Uninformed Search

CS161

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What is uninformed search?

- Structure: Search 'engine'
- Construct a search tree of the state space
- Two important notions:
 - Expanding a state
 - Generating a state
- Fringe/frontier: nodes not yet expanded
- Essence of search: which state to expand next?
 Leads to different search strategies
- Blind/uninformed vs. Heuristic/informed search

Tree Search Algorithm

```
frontier = {initial state}

loop do

if frontier is empty return fail

node = choose leaf to remove from frontier

if node is goal state return node's state

frontier += node.expand()
```

Graph Search Algorithm

```
frontier = {initial state}

loop do

if frontier is empty return fail

node = choose leaf to remove from frontier

if node is goal state return node's state

frontier += node.expand()
```

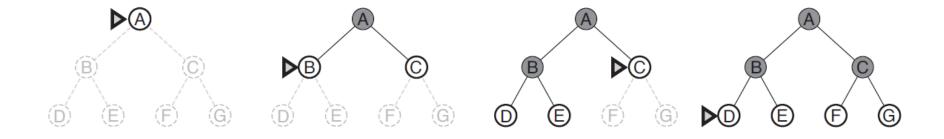
- + Add chosen leaf to explored set (initially empty)
- + Add only new nodes to frontier

 Nodes not in frontier or explored set

How Many Nodes in Search Tree?

• Branching factor b; depth d; node count N(b,d) $N(b,d) = 1 + b + b^2 + \cdots + b^d$ $b \cdot N(b,d) = b + b^2 + b^3 + \dots + b^{d+1}$ $b \cdot N(b,d) - N(b,d) = b^{d+1} - 1$ $N(b,d) = \frac{b^{d+1} - 1}{b-1} \approx \frac{b^{d+1}}{b-1}$ $= b^d \left(\frac{b}{b-1}\right)$ $= O(b^d)$

Breadth-First Search



Properties



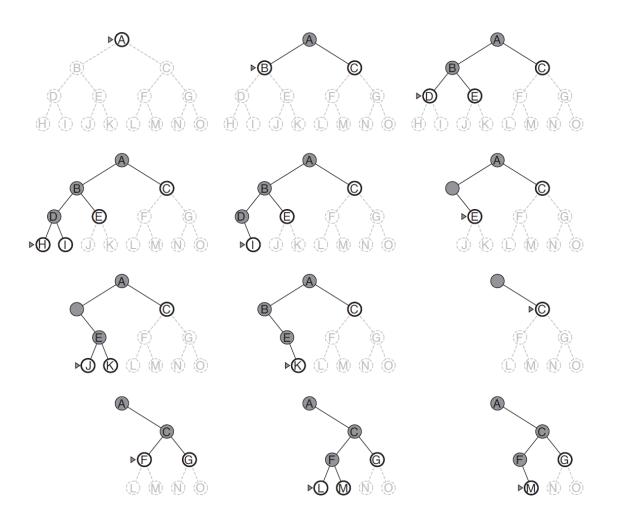
- Complete? Yes
- Optimal? Yes

Frontier separates explored from unexplored states

- Time and space complexity depend on whether goal test happens on expand or on generate.
 - On expand: $O(b^{d+1})$
 - On generate: $O(b^d)$

(d is optimal solution depth, b is branching factor)

Depth-First Search



Properties

- Complete? No
 - Fails in infinite-depth spaces:
 - Loops (run in circles)
 - Infinite state space (e.g., Knuth's problem)
- Optimal? No
- Time complexity: $O(b^m)$ When is this good/bad?
- Space complexity: O(bm)
 (m is max depth of search tree)

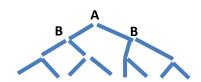


What about repeated states?

Can turn a linear problem into exponential

— E.g.:





- E.g.: moving in a grid
 - Search tree at depth d has O(4^d) nodes
 - Only O(d^2) distinct leaves (a circle in the grid)
 - For d=20: trillion vs. hundred nodes.
- DFS is not for free!



How to deal with repeated states?

- 1. Check your parents
- 2. Check your ancestors
- 3. Check every node visited already

- (1-2) is cheap with DFS
- (3) is graph search instead of tree search
 - Complexity O(s) where s is number of states
 - Can be less than O(b^d) but more than O(bd)

Can we make DFS terminate?

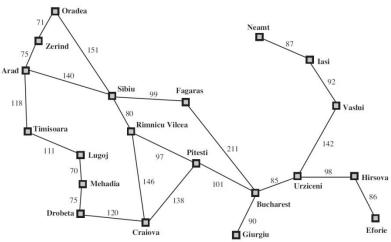
Depth-Limited Search

- Pretend search tree stops at depth limit l Nodes at depth l have no successor
- Run DFS

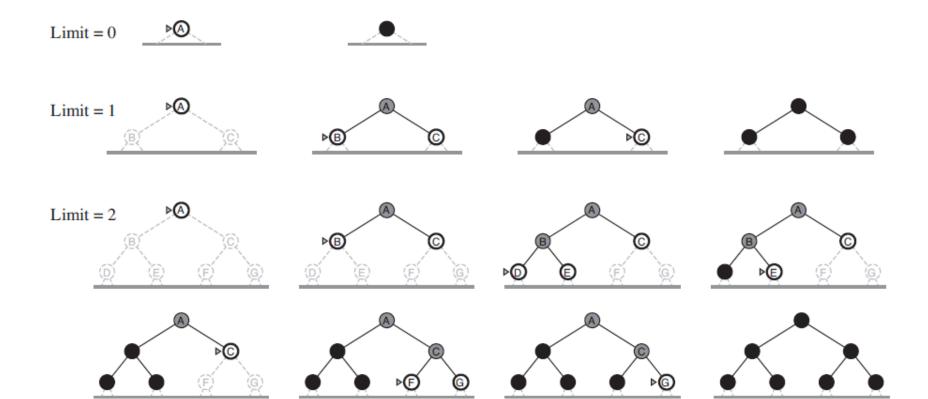
- Complete? Yes, if $l \ge d$.
- Optimal? No
- Time complexity? $O(b^l)$
- Space complexity? O(bl)

Can we make DLS complete?

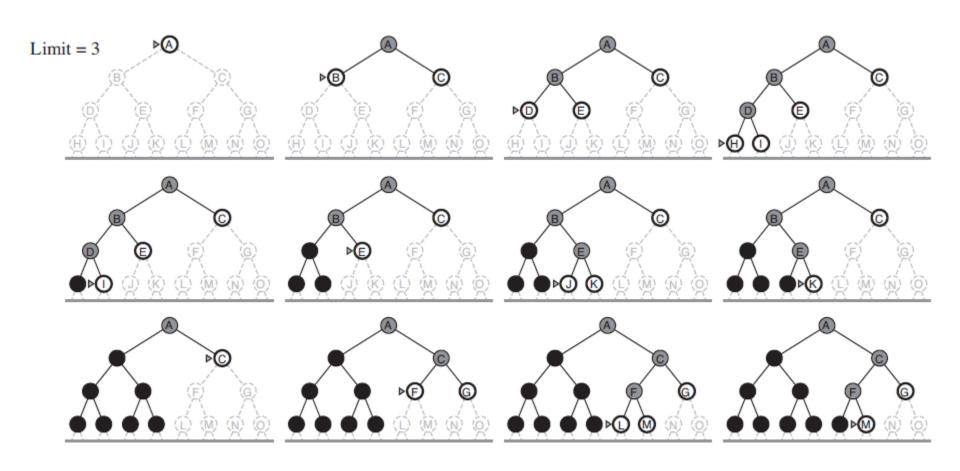
- How do we set depth limit !?
 - Maximum length path without repeated states
 - Compute the <u>diameter</u> of search space:
 Maximum shortest path between any two nodes
 - E.g., Romania has 20 cities:
 - Depth limit 19 is trivial
 - Diameter is 9, therefore deptl
- More general solution?



Iterative Deepening



Iterative Deepening



Properties

- Complete? Yes
- Optimal? Yes
- Space? O(*bd*)
- Time?



ID Time Complexity

• Time?





nodes explored in total

$$\approx b^0 \left(\frac{b}{b-1}\right) + b^1 \left(\frac{b}{b-1}\right) + \cdots = b^d \left(\frac{b}{b-1}\right)^2$$

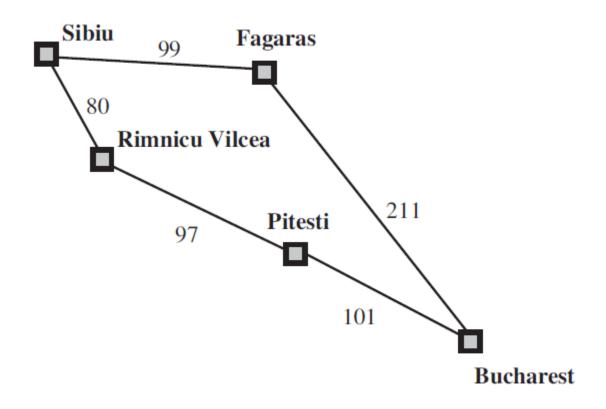
- ID is $\left(\frac{b}{b-1}\right)$ times slower than BFS (at most 2 times)
- b=10,d=5: 111k nodes for BFS/DFS, 123k for ID
- Can ID be better than BFS?

Yes if BFS goal test on expand: 1111k nodes for BFS!

Bidirectional Search

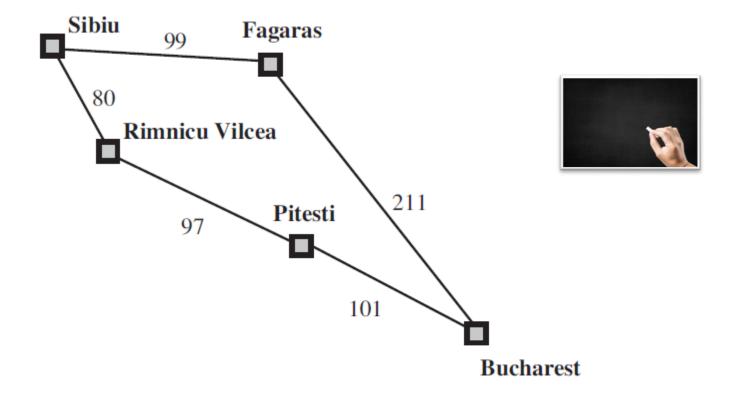


What if costs not 1 per action?



Uniform-Cost Search

f(n) is distance g(n) from start



Properties

- Optimality: Careful about goal test!!!
- Complexity analysis
 - $-C^*$ is best solution cost
 - $-\epsilon$ is cheapest action cost

