	8 8	1.2440×10^{-11} 1.4288×10^{-11}	2 2	$6.283 \times 10^{-13} \\ 8.487 \times 10^{-13}$	$5.9324 \times 10^{-4} 4.0888 \times 10^{-4}$	0.689
pdb1mpe 1352	ClassicAll QuaternionAll	8	$5.1722 \times 10^{-10} 5.1751 \times 10^{-10}$	2 2	$2.617 \times 10^{-11} \\ 2.624 \times 10^{-11}$	$2.4245 \times 10^{-2} 1.4071 \times 10^{-2}$	0.580
pdb1nd9 296	ClassicAll QuaternionAll	24 24	$1.0508 \times 10^{-12} \\ 8.9082 \times 10^{-13}$	2 2	$3.026 \times 10^{-13} \\ 3.845 \times 10^{-13}$	$2.6582 \times 10^{-3} 2.1501 \times 10^{-3}$	0.809
pdb1ne5 254	ClassicAll QuaternionAll	128 128	$1.4845 \times 10^{-11} \\ 1.5105 \times 10^{-11}$	33 33	$1.214 \times 10^{-12} $ 1.384×10^{-12}	$2.2463 \times 10^{-2} 1.5027 \times 10^{-2}$	0.669
pdb1nmj 170	ClassicAll QuaternionAll	8	$2.3883 \times 10^{-13} $ 2.3832×10^{-13}	7 7	$1.236 \times 10^{-14} $ 1.422×10^{-14}	$9.7190 \times 10^{-4} \\ 6.6399 \times 10^{-4}$	0.683
pdb1o53 92	ClassicAll QuaternionAll	8 8	1.0887×10^{-11} 1.1252×10^{-11}	2 2	$3.999 \times 10^{-13} $ 4.527×10^{-13}	3.3305×10^{-4} 2.8306×10^{-4}	0.850
pdb1oqp 580	ClassicAll QuaternionAll	8	$2.9348 \times 10^{-3} $ 2.9348×10^{-3}	2 2	$7.045 \times 10^{-14} \\ 8.314 \times 10^{-14}$	$1.2779 \times 10^{-2} \\ 8.1624 \times 10^{-3}$	0.639
pdb1plw 32	ClassicAll QuaternionAll	8 8	$3.0310 \times 10^{-13} 3.2973 \times 10^{-13}$	2 2	$2.830 \times 10^{-14} \\ 3.112 \times 10^{-14}$	$1.0773 \times 10^{-4} \\ 8.8610 \times 10^{-5}$	0.823
pdb1plx 32	ClassicAll QuaternionAll	8 8	$2.8525 \times 10^{-4} $ 2.8525×10^{-4}	1 1	$1.574 \times 10^{-13} 2.060 \times 10^{-13}$	$1.0619 \times 10^{-4} \\ 8.7592 \times 10^{-5}$	0.825
pdb1pv0 278	ClassicAll QuaternionAll	32 32	$1.3024 \times 10^{-11} $ 1.3017×10^{-11}	1 1	$2.409 \times 10^{-13} 2.723 \times 10^{-13}$	$4.0445 \times 10^{-3} 3.3245 \times 10^{-3}$	0.822
pdb1pzr 724	ClassicAll QuaternionAll ClassicAll	8 8 32	3.9940×10^{-10} 3.9046×10^{-10} 3.1378×10^{-5}	1 17	5.644×10^{-12} 5.871×10^{-12} 2.634×10^{-13}	$ \begin{array}{r} 1.8975 \times 10^{-1} \\ 1.1706 \times 10^{-1} \end{array} $ $ 2.3192 \times 10^{-2} $	0.617
pdb1qlk 1108	Quaternion All Classic All	32 32 8	3.1378×10^{-5} 3.1378×10^{-5} 4.3330×10^{-3}	17 17 2	2.870×10^{-13} 2.870×10^{-13} 1.847×10^{-13}	2.3192×10^{-2} 1.8448×10^{-2} 2.3996×10^{-3}	0.795
pdb1r57 614 pdb1ry3	Quaternion All Classic All	8	4.3330×10^{-3} 4.3330×10^{-3} 9.1924×10^{-12}	2 2	$ \begin{array}{c} 1.847 \times 10 \\ 2.054 \times 10^{-13} \\ 4.938 \times 10^{-13} \end{array} $	2.3990×10 2.0309×10^{-3} 2.8989×10^{-3}	0.846
386 pdb1s4h	QuaternionAll ClassicAll	16 32	9.4285×10^{-12} 1.4643×10^{-4}	10	$ \begin{array}{c} 4.938 \times 10 \\ 5.913 \times 10^{-13} \\ 4.696 \times 10^{-13} \end{array} $	2.8969×10 2.3999×10^{-3} 9.0118×10^{-4}	0.828
80 pdb1s4j	Quaternion All Classic All	32 32	$ \begin{array}{r} 1.4043 \times 10 \\ 1.4643 \times 10^{-4} \\ 5.8507 \times 10^{-12} \end{array} $	10 10 2	6.351×10^{-13} 1.520×10^{-13}	7.8235×10^{-4} 3.9940×10^{-4}	0.868
80 pdb1s6j	Quaternion All Classic All	16	5.8479×10^{-12} 6.0202×10^{-5}	2 1	$ \begin{array}{c} 1.320 \times 10 \\ 2.083 \times 10^{-13} \\ 6.073 \times 10^{-13} \end{array} $	3.6789×10^{-4} 3.5253×10^{-3}	0.921
524 pdb1sa8	Quaternion All Classic All	24 8	6.0202×10^{-5} 6.0202×10^{-5} 1.7170×10^{-3}	1	$ \begin{array}{c} 0.073 \times 10 \\ 7.660 \times 10^{-13} \\ 9.340 \times 10^{-13} \end{array} $	3.1956×10^{-3} 2.5239×10^{-3}	0.906
638 pdb1t2y	Quaternion All Classic All	8	1.7170×10^{-3} 1.7170×10^{-3} 2.5460×10^{-4}	1	$ \begin{array}{c} 3.840 \times 10 \\ 1.034 \times 10^{-12} \\ \hline 1.887 \times 10^{-13} \end{array} $	$ \begin{array}{c} 2.0265 \times 10 \\ 2.1580 \times 10^{-3} \\ 5.8395 \times 10^{-4} \end{array} $	0.855
152 pdb1t5q	Quaternion All Classic All	8	2.5460×10^{-4} 2.5460×10^{-4} 1.0265×10^{-12}	1	2.396×10^{-13} 3.877×10^{-14}	4.9999×10^{-4} 4.8259×10^{-4}	0.856
180 pdb1tot	Quaternion All Classic All	2 8	$ \begin{array}{c} 1.0480 \times 10^{-12} \\ \hline 3.4218 \times 10^{-3} \end{array} $	1 5	5.093×10^{-14} 6.151×10^{-14}	3.5479×10^{-4} 1.2371×10^{-3}	0.735
314 pdb1v6r	Quaternion All Classic All	8	3.4218×10^{-3} 1.3650×10^{-4}	5 2	6.855×10^{-14} 6.835×10^{-13}	$ \begin{array}{c} 1.2871 \times 10 \\ 1.0570 \times 10^{-3} \\ \hline 7.2989 \times 10^{-4} \end{array} $	0.854
128 pdb1v92	Quaternion All Classic All	8	1.3650×10^{-4} 3.1327×10^{-5}	$\frac{2}{1}$	6.971×10^{-13} 1.463×10^{-13}	5.8035×10^{-4} 1.0816×10^{-3}	0.795
278 pdb1vd7	Quaternion All Classic All	8	3.1327×10^{-5} 7.8801×10^{-12}	1 5	$ \begin{array}{c} 1.406 \times 10 \\ 1.630 \times 10^{-13} \\ 6.342 \times 10^{-13} \end{array} $	9.1192×10^{-4} 6.9567×10^{-4}	0.843
140 pdb1vd9	Quaternion All Classic All	16	7.9022×10^{-12} 1.5514×10^{-11}	5 1	$ \begin{array}{c} 0.342 \times 10 \\ 7.439 \times 10^{-13} \\ \hline 1.290 \times 10^{-12} \end{array} $	6.307×10^{-4} 6.3072×10^{-4} 5.4786×10^{-4}	0.907
140	QuaternionAll	8	1.5514×10 1.5541×10^{-11}	1	1.290×10 1.554×10^{-12}	4.5883×10^{-4}	0.838

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb1vdb 140	ClassicAll QuaternionAll	8 8	$8.5740 \times 10^{-12} \\ 8.5291 \times 10^{-12}$	$\frac{2}{2}$	9.108×10^{-13} 1.082×10^{-12}	$5.1276 \times 10^{-4} 4.2892 \times 10^{-4}$	0.836
pdb1vpc 272	ClassicAll QuaternionAll	8 8	$4.3482 \times 10^{-4} 4.3482 \times 10^{-4}$	6 6	$8.510 \times 10^{-15} \\ 1.002 \times 10^{-14}$	$\begin{array}{c} 1.0645 \times 10^{-3} \\ 8.7887 \times 10^{-4} \end{array}$	0.826
pdb1wnk 140	ClassicAll QuaternionAll	16 16	$2.2292 \times 10^{-10} 2.2177 \times 10^{-10}$	1 1	$4.112 \times 10^{-12} 4.632 \times 10^{-12}$	$7.2754 \times 10^{-4} 6.5065 \times 10^{-4}$	0.894
pdb1wo4 152	ClassicAll QuaternionAll	8	$4.6193 \times 10^{-5} 4.6193 \times 10^{-5}$	2 2	$9.957 \times 10^{-13} 9.634 \times 10^{-13}$	$5.5957 \times 10^{-4} 4.7131 \times 10^{-4}$	0.842
pdb1wo5 152	ClassicAll QuaternionAll	32 32	$2.7147 \times 10^{-10} 2.7625 \times 10^{-10}$	13 13	$2.372 \times 10^{-12} 2.514 \times 10^{-12}$	1.2759×10^{-3} 1.2096×10^{-3}	0.948
pdb1x60 476	ClassicAll QuaternionAll	16 16	$6.7449 \times 10^{-12} $ 6.9447×10^{-12}	1 1	$1.076 \times 10^{-12} 1.179 \times 10^{-12}$	3.6767×10^{-3} 3.0802×10^{-3}	0.838
pdb1x9v 544	ClassicAll QuaternionAll	8 8	$1.1547 \times 10^{-4} \\ 1.1547 \times 10^{-4}$	6	$8.968 \times 10^{-13} 9.611 \times 10^{-13}$	$3.7460 \times 10^{-2} $ 2.6436×10^{-2}	0.706
pdb1y5c 68	ClassicAll QuaternionAll	16 16	$8.7435 \times 10^{-13} \\ 8.2242 \times 10^{-13}$	5 5	$7.693 \times 10^{-14} 9.383 \times 10^{-14}$	$3.2191 \times 10^{-4} 2.8941 \times 10^{-4}$	0.899
pdb1yx7 500	ClassicAll QuaternionAll	16 16	$1.3647 \times 10^{-10} 1.4245 \times 10^{-10}$	9	$3.509 \times 10^{-12} 4.348 \times 10^{-12}$	$3.0816 \times 10^{-3} 2.6598 \times 10^{-3}$	0.863
pdb1yx8 500	ClassicAll QuaternionAll	8	$2.5841 \times 10^{-10} $ 2.6921×10^{-10}	6 6	$7.284 \times 10^{-12} \\ 8.217 \times 10^{-12}$	2.2038×10^{-3} 1.8184×10^{-3}	0.825
pdb1yxr 464	ClassicAll QuaternionAll	128 128	$9.2421 \times 10^{-4} 9.2421 \times 10^{-4}$	29 29	$3.514 \times 10^{-10} \\ 3.515 \times 10^{-10}$	$2.2011 \times 10^{-2} 1.9457 \times 10^{-2}$	0.884
$\begin{array}{c} \mathrm{pdb2a2y} \\ 1072 \end{array}$	ClassicAll QuaternionAll	8	$8.1076 \times 10^{-5} \\ 8.1076 \times 10^{-5}$	2 2	$1.150 \times 10^{-12} \\ 1.151 \times 10^{-12}$	$1.0906 \times 10^{-1} 6.5621 \times 10^{-2}$	0.602
pdb2a4j 580	ClassicAll QuaternionAll	16 16	$1.0516 \times 10^{-4} 1.0516 \times 10^{-4}$	2 2	$2.085 \times 10^{-14} 2.727 \times 10^{-14}$	$5.0774 \times 10^{-3} 4.0510 \times 10^{-3}$	0.798
pdb2adl 868	ClassicAll QuaternionAll	384 384	3.1161×10^{-11} 3.3255×10^{-11}	1 1	$1.752 \times 10^{-11} 1.787 \times 10^{-11}$	1.8966×10^{-1} 1.6590×10^{-1}	0.875
pdb2adn 868	ClassicAll QuaternionAll	8 8	2.3364×10^{-10} 2.3188×10^{-10}	1 1	$6.693 \times 10^{-12} 6.465 \times 10^{-12}$	$7.5138 \times 10^{-3} 5.4531 \times 10^{-3}$	0.726
pdb2ajj 170	ClassicAll QuaternionAll	8 8	$2.9810 \times 10^{-4} 2.9810 \times 10^{-4}$	1 1	$5.641 \times 10^{-14} $ 6.584×10^{-14}	$6.3314 \times 10^{-4} 5.2482 \times 10^{-4}$	0.829
pdb2ajm 170	ClassicAll QuaternionAll	8 8	$2.4063 \times 10^{-12} 2.7001 \times 10^{-12}$	2 2	$1.183 \times 10^{-13} \\ 1.555 \times 10^{-13}$	$6.4210 \times 10^{-4} 5.3770 \times 10^{-4}$	0.837
pdb2ajn 170	ClassicAll QuaternionAll	8	$4.3268 \times 10^{-4} $ 4.3268×10^{-4}	1 1	$1.076 \times 10^{-13} 1.217 \times 10^{-13}$	$6.3529 \times 10^{-4} 5.2296 \times 10^{-4}$	0.823
pdb2ajo 170	ClassicAll QuaternionAll	8	$2.4063 \times 10^{-12} 2.7001 \times 10^{-12}$	2 2	$1.183 \times 10^{-13} \\ 1.555 \times 10^{-13}$	$6.4399 \times 10^{-4} 5.3730 \times 10^{-4}$	0.834
pdb2akk 446	ClassicAll QuaternionAll	8 8	$3.0416 \times 10^{-3} 3.0416 \times 10^{-3}$	2 2	$1.289 \times 10^{-13} 1.279 \times 10^{-13}$	$2.5814 \times 10^{-3} 2.1104 \times 10^{-3}$	0.818
pdb2bzb 748	ClassicAll QuaternionAll	8 8	$4.6498 \times 10^{-13} $ 6.0113×10^{-13}	5 5	$9.361 \times 10^{-14} \\ 1.224 \times 10^{-13}$	$2.0888 \times 10^{-2} $ 1.3703×10^{-2}	0.656
pdb2c0s 386	ClassicAll QuaternionAll	8	$1.0793 \times 10^{-2} 1.0793 \times 10^{-2}$	6	$3.028 \times 10^{-13} 3.380 \times 10^{-13}$	1.5198×10^{-3} 1.2435×10^{-3}	0.818
pdb2dci 120	ClassicAll QuaternionAll	2 2	$2.0907 \times 10^{-13} 3.3732 \times 10^{-13}$	1 1	$2.366 \times 10^{-14} 2.950 \times 10^{-14}$	$3.3135 \times 10^{-4} 2.4787 \times 10^{-4}$	0.748
pdb2eem 206	ClassicAll QuaternionAll	8	$9.5324 \times 10^{-12} 9.5866 \times 10^{-12}$	1 1	$5.190 \times 10^{-13} 5.461 \times 10^{-13}$	$8.2362 \times 10^{-4} 6.8483 \times 10^{-4}$	0.831
pdb2fva 494	ClassicAll QuaternionAll	8 8	1.2680×10^{-11} 1.2689×10^{-11}	2 2	$1.047 \times 10^{-12} \\ 1.195 \times 10^{-12}$	2.4007×10^{-3} 1.9216×10^{-3}	0.800
pdb2fvf 494	ClassicAll QuaternionAll	8	$3.5796 \times 10^{-12} 3.3286 \times 10^{-12}$	1 1	$3.106 \times 10^{-13} 3.445 \times 10^{-13}$	1.9213×10^{-3} 1.6189×10^{-3}	0.843
pdb2fxz 80	ClassicAll QuaternionAll	8 8	$4.2293 \times 10^{-12} 5.3169 \times 10^{-12}$	1 1	$1.489 \times 10^{-12} 1.749 \times 10^{-12}$	$2.9894 \times 10^{-4} 2.5279 \times 10^{-4}$	0.846

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2g9j 848	ClassicAll QuaternionAll	8 8	$5.8011 \times 10^{-4} \\ 5.8011 \times 10^{-4}$	$\frac{2}{2}$	3.282×10^{-12} 3.535×10^{-12}	$1.2584 \times 10^{-1} 7.7182 \times 10^{-2}$	0.613
pdb2g9l 224	ClassicAll QuaternionAll	8 8	$1.0333 \times 10^{-4} \\ 1.0333 \times 10^{-4}$	$\frac{2}{2}$	$6.365 \times 10^{-14} \\ 8.666 \times 10^{-14}$	$8.5955 \times 10^{-4} 7.2341 \times 10^{-4}$	0.842
pdb2h5m 614	ClassicAll QuaternionAll	8 8	1.2267×10^{-3} 1.2267×10^{-3}	1 1	9.692×10^{-13} 1.032×10^{-12}	$2.4232 \times 10^{-3} 2.0332 \times 10^{-3}$	0.839
pdb2hep 252	ClassicAll QuaternionAll	2 2	$2.1758 \times 10^{-11} 2.2038 \times 10^{-11}$	1 1	$1.191 \times 10^{-12} 1.268 \times 10^{-12}$	$7.1164 \times 10^{-4} 5.0791 \times 10^{-4}$	0.714
pdb2j0z 752	ClassicAll QuaternionAll	16 16	$1.3100 \times 10^{-10} 1.3116 \times 10^{-10}$	10 10	$4.392 \times 10^{-12} 4.954 \times 10^{-12}$	$5.3475 \times 10^{-1} 3.3539 \times 10^{-1}$	0.627
pdb2j10 752	ClassicAll QuaternionAll	8192 8192	2.9618×10^{-5} 2.9618×10^{-5}	6386 6386	$1.744 \times 10^{-10} \\ 1.747 \times 10^{-10}$	7.9941 5.1469	0.644
pdb2j11 752	ClassicAll QuaternionAll	4096 4096	$2.7803 \times 10^{-11} $ 2.7661×10^{-11}	2125 2125	$5.256 \times 10^{-12} 5.631 \times 10^{-12}$	3.8061 3.0344	0.797
pdb2jmy 92	ClassicAll QuaternionAll	8 8	$7.0432 \times 10^{-5} 7.0432 \times 10^{-5}$	1 1	$9.834 \times 10^{-13} 9.967 \times 10^{-13}$	$3.4466 \times 10^{-4} 2.9224 \times 10^{-4}$	0.848
pdb2jn5 74	ClassicAll QuaternionAll	16 16	$6.6339 \times 10^{-12} 2.0459 \times 10^{-11}$	5 5	$1.104 \times 10^{-11} \\ 2.456 \times 10^{-11}$	$5.0437 \times 10^{-4} 4.2350 \times 10^{-4}$	0.840
pdb2jnk 842	ClassicAll QuaternionAll	32 32	3.4995×10^{-11} 3.4653×10^{-11}	13 13	$2.246 \times 10^{-12} 2.319 \times 10^{-12}$	$7.3404 \times 10^{-3} $ 6.6662×10^{-3}	0.908
pdb2jpn 476	ClassicAll QuaternionAll	8	$6.4192 \times 10^{-12} 6.5904 \times 10^{-12}$	2 2	$6.730 \times 10^{-14} 6.984 \times 10^{-14}$	$2.4044 \times 10^{-3} 1.9034 \times 10^{-3}$	0.792
pdb2jua 614	ClassicAll QuaternionAll	16 16	$1.8732 \times 10^{-4} 1.8732 \times 10^{-4}$	6 6	$1.384 \times 10^{-9} \\ 1.385 \times 10^{-9}$	$3.4556 \times 10^{-3} 2.9831 \times 10^{-3}$	0.863
pdb2jvd 288	ClassicAll QuaternionAll	4	$9.4244 \times 10^{-13} 9.4967 \times 10^{-13}$	1 1	$3.339 \times 10^{-14} 3.898 \times 10^{-14}$	$9.8853 \times 10^{-4} 7.5355 \times 10^{-4}$	0.762
pdb2jwe 984	ClassicAll QuaternionAll	2 2	$9.2597 \times 10^{-11} 9.2052 \times 10^{-11}$	1 1	$2.695 \times 10^{-11} 2.734 \times 10^{-11}$	$5.0637 \times 10^{-3} 3.7322 \times 10^{-3}$	0.737
pdb2jws 338	ClassicAll QuaternionAll	8	$4.5612 \times 10^{-4} 4.5612 \times 10^{-4}$	2 2	$1.251 \times 10^{-13} 1.543 \times 10^{-13}$	$1.3498 \times 10^{-3} 1.1160 \times 10^{-3}$	0.827
pdb2jwu 338	ClassicAll QuaternionAll	8	$3.0876 \times 10^{-4} 3.0876 \times 10^{-4}$	1 1	$4.421 \times 10^{-12} 4.373 \times 10^{-12}$	$1.6610 \times 10^{-3} 1.3370 \times 10^{-3}$	0.805
pdb2jxf 182	ClassicAll QuaternionAll	8	$2.4000 \times 10^{-4} 2.4000 \times 10^{-4}$	1 1	$1.399 \times 10^{-13} 1.734 \times 10^{-13}$	$6.7586 \times 10^{-4} 5.5838 \times 10^{-4}$	0.826
pdb2jz5 548	ClassicAll QuaternionAll	8	1.7460×10^{-3} 1.7460×10^{-3}	1 1	$2.860 \times 10^{-13} $ 2.854×10^{-13}	$2.2567 \times 10^{-3} $ 1.8603×10^{-3}	0.824
pdb2k2a 422	ClassicAll QuaternionAll	8	$4.7195 \times 10^{-3} 4.7195 \times 10^{-3}$	5 5	$3.810 \times 10^{-14} 5.148 \times 10^{-14}$	$1.6479 \times 10^{-3} 1.3823 \times 10^{-3}$	0.839
pdb2k2f 1268	ClassicAll QuaternionAll	8	$1.2926 \times 10^{-11} 1.2956 \times 10^{-11}$	1 1	$2.639 \times 10^{-13} $ 2.818×10^{-13}	1.5802×10^{1} 9.4318	0.597
pdb2k36 896	ClassicAll QuaternionAll	8	$1.6972 \times 10^{-12} 1.6007 \times 10^{-12}$	1 1	$1.922 \times 10^{-13} 2.045 \times 10^{-13}$	3.5868×10^{-3} 2.9596×10^{-3}	0.825
pdb2k37 356	ClassicAll QuaternionAll	8	$3.7147 \times 10^{-12} 3.6185 \times 10^{-12}$	1 1	$1.921 \times 10^{-13} 2.525 \times 10^{-13}$	1.3966×10^{-3} 1.1705×10^{-3}	0.838
pdb2k3i 656	ClassicAll QuaternionAll	8	$4.6225 \times 10^{-3} 4.6225 \times 10^{-3}$	2 2	$3.810 \times 10^{-13} 4.009 \times 10^{-13}$	$3.2188 \times 10^{-3} $ 2.5698×10^{-3}	0.798
pdb2k6s 494	ClassicAll QuaternionAll	8	$8.2998 \times 10^{-12} 8.4519 \times 10^{-12}$	2 2	$2.100 \times 10^{-13} 2.651 \times 10^{-13}$	3.7628×10^{-3} 2.8168×10^{-3}	0.749
pdb2k7o 1096	ClassicAll QuaternionAll	8	$1.8663 \times 10^{-4} $ 1.8663×10^{-4}	1 1	1.279×10^{-13} 1.416×10^{-13}	$2.4780 \times 10^{-2} 1.6457 \times 10^{-2}$	0.664
pdb2kbm 1268	ClassicAll QuaternionAll	8 8	$1.5487 \times 10^{-12} 1.6865 \times 10^{-12}$	2 2	$2.165 \times 10^{-13} 2.226 \times 10^{-13}$	1.2294×10^{1} 7.7658	0.632
pdb2kdh 434	ClassicAll QuaternionAll	8 8	$7.2209 \times 10^{-5} 7.2209 \times 10^{-5}$	2 2	$1.947 \times 10^{-11} 2.228 \times 10^{-11}$	1.9023×10^{-3} 1.5544×10^{-3}	0.817

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2kdl 338	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.4591 \times 10^{-12} \\ 4.4513 \times 10^{-12} \end{array}$	$\frac{2}{2}$	2.301×10^{-13} 2.919×10^{-13}	$1.3040 \times 10^{-3} 1.0803 \times 10^{-3}$	0.828
pdb2kdm 338	ClassicAll QuaternionAll	8 8	$2.1896 \times 10^{-11} 2.1643 \times 10^{-11}$	1 1	3.191×10^{-12} 3.284×10^{-12}	$1.5321 \times 10^{-3} 1.2579 \times 10^{-3}$	0.821
$\begin{array}{c} \rm pdb2kdp\\ 428\end{array}$	ClassicAll QuaternionAll	8 8	$3.0283 \times 10^{-12} 3.0741 \times 10^{-12}$	1 1	$2.621 \times 10^{-13} 2.865 \times 10^{-13}$	1.6850×10^{-3} 1.4041×10^{-3}	0.833
pdb2kdr 170	ClassicAll QuaternionAll	8 8	$6.3024 \times 10^{-5} 6.3024 \times 10^{-5}$	2 2	$6.618 \times 10^{-14} \\ 8.490 \times 10^{-14}$	$6.2422 \times 10^{-4} 5.0940 \times 10^{-4}$	0.816
pdb2kes 290	ClassicAll QuaternionAll	8	$1.8528 \times 10^{-4} $ 1.8528×10^{-4}	7 7	$4.467 \times 10^{-14} 5.425 \times 10^{-14}$	$1.0982 \times 10^{-3} 8.9069 \times 10^{-4}$	0.811
pdb2kib 352	ClassicAll QuaternionAll	8	2.9706×10^{-5} 2.9706×10^{-5}	1 1	$2.533 \times 10^{-12} 2.539 \times 10^{-12}$	$1.6648 \times 10^{-2} 1.0713 \times 10^{-2}$	0.644
pdb2kjn 158	ClassicAll QuaternionAll	16 16	1.9764×10^{-12} 1.9265×10^{-12}	6 6	$9.827 \times 10^{-14} \\ 1.174 \times 10^{-13}$	$1.1418 \times 10^{-3} 9.5536 \times 10^{-4}$	0.837
pdb2kjo 158	ClassicAll QuaternionAll	8	$1.2876 \times 10^{-11} \\ 1.2921 \times 10^{-11}$	1 1	$2.284 \times 10^{-13} 2.421 \times 10^{-13}$	$5.8413 \times 10^{-4} 4.8707 \times 10^{-4}$	0.834
pdb2kjr 572	ClassicAll QuaternionAll	8 8	$5.1341 \times 10^{-11} 5.1082 \times 10^{-11}$	2 2	$3.247 \times 10^{-12} 3.252 \times 10^{-12}$	$2.8138 \times 10^{-3} 2.2933 \times 10^{-3}$	0.815
pdb2kko 1300	ClassicAll QuaternionAll	8	$6.9643 \times 10^{-4} $ 6.9643×10^{-4}	2 2	$1.191 \times 10^{-13} 1.284 \times 10^{-13}$	2.7434×10^{-2} 1.8182×10^{-2}	0.663
pdb2kl5 662	ClassicAll QuaternionAll	8	$2.4505 \times 10^{-12} $ 2.5206×10^{-12}	1 1	$1.820 \times 10^{-13} 2.020 \times 10^{-13}$	$2.6080 \times 10^{-3} $ 2.1826×10^{-3}	0.837
pdb2klz 276	ClassicAll QuaternionAll	2 2	$3.9786 \times 10^{-13} \\ 3.7834 \times 10^{-13}$	1 1	$3.439 \times 10^{-14} 4.443 \times 10^{-14}$	$7.7313 \times 10^{-4} 5.6948 \times 10^{-4}$	0.737
pdb2ko1 1060	ClassicAll QuaternionAll	8	9.3273×10^{-4} 9.3273×10^{-4}	2 2	$1.150 \times 10^{-12} \\ 1.151 \times 10^{-12}$	$3.7416 \times 10^{-2} 2.7706 \times 10^{-2}$	0.740
pdb2koz 200	ClassicAll QuaternionAll	32 32	$4.5817 \times 10^{-5} $ 4.5817×10^{-5}	2 2	$1.075 \times 10^{-9} $ 1.075×10^{-9}	1.6365×10^{-3} 1.5663×10^{-3}	0.957
pdb2kp0 200	ClassicAll QuaternionAll	8	$7.8392 \times 10^{-11} \\ 8.2404 \times 10^{-11}$	2 2	$4.894 \times 10^{-12} 5.595 \times 10^{-12}$	$7.5902 \times 10^{-4} 6.5000 \times 10^{-4}$	0.856
pdb2ksg 290	ClassicAll QuaternionAll	8 8	$9.2027 \times 10^{-13} 9.2208 \times 10^{-13}$	1 1	$3.215 \times 10^{-14} 3.967 \times 10^{-14}$	$1.1118 \times 10^{-3} \\ 9.2627 \times 10^{-4}$	0.833
pdb2kt8 458	ClassicAll QuaternionAll	8 8	$4.1573 \times 10^{-4} 4.1573 \times 10^{-4}$	1 1	$3.314 \times 10^{-12} 3.535 \times 10^{-12}$	1.7820×10^{-3} 1.4955×10^{-3}	0.839
pdb2kuh 404	ClassicAll QuaternionAll	8 8	1.1667×10^{-3} 1.1667×10^{-3}	6 6	$2.015 \times 10^{-14} 2.491 \times 10^{-14}$	$1.5892 \times 10^{-3} $ 1.3496×10^{-3}	0.849
pdb2kwh 338	ClassicAll QuaternionAll	8 8	$2.0587 \times 10^{-3} 2.0587 \times 10^{-3} 3.9712 \times 10^{-12}$	2 2	$1.408 \times 10^{-13} 1.825 \times 10^{-13}$	$1.3052 \times 10^{-3} 1.0751 \times 10^{-3}$	0.824
pdb2kxa 144	ClassicAll QuaternionAll	2 2	3.7392×10^{-12}	1 1	1.325×10^{-12} 1.351×10^{-12} 1.321×10^{-11}	4.0738×10^{-4} 3.1087×10^{-4}	0.763
pdb2kyb 362	ClassicAll QuaternionAll	8 8	3.1200×10^{-6} 3.1200×10^{-6}	2 2	1.373×10^{-11}	$3.0612 \times 10^{-3} 2.3317 \times 10^{-3}$	0.762
pdb2l3m 428	ClassicAll QuaternionAll	8 8	1.5178×10^{-3} 1.5178×10^{-3}	1 1	$1.028 \times 10^{-12} 9.340 \times 10^{-13}$	1.7016×10^{-3} 1.4289×10^{-3}	0.840
pdb2l3n 626	ClassicAll QuaternionAll	8 8	$3.9987 \times 10^{-4} 3.9987 \times 10^{-4}$	5 5	3.024×10^{-14} 3.632×10^{-14}	8.3802×10^{-3} 6.0117×10^{-3}	0.717
pdb2l45 116	ClassicAll QuaternionAll	8 8	$5.9466 \times 10^{-13} $ 6.7808×10^{-13}	1 1	$2.236 \times 10^{-14} 3.033 \times 10^{-14}$	4.2996×10^{-4} 3.6979×10^{-4}	0.860
pdb2l5r 138	ClassicAll QuaternionAll	2 2	$3.0491 \times 10^{-13} 3.0031 \times 10^{-13}$	2 2	3.535×10^{-14} 4.436×10^{-14}	3.6933×10^{-4} 2.7283×10^{-4}	0.739
pdb2l6q 374	ClassicAll QuaternionAll	16 16	1.6115×10^{-9} 1.6752×10^{-9}	13 13	$4.435 \times 10^{-11} \\ 5.413 \times 10^{-11}$	$2.0383 \times 10^{-3} 1.7964 \times 10^{-3}$	0.881
pdb2l6r 374	ClassicAll QuaternionAll	16 16	$1.0970 \times 10^{-10} 9.8250 \times 10^{-11}$	6	$2.060 \times 10^{-12} \\ 2.174 \times 10^{-12}$	1.9774×10^{-3} 1.7484×10^{-3}	0.884

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2l98 434	ClassicAll QuaternionAll	8 8	$5.6413 \times 10^{-12} 6.2089 \times 10^{-12}$	$\frac{2}{2}$	3.273×10^{-13} 3.637×10^{-13}	$1.6907 \times 10^{-3} 1.4160 \times 10^{-3}$	0.838
pdb2lci 806	ClassicAll QuaternionAll	8 8	$1.2015 \times 10^{-12} \\ 1.1830 \times 10^{-12}$	1 1	$2.579 \times 10^{-13} 2.404 \times 10^{-13}$	3.1904×10^{-3} 2.6363×10^{-3}	0.826
$\begin{array}{c} \text{pdb2lde} \\ 152 \end{array}$	ClassicAll QuaternionAll	8 8	6.0406×10^{-3} 6.0406×10^{-3}	2 2	$3.154 \times 10^{-14} 3.766 \times 10^{-14}$	$5.5682 \times 10^{-4} $ 4.6581×10^{-4}	0.837
pdb2le2 676	ClassicAll QuaternionAll	8	$1.5317 \times 10^{-12} 1.4989 \times 10^{-12}$	2 2	$2.064 \times 10^{-13} 2.042 \times 10^{-13}$	$1.0676 \times 10^{-1} 7.1841 \times 10^{-2}$	0.673
pdb2le7 122	ClassicAll QuaternionAll	8	$8.8940 \times 10^{-14} $ 1.1008×10^{-13}	2 2	$2.111 \times 10^{-14} 2.749 \times 10^{-14}$	$4.4564 \times 10^{-4} 3.7379 \times 10^{-4}$	0.839
pdb2ler 68	ClassicAll QuaternionAll	8	$5.1096 \times 10^{-14} $ 6.2001×10^{-14}	2 2	$1.314 \times 10^{-14} \\ 1.532 \times 10^{-14}$	$2.3987 \times 10^{-4} 1.9802 \times 10^{-4}$	0.826
pdb2lgi 338	ClassicAll QuaternionAll	8 8	$9.7255 \times 10^{-12} 9.6518 \times 10^{-12}$	2 2	$1.068 \times 10^{-12} \\ 1.052 \times 10^{-12}$	$1.3243 \times 10^{-3} \\ 1.1174 \times 10^{-3}$	0.844
pdb2lhc 338	ClassicAll QuaternionAll	64 64	3.8367×10^{-10} 3.8166×10^{-10}	17 17	$2.902 \times 10^{-12} 2.997 \times 10^{-12}$	$5.8791 \times 10^{-3} 5.2790 \times 10^{-3}$	0.898
pdb2lhd 338	ClassicAll QuaternionAll	8	1.3048×10^{-11} 1.4592×10^{-11}	2 2	$1.930 \times 10^{-12} 2.033 \times 10^{-12}$	$2.0522 \times 10^{-3} $ 1.6262×10^{-3}	0.792
pdb2lhe 338	ClassicAll QuaternionAll	16 16	$9.7862 \times 10^{-10} $ 9.7867×10^{-10}	2 2	$4.963 \times 10^{-11} 4.967 \times 10^{-11}$	$2.0862 \times 10^{-3} $ 1.8307×10^{-3}	0.878
pdb2lhg 338	ClassicAll QuaternionAll	8 8	$5.0995 \times 10^{-13} $ 5.4683×10^{-13}	6	$6.485 \times 10^{-14} 7.343 \times 10^{-14}$	1.3246×10^{-3} 1.1140×10^{-3}	0.841
pdb2lix 162	ClassicAll QuaternionAll	2 2	$4.9988 \times 10^{-13} \\ 5.1517 \times 10^{-13}$	1 1	$4.842 \times 10^{-14} \\ 5.614 \times 10^{-14}$	$4.9641 \times 10^{-4} \\ 3.4416 \times 10^{-4}$	0.693
pdb2lld 242	ClassicAll QuaternionAll	8	$3.3972 \times 10^{-3} 3.3972 \times 10^{-3}$	5 5	$1.938 \times 10^{-13} $ 2.216×10^{-13}	$9.3635 \times 10^{-4} 7.9552 \times 10^{-4}$	0.850
pdb2lm9 578	ClassicAll QuaternionAll	8	$2.2967 \times 10^{-3} $ 2.2967×10^{-3}	2 2	$6.254 \times 10^{-14} 7.713 \times 10^{-14}$	$2.2442 \times 10^{-3} \\ 1.8522 \times 10^{-3}$	0.825
pdb2lmf 140	ClassicAll QuaternionAll	8	$1.0942 \times 10^{-4} 1.0942 \times 10^{-4}$	1 1	$1.282 \times 10^{-13} \\ 1.462 \times 10^{-13}$	$5.2052 \times 10^{-4} 4.2699 \times 10^{-4}$	0.820
pdb2ln3 500	ClassicAll QuaternionAll	8	$2.5821 \times 10^{-13} $ 2.9987×10^{-13}	1 1	$1.292 \times 10^{-13} 1.359 \times 10^{-13}$	1.9563×10^{-3} 1.6498×10^{-3}	0.843
pdb2lo2 230	ClassicAll QuaternionAll	8	1.4423×10^{-2} 1.4423×10^{-2}	2 2	$2.068 \times 10^{-14} $ 2.571×10^{-14}	$8.6907 \times 10^{-4} 7.3205 \times 10^{-4}$	0.842
pdb2lqp 428	ClassicAll QuaternionAll	8	$5.7815 \times 10^{-4} 5.7815 \times 10^{-4}$	2 2	$2.950 \times 10^{-13} 3.085 \times 10^{-13}$	$1.6623 \times 10^{-3} 1.4024 \times 10^{-3}$	0.844
pdb2lr0 806	ClassicAll QuaternionAll	8 8	$1.2202 \times 10^{-11} $ 1.1747×10^{-11}	1	$3.549 \times 10^{-12} \\ 3.440 \times 10^{-12}$	$3.2038 \times 10^{-3} $ 2.6563×10^{-3}	0.829
pdb2lrh 806	ClassicAll QuaternionAll	8 8	$2.9721 \times 10^{-12} $ 2.9099×10^{-12}	1 1	$5.631 \times 10^{-13} \\ 6.564 \times 10^{-13}$	3.1735×10^{-3} 2.5988×10^{-3}	0.819
pdb2ls9 152	ClassicAll QuaternionAll	8	$2.7045 \times 10^{-12} 3.0425 \times 10^{-12}$	1 1	$1.122 \times 10^{-13} \\ 1.471 \times 10^{-13}$	5.6740×10^{-4} 4.7760×10^{-4}	0.842
pdb2lsa 140	ClassicAll QuaternionAll	8	$2.5535 \times 10^{-3} $ 2.5535×10^{-3}	2 2	$5.235 \times 10^{-14} 6.998 \times 10^{-14}$	$5.3337 \times 10^{-4} 4.5261 \times 10^{-4}$	0.849
pdb2lss 422	ClassicAll QuaternionAll	8 8	1.2372×10^{-3} 1.2372×10^{-3}	1 1	$1.230 \times 10^{-13} 1.455 \times 10^{-13}$	$1.6896 \times 10^{-3} $ 1.4495×10^{-3}	0.858
pdb2lt3 680	ClassicAll QuaternionAll	8 8	$9.6961 \times 10^{-13} 1.0253 \times 10^{-12}$	6 6	$7.245 \times 10^{-14} 7.760 \times 10^{-14}$	$2.6966 \times 10^{-3} 2.2362 \times 10^{-3}$	0.829
pdb2lu6 86	ClassicAll QuaternionAll	8 8	$7.7550 \times 10^{-3} 7.7550 \times 10^{-3}$	1 1	$5.356 \times 10^{-15} \\ 6.922 \times 10^{-15}$	3.0108×10^{-4} 2.4724×10^{-4}	0.821
pdb2lwa 432	ClassicAll QuaternionAll	4096 4096	$4.9078 \times 10^{-12} $ 4.0818×10^{-12}	897 897	$3.616 \times 10^{-13} $ 4.436×10^{-13}	1.6526 1.2454	0.754
pdb2lx0 194	ClassicAll QuaternionAll	16 16	$7.4851 \times 10^{-12} 7.5304 \times 10^{-12}$	5 5	$3.569 \times 10^{-13} 4.035 \times 10^{-13}$	$1.0126 \times 10^{-3} 9.2091 \times 10^{-4}$	0.909

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2lxb 892	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 9.0172 \times 10^{-13} \\ 8.6577 \times 10^{-13} \end{array}$	1 1	$1.542 \times 10^{-13} \\ 1.585 \times 10^{-13}$	$7.5076 \times 10^{-3} 5.5303 \times 10^{-3}$	0.737
pdb2lxy 404	ClassicAll QuaternionAll	8 8	$1.1155 \times 10^{-10} \\ 1.1215 \times 10^{-10}$	$\frac{2}{2}$	$9.313 \times 10^{-13} \\ 1.025 \times 10^{-12}$	$1.7815 \times 10^{-3} 1.4485 \times 10^{-3}$	0.813
pdb2lxz 194	ClassicAll QuaternionAll	8 8	$1.1003 \times 10^{-4} 1.1003 \times 10^{-4}$	2 2	$2.371 \times 10^{-12} 2.792 \times 10^{-12}$	$7.4569 \times 10^{-4} 6.3464 \times 10^{-4}$	0.851
pdb2lzf 820	ClassicAll QuaternionAll	8 8	$5.9653 \times 10^{-4} 5.9653 \times 10^{-4}$	2 2	$3.217 \times 10^{-14} 3.959 \times 10^{-14}$	$1.3323 \times 10^{-1} \\ 8.6171 \times 10^{-2}$	0.647
pdb2m1a 158	ClassicAll QuaternionAll	8	$9.1771 \times 10^{-14} 9.0451 \times 10^{-14}$	1 1	$6.346 \times 10^{-15} 7.612 \times 10^{-15}$	$5.8889 \times 10^{-4} $ 4.9233×10^{-4}	0.836
pdb2m1j 182	ClassicAll QuaternionAll	8	1.5890×10^{-13} 1.6894×10^{-13}	2 2	$1.865 \times 10^{-14} $ 2.212×10^{-14}	$6.9861 \times 10^{-4} 5.8270 \times 10^{-4}$	0.834
pdb2m2y 110	ClassicAll QuaternionAll	8 8	$1.8177 \times 10^{-3} $ 1.8177×10^{-3}	1 1	$2.699 \times 10^{-13} 2.808 \times 10^{-13}$	$4.0431 \times 10^{-4} \\ 3.4452 \times 10^{-4}$	0.852
pdb2m3f 134	ClassicAll QuaternionAll	8	$9.5240 \times 10^{-14} \\ 5.7597 \times 10^{-14}$	1 1	$3.629 \times 10^{-14} $ 4.641×10^{-14}	$4.9801 \times 10^{-4} 4.1603 \times 10^{-4}$	0.835
pdb2m4j 2178	ClassicAll QuaternionAll	8	$5.2912 \times 10^{-4} 5.2912 \times 10^{-4}$	1 1	$1.463 \times 10^{-11} \\ 1.455 \times 10^{-11}$	$5.9080 \times 10^{-2} $ 4.0903×10^{-2}	0.692
pdb2m8m 170	ClassicAll QuaternionAll	8	6.9769×10^{-3} 6.9769×10^{-3}	5 5	$2.424 \times 10^{-14} 3.058 \times 10^{-14}$	$6.3311 \times 10^{-4} 5.2295 \times 10^{-4}$	0.826
pdb2m8o 170	ClassicAll QuaternionAll	8 8	$4.7097 \times 10^{-3} $ 4.7097×10^{-3}	5 5	$1.798 \times 10^{-14} $ 2.301×10^{-14}	$6.3288 \times 10^{-4} 5.2896 \times 10^{-4}$	0.836
pdb2m97 416	ClassicAll QuaternionAll	8 8	$2.4560 \times 10^{-12} $ 2.4592×10^{-12}	6	$4.654 \times 10^{-14} 5.847 \times 10^{-14}$	1.6126×10^{-3} 1.3448×10^{-3}	0.834
pdb2m9g 1108	ClassicAll QuaternionAll	8 8	$4.9692 \times 10^{-12} $ 4.9567×10^{-12}	1 1	2.939×10^{-13} 3.170×10^{-13}	4.5864×10^{-3} 3.7468×10^{-3}	0.817
pdb2m9r 242	ClassicAll QuaternionAll	8 8	$3.7505 \times 10^{-12} $ 3.6480×10^{-12}	1 1	3.537×10^{-14} 4.406×10^{-14}	8.6972×10^{-4} 6.9111×10^{-4}	0.795
pdb2mdv 460	ClassicAll QuaternionAll	8 8	$4.7210 \times 10^{-4} 4.7210 \times 10^{-4}$	2 2	$3.178 \times 10^{-12} \\ 3.178 \times 10^{-12}$	$3.4884 \times 10^{-3} $ 2.7665×10^{-3}	0.793
pdb2me1 164	ClassicAll QuaternionAll	16 16	$ \begin{array}{r} 1.4934 \times 10^{-4} \\ 1.4934 \times 10^{-4} \end{array} $ $ \begin{array}{r} 1.3863 \times 10^{-4} \end{array} $	2 2	1.886×10^{-13} 2.202×10^{-13} 3.667×10^{-13}	1.1941×10^{-3} 1.0009×10^{-3} 6.3553×10^{-4}	0.838
pdb2me2 164 pdb2me3	ClassicAll QuaternionAll ClassicAll	8 8	1.3863×10^{-4} 1.3863×10^{-4} 3.4823×10^{-5}	1 1	5.098×10^{-13} 1.425×10^{-13}	6.3553×10^{-4} 5.2257×10^{-4} 8.2655×10^{-4}	0.822
164	QuaternionAll	16 16	3.4823×10^{-5} 3.4823×10^{-5} 2.9902×10^{-5}	6 6	1.425×10^{-13} 1.590×10^{-13} 2.854×10^{-9}	8.2655×10^{-2} 7.4826×10^{-4} 2.4576×10^{-3}	0.905
pdb2me4 164	ClassicAll QuaternionAll ClassicAll	32 32 8	2.9902×10^{-5} 2.9902×10^{-5} 4.4954×10^{-13}	2 2	2.854×10^{-9} 2.854×10^{-9} 4.400×10^{-14}	2.4376×10^{-3} 2.0387×10^{-3} 6.1082×10^{-4}	0.830
pdb2mg1 164 pdb2mg2	QuaternionAll ClassicAll	8	$ \begin{array}{r} 4.4934 \times 10 \\ 5.4976 \times 10^{-13} \\ \hline 1.0745 \times 10^{-3} \end{array} $	6	5.374×10^{-14} 1.831×10^{-14}	6.1082×10 5.0505×10^{-4} 6.3255×10^{-4}	0.827
pdb2mg2 170 pdb2mg3	QuaternionAll ClassicAll	8	$ \begin{array}{c} 1.0745 \times 10^{-3} \\ 1.0745 \times 10^{-3} \end{array} $ $ 6.2977 \times 10^{-13} $	6	$ \begin{array}{c} 1.631 \times 10 \\ 2.481 \times 10^{-14} \\ 3.542 \times 10^{-14} \end{array} $	$\begin{array}{c} 0.3233 \times 10 \\ 5.2713 \times 10^{-4} \\ \hline 6.3005 \times 10^{-4} \end{array}$	0.833
170	QuaternionAll	8	6.7812×10^{-13} 4.2246×10^{-12}	6	$ \begin{array}{c} 3.342 \times 10 \\ 4.459 \times 10^{-14} \\ \hline 1.547 \times 10^{-13} \end{array} $	$\begin{array}{c} 0.3003 \times 10 \\ 5.3291 \times 10^{-4} \\ \hline 1.3050 \times 10^{-3} \end{array}$	0.846
pdb2mh8 338	ClassicAll QuaternionAll ClassicAll	8 8	4.2240×10 4.0208×10^{-12} 3.6932×10^{-3}	6 6	$ \begin{array}{c} 1.347 \times 10 \\ 1.883 \times 10^{-13} \\ 6.229 \times 10^{-14} \end{array} $	$ \begin{array}{c} 1.3030 \times 10^{-4} \\ 1.0860 \times 10^{-3} \\ 6.3258 \times 10^{-4} \end{array} $	0.832
pdb2mhw 164	QuaternionAll	8 8	3.6932×10^{-3} 3.6932×10^{-3} 2.1485×10^{-11}	2 2	$ \begin{array}{c} 6.229 \times 10 \\ 7.130 \times 10^{-14} \\ \hline 1.828 \times 10^{-12} \end{array} $	5.4329×10^{-4} 9.0992×10^{-4}	0.859
pdb2mi1 84	Classic All	4 4	2.1485×10^{-11} 2.2963×10^{-11} 8.0637×10^{-12}	4 4	$ \begin{array}{c} 1.828 \times 10^{-12} \\ 2.053 \times 10^{-12} \\ \hline 6.022 \times 10^{-13} \end{array} $	9.0992×10^{-4} 6.4894×10^{-4} 1.7688×10^{-3}	0.713
pdb2mi7 404	Classic All	8 8	8.0637×10^{-12} 8.8714×10^{-12} 1.2077×10^{-12}	2 2	6.022×10^{-13} 6.815×10^{-13} 1.244×10^{-13}	1.7688×10^{-3} 1.4338×10^{-3} 8.5096×10^{-4}	0.811
pdb2mij 224	ClassicAll QuaternionAll	8	$1.2077 \times 10^{-12} $ 1.2294×10^{-12}	1 1	$1.244 \times 10^{-13} 1.522 \times 10^{-13}$	$8.5096 \times 10^{-4} $ 7.1647×10^{-4}	0.842

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2mix 128	ClassicAll QuaternionAll	8 8	3.7545×10^{-13} 3.4098×10^{-13}	1 1	$4.816 \times 10^{-14} 4.684 \times 10^{-14}$	$4.8667 \times 10^{-4} 4.1436 \times 10^{-4}$	0.851
pdb2mj1 110	ClassicAll QuaternionAll	8 8	$2.0809 \times 10^{-3} 2.0809 \times 10^{-3}$	1 1	$1.309 \times 10^{-13} \\ 1.646 \times 10^{-13}$	$\begin{array}{c} 4.0553 \times 10^{-4} \\ 3.4633 \times 10^{-4} \end{array}$	0.854
pdb2mj2 218	ClassicAll QuaternionAll	8 8	3.9018×10^{-3} 3.9018×10^{-3}	2 2	9.775×10^{-14} 1.192×10^{-13}	$8.0254 \times 10^{-4} $ 6.6622×10^{-4}	0.830
pdb2mjg 556	ClassicAll QuaternionAll	8 8	$1.4497 \times 10^{-3} 1.4497 \times 10^{-3}$	2 2	$5.503 \times 10^{-14} 6.579 \times 10^{-14}$	$9.7856 \times 10^{-3} 6.7540 \times 10^{-3}$	0.690
pdb2mji 788	ClassicAll QuaternionAll	8 8	$1.3090 \times 10^{-11} 1.2949 \times 10^{-11}$	1 1	$3.207 \times 10^{-12} 3.247 \times 10^{-12}$	$3.2691 \times 10^{-3} 2.7451 \times 10^{-3}$	0.840
pdb2mle 434	ClassicAll QuaternionAll	8 8	1.6719×10^{-3} 1.6719×10^{-3}	2 2	$1.491 \times 10^{-13} 1.535 \times 10^{-13}$	1.7083×10^{-3} 1.4259×10^{-3}	0.835
pdb2mlf 434	ClassicAll QuaternionAll	8	$8.3036 \times 10^{-13} \\ 8.8493 \times 10^{-13}$	2 2	$9.918 \times 10^{-14} \\ 1.127 \times 10^{-13}$	1.6983×10^{-3} 1.4242×10^{-3}	0.839
pdb2mo5 854	ClassicAll QuaternionAll	16 16	1.9007×10^{-11} 1.8458×10^{-11}	5 5	$1.394 \times 10^{-12} 1.403 \times 10^{-12}$	6.9065×10^{-3} 5.6456×10^{-3}	0.817
pdb2mpu 554	ClassicAll QuaternionAll	8	$2.5305 \times 10^{-12} 2.5592 \times 10^{-12}$	1 1	$9.785 \times 10^{-14} \\ 1.016 \times 10^{-13}$	$2.1868 \times 10^{-3} $ 1.8557×10^{-3}	0.849
pdb2mra 704	ClassicAll QuaternionAll	8	$4.3616 \times 10^{-12} $ 4.3117×10^{-12}	1 1	$2.632 \times 10^{-13} $ 2.768×10^{-13}	$3.2218 \times 10^{-3} 2.6057 \times 10^{-3}$	0.809
pdb2msu 122	ClassicAll QuaternionAll	8	$3.6237 \times 10^{-12} \\ 3.6441 \times 10^{-12}$	1 1	$7.813 \times 10^{-14} \\ 8.765 \times 10^{-14}$	$4.5330 \times 10^{-4} 3.8733 \times 10^{-4}$	0.854
pdb2mty 120	ClassicAll QuaternionAll	2 2	$5.1232 \times 10^{-12} 5.2129 \times 10^{-12}$	2 2	$1.848 \times 10^{-14} $ 2.363×10^{-14}	$3.4654 \times 10^{-4} $ 2.5168×10^{-4}	0.726
pdb2muh 98	ClassicAll QuaternionAll	16 16	$8.0615 \times 10^{-5} 8.0615 \times 10^{-5}$	2 2	$2.008 \times 10^{-13} 2.279 \times 10^{-13}$	$6.8039 \times 10^{-4} 5.6829 \times 10^{-4}$	0.835
pdb2mvj 156	ClassicAll QuaternionAll	4	$6.1752 \times 10^{-12} $ 6.1858×10^{-12}	1 1	$1.534 \times 10^{-13} 1.647 \times 10^{-13}$	$4.9138 \times 10^{-4} 3.7955 \times 10^{-4}$	0.772
pdb2mvt 284	ClassicAll QuaternionAll	8	$1.5441 \times 10^{-4} \\ 1.5441 \times 10^{-4}$	2 2	$6.053 \times 10^{-12} \\ 6.225 \times 10^{-12}$	$1.2472 \times 10^{-3} 1.0370 \times 10^{-3}$	0.831
pdb2mvx 2360	ClassicAll QuaternionAll	16 16	$5.8655 \times 10^{-5} 5.8655 \times 10^{-5}$	10 10	$1.968 \times 10^{-10} \\ 1.971 \times 10^{-10}$	$9.9972 \times 10^{-2} 5.0179 \times 10^{-2}$	0.502
pdb2mz6 220	ClassicAll QuaternionAll	16 16	$2.3371 \times 10^{-10} 2.3374 \times 10^{-10}$	5 5	$2.141 \times 10^{-11} \\ 2.153 \times 10^{-11}$	$9.6047 \times 10^{-2} 6.2469 \times 10^{-2}$	0.650
pdb2n00 572	ClassicAll QuaternionAll	8	$1.2439 \times 10^{-4} 1.2439 \times 10^{-4}$	2 2	$2.703 \times 10^{-13} 3.466 \times 10^{-13}$	$2.2331 \times 10^{-3} 1.8714 \times 10^{-3}$	0.838
pdb2n0b 60	ClassicAll QuaternionAll	4	$1.0219 \times 10^{-11} 1.0781 \times 10^{-11}$	4 4	$7.123 \times 10^{-13} 9.477 \times 10^{-13}$	$1.6915 \times 10^{-4} 1.2827 \times 10^{-4}$	0.758
pdb2n0c 60	ClassicAll QuaternionAll	2 2	$1.0471 \times 10^{-12} \\ 9.1394 \times 10^{-13}$	1 1	$1.293 \times 10^{-13} 1.682 \times 10^{-13}$	$1.4821 \times 10^{-4} 1.0619 \times 10^{-4}$	0.716
pdb2n0d 60	ClassicAll QuaternionAll	4	$5.2061 \times 10^{-11} 5.7645 \times 10^{-11}$	3 3	$3.639 \times 10^{-12} 4.540 \times 10^{-12}$	$2.6262 \times 10^{-4} 1.9204 \times 10^{-4}$	0.731
pdb2n0e 60	ClassicAll QuaternionAll	2 2	1.1503×10^{-11} 1.8786×10^{-11}	2 2	$3.314 \times 10^{-12} 4.286 \times 10^{-12}$	$1.5636 \times 10^{-4} $ 1.1376×10^{-4}	0.728
pdb2n0f 60	ClassicAll QuaternionAll	4	$2.2697 \times 10^{-12} 2.7490 \times 10^{-12}$	2 2	$3.185 \times 10^{-13} 4.023 \times 10^{-13}$	$1.7095 \times 10^{-4} 1.3283 \times 10^{-4}$	0.777
pdb2n0g 60	ClassicAll QuaternionAll	2 2	$1.4896 \times 10^{-11} \\ 1.4974 \times 10^{-11}$	1 1	$8.315 \times 10^{-13} 9.618 \times 10^{-13}$	$1.5588 \times 10^{-4} 1.1273 \times 10^{-4}$	0.723
pdb2n0h 60	ClassicAll QuaternionAll	2 2	$4.1935 \times 10^{-12} 4.1379 \times 10^{-12}$	2 2	$7.716 \times 10^{-13} \\ 8.755 \times 10^{-13}$	$1.5529 \times 10^{-4} 1.1375 \times 10^{-4}$	0.732
pdb2n35 314	ClassicAll QuaternionAll	8	1.4478×10^{-4} 1.4478×10^{-4}	6 6	$3.658 \times 10^{-14} $ 4.617×10^{-14}	1.2227×10^{-3} 1.0060×10^{-3}	0.823
pdb2n3a 574	ClassicAll QuaternionAll	8 8	$2.1457 \times 10^{-3} 2.1457 \times 10^{-3}$	5 5	$8.770 \times 10^{-14} 1.049 \times 10^{-13}$	$3.4952 \times 10^{-2} 2.2720 \times 10^{-2}$	0.650

Table 4: Results - continued

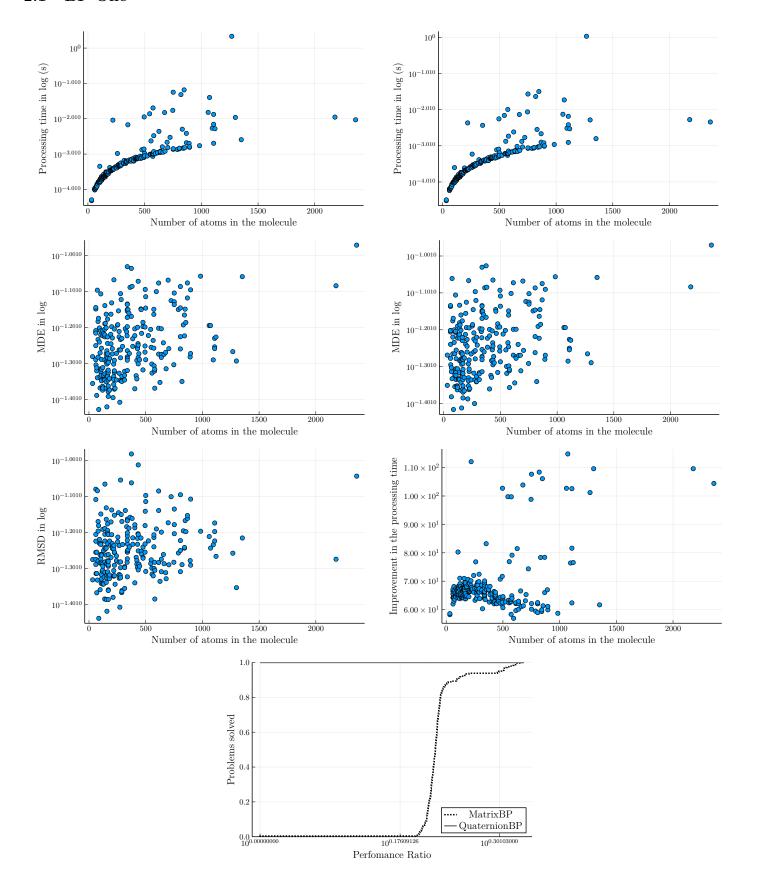
Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2n41 638	ClassicAll QuaternionAll	8 8	$5.9366 \times 10^{-3} 5.9366 \times 10^{-3}$	$\frac{2}{2}$	$1.812 \times 10^{-13} \\ 1.836 \times 10^{-13}$	$2.4931 \times 10^{-3} 2.0916 \times 10^{-3}$	0.839
pdb2n4e 638	ClassicAll QuaternionAll	8 8	$5.1960 \times 10^{-3} 5.1960 \times 10^{-3}$	$\frac{2}{2}$	$1.494 \times 10^{-13} 1.687 \times 10^{-13}$	$2.5130 \times 10^{-3} 2.0954 \times 10^{-3}$	0.834
pdb2n5q 164	ClassicAll QuaternionAll	16 16	$1.1051 \times 10^{-11} 9.3428 \times 10^{-12}$	1 1	$1.732 \times 10^{-12} 1.745 \times 10^{-12}$	1.2396×10^{-3} 1.0592×10^{-3}	0.854
pdb2n67 566	ClassicAll QuaternionAll	8	$2.0736 \times 10^{-12} 2.0936 \times 10^{-12}$	1 1	$4.443 \times 10^{-13} 4.465 \times 10^{-13}$	$2.2246 \times 10^{-3} 1.8900 \times 10^{-3}$	0.850
pdb2n6n 192	ClassicAll QuaternionAll	4	$1.6681 \times 10^{-12} $ 1.2630×10^{-12}	3	$6.557 \times 10^{-13} 7.492 \times 10^{-13}$	$7.3330 \times 10^{-4} 5.7182 \times 10^{-4}$	0.780
pdb2n7i 224	ClassicAll QuaternionAll	16 16	1.3998×10^{-4} 1.3998×10^{-4}	1 1	$9.212 \times 10^{-13} \\ 1.126 \times 10^{-12}$	$1.5787 \times 10^{-3} $ 1.3360×10^{-3}	0.846
pdb2n7j 336	ClassicAll QuaternionAll	2 2	$2.5110 \times 10^{-12} $ 2.6436×10^{-12}	1 1	$5.969 \times 10^{-13} \\ 6.094 \times 10^{-13}$	$9.6902 \times 10^{-4} 7.2525 \times 10^{-4}$	0.748
pdb2n9b 832	ClassicAll QuaternionAll	16 16	$4.0200 \times 10^{-10} $ 4.0126×10^{-10}	1 1	1.196×10^{-12} 1.238×10^{-12} 5.440×10^{-14}	9.5952×10^{-2} 5.9806×10^{-2}	0.623
pdb2na9 266	ClassicAll QuaternionAll	8 8	2.3390×10^{-12} 2.3721×10^{-12} 3.1313×10^{-3}	1 1	6.690×10^{-14} 3.365×10^{-14}	1.0077×10^{-3} 8.3528×10^{-4} 4.0529×10^{-4}	0.829
pdb2ndc 110	ClassicAll QuaternionAll ClassicAll	8 8 8	3.1313×10^{-3} 3.1313×10^{-3} 8.5286×10^{-5}	2 2	$ \begin{array}{c} 3.365 \times 10^{-14} \\ 4.481 \times 10^{-14} \\ \hline 7.022 \times 10^{-14} \end{array} $	4.0329×10^{-2} 3.4510×10^{-4} 4.0262×10^{-4}	0.851
pdb2nde 110 pdb2ndk	QuaternionAll ClassicAll	8 8	8.5286×10^{-5} 8.5286×10^{-5} 9.0150×10^{-5}	2 2 1	$ \begin{array}{c} 7.022 \times 10^{-14} \\ 8.855 \times 10^{-14} \\ \hline 5.022 \times 10^{-13} \end{array} $	$ \begin{array}{c} 4.0202 \times 10^{-2} \\ 3.3735 \times 10^{-4} \\ 1.1188 \times 10^{-3} \end{array} $	0.838
pdb2ndk 290 pdb2nvj	Quaternion All Classic All	8	9.0150×10^{-5} 9.0150×10^{-5} 6.7520×10^{-3}	7	$ \begin{array}{c} 3.022 \times 10 \\ 6.279 \times 10^{-13} \\ 2.082 \times 10^{-14} \end{array} $	9.4109×10^{-4} 5.8298×10^{-4}	0.841
152 pdb2p6j	Quaternion All Classic All	8	6.7520×10^{-3} 6.7520×10^{-3} 3.2640×10^{-13}	7	2.082×10 2.293×10^{-14} 4.795×10^{-14}	5.0233×10 5.0042×10^{-4} 1.2223×10^{-3}	0.858
314 pdb2p81	Quaternion All Classic All	8 32	3.5480×10^{-13} 6.8538×10^{-11}	1 2	6.389×10^{-14} 7.881×10^{-13}	$ \begin{array}{c} 1.2226 \times 10 \\ 1.0205 \times 10^{-3} \\ 2.7283 \times 10^{-3} \end{array} $	0.835
266 pdb2pqe	Quaternion All Classic All	$\frac{32}{32}$	6.8914×10^{-11} 2.0306×10^{-5}	26	8.226×10^{-13} 5.532×10^{-10}	$ \begin{array}{c} 2.7253 \times 10 \\ 2.4064 \times 10^{-3} \\ \hline 1.5317 \times 10^{-2} \end{array} $	0.882
896 pdb2rlg	Quaternion All Classic All	64	2.0306×10^{-5} 2.0306×10^{-13} 4.8140×10^{-13}	26 1	5.544×10^{-10} 5.501×10^{-14}	$ \begin{array}{c} 1.6317 \times 10 \\ 1.4398 \times 10^{-2} \\ \hline 2.8883 \times 10^{-4} \end{array} $	0.940
108 pdb2rlh	Quaternion All Classic All	2	5.3066×10^{-13} 1.0750×10^{-12}	1	6.973×10^{-14} 4.772×10^{-14}	$ \begin{array}{c} 2.0006 \times 10 \\ 2.1323 \times 10^{-4} \\ 2.9126 \times 10^{-4} \end{array} $	0.738
108 pdb2rmy	Quaternion All Classic All	2 8	1.0423×10^{-12} 1.2240×10^{-4}	1	5.801×10^{-14} 1.872×10^{-13}	$ \begin{array}{c} 2.1750 \times 10^{-4} \\ 7.6720 \times 10^{-4} \end{array} $	0.747
206 pdb2rnd	QuaternionAll ClassicAll	8 256	1.2240×10^{-4} 3.4031×10^{-12}	33	2.498×10^{-13} 2.626×10^{-13}	6.3644×10^{-4} 2.4660×10^{-2}	0.830
206 pdb2roo	QuaternionAll ClassicAll	256 8	3.8842×10^{-12} 3.3639×10^{-4}	33 6	3.569×10^{-13} 2.933×10^{-12}	2.1352×10^{-2} 1.6999×10^{-3}	0.866
260 pdb2rql	QuaternionAll ClassicAll	8	3.3639×10^{-4} 9.9510×10^{-11}	6	3.525×10^{-12} 2.345×10^{-12}	1.2858×10^{-3} 2.6441×10^{-3}	0.756
572 pdb2rut	QuaternionAll ClassicAll	8	1.0013×10^{-10} 2.0579×10^{-13}	2	2.496×10^{-12} 4.389×10^{-14}	2.1668×10^{-3} 8.1021×10^{-4}	0.819
218 pdb2ruv	QuaternionAll ClassicAll	8	4.0527×10^{-13} 5.4278×10^{-13}	2	5.013×10^{-14} 5.775×10^{-14}	6.7853×10^{-4} 8.3265×10^{-4}	0.837
224 pdb2rux	QuaternionAll ClassicAll	8	6.5510×10^{-13} 3.6084×10^{-3}	1	7.404×10^{-14} 2.671×10^{-14}	6.9562×10^{-4} 8.1062×10^{-4}	0.835
218 pdb2ruy	QuaternionAll ClassicAll	8	3.6084×10^{-3} 4.1535×10^{-13}	1 1	3.016×10^{-14} 1.968×10^{-14}	6.8615×10^{-4} 8.2476×10^{-4}	0.846
224 pdb2rv3	QuaternionAll ClassicAll	8	3.5981×10^{-13} 3.0630×10^{-4}	1	2.387×10^{-14} 3.656×10^{-14}	6.8436×10^{-4} 8.1289×10^{-4}	0.830
218	QuaternionAll	8	3.0630×10^{-4}	1	4.118×10^{-14}	6.8247×10^{-4}	0.840

Table 4: Results - continued

Problem Size	Method	$ \mathcal{X} $	$\min_{\mathbf{x} \in \mathcal{X}} \text{RMSD}(\mathbf{x}, \mathbf{x}_o)$	$i: \mathbf{x_i} \sim \mathbf{x}_o$	$\text{MDE}(\mathbf{x}_i)$	Time	Ratio
pdb2rv5 212	ClassicAll QuaternionAll	8 8	$8.6519 \times 10^{-4} \\ 8.6519 \times 10^{-4}$	1 1	$1.145 \times 10^{-14} \\ 1.338 \times 10^{-14}$	$7.9604 \times 10^{-4} 6.7290 \times 10^{-4}$	0.845
pdb2y4q 476	ClassicAll QuaternionAll	8 8	$\begin{array}{c} 4.6451 \times 10^{-11} \\ 4.6324 \times 10^{-11} \end{array}$	2 2	$1.410 \times 10^{-12} \\ 1.451 \times 10^{-12}$	1.8643×10^{-3} 1.5702×10^{-3}	0.842

2 Visual analysis

2.1 BP-One



2.2 BP-All

