

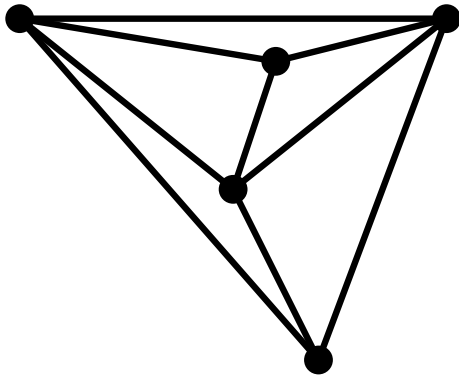
Compact Drawings of 1-Planar Graphs with Right-Angle Crossings and Few Bends

Steven Chaplick, Fabian Lipp,
Alexander Wolff, and **Johannes Zink**

Introduction: Beyond-Planar Graphs

2

Types of drawings:



Planar:

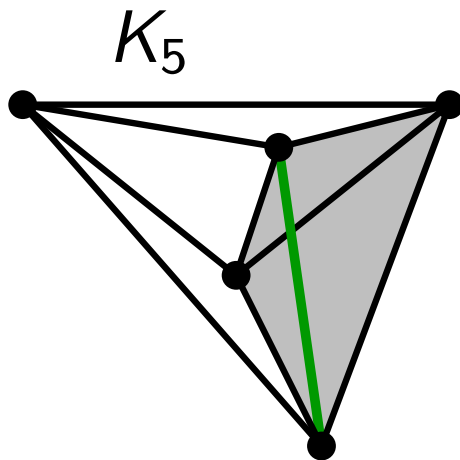
No crossings

Introduction: Beyond-Planar Graphs

2

Types of drawings:

1-Planar: ≤ 1 crossings per edge



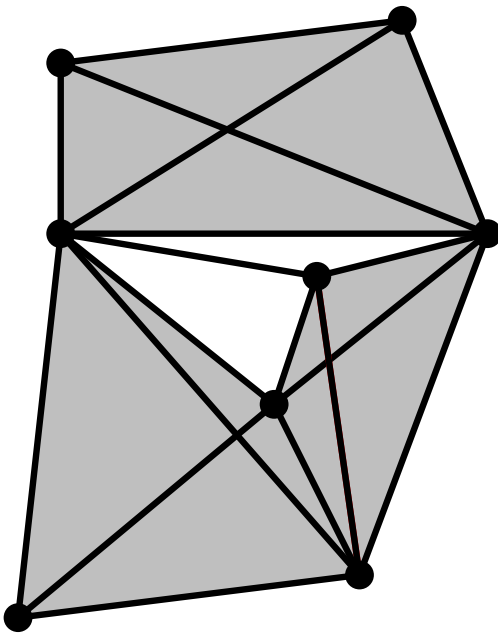
Planar: No crossings

Introduction: Beyond-Planar Graphs

2

Types of drawings:

1-Planar: ≤ 1 crossings per edge



Planar: No crossings

Introduction: Beyond-Planar Graphs

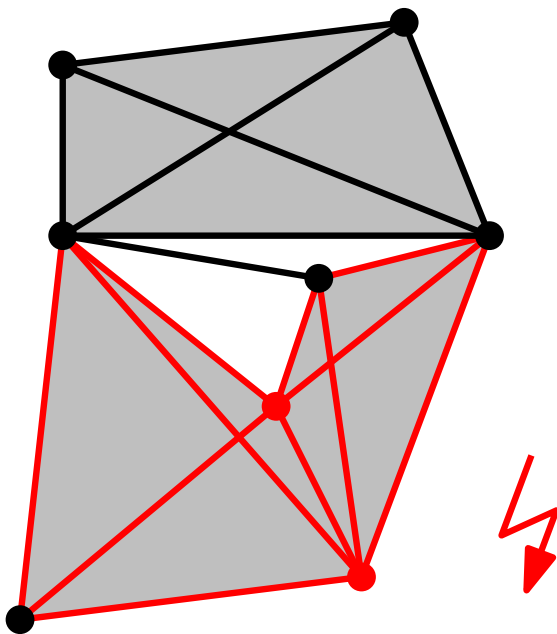
2

Types of drawings:

1-Planar: ≤ 1 crossings per edge

NIC-Planar: Two crossings share ≤ 1 vertices

Planar: No crossings



Introduction: Beyond-Planar Graphs

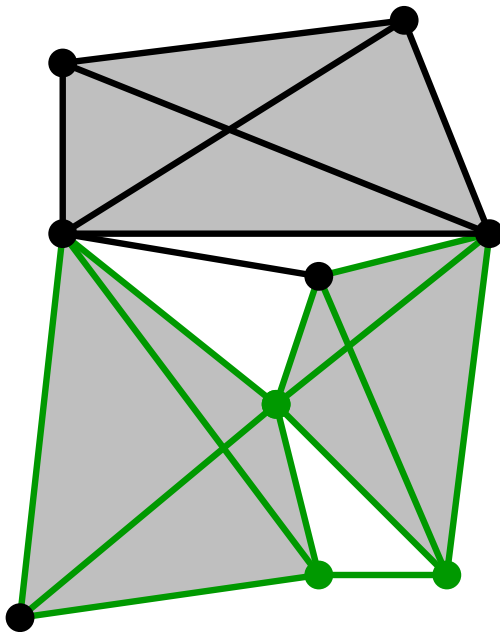
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Introduction: Beyond-Planar Graphs

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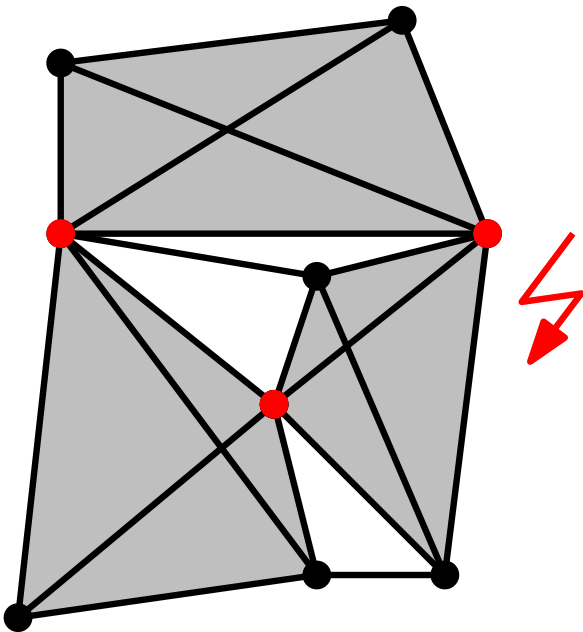
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Introduction: Beyond-Planar Graphs

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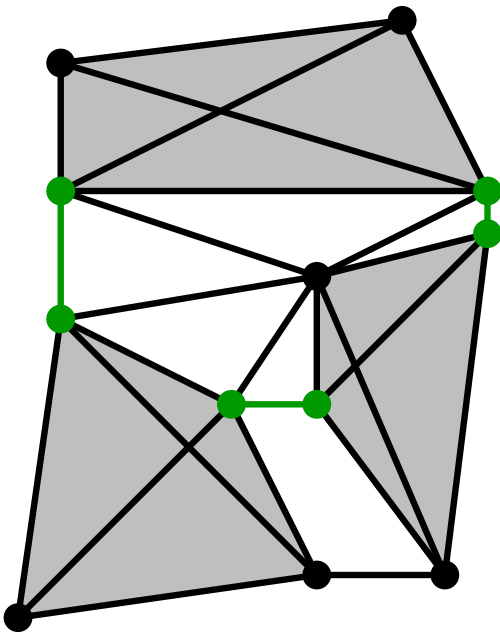
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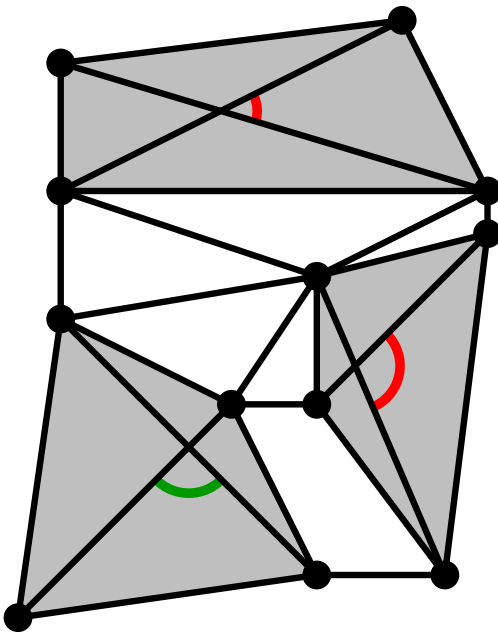
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IC-Planar: Two crossings share no vertices

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RAC: Right angle crossings



Introduction: Beyond-Planar Graphs

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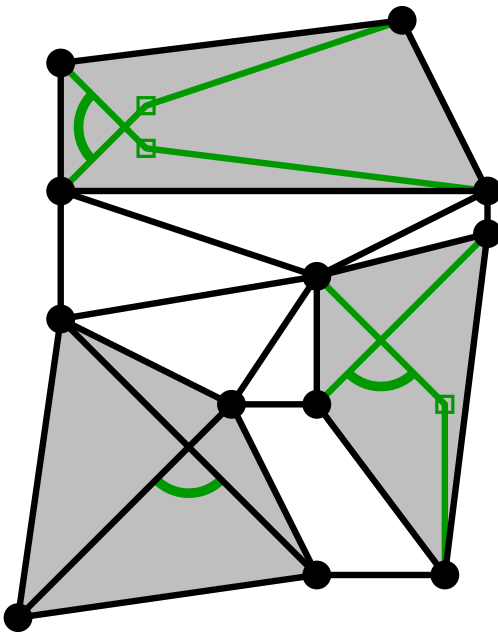
IC-Planar: Two crossings share no vertices

Planar: No crossings

RAC: Right angle crossings

RAC_k : with $\leq k$ bends per edge

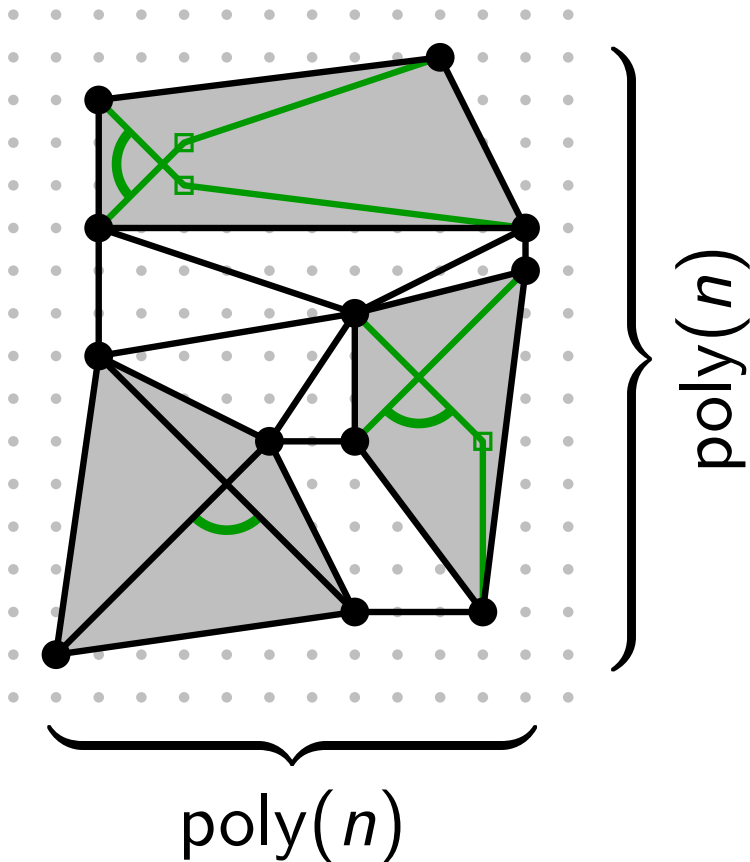
RAC_0 : with straight-line edges



Introduction: Beyond-Planar Graphs

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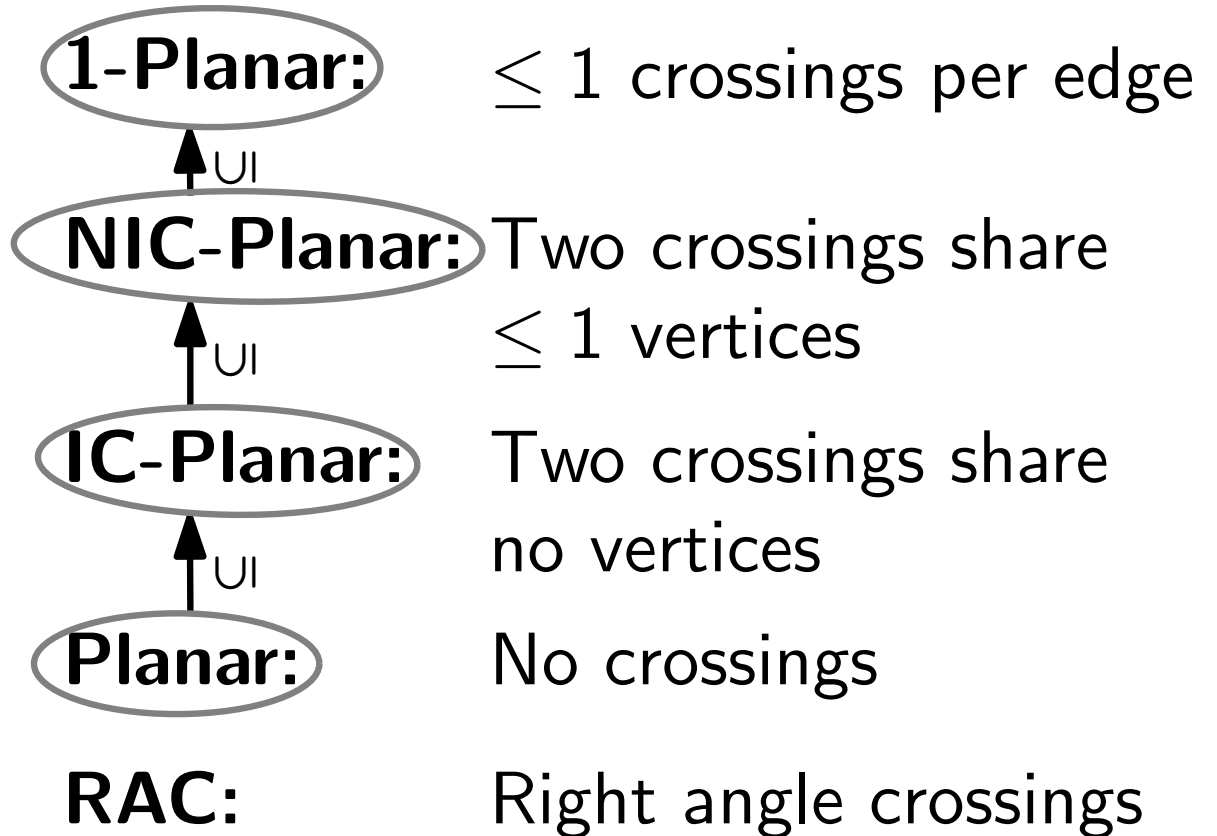
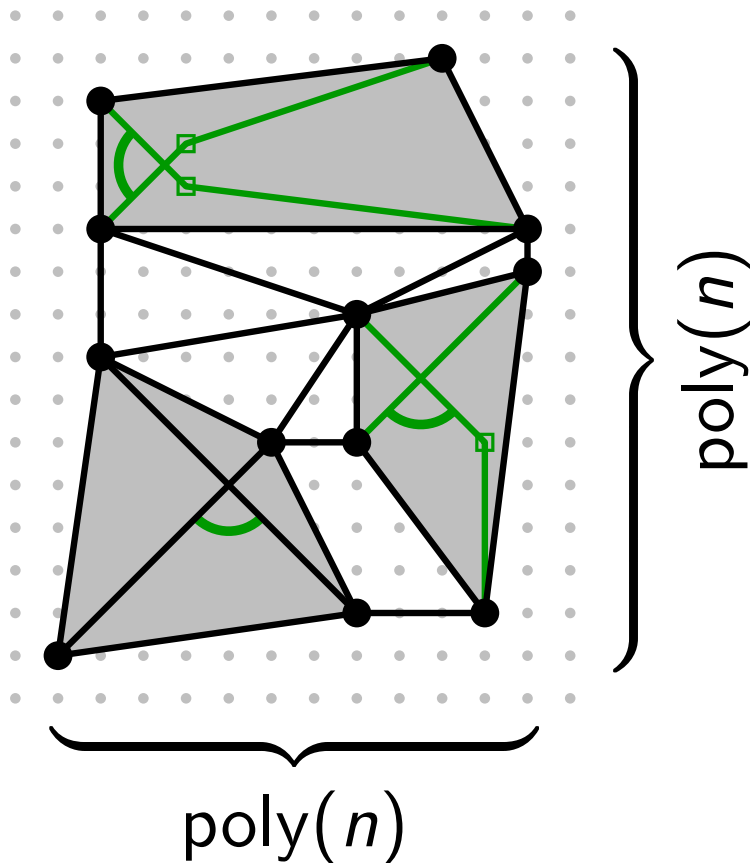
RAC_0 : with straight-line edges

RAC^{poly} : in polynomial area

Introduction: Beyond-Planar Graphs

2

Types of drawings:



RAC_k : with $\leq k$ bends per edge

RAC_0 : with straight-line edges

RAC^{poly} : in polynomial area

Introduction: The Shift Algorithm

3

[de Fraysseix, Pach, and Pollack, 1990]

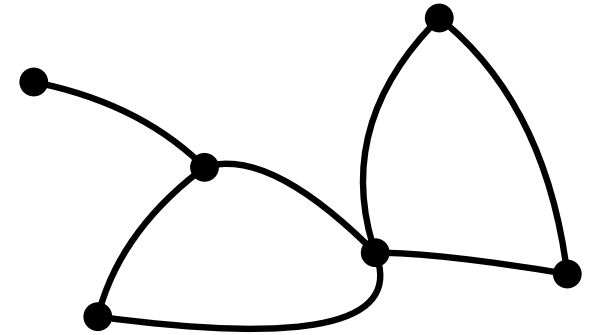
[Chrobak and Payne, 1995]

Introduction: The Shift Algorithm

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[Chrobak and Payne, 1995]

Idea:



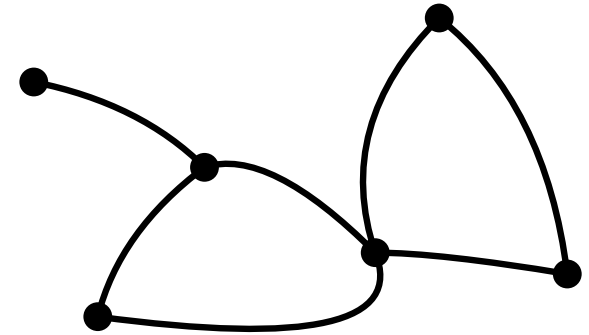
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Idea:

- Triangulate given plane graph.



Introduction: The Shift Algorithm

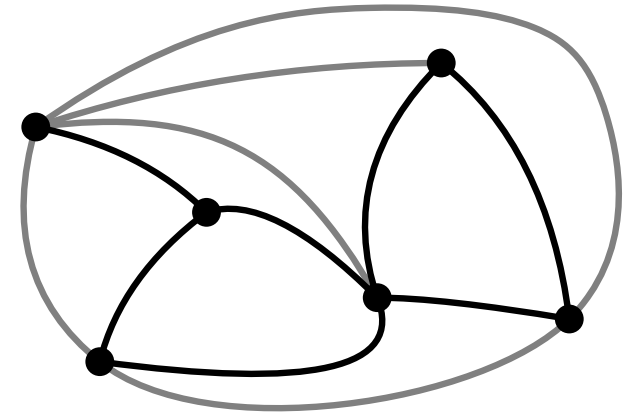
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Introduction: The Shift Algorithm

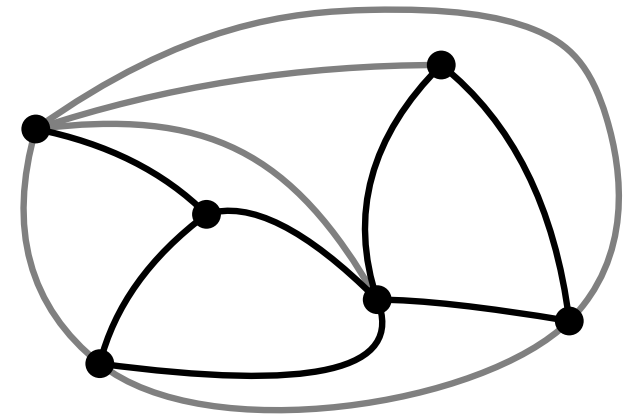
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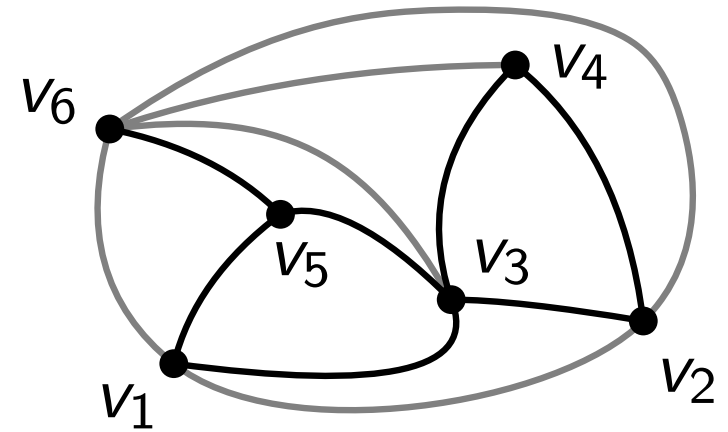
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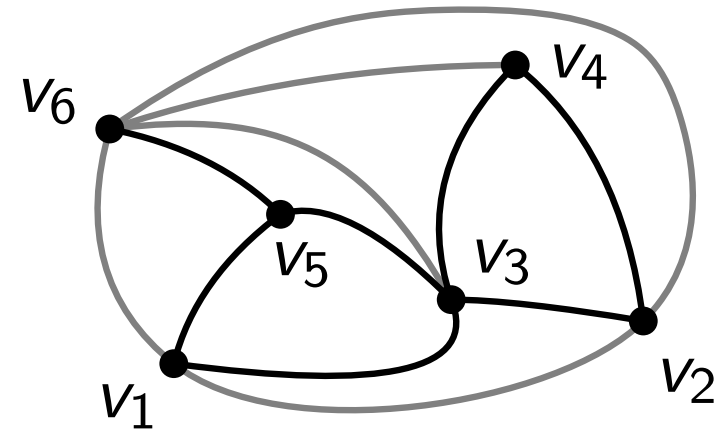
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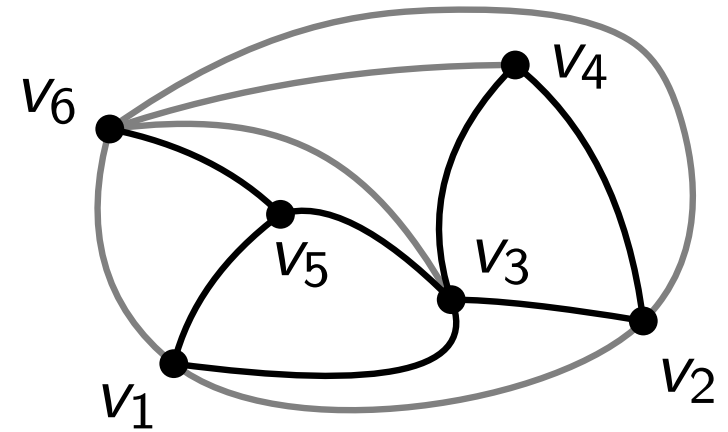
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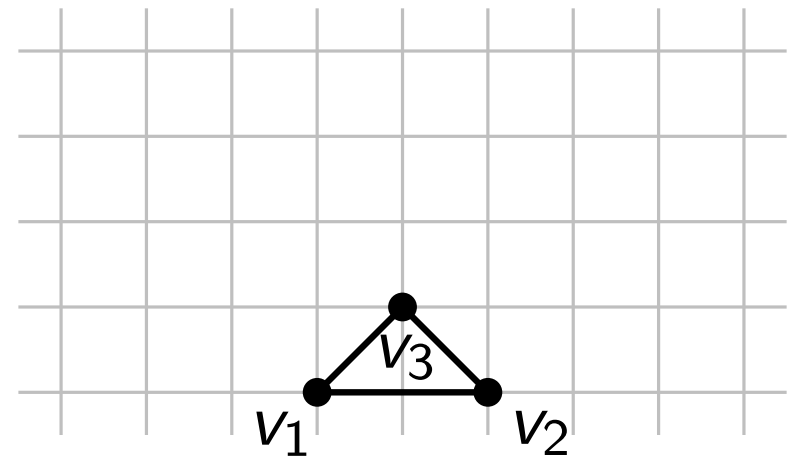
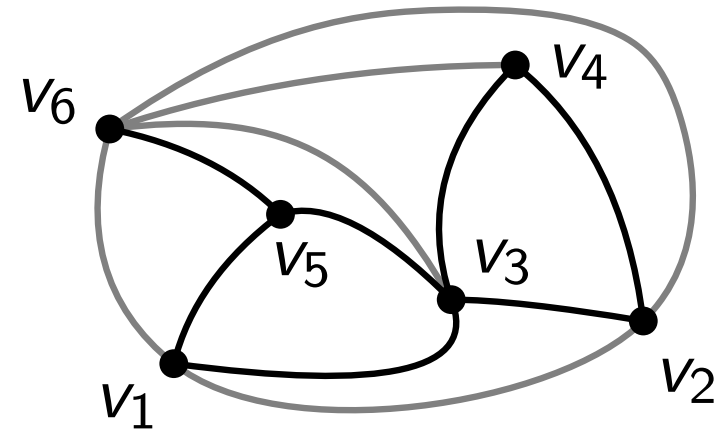
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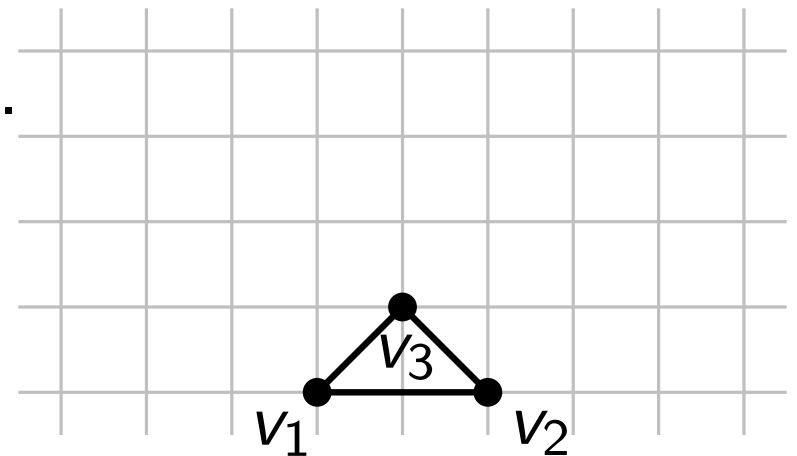
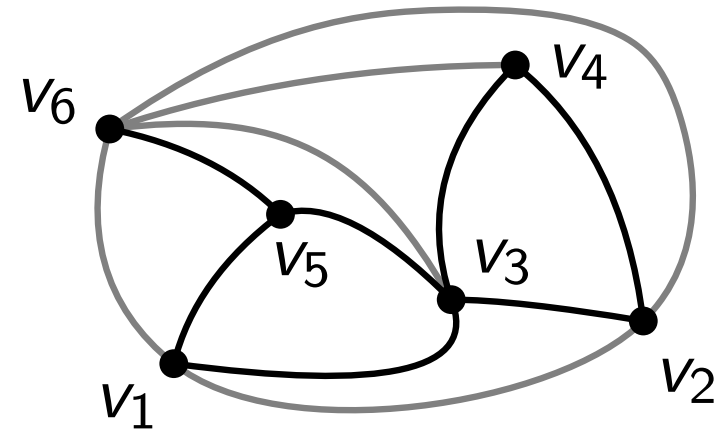
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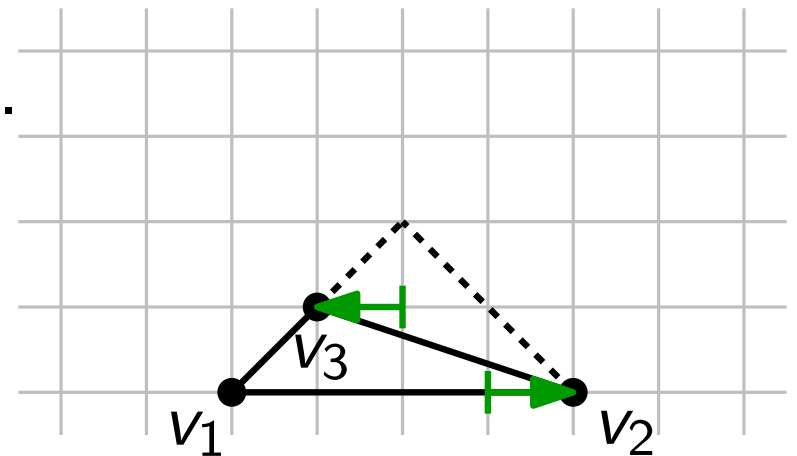
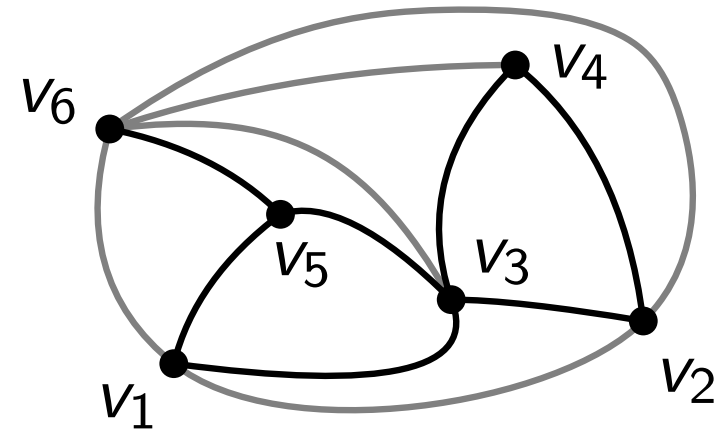
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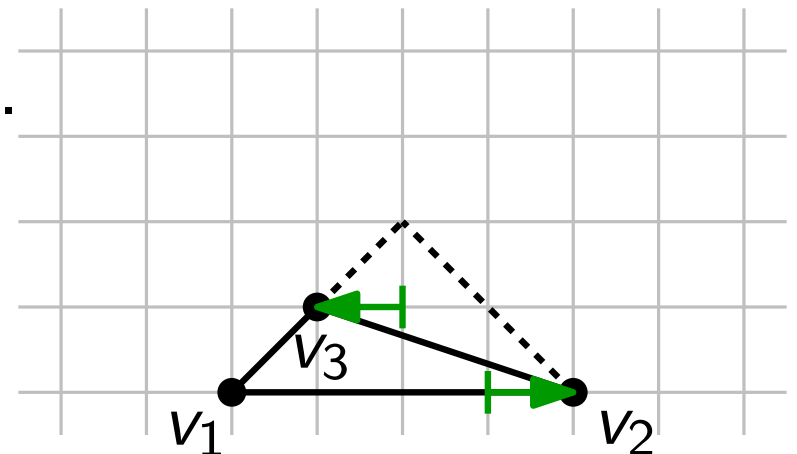
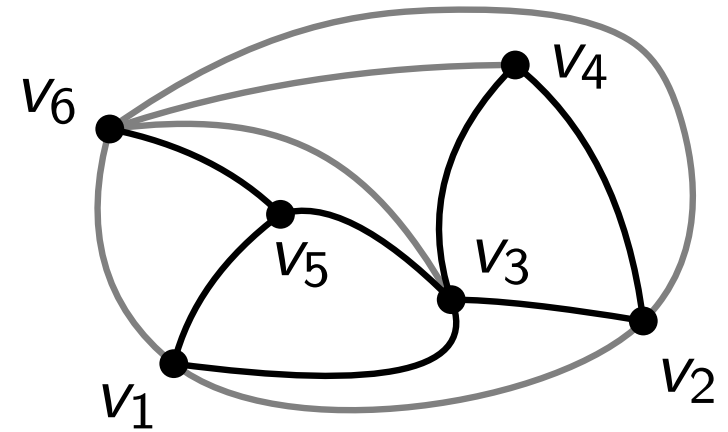
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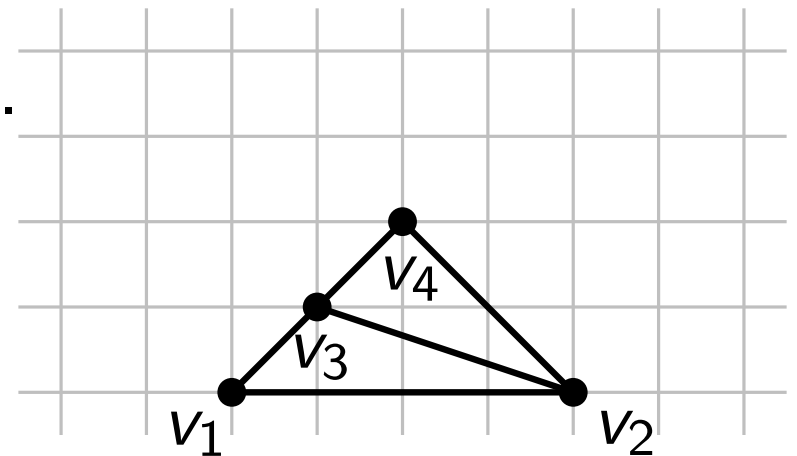
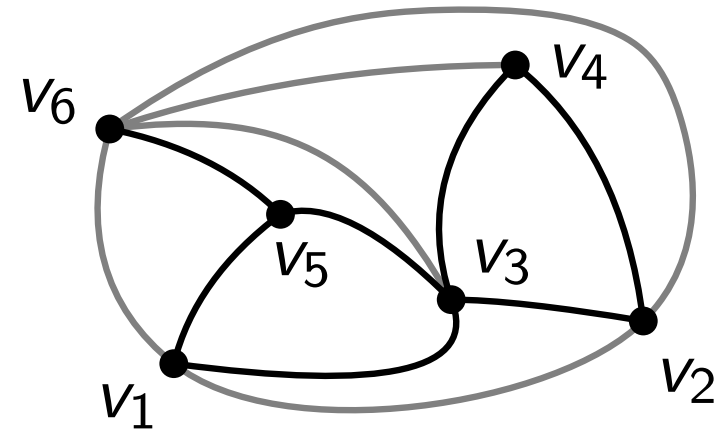
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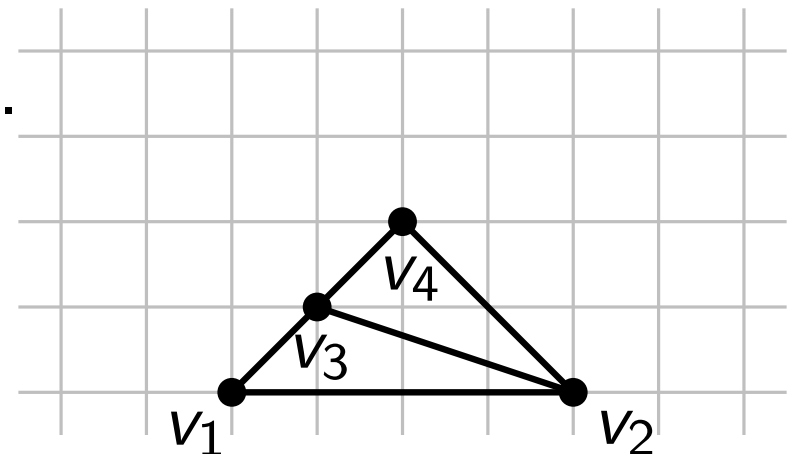
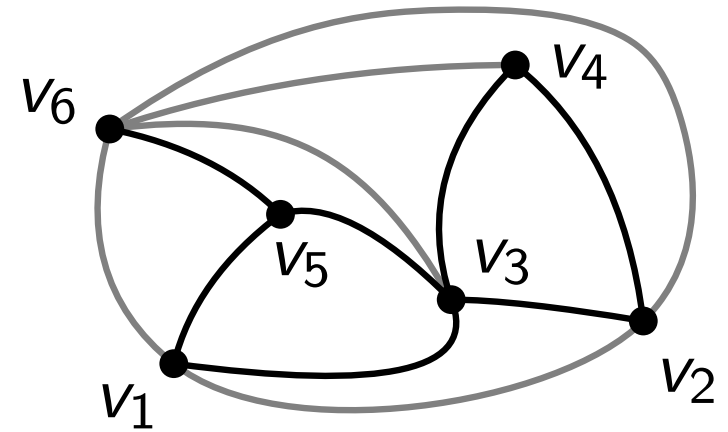
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- \Rightarrow all slopes on outer face ± 1
(except for $v_1 v_2$)



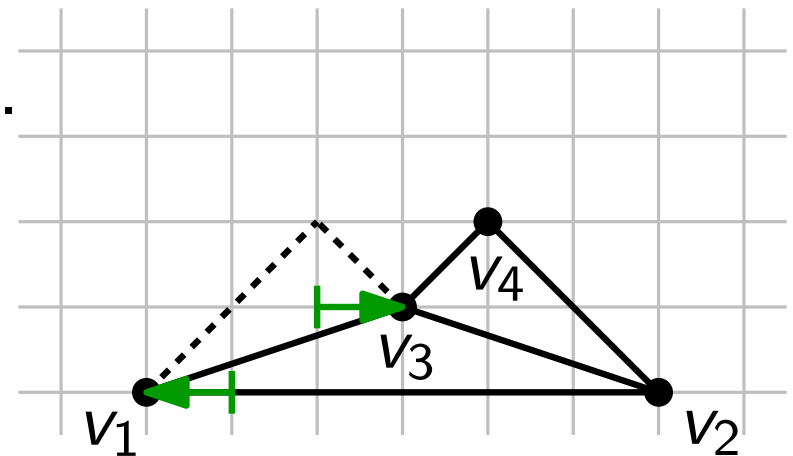
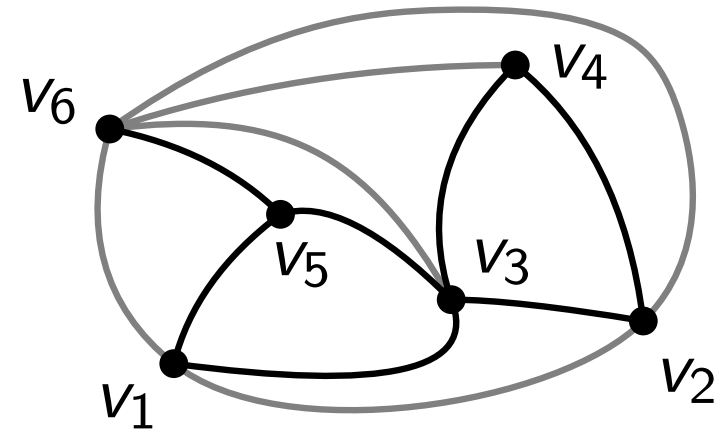
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Introduction: The Shift Algorithm

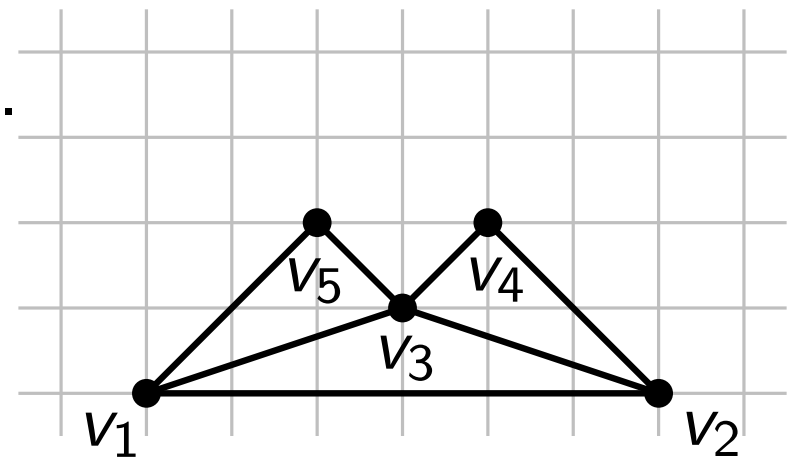
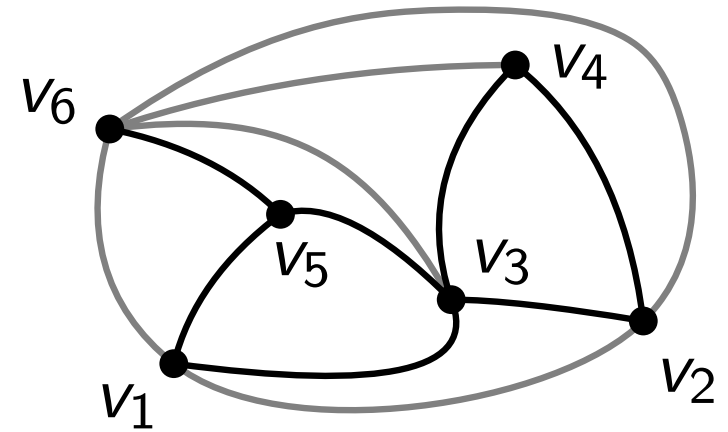
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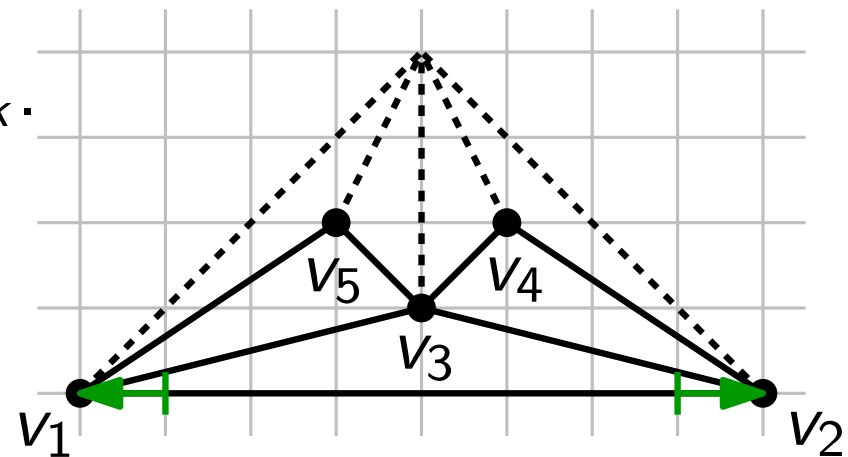
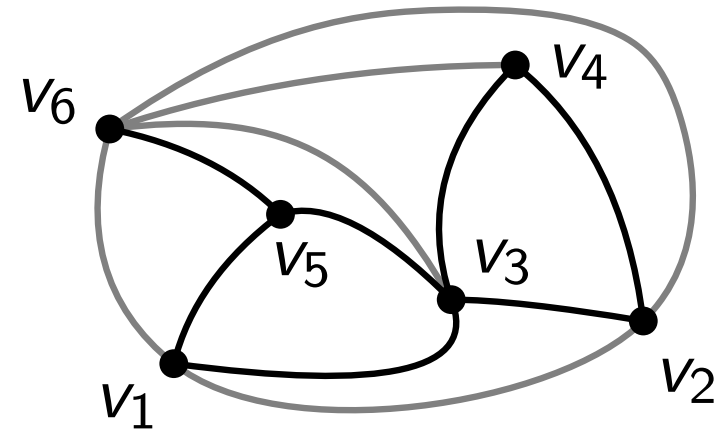
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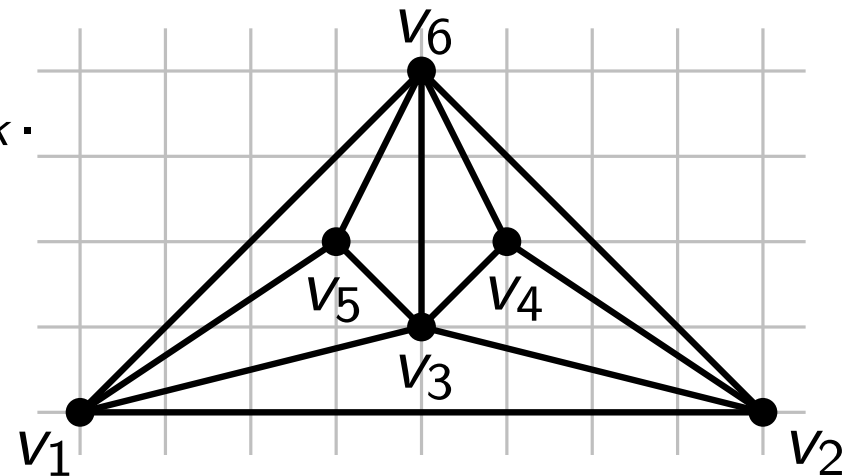
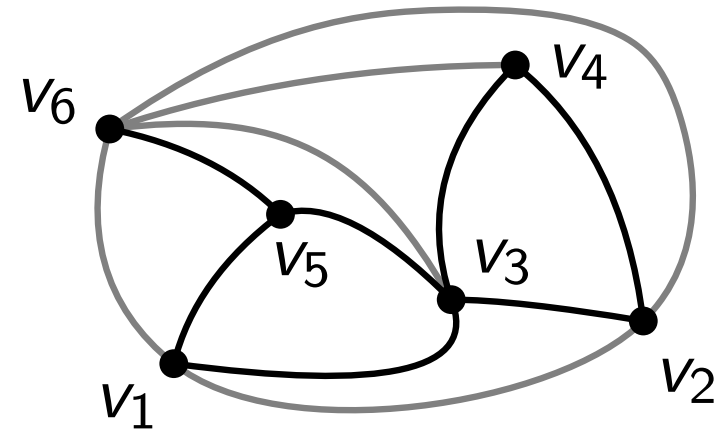
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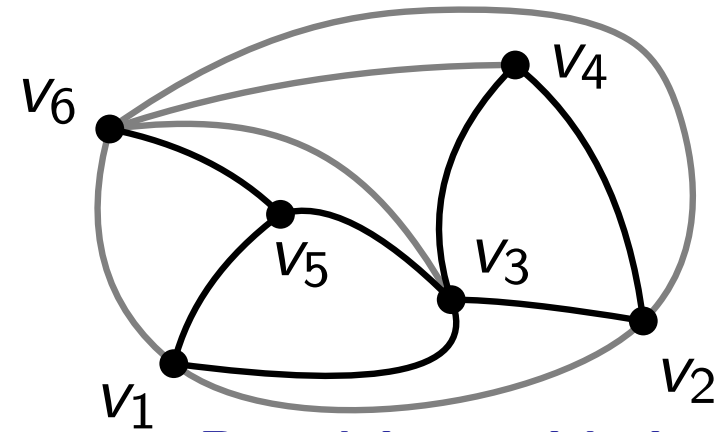
Introduction: The Shift Algorithm

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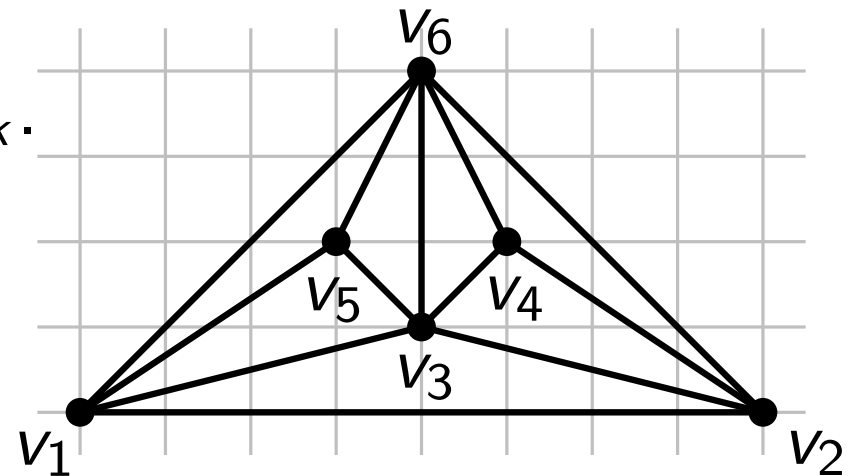
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Resulting grid size:
 $(2n - 4) \times (n - 2)$



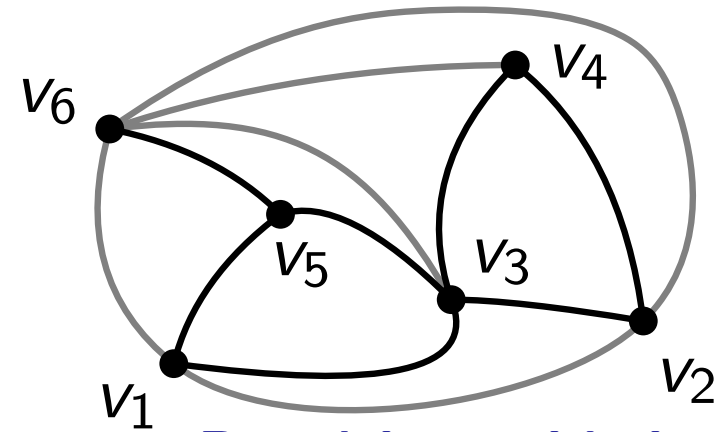
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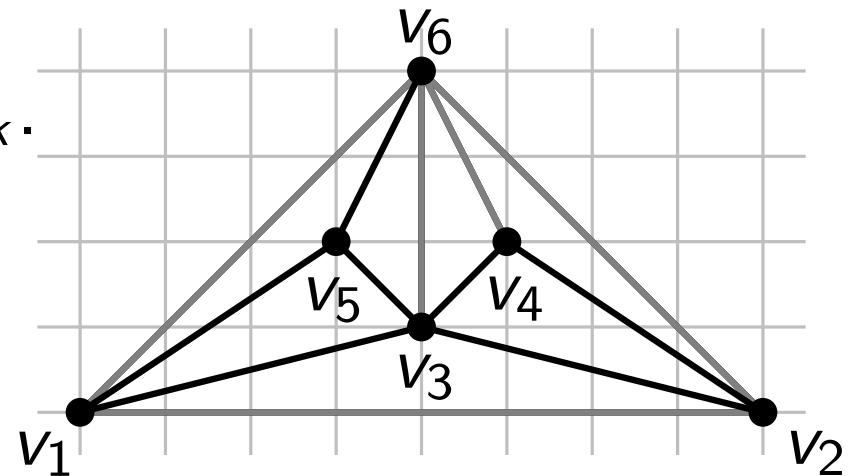
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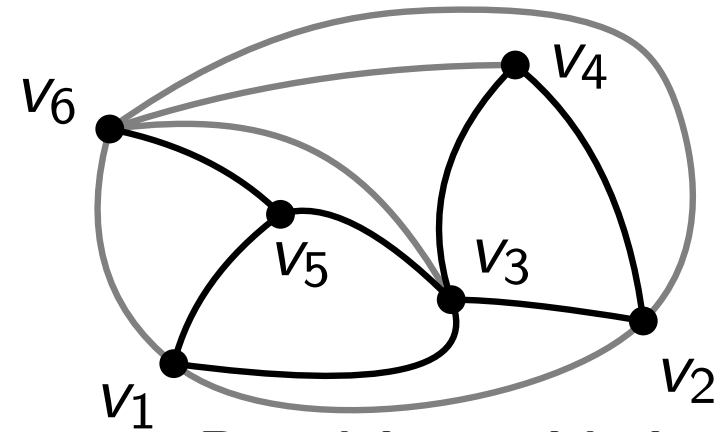
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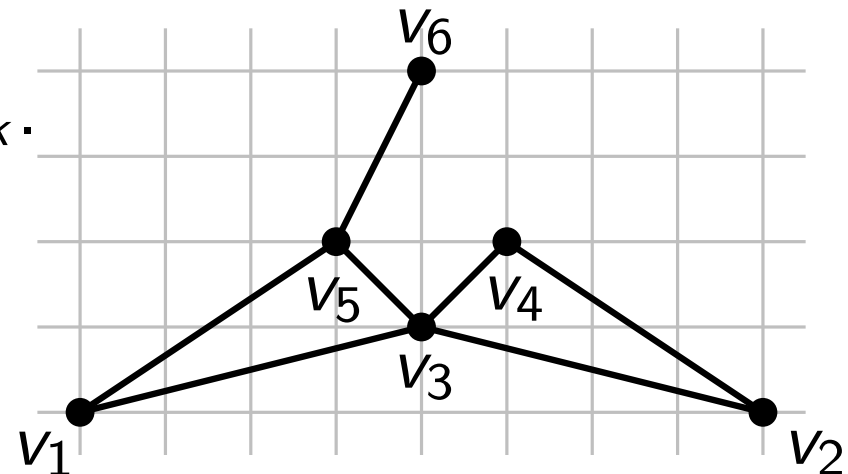
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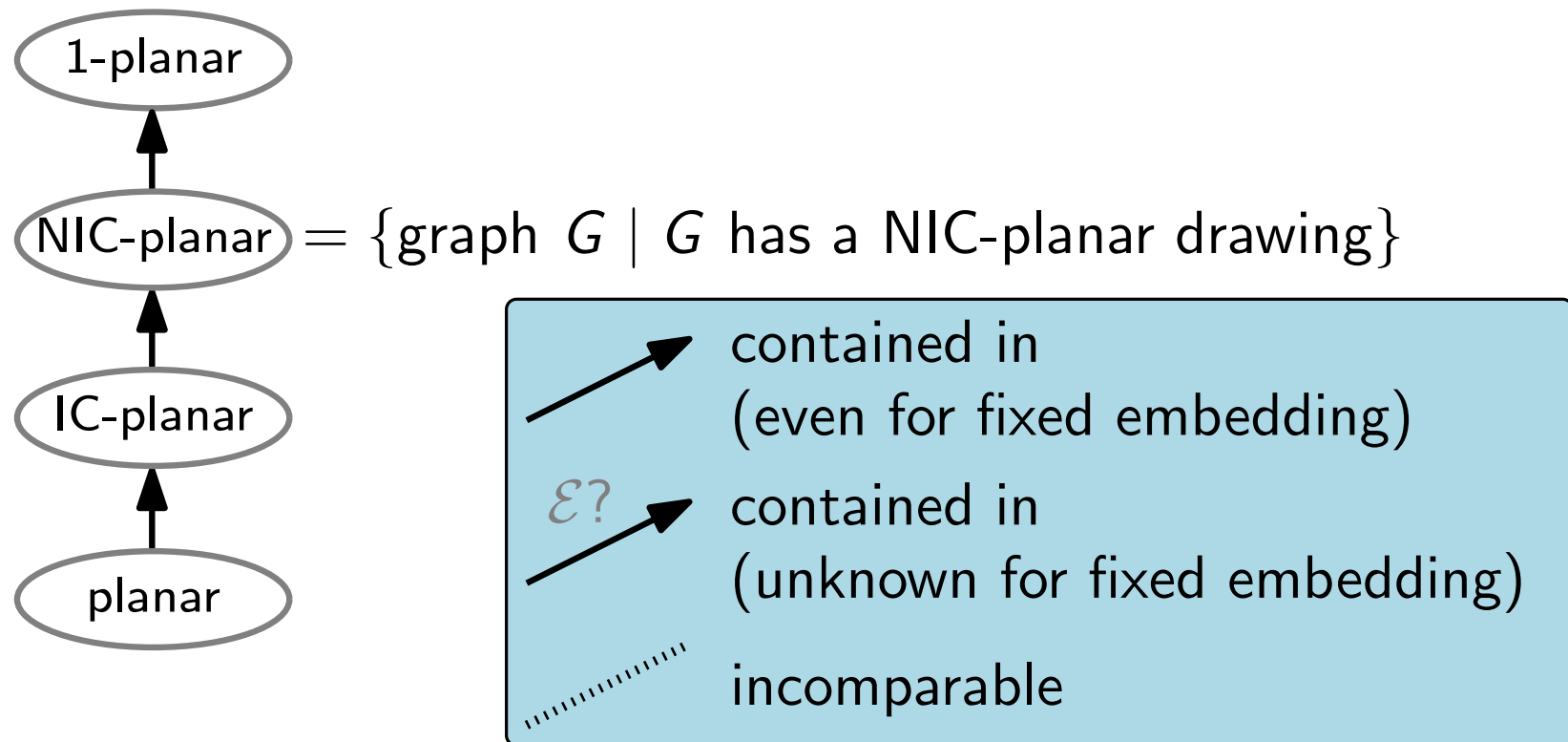


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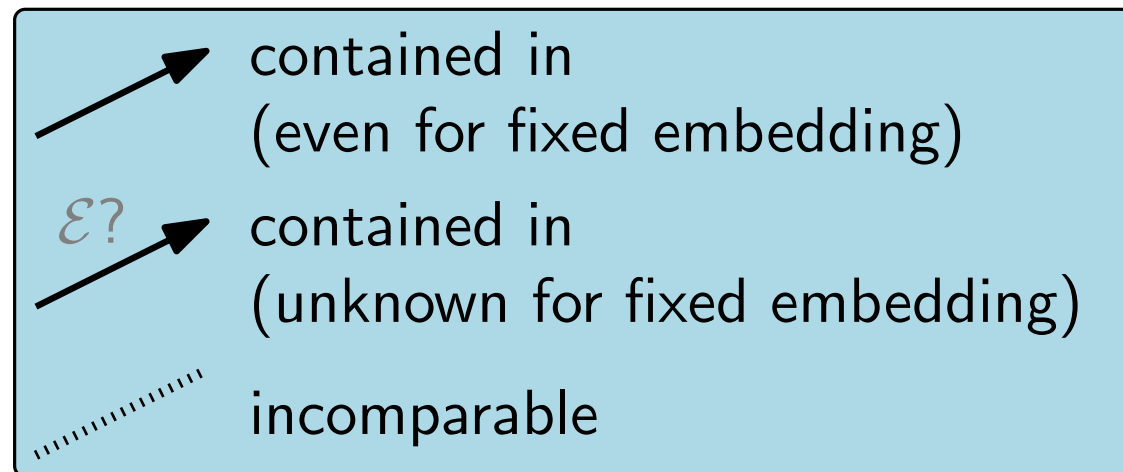
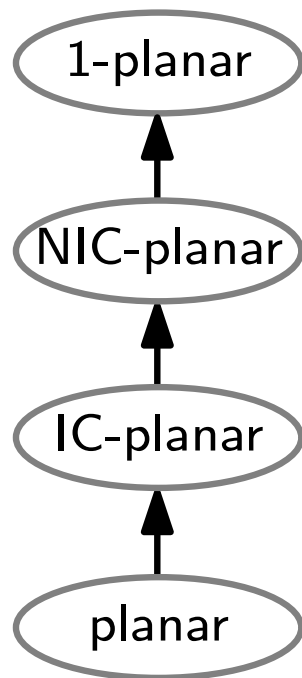
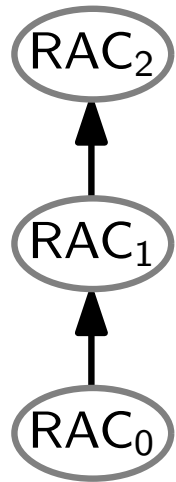
Introduction: Related Work

4



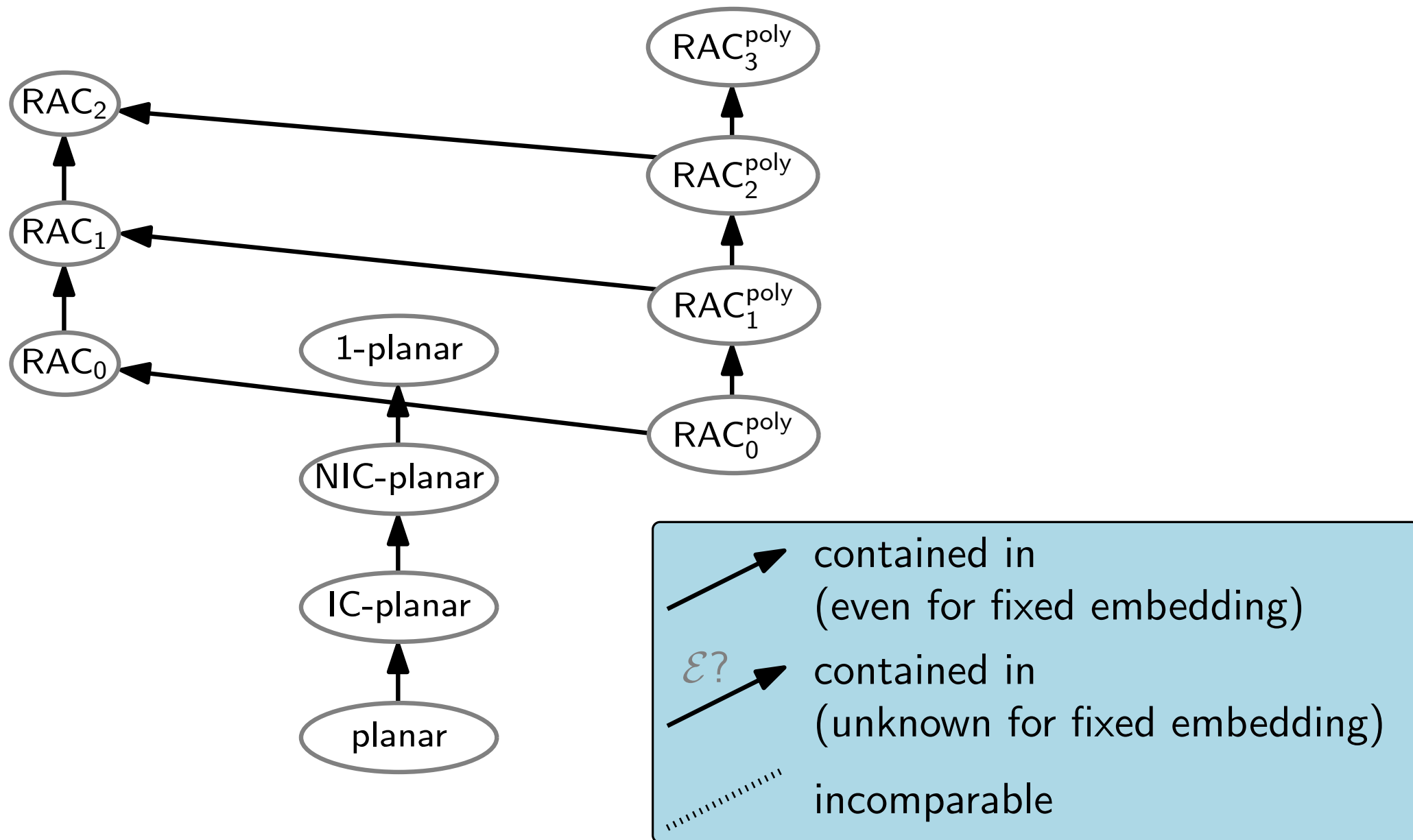
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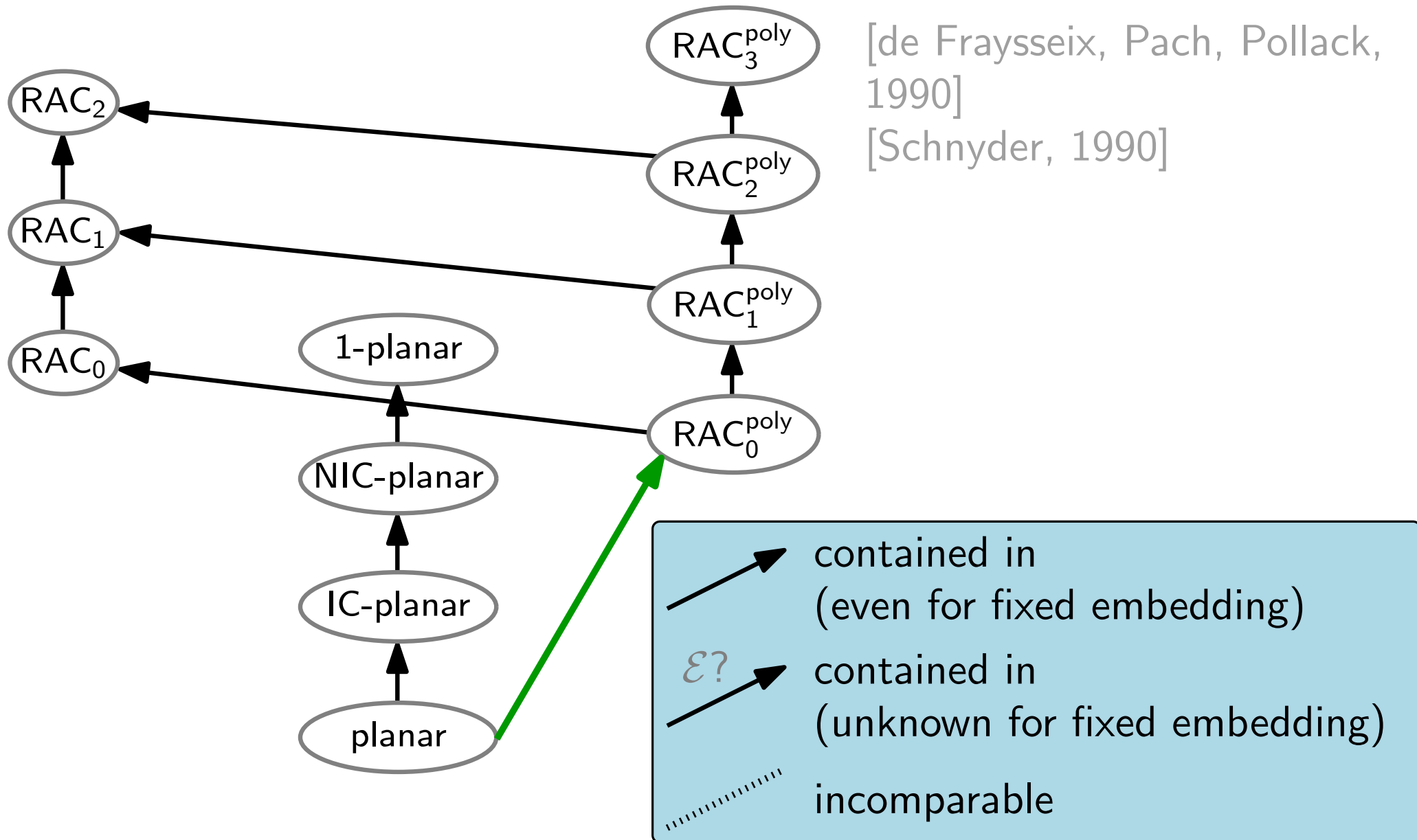
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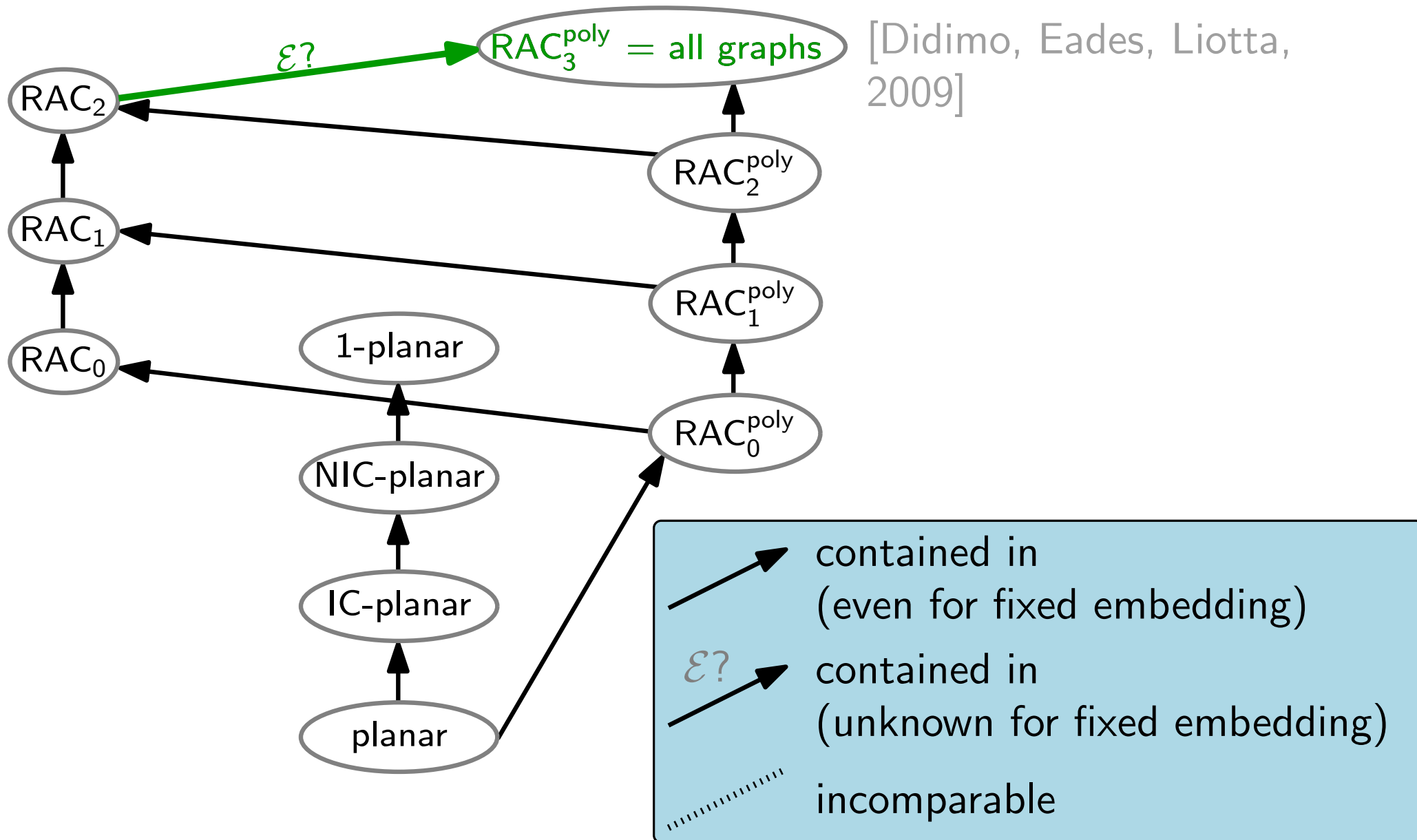
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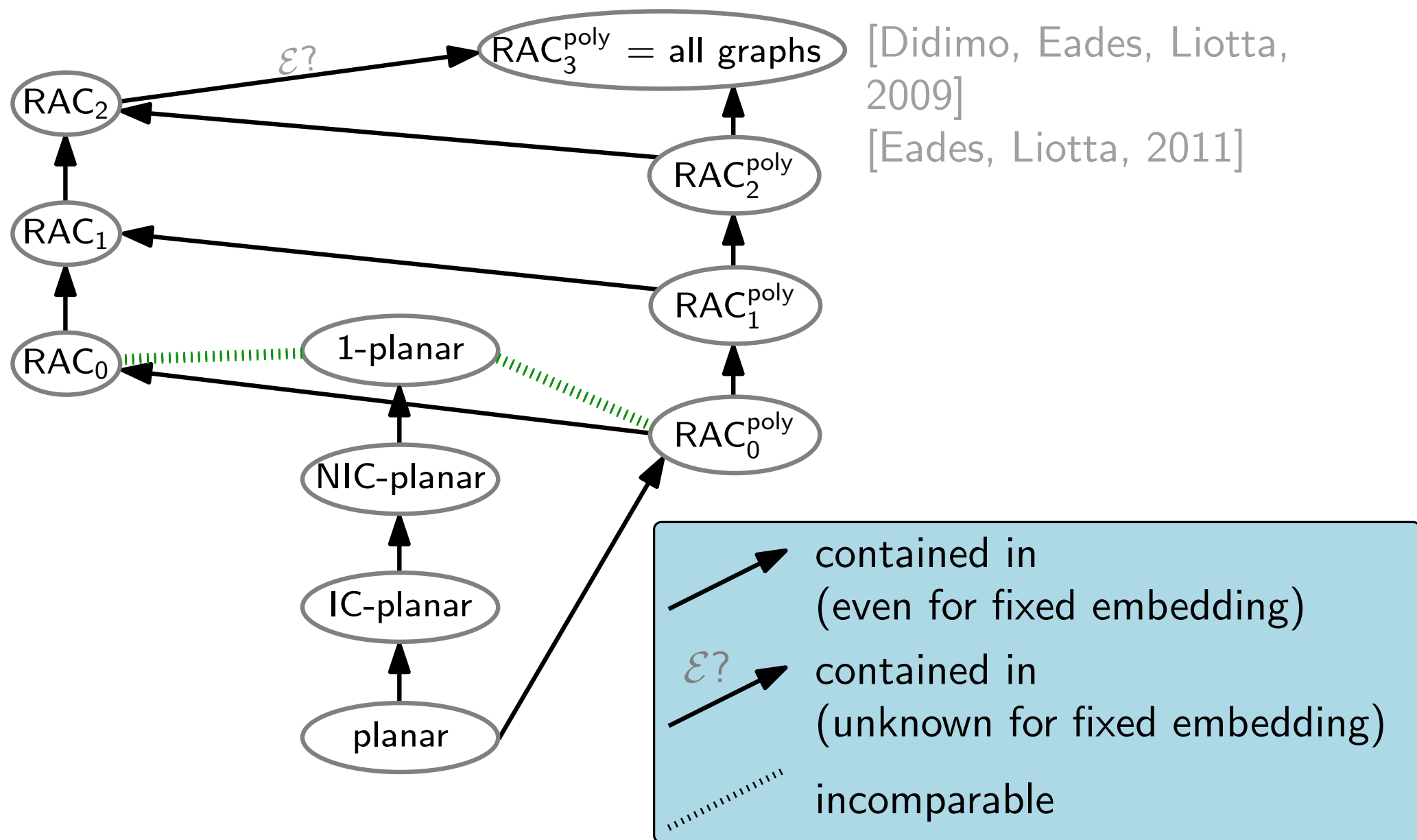
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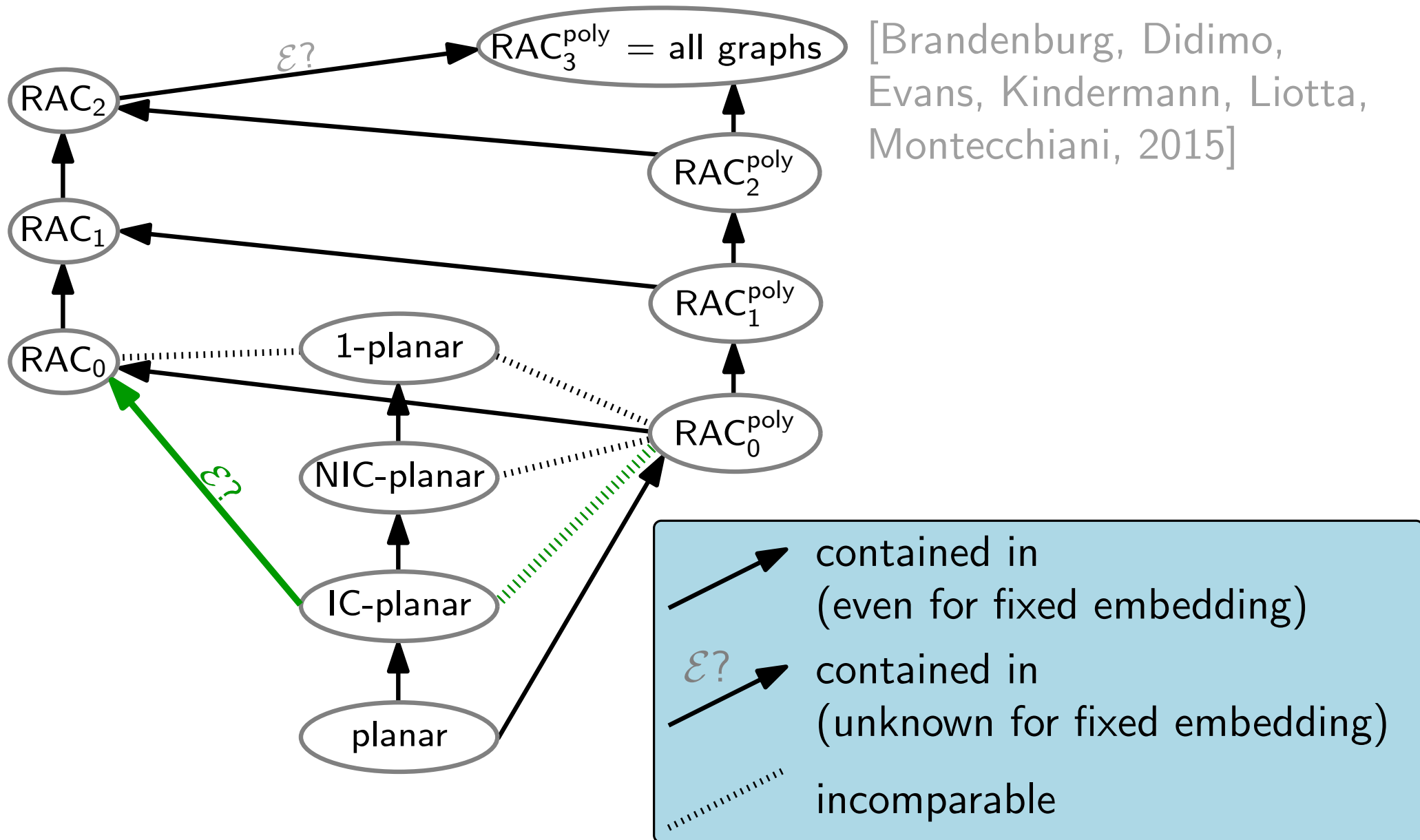
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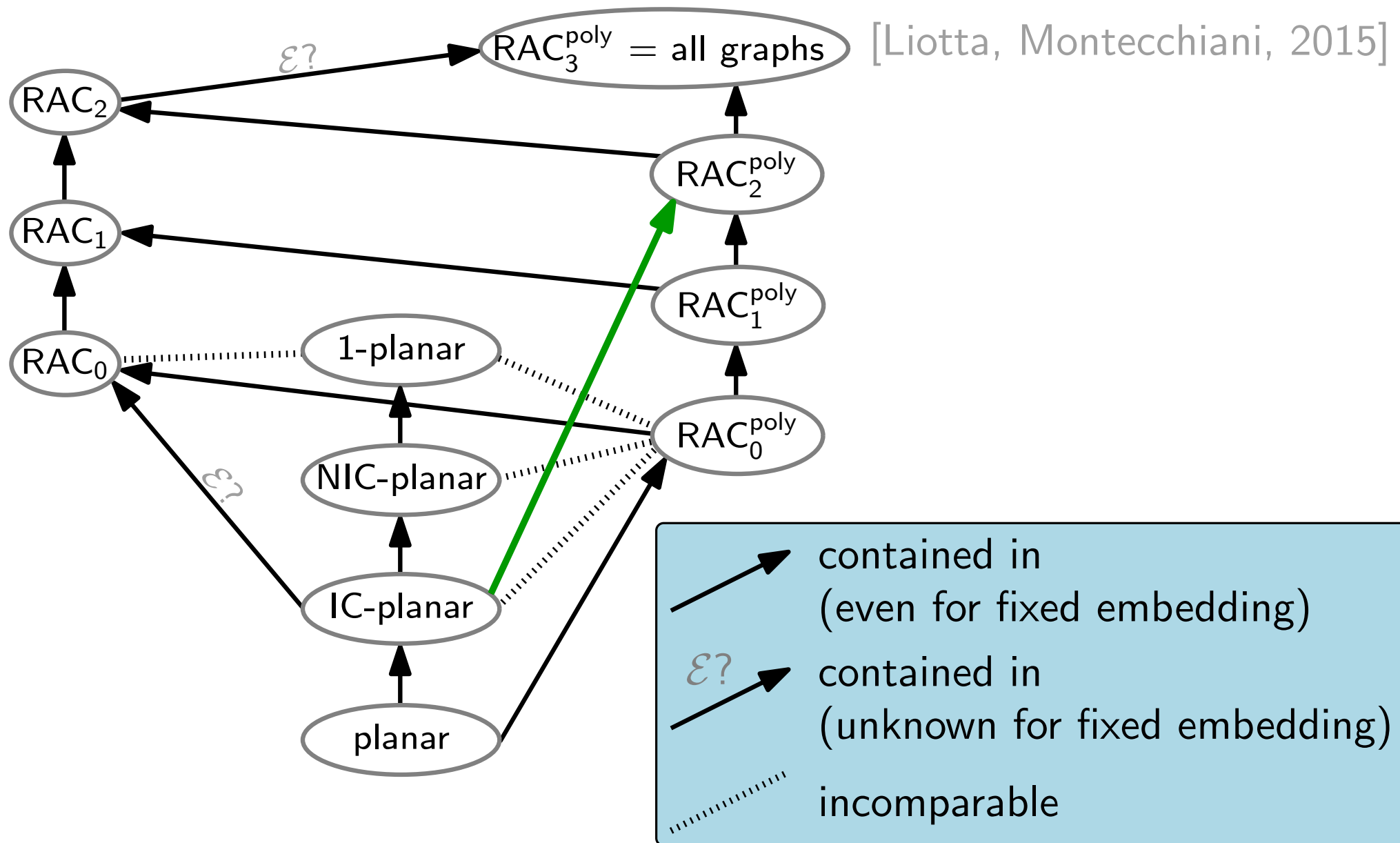
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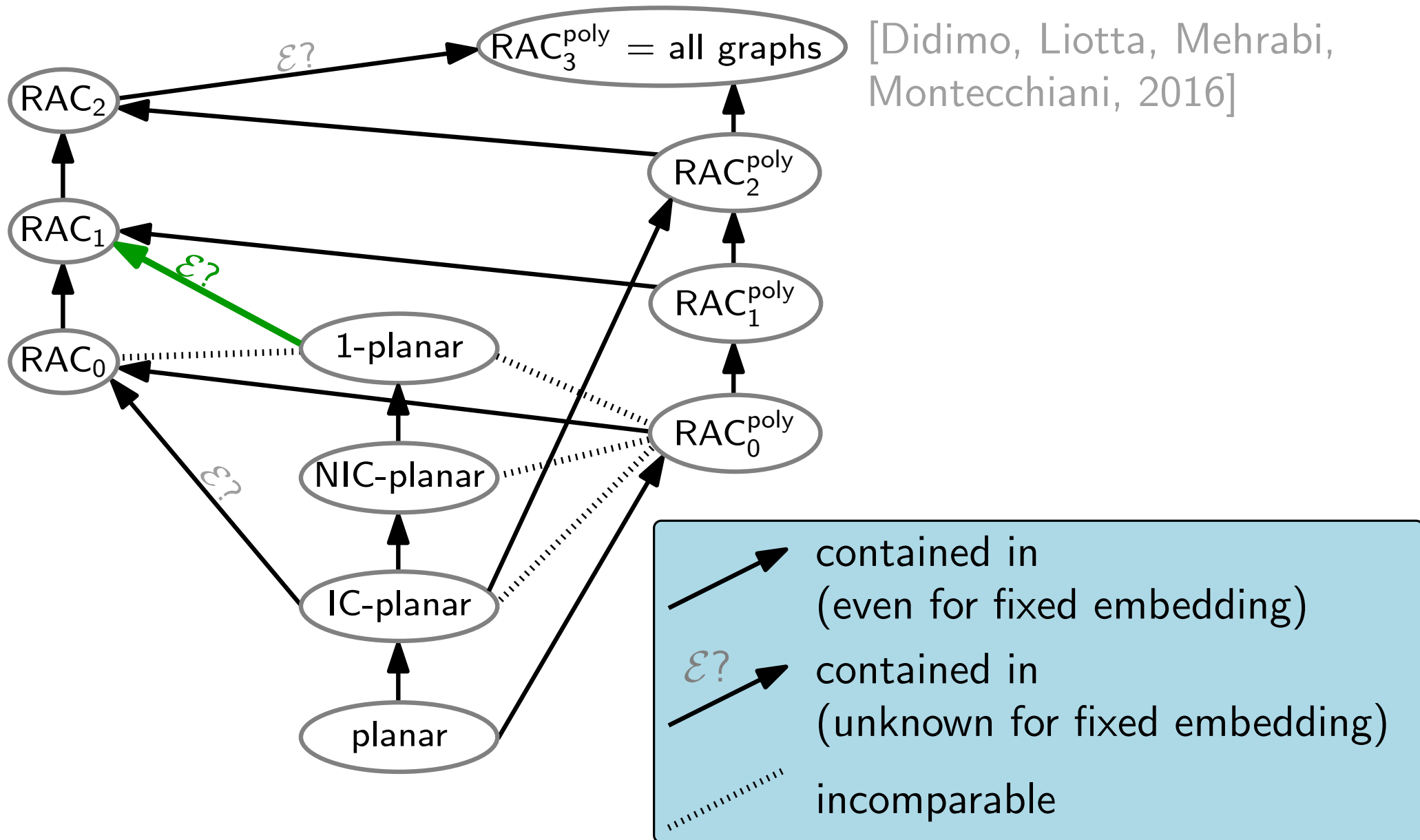
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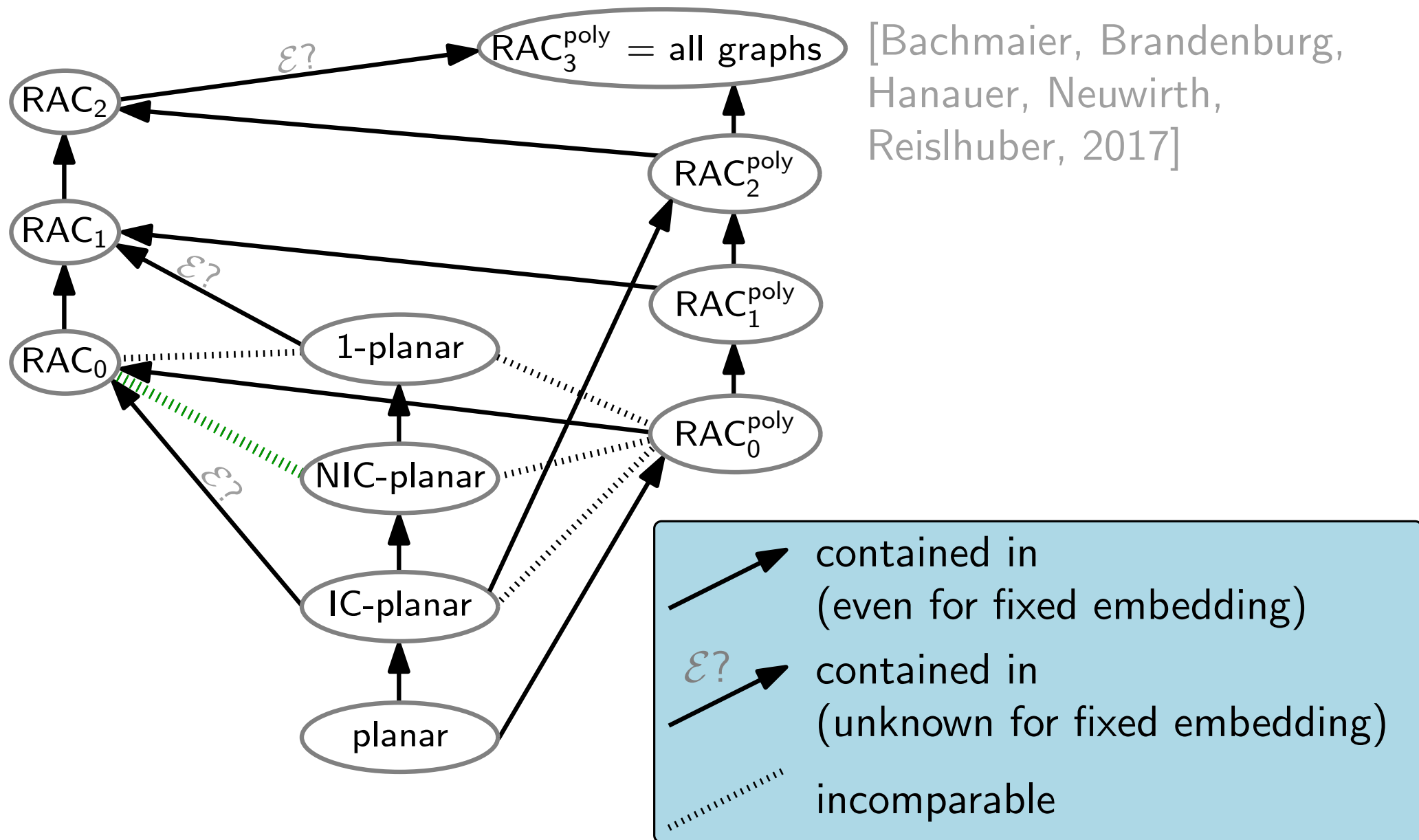
Introduction: Related Work

4



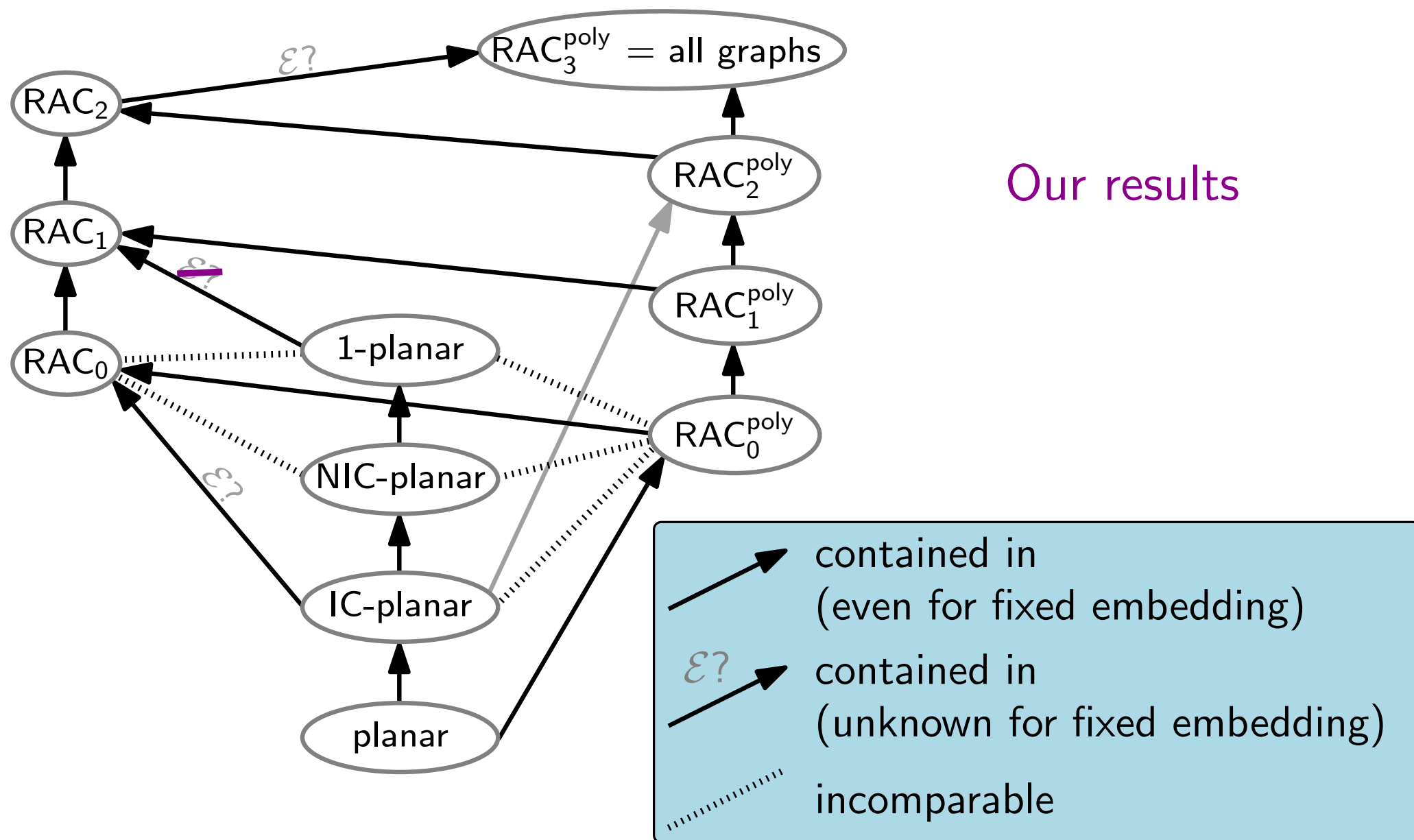
Introduction: Related Work

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Introduction: Related Work

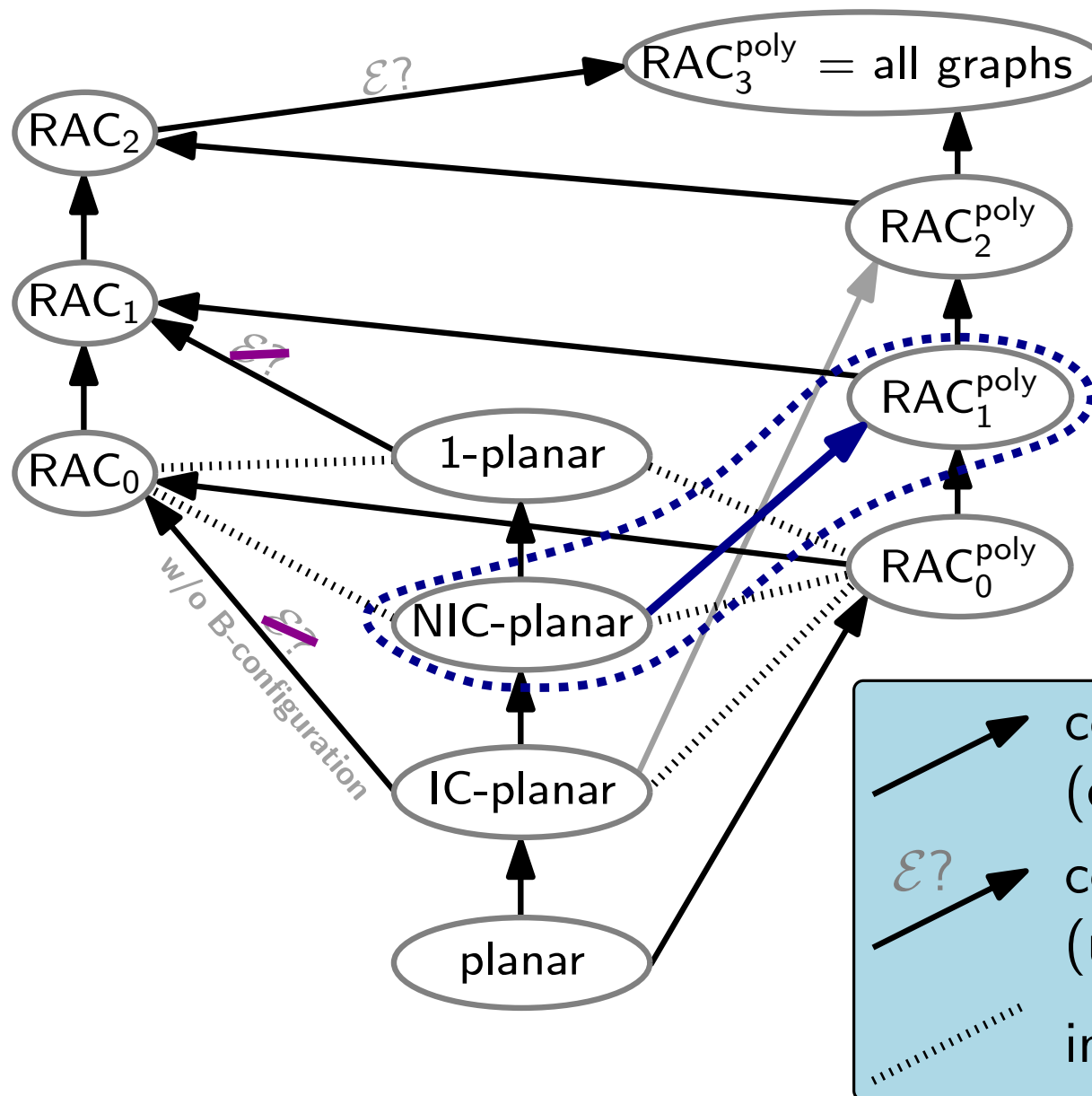
4





Introduction: Related Work

4

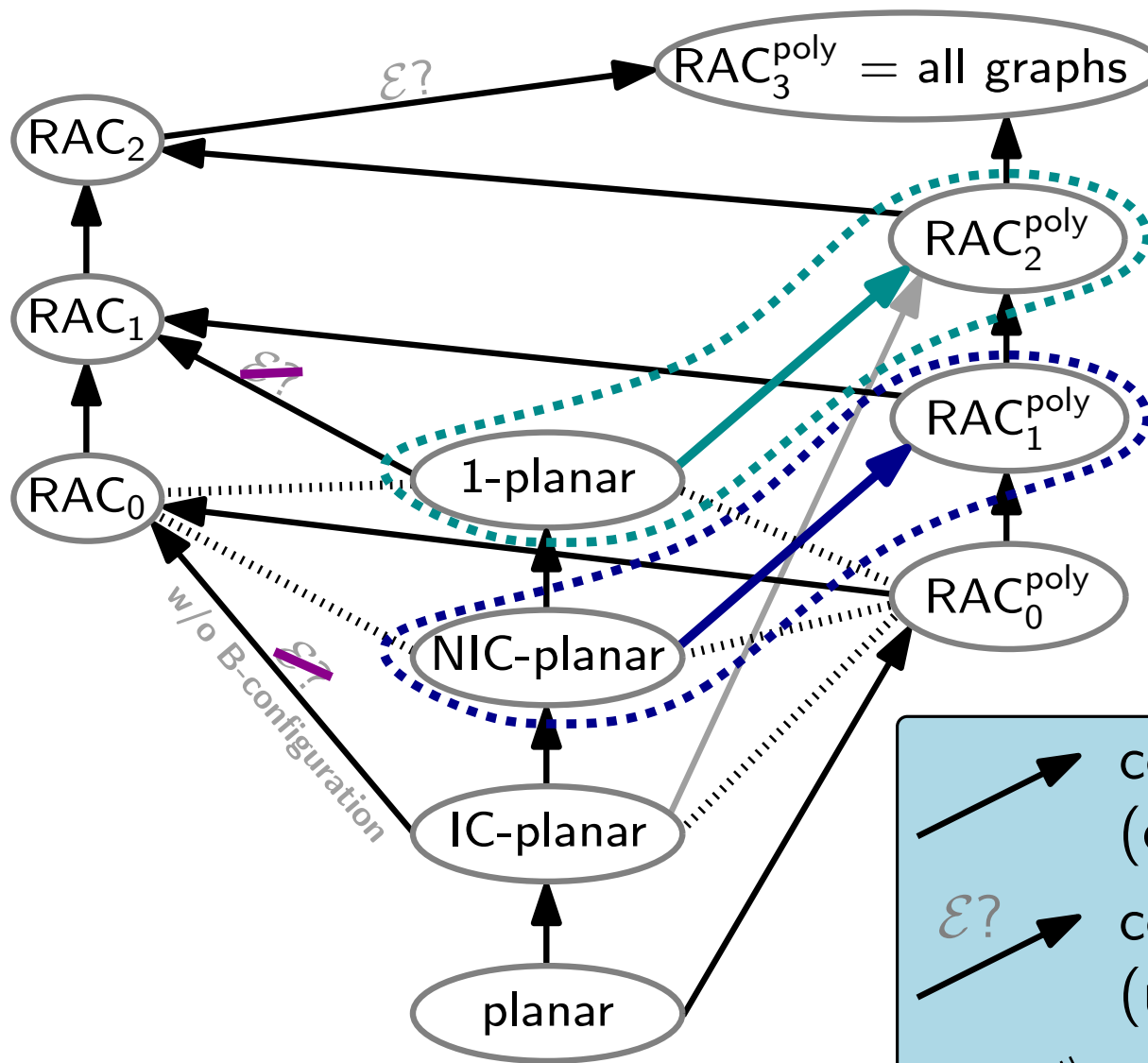


Our first main result:

$$\text{NIC-plane graphs} \subseteq \text{RAC}_1^{\text{poly}}$$

Introduction: Related Work

4

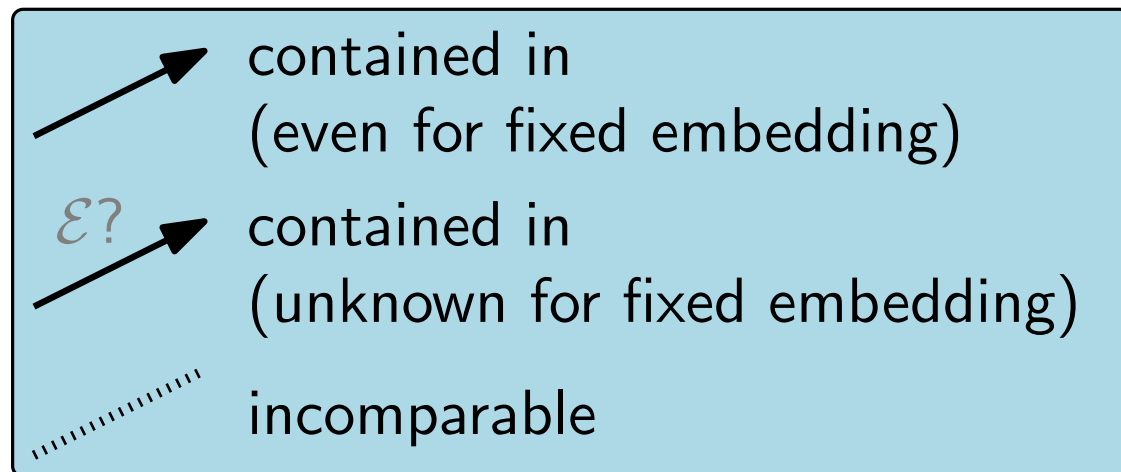


Our second main result:

1-plane graphs
 $\subseteq \text{RAC}_2^{\text{poly}}$

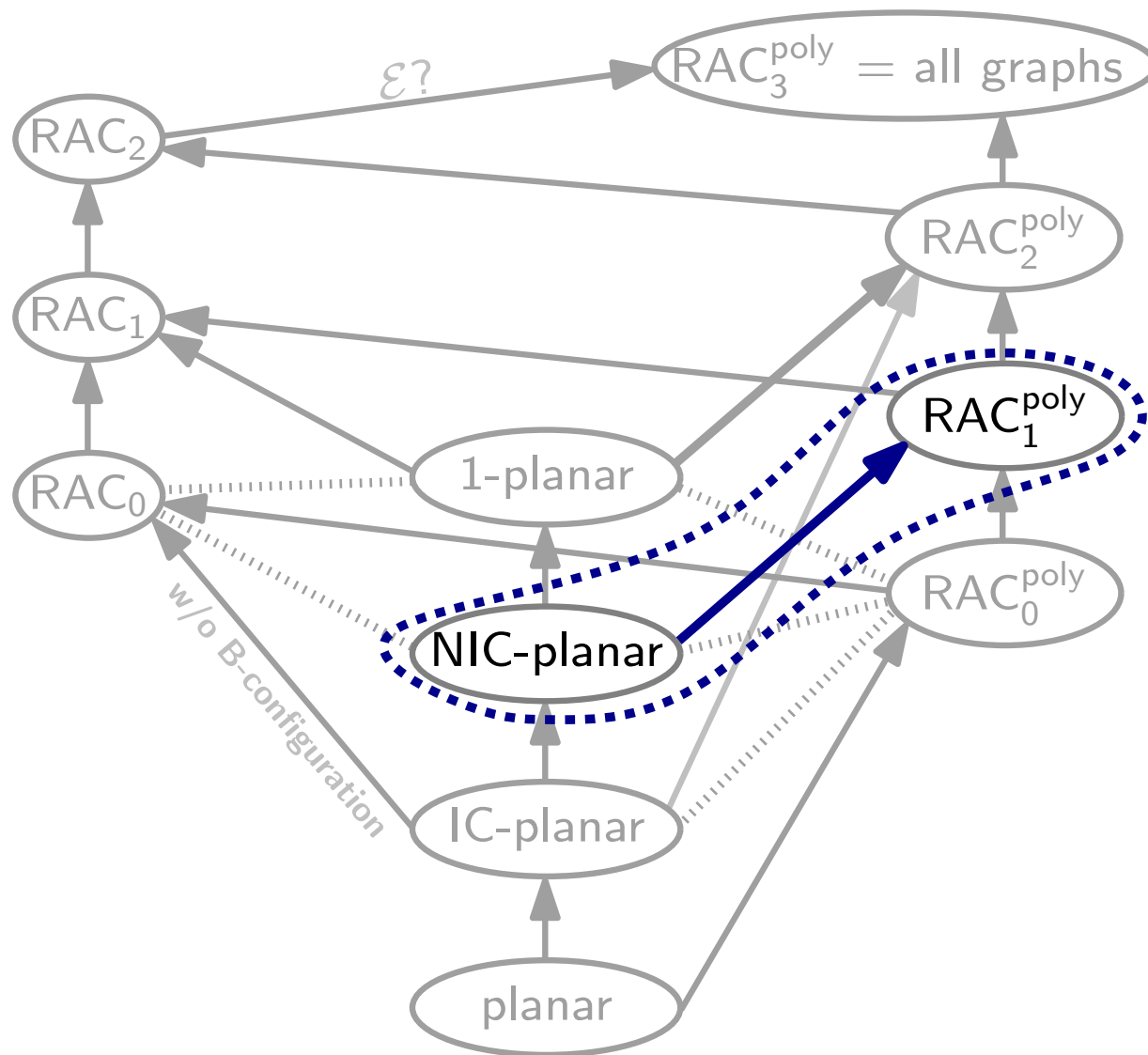
Our first main result:

NIC-plane graphs
 $\subseteq \text{RAC}_1^{\text{poly}}$



Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

5



Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

6

- Input: a NIC-plane graph

Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

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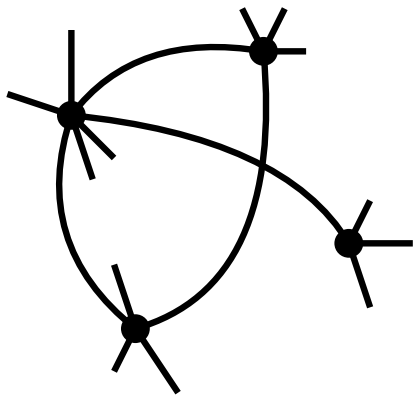
Approach that nearly works:

Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

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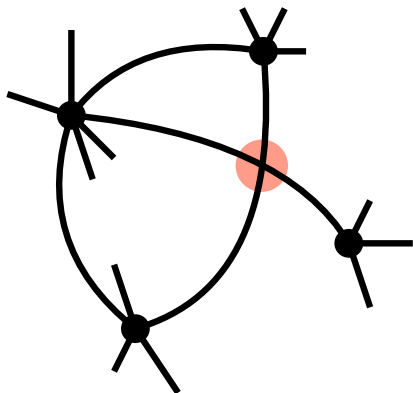
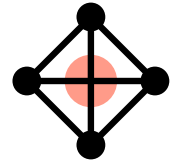
Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

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- Input: a NIC-plane graph

Approach that nearly works:

- Enclose each **crossing** by a so called *empty kite*:



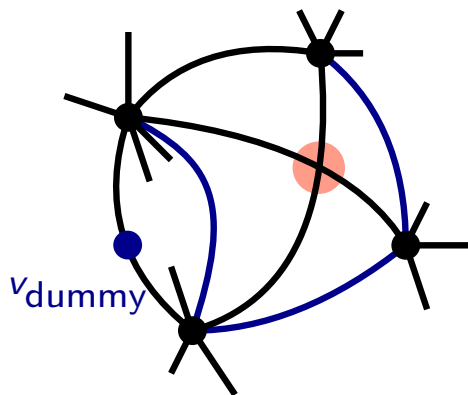
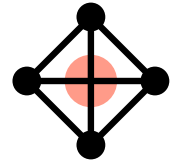
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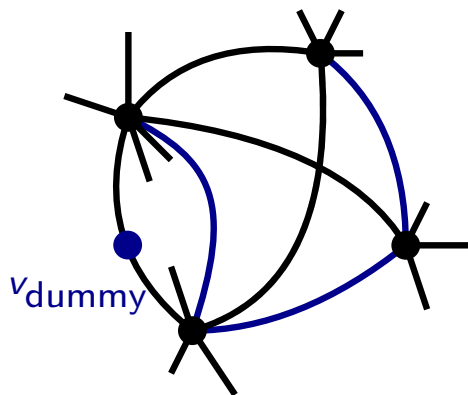
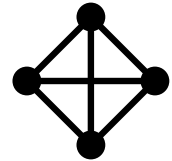
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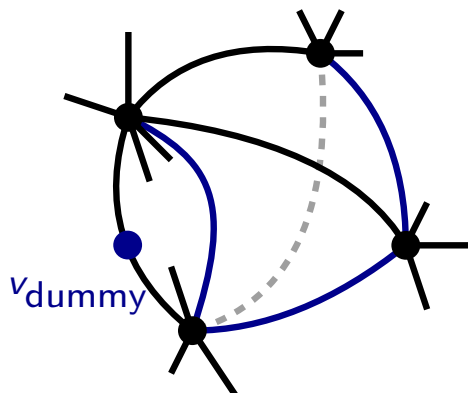
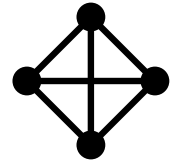
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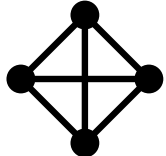


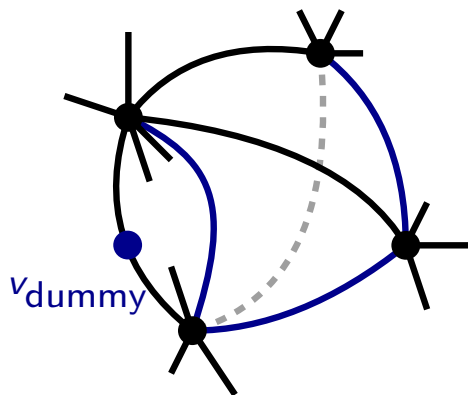
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Approach that nearly works:

- Enclose each crossing by a so called *empty kite*: 
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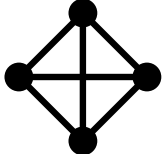


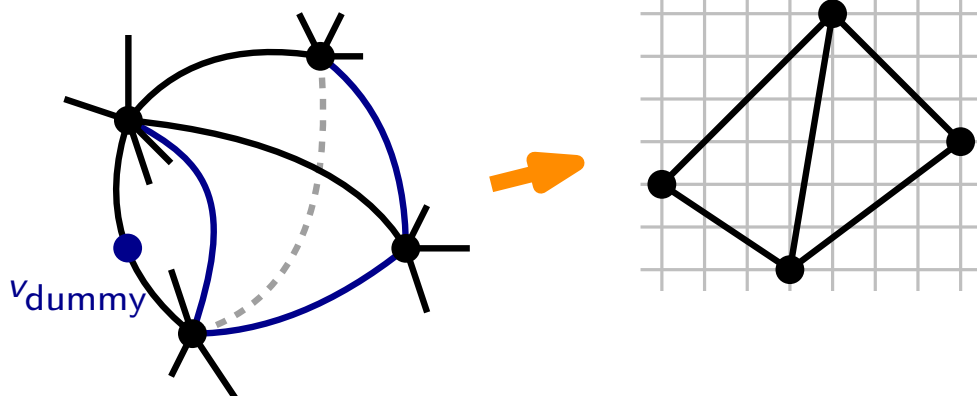
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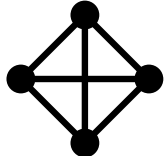


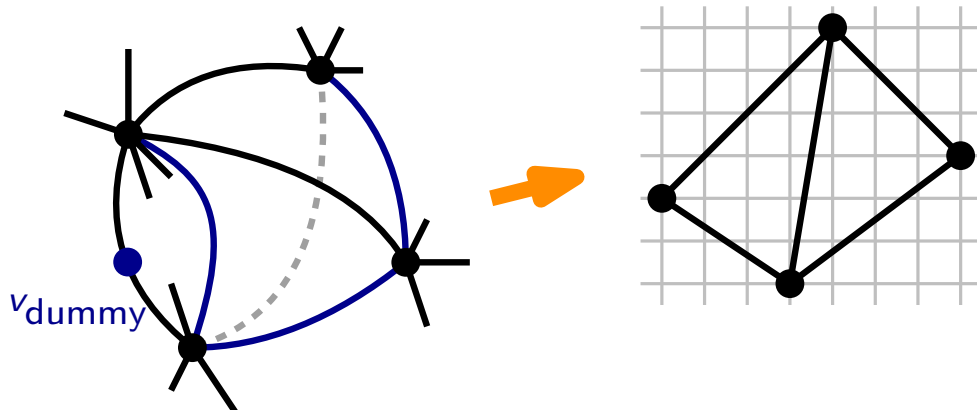
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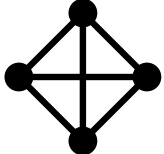


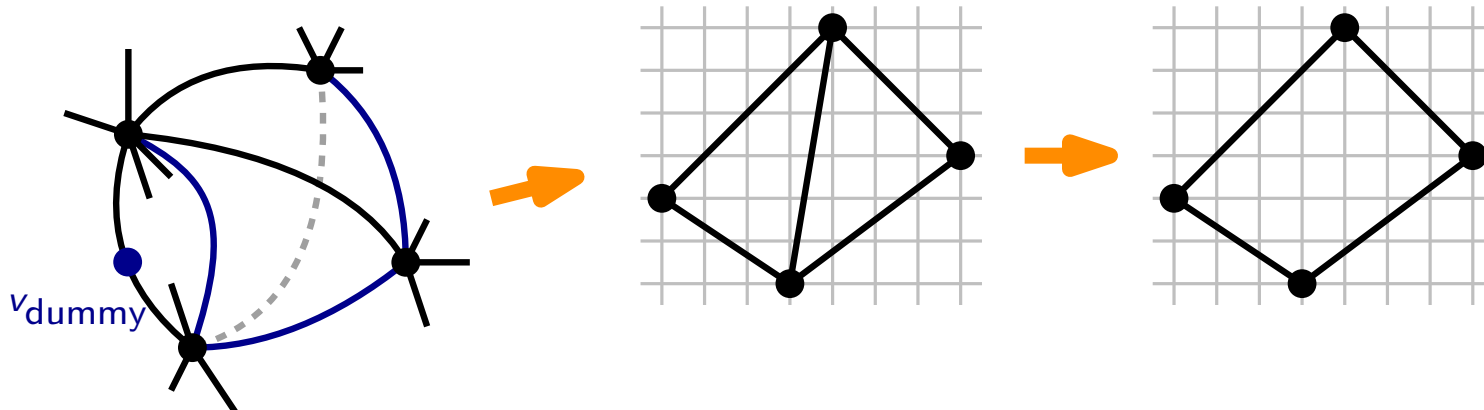
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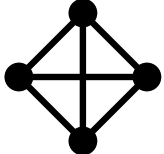


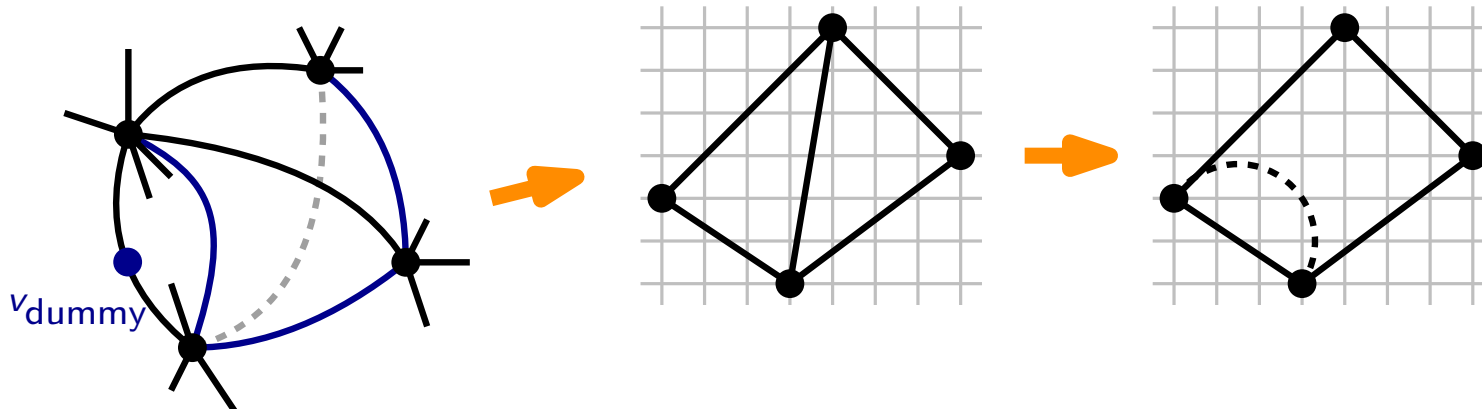
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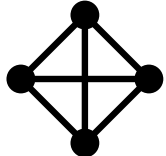


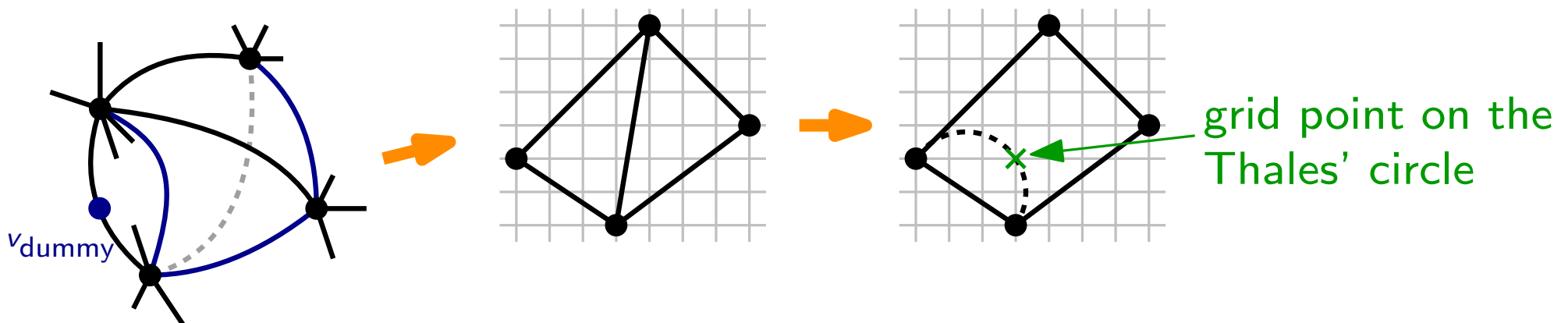
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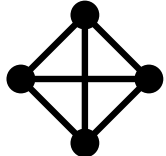


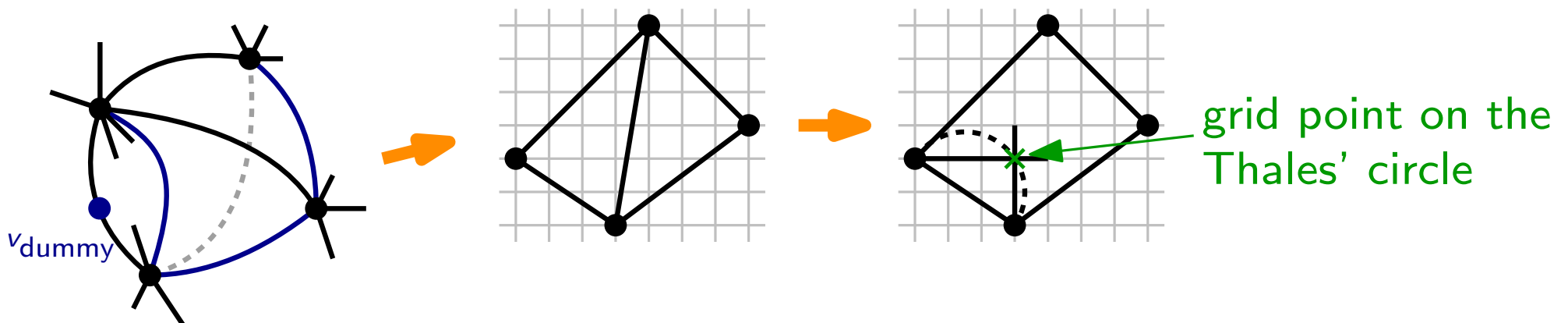
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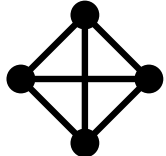


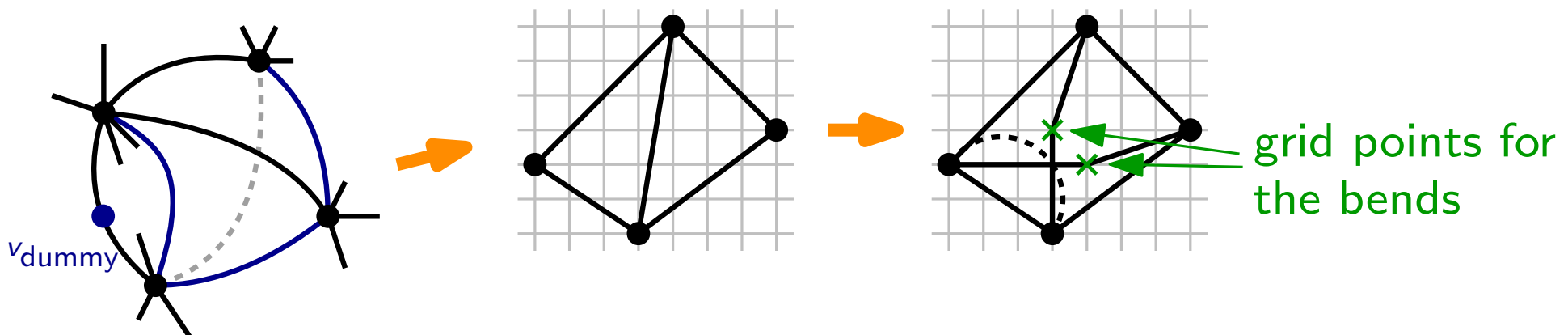
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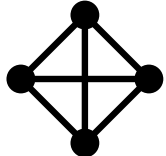


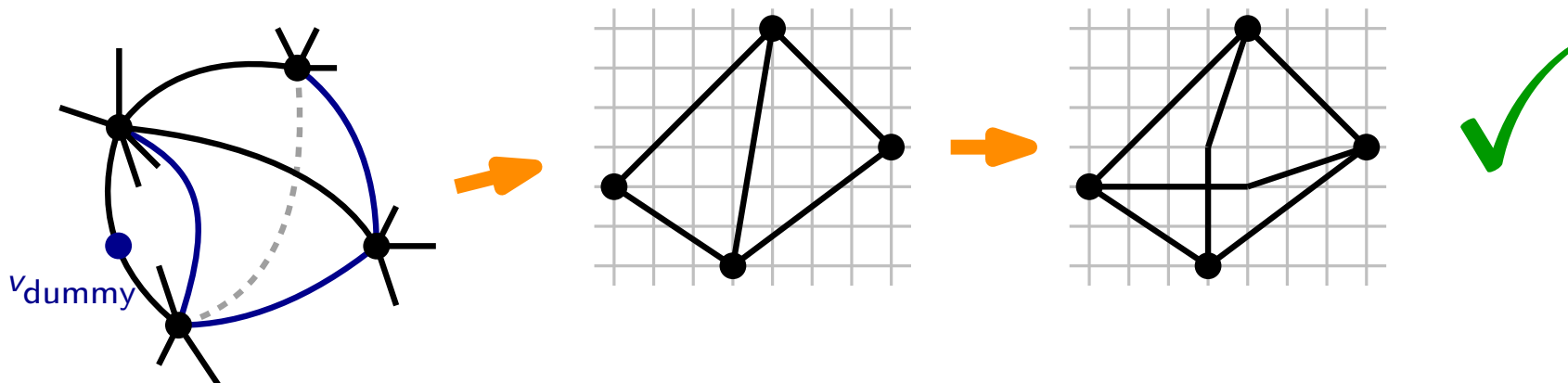
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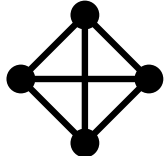


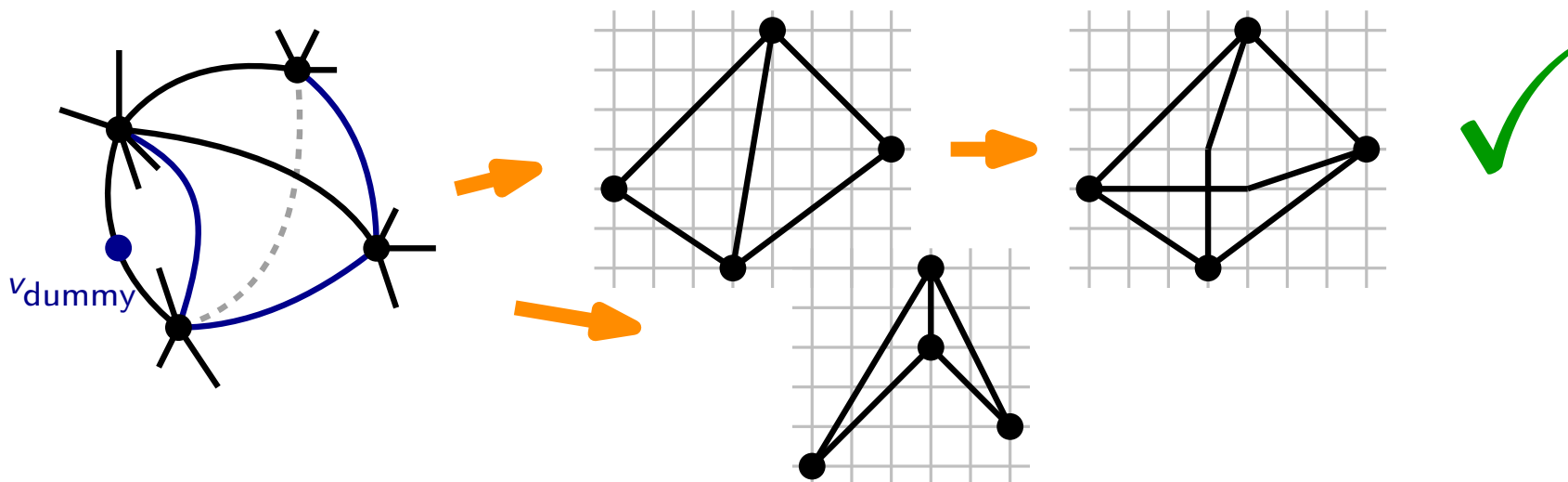
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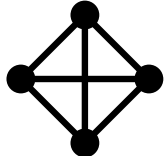


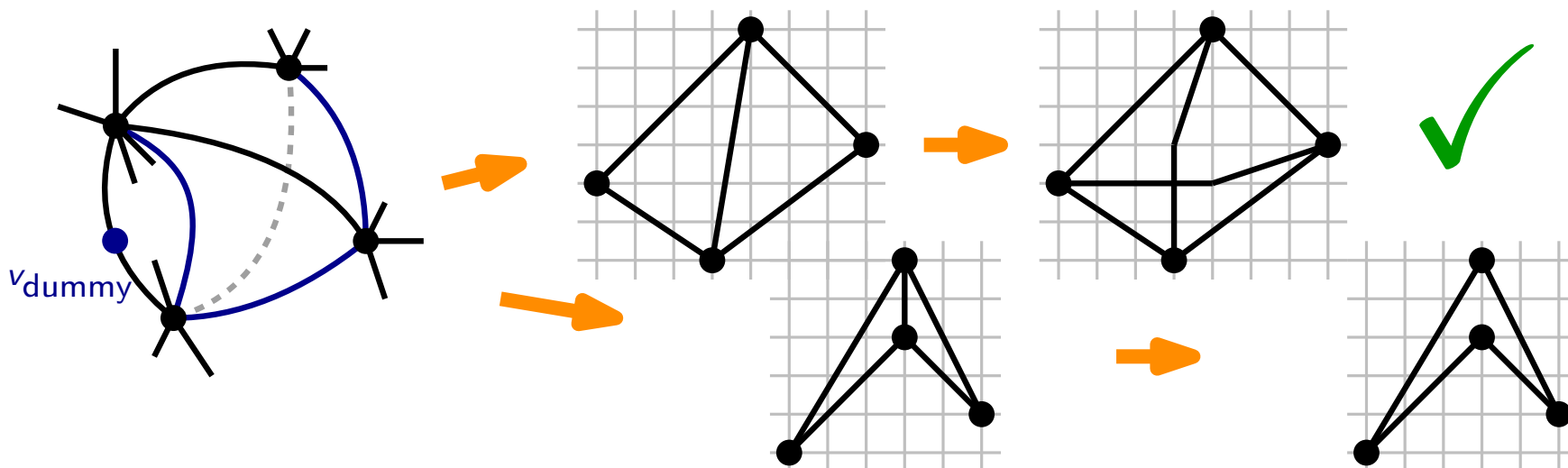
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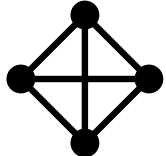


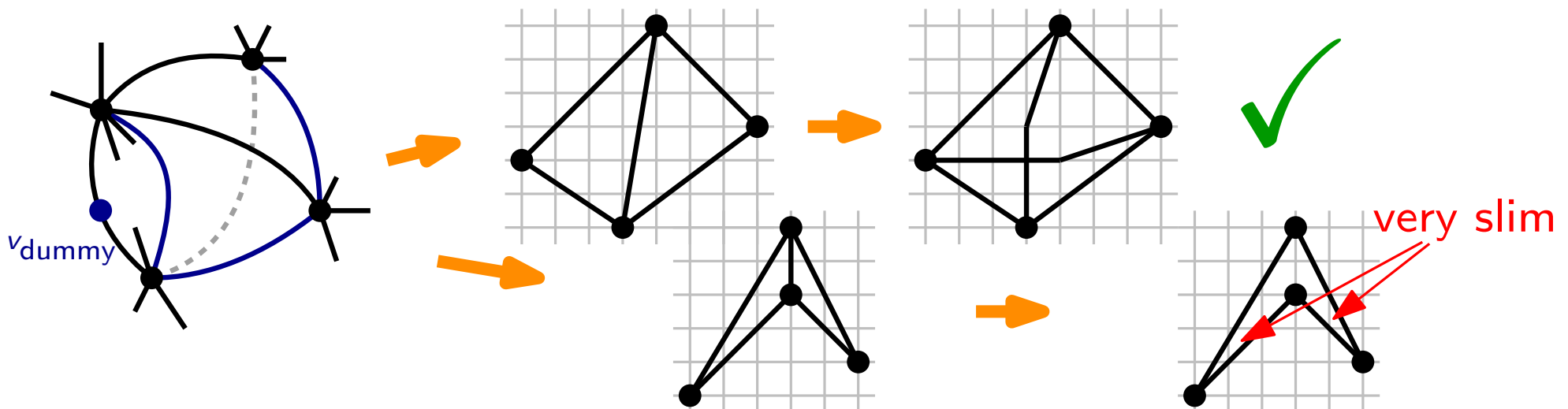
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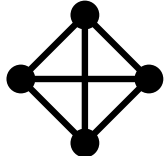


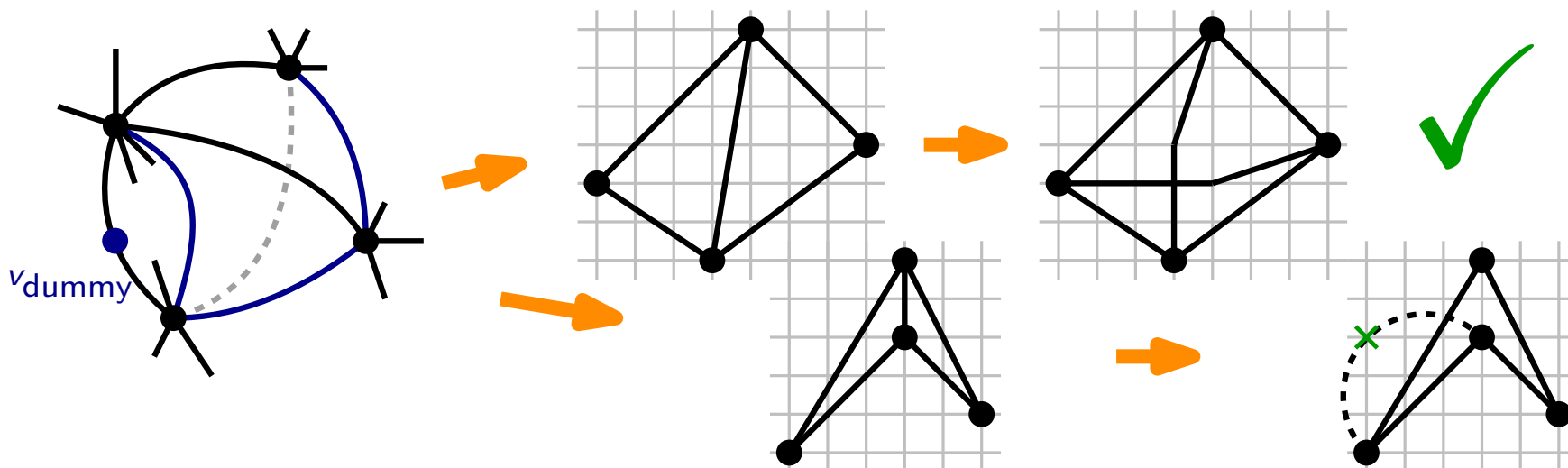
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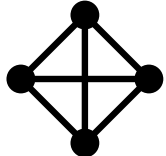


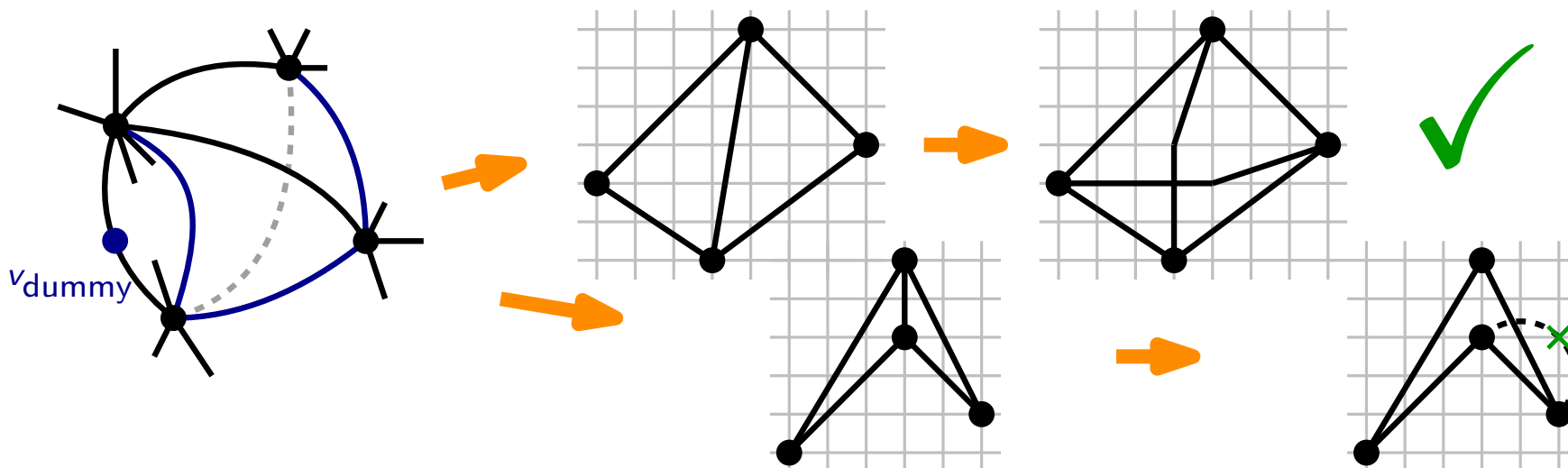
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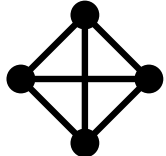


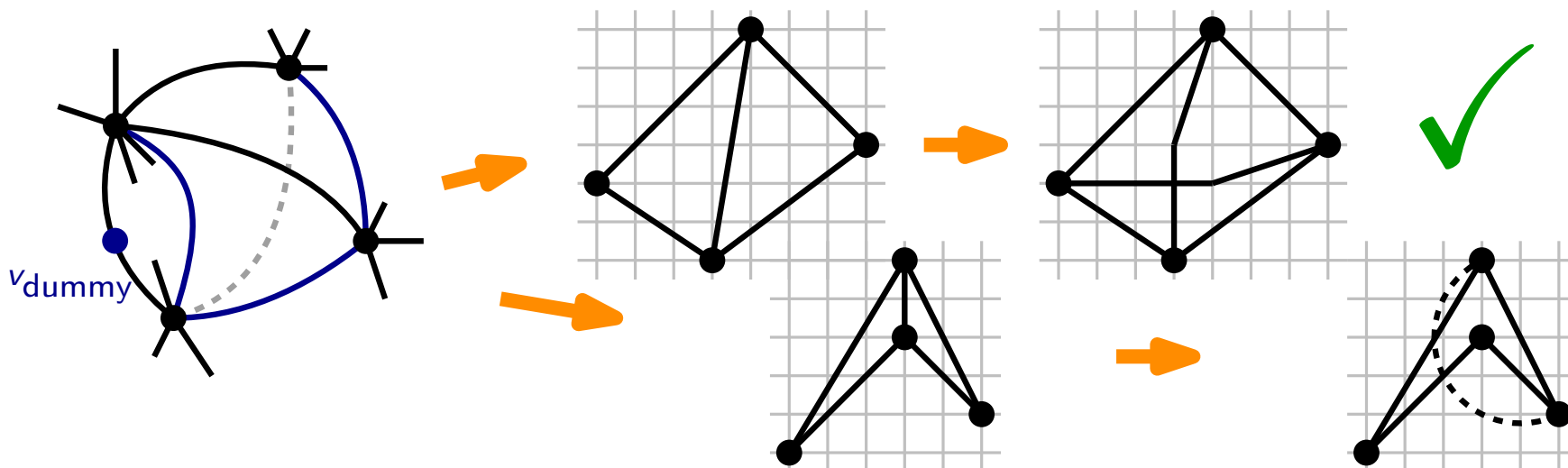
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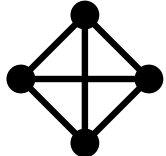


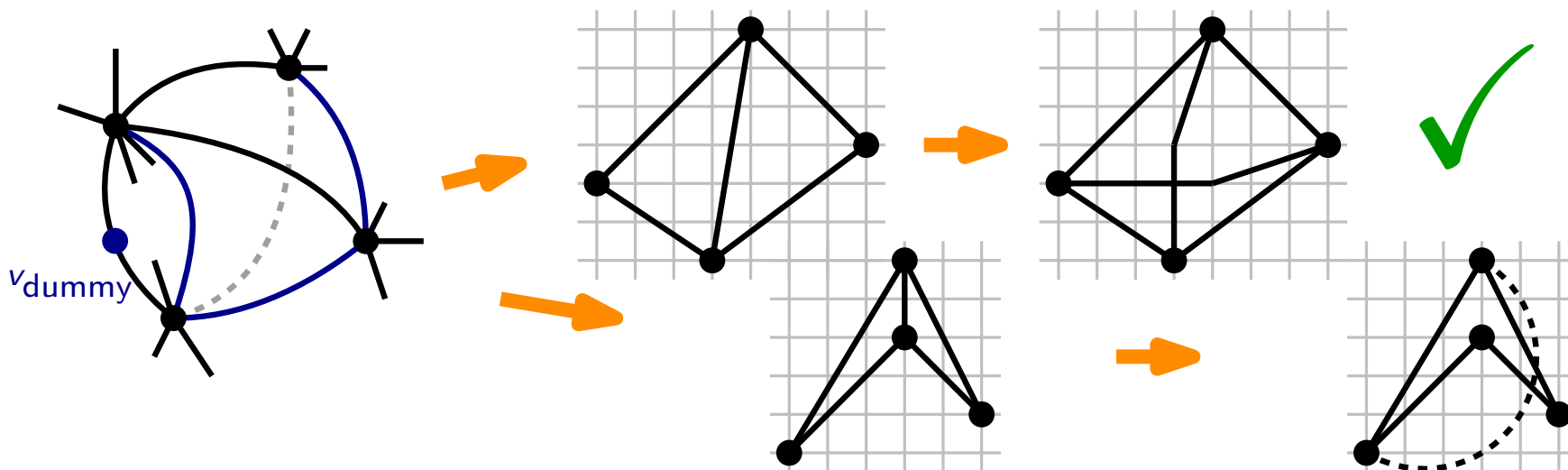
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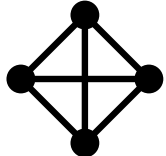


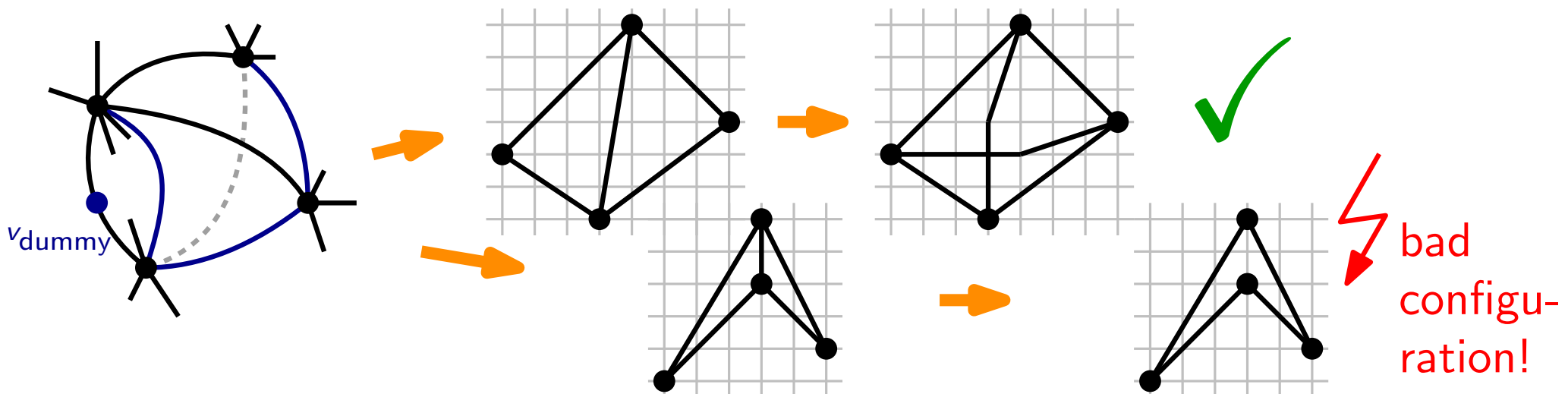
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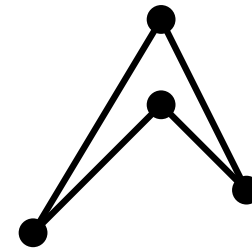
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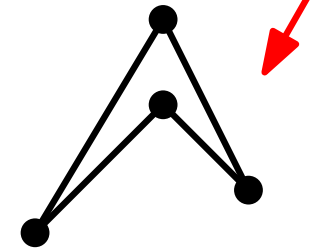
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Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

7

Solution:

- Make the first vertex in the quadrangle (regarding the canonical ordering) adjacent to the other three vertices.



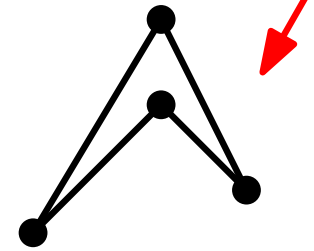
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- Make the first vertex in the quadrangle (regarding the canonical ordering) adjacent to the other three vertices.
- Use the algorithm by Harel and Sardas (Shift Algorithm for biconnected graphs).



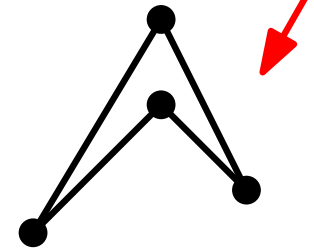
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- Use the algorithm by Harel and Sardas (Shift Algorithm for biconnected graphs). It builds a canonical ordering bottom-up instead of top-down.



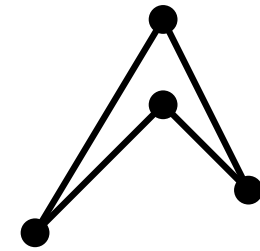
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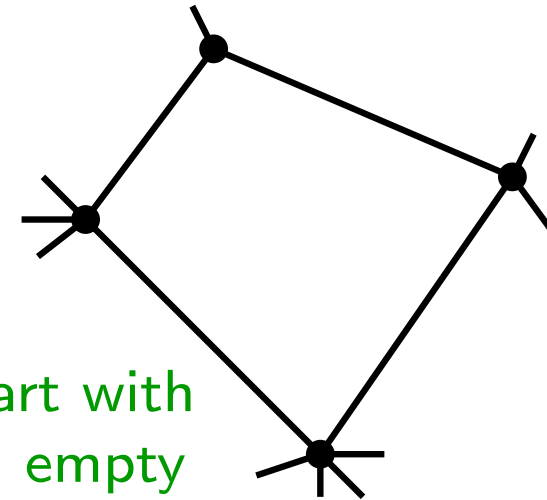
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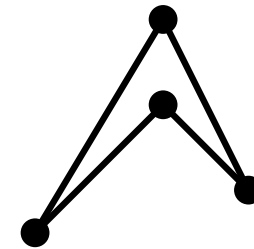
start with
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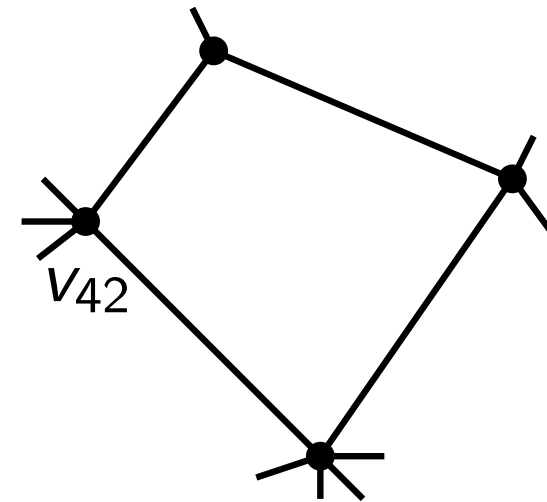
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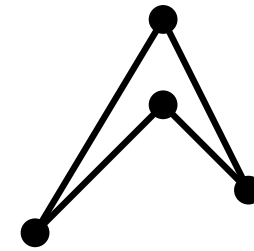
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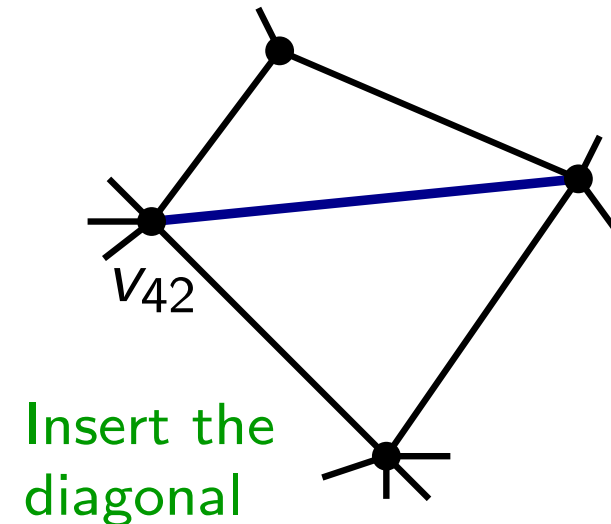
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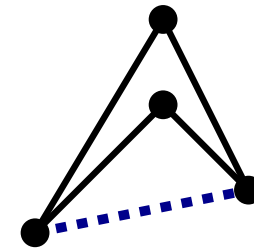
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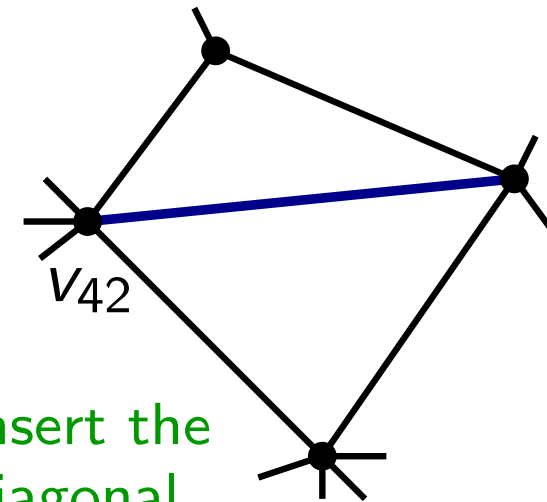
Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

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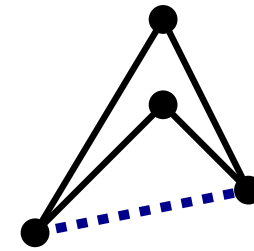
Insert the
diagonal

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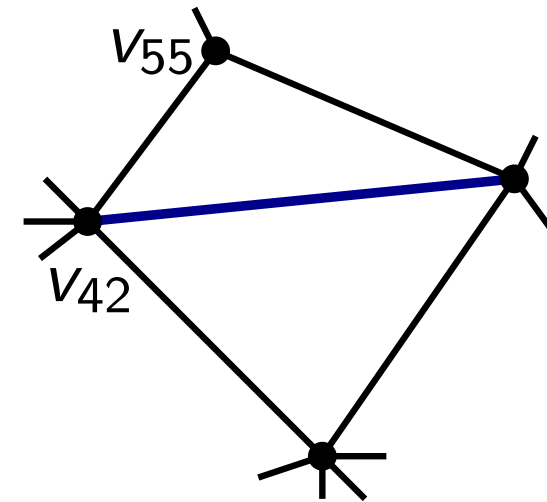
7

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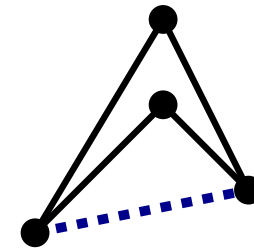
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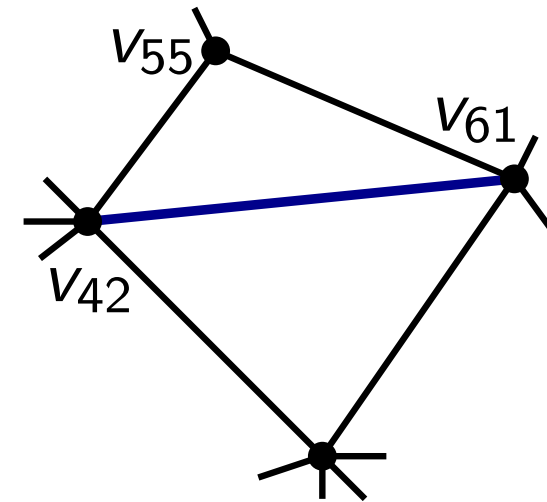
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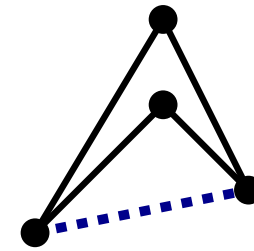
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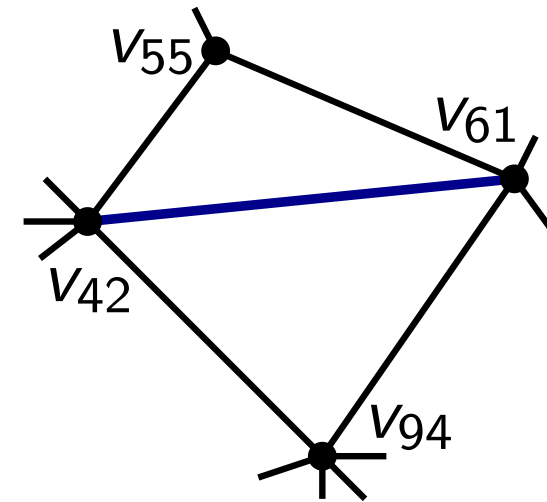
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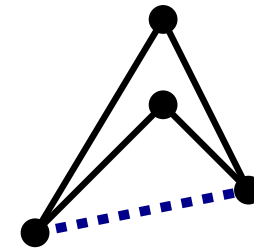
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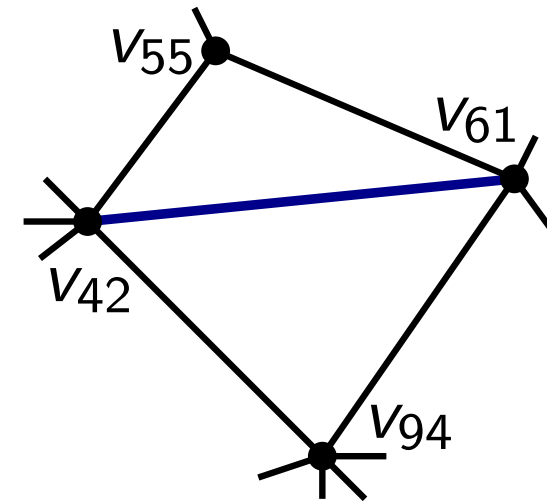
Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$ 7

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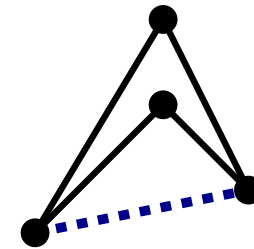
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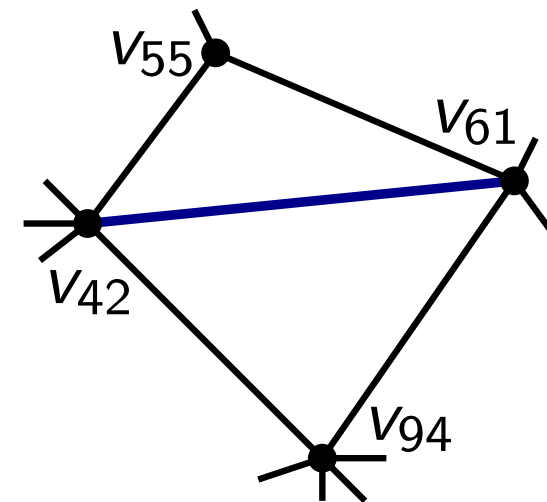
Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

Solution:

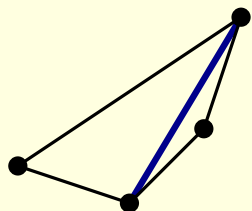
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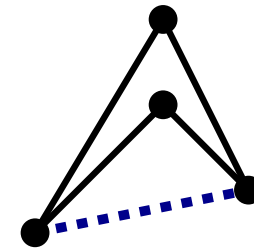
Case 1



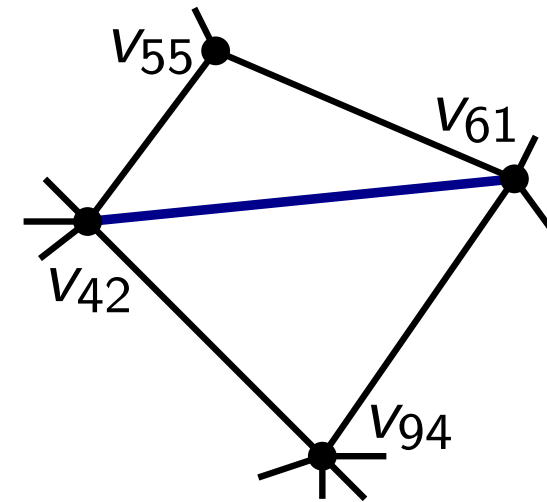
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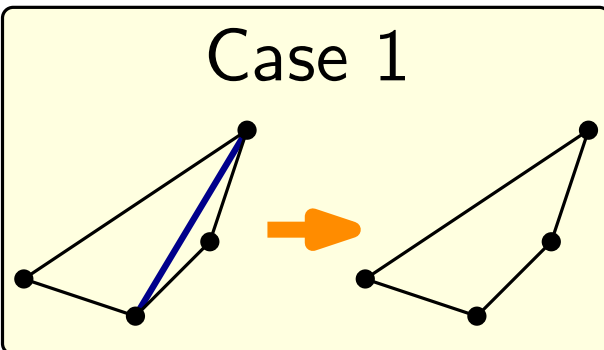
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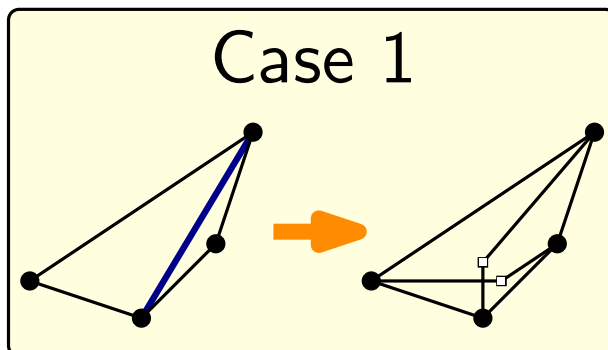
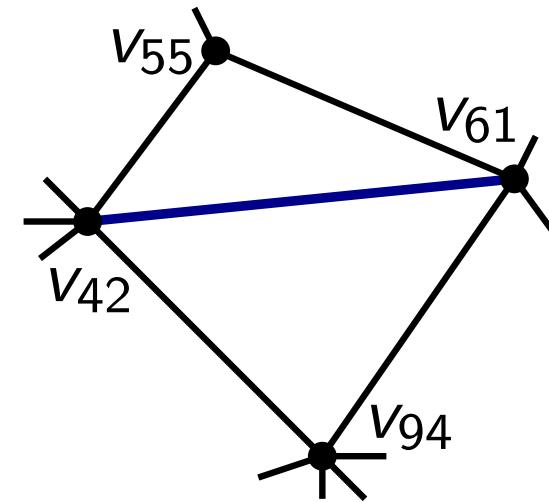
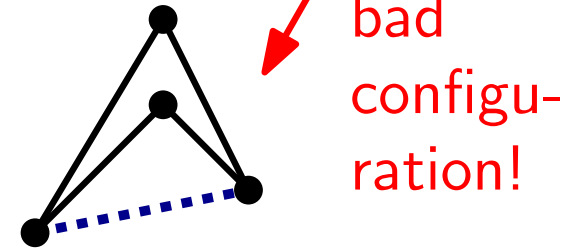
Case 1



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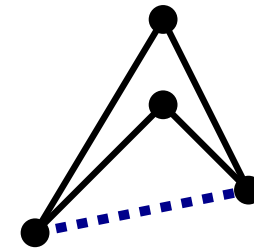
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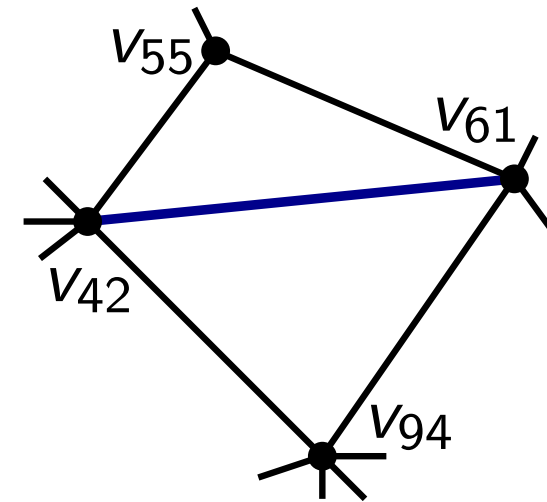
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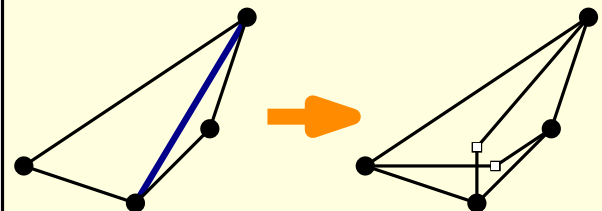
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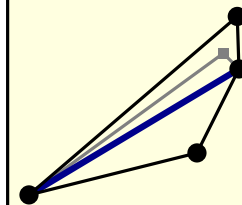
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Case 1



Case 2

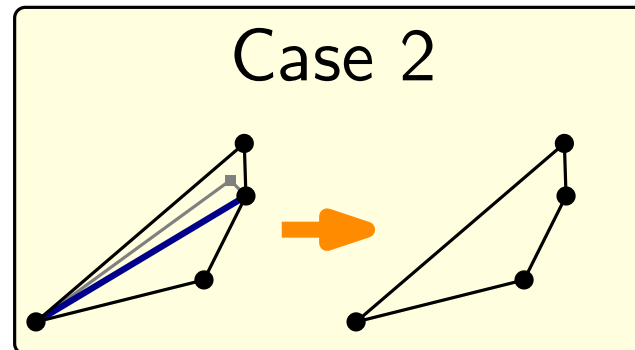
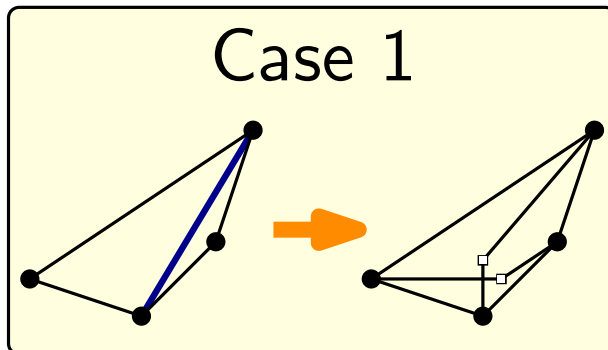
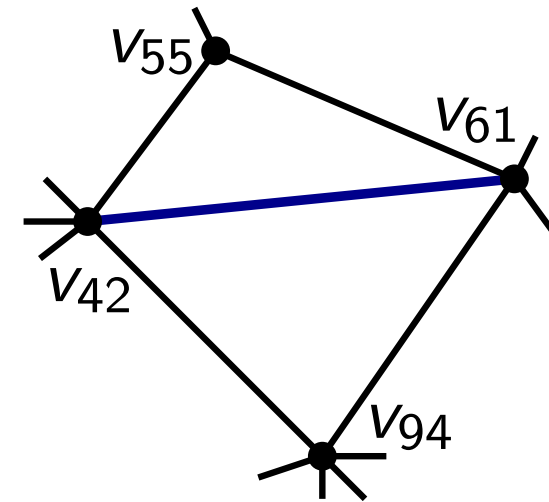
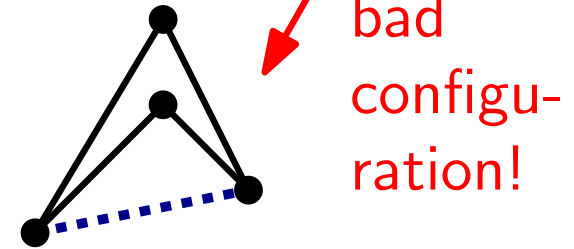


Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

7

Solution:

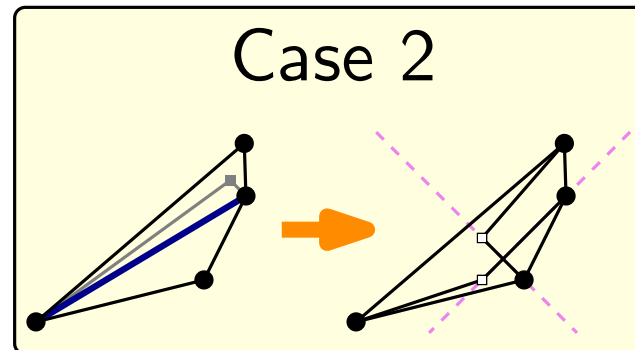
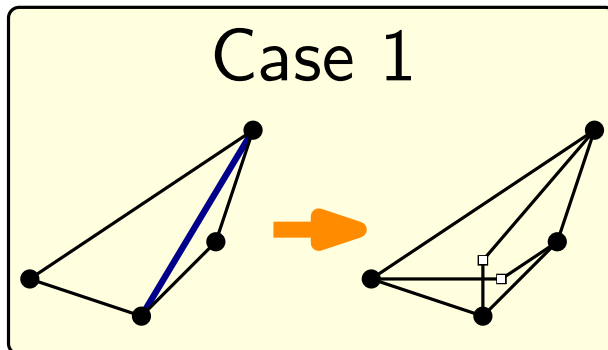
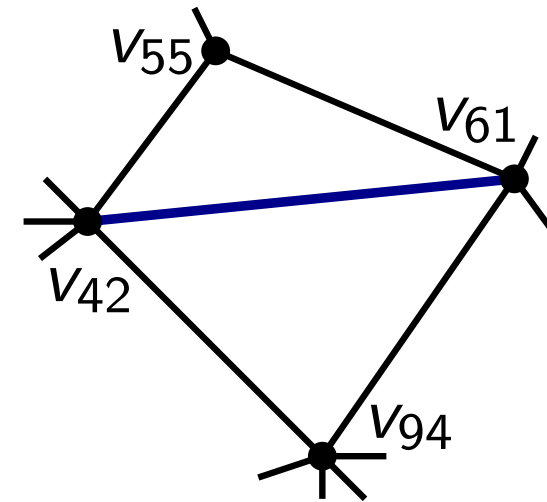
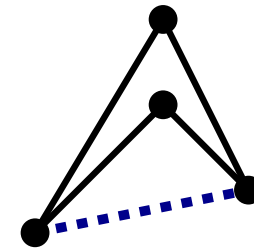
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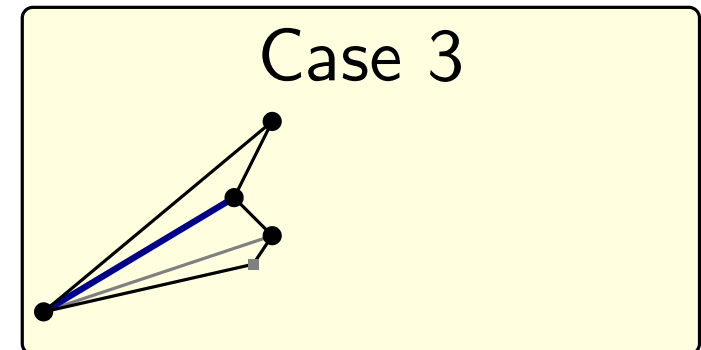
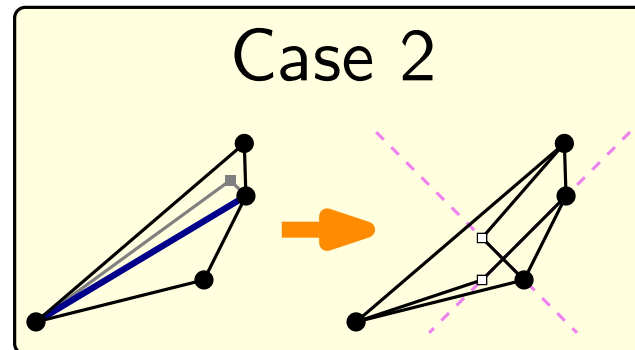
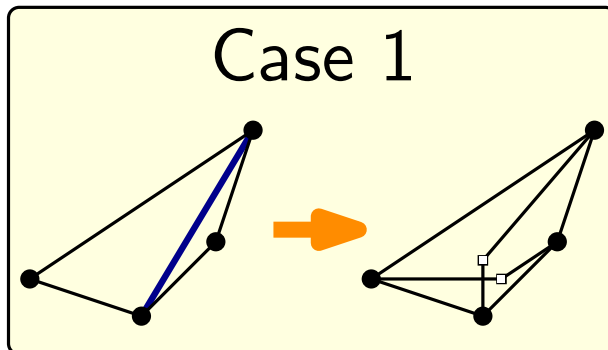
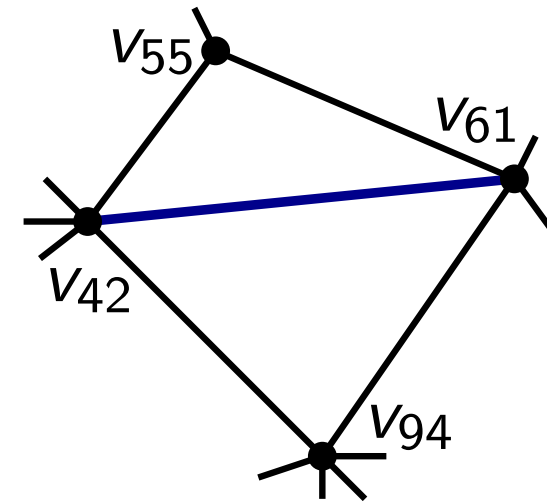
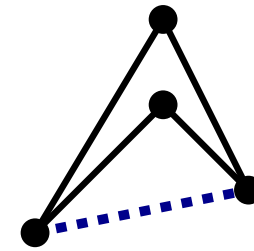
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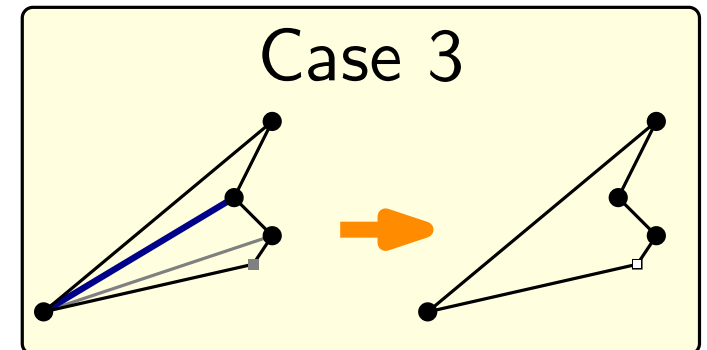
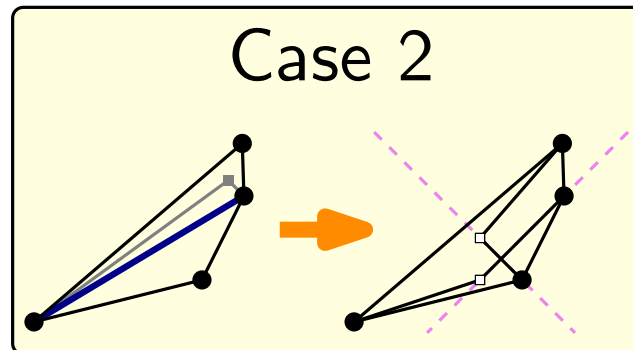
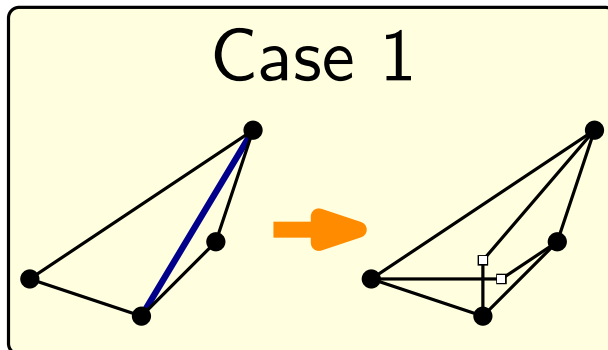
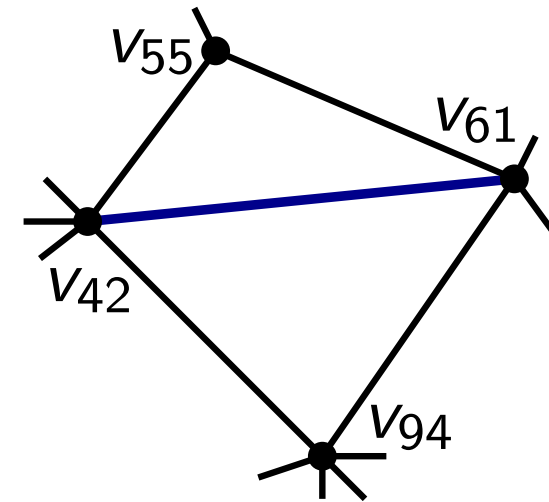
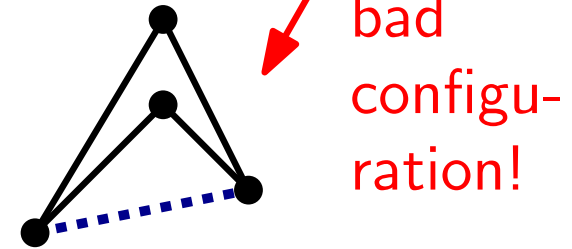


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7

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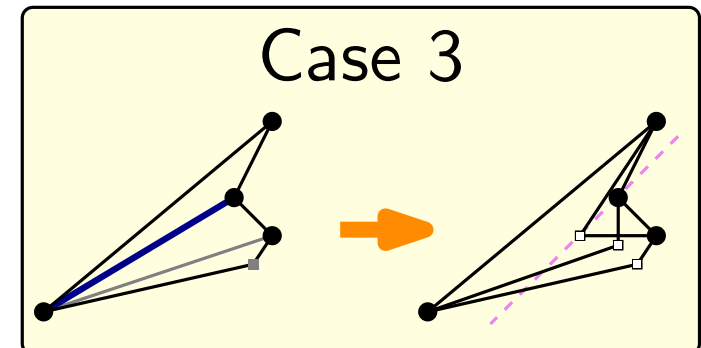
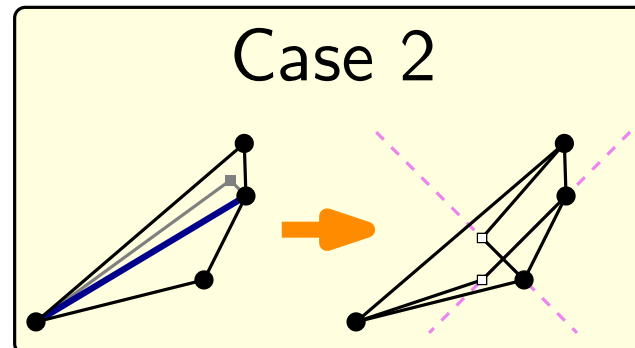
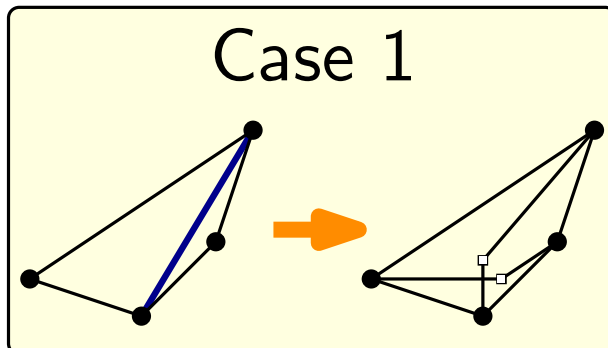
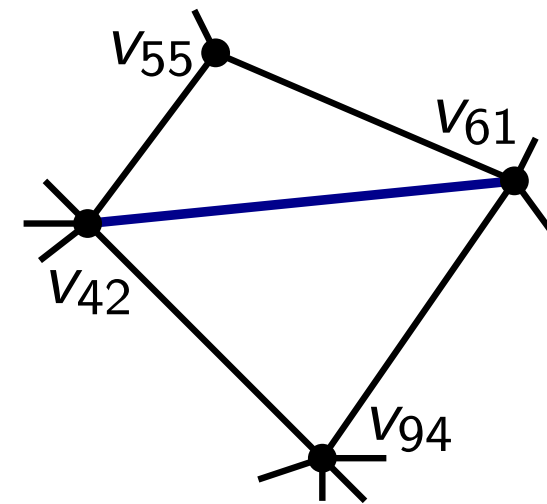
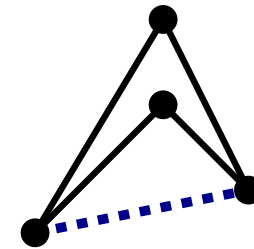
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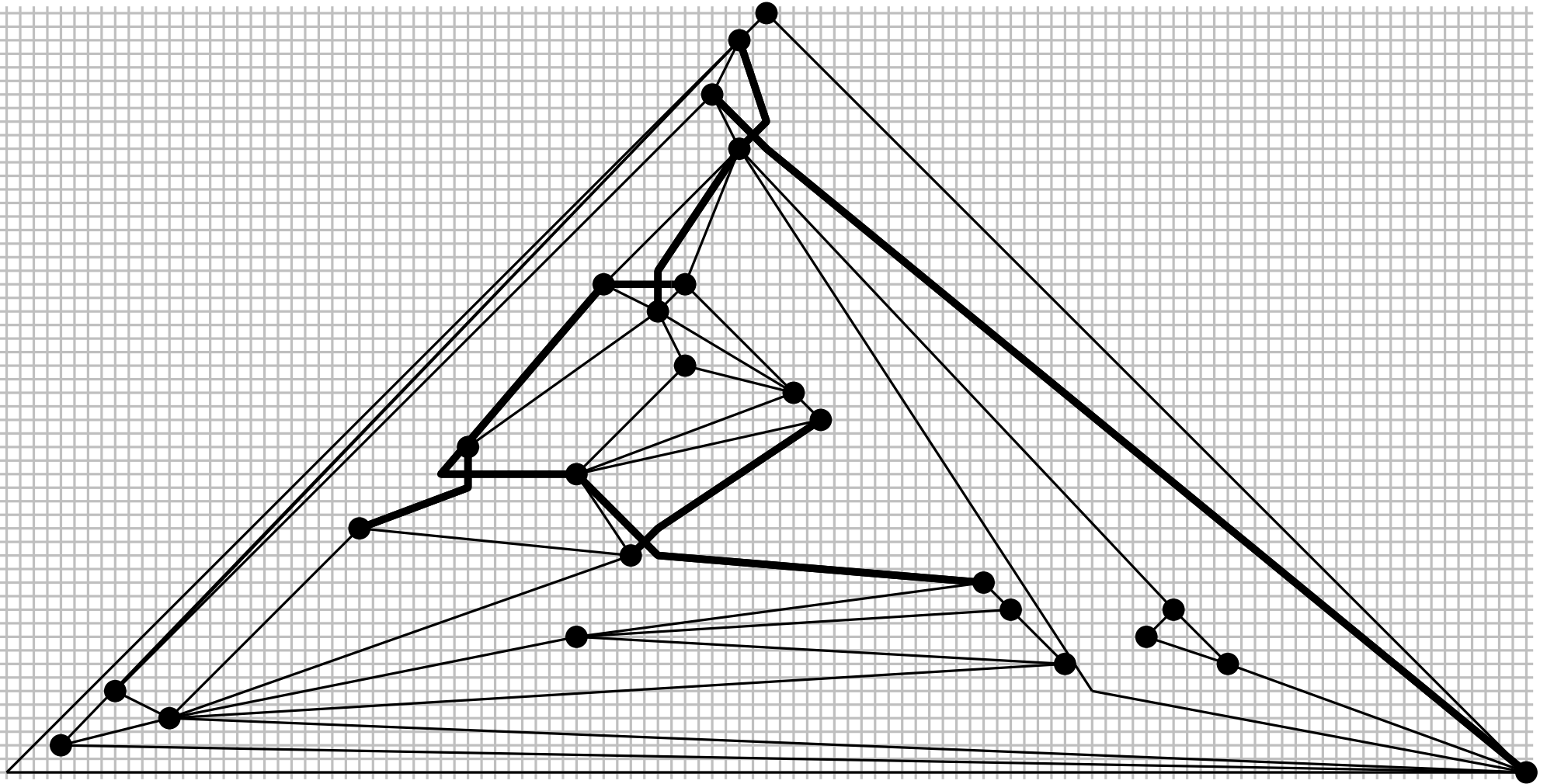
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8

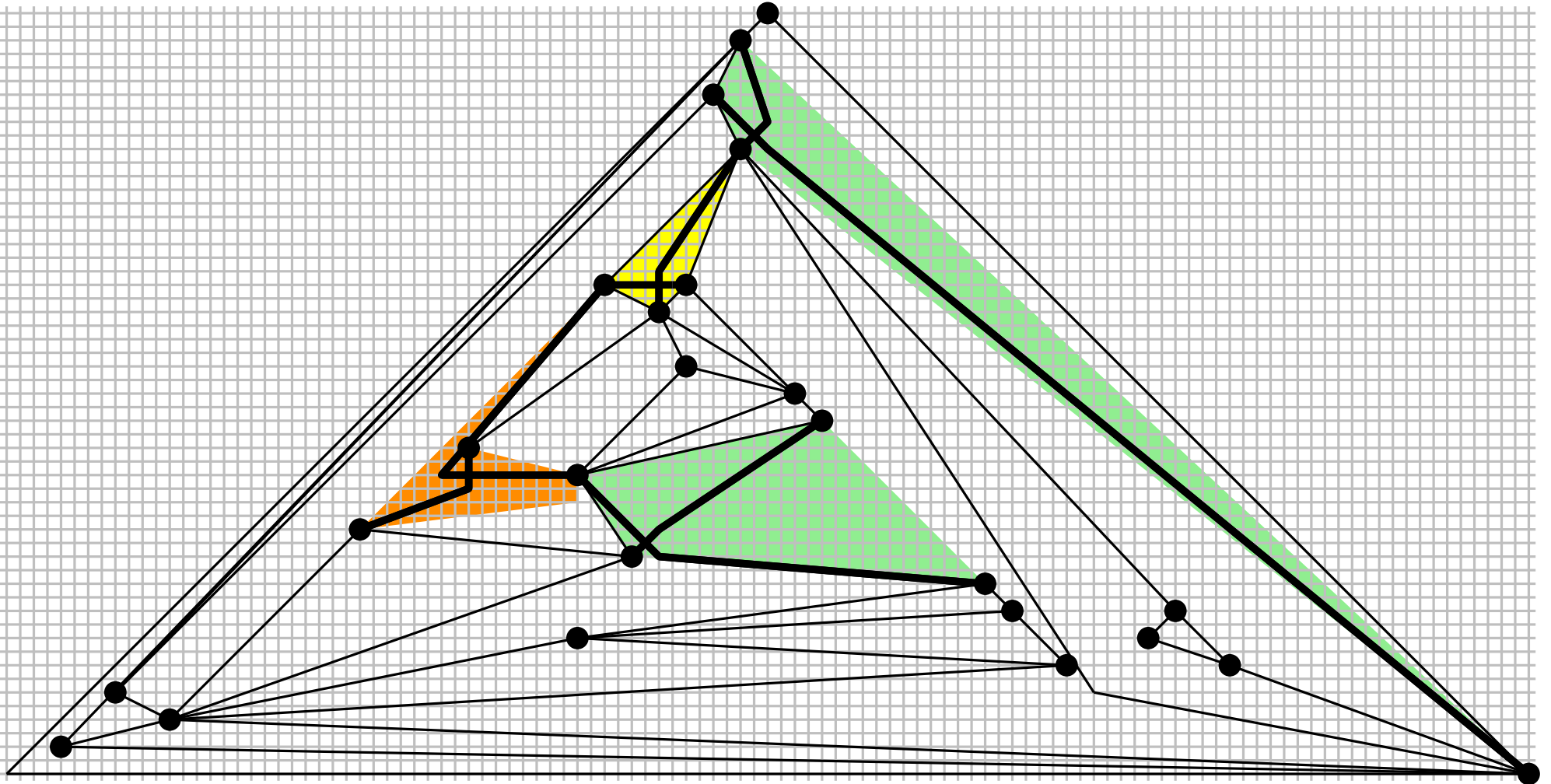
Full example:



Result 1: NIC-Plane Graphs $\subseteq \text{RAC}_1^{\text{poly}}$

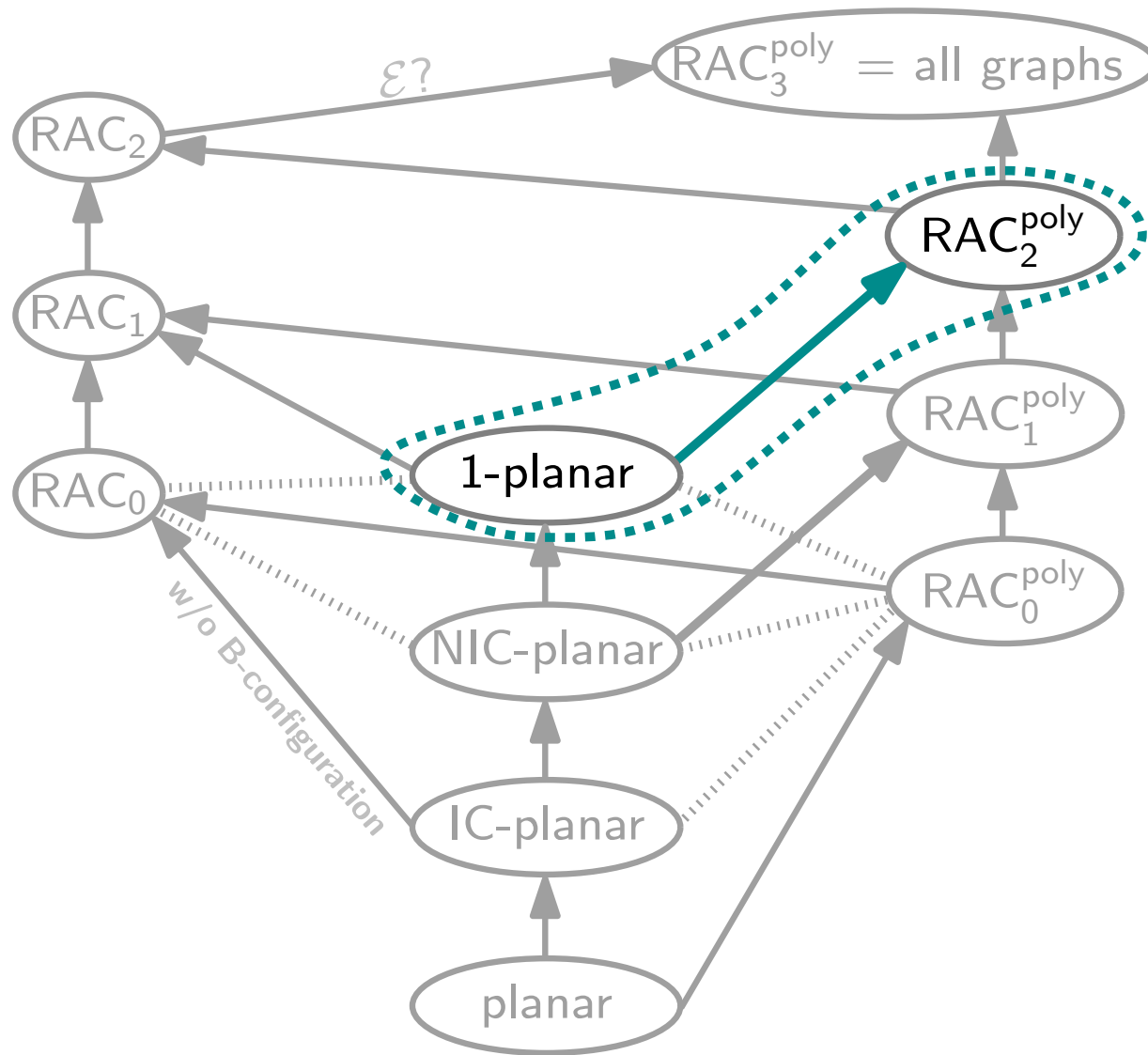
8

Full example:



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

9



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

10

- Input: a 1-plane graph

Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

10

- Input: a 1-plane graph

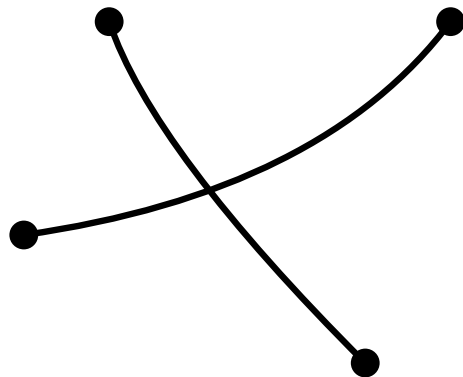
Preprocessing:

Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

10

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Preprocessing:



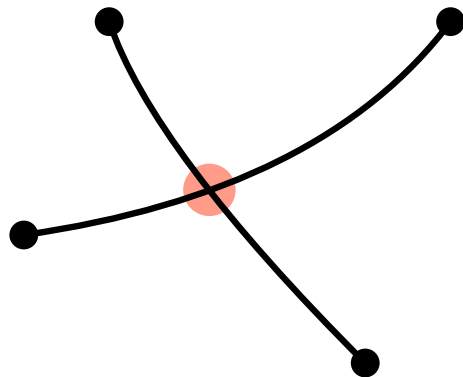
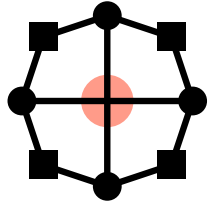
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

10

- Input: a 1-plane graph

Preprocessing:

- Enclose each **crossing** by a so called *subdivided kite*:



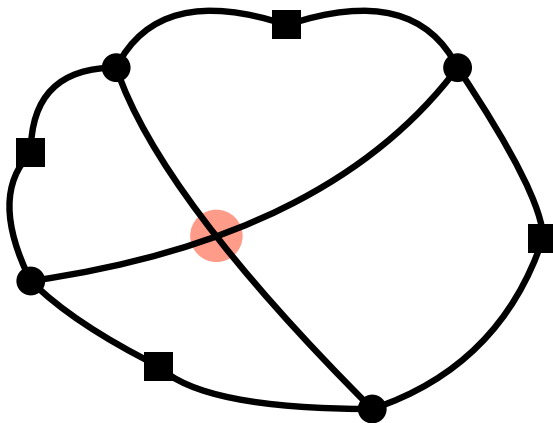
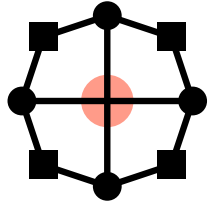
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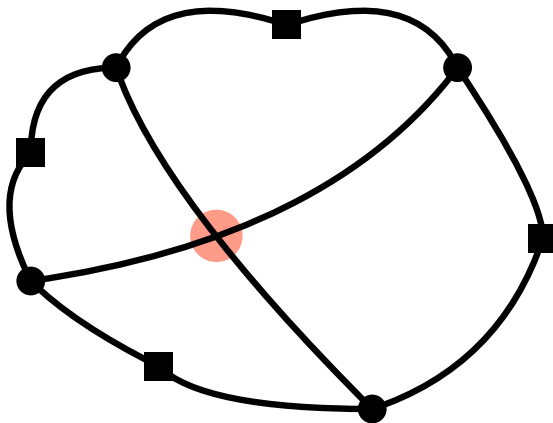
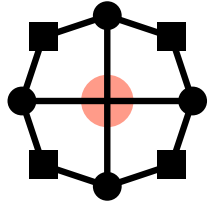
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- Input: a 1-plane graph

Preprocessing:

- Enclose each **crossing** by a so called *subdivided kite*:
- Planarize the graph by replacing each crossing by a vertex



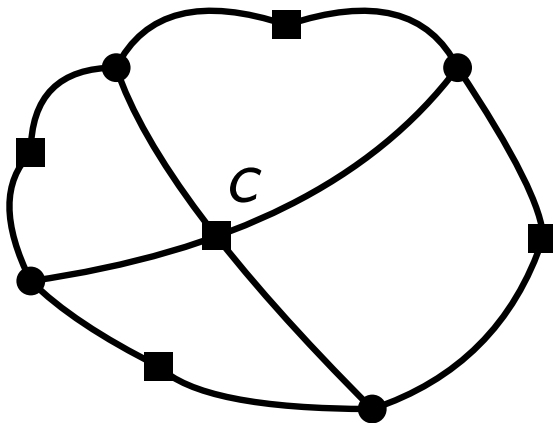
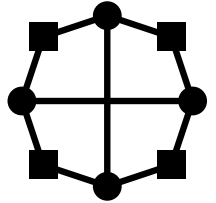
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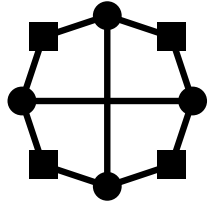
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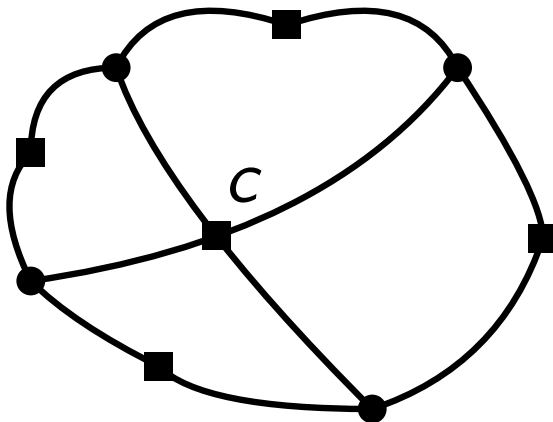
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Drawing phase:

- Draw the obtained plane graph using the Shift Algorithm



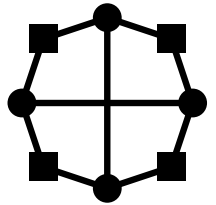
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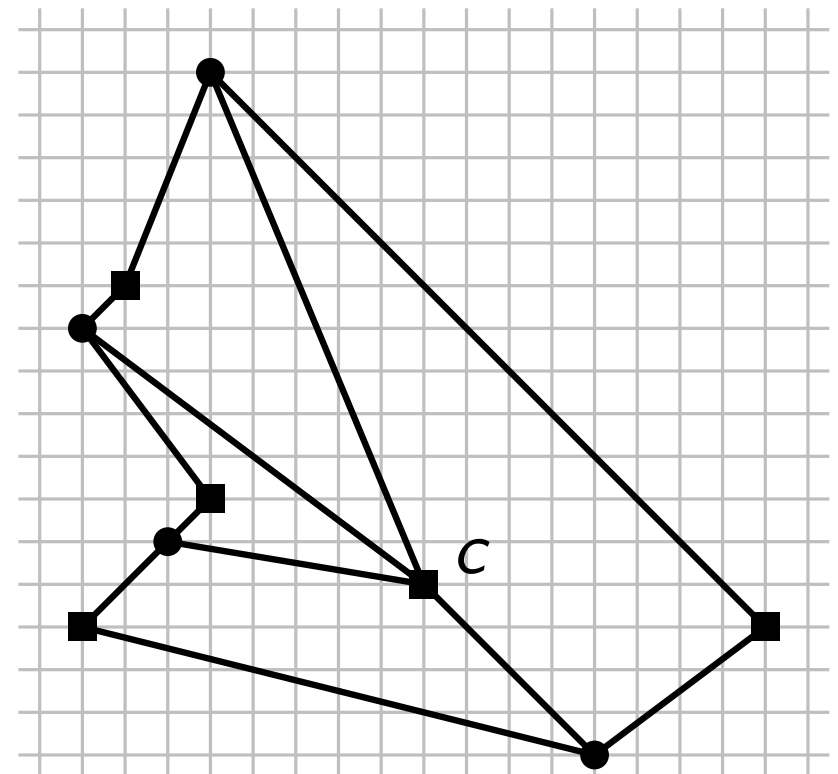
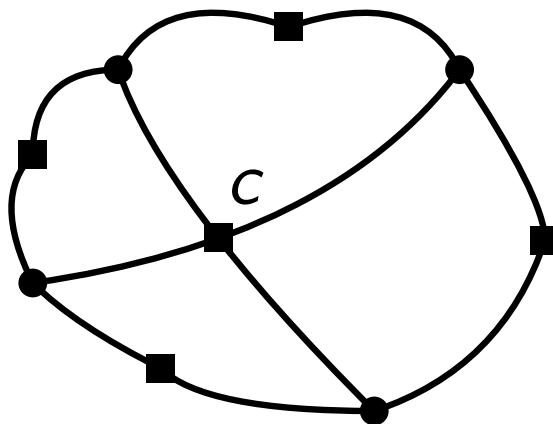
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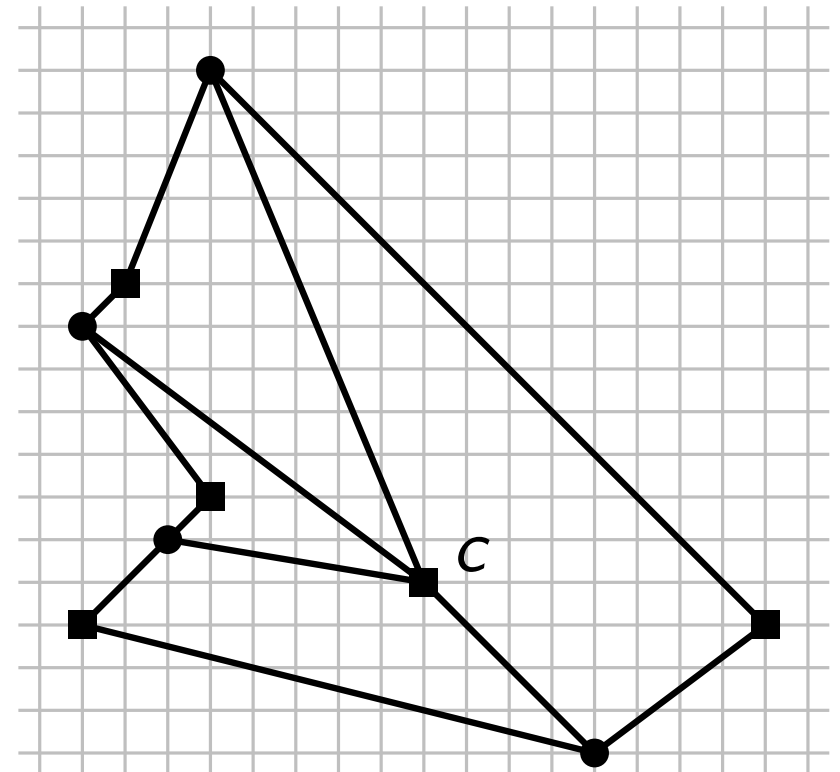
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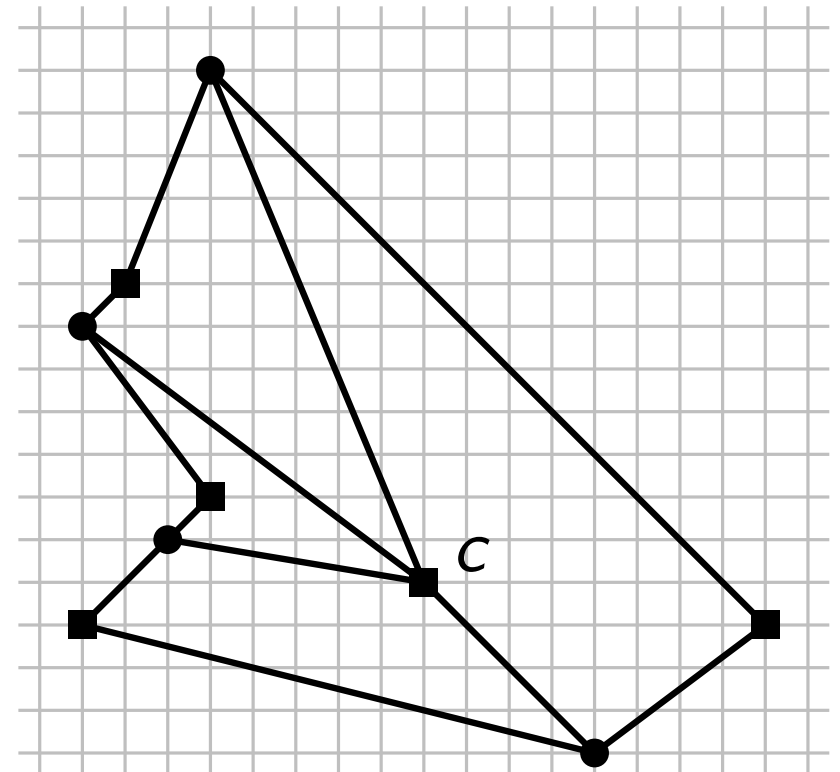
11



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

11

Postprocessing (obtaining crossings at right angles):

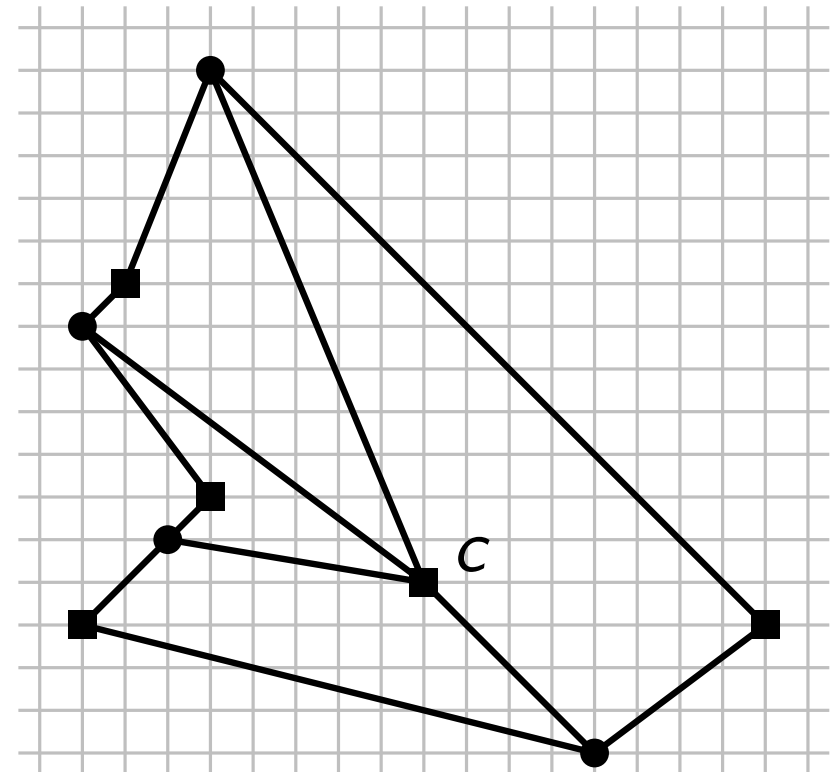


Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

11

Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c

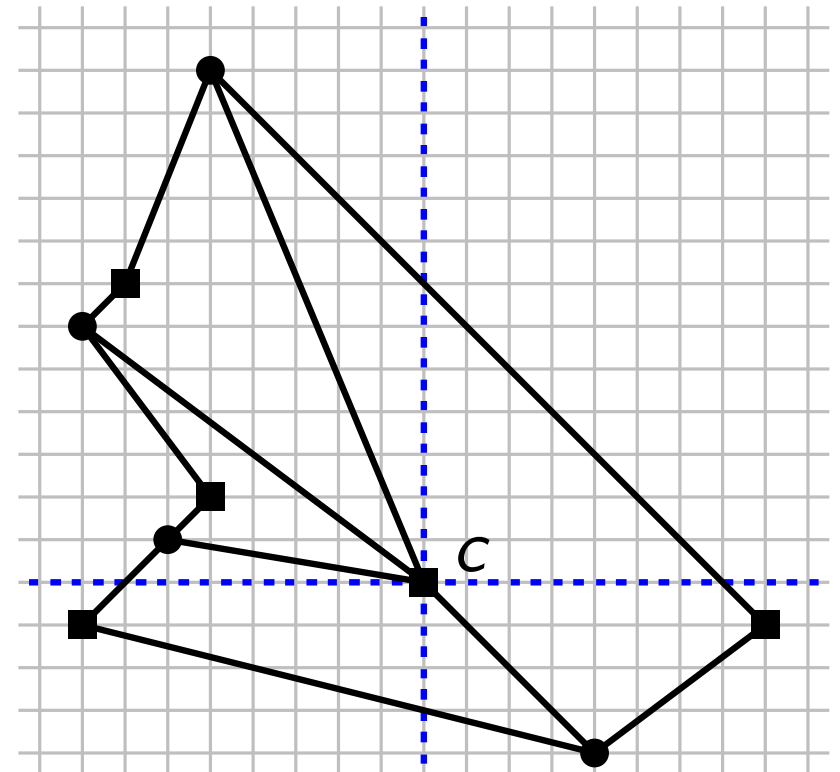


Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

11

Postprocessing (obtaining crossings at right angles):

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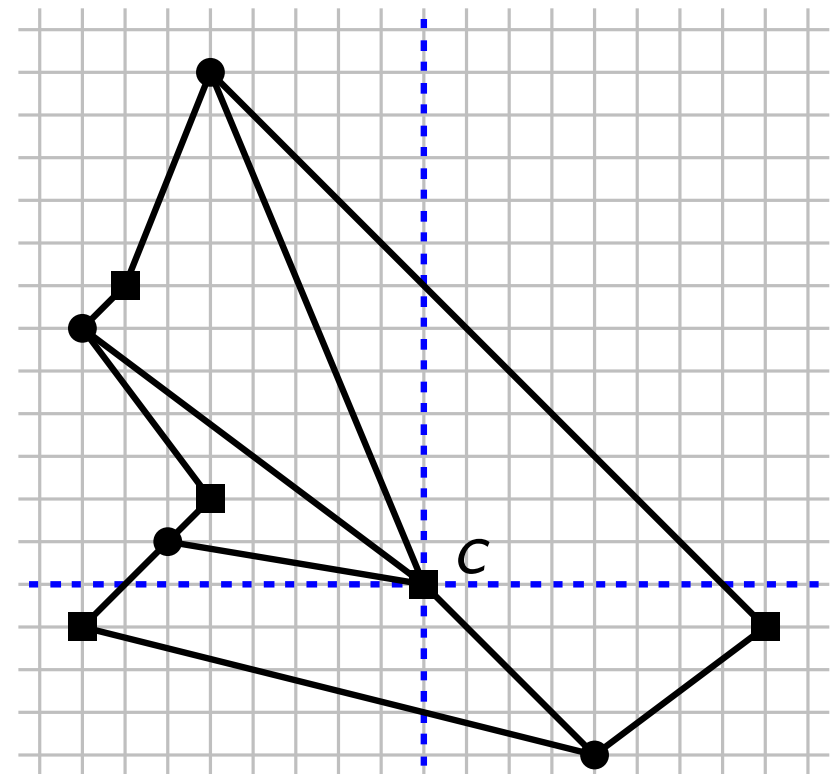


Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

11

Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
- Assign the four edges being incident to c to these half-lines

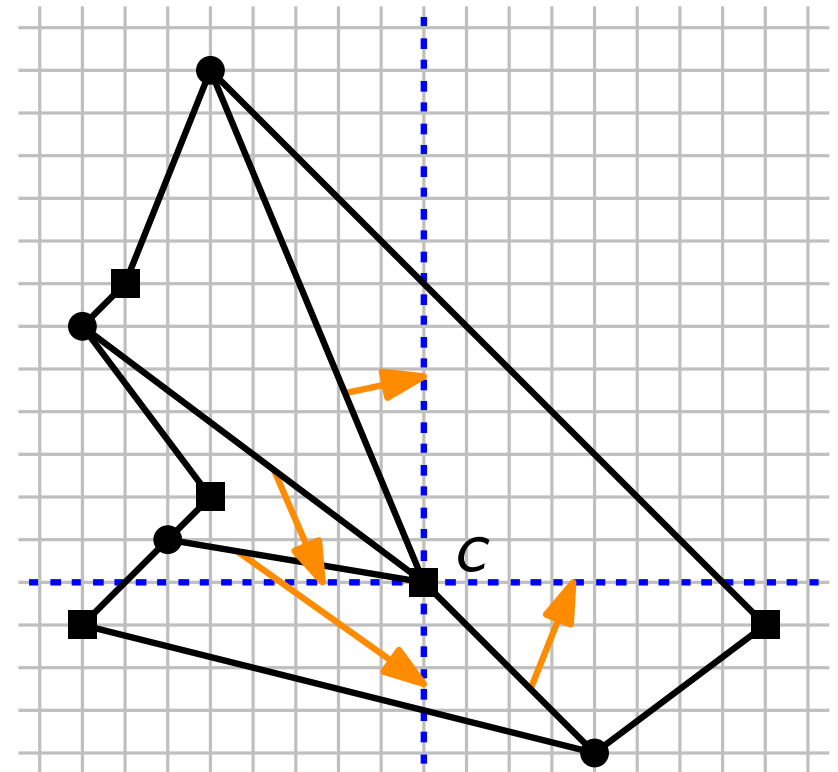


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Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
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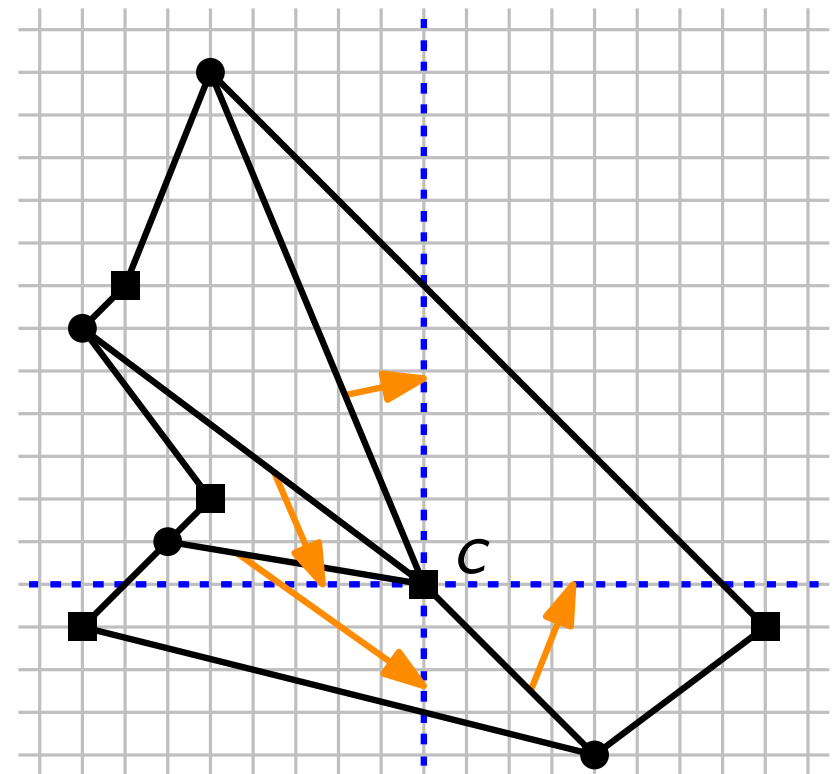


Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
- Assign the four edges being incident to c to these half-lines
- Bend these edges at their assigned half-lines:

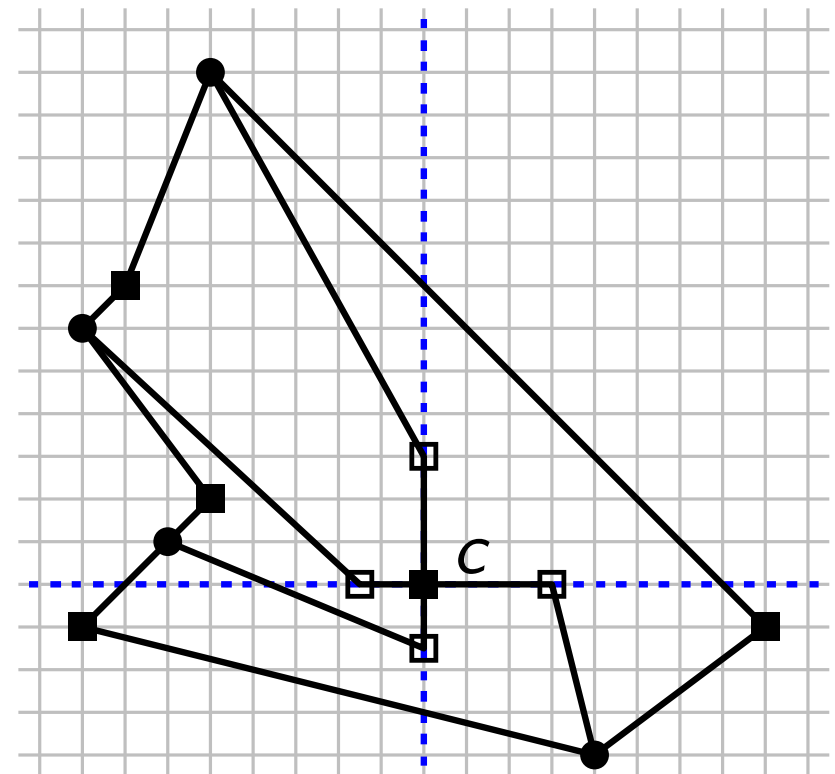


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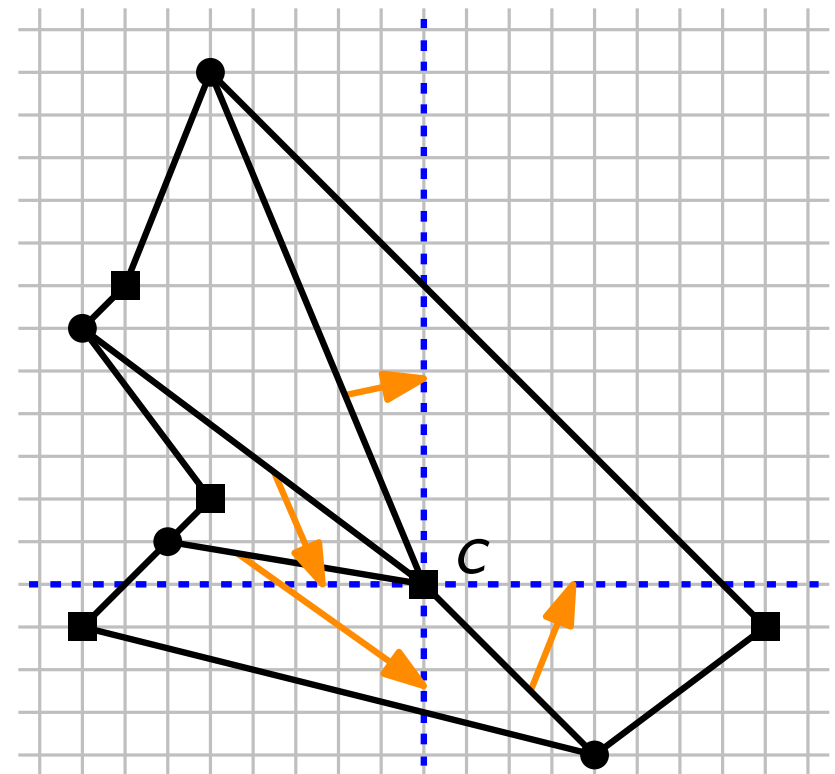


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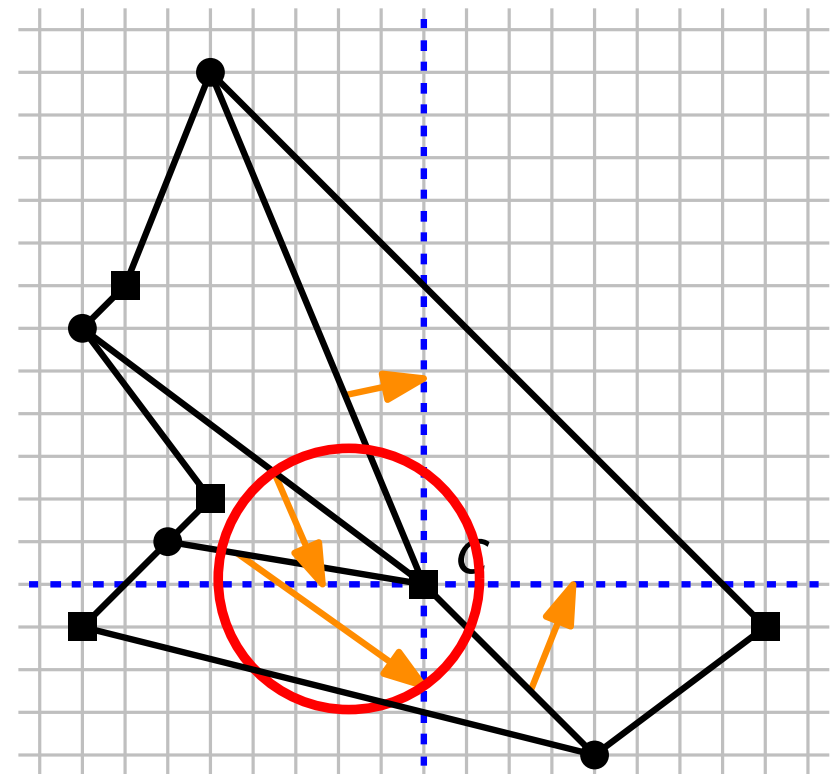
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
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- Bend these edges at their assigned half-lines:

Be careful:
One assignment
might depend on
another one



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

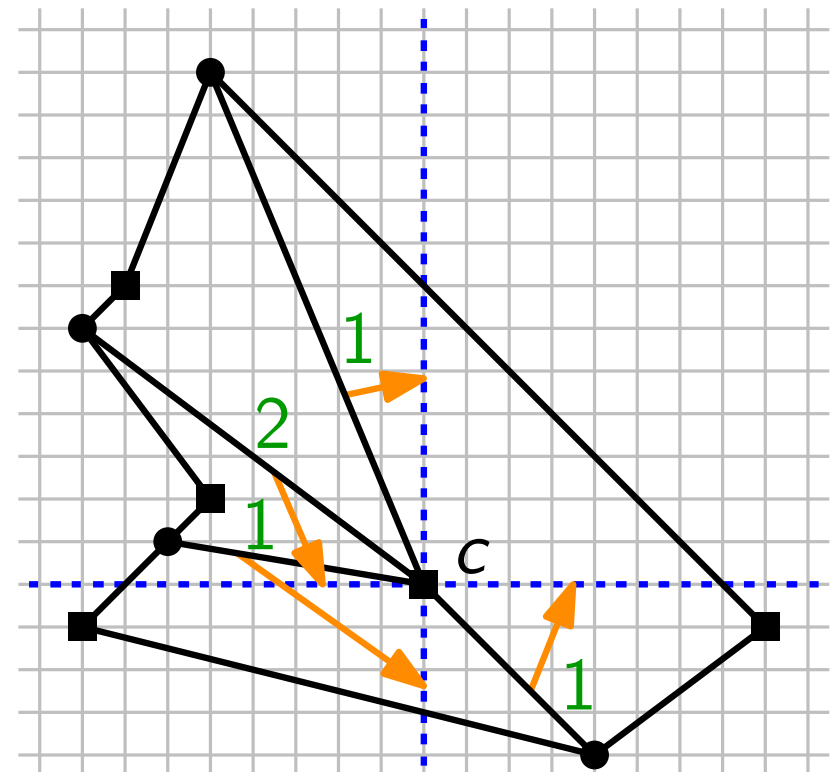
11

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- Assign the four edges being incident to c to these half-lines
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Solution:
re-draw the
independent
ones first



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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- Consider the four axis-parallel half-lines originating at c
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- Bend these edges at their assigned half-lines:

Be careful:

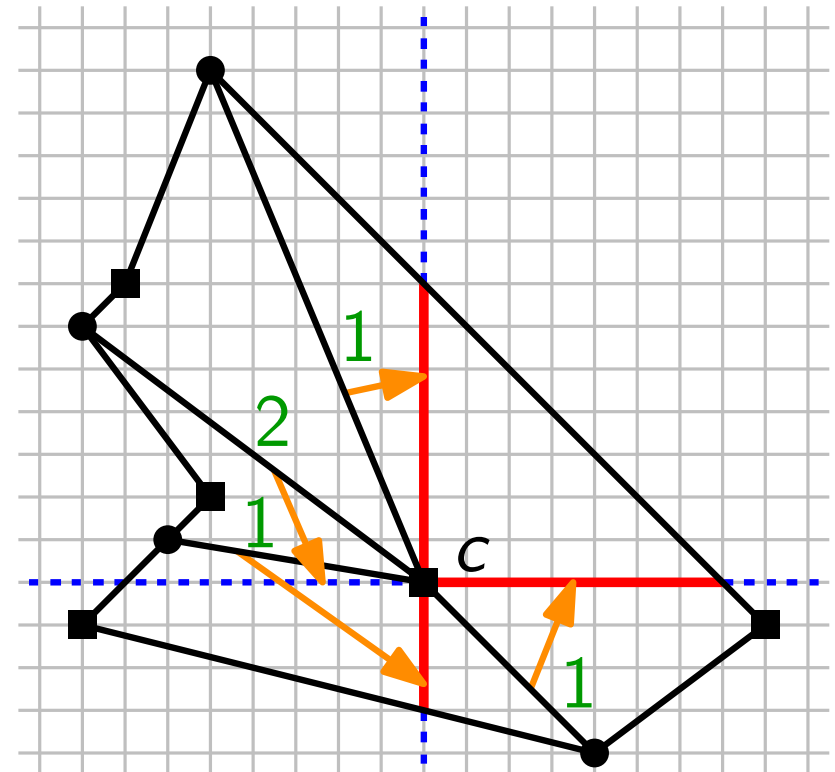
One assignment might depend on another one

Be careful:

There might be no grid points to bend the edges

Solution:

re-draw the independent ones first



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
- Assign the four edges being incident to c to these half-lines
- Bend these edges at their assigned half-lines:

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Be careful:

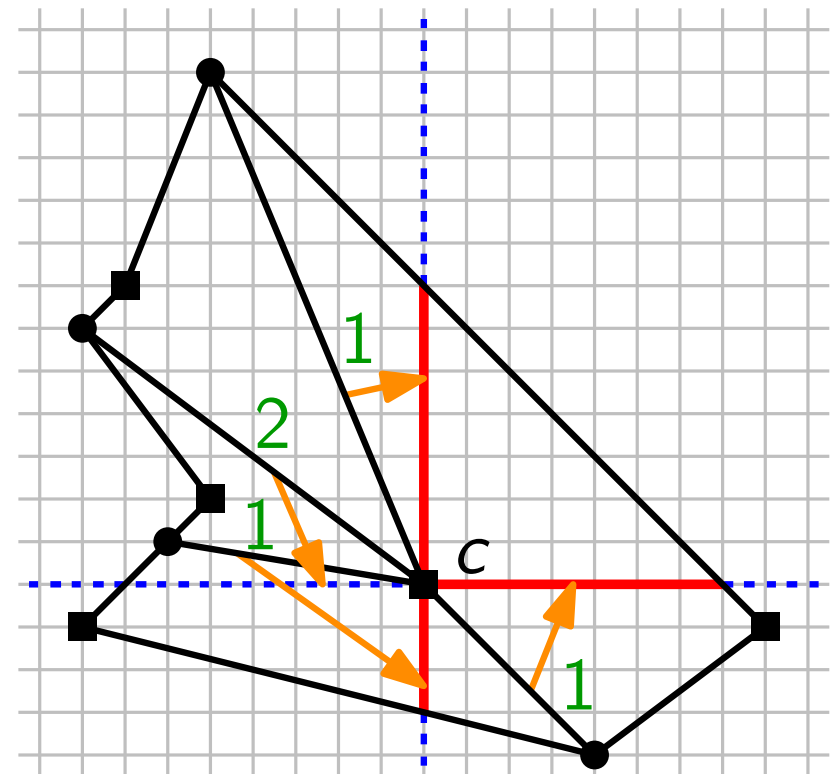
There might be no grid points to bend the edges

Solution:

re-draw the independent ones first

Solution:

make the grid sufficiently fine



Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

11

Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
- Assign the four edges being incident to c to these half-lines
- Bend these edges at their assigned half-lines:

grid size:
 $O(n) \times O(n)$

Be careful:

One assignment
might depend on
another one

Solution:

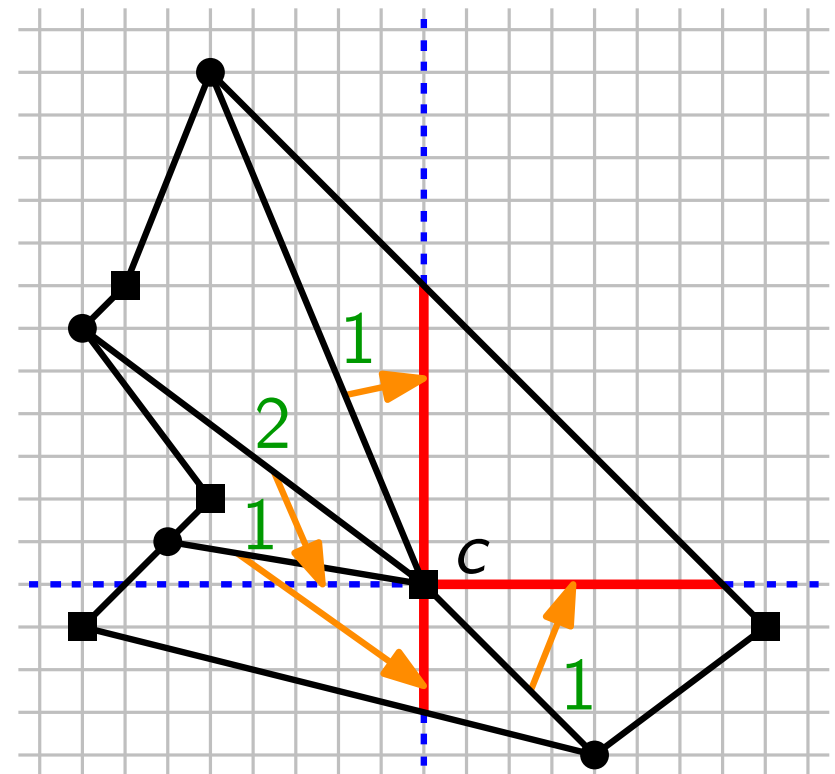
re-draw the
independent
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Be careful:

There might be
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Solution:

make the grid
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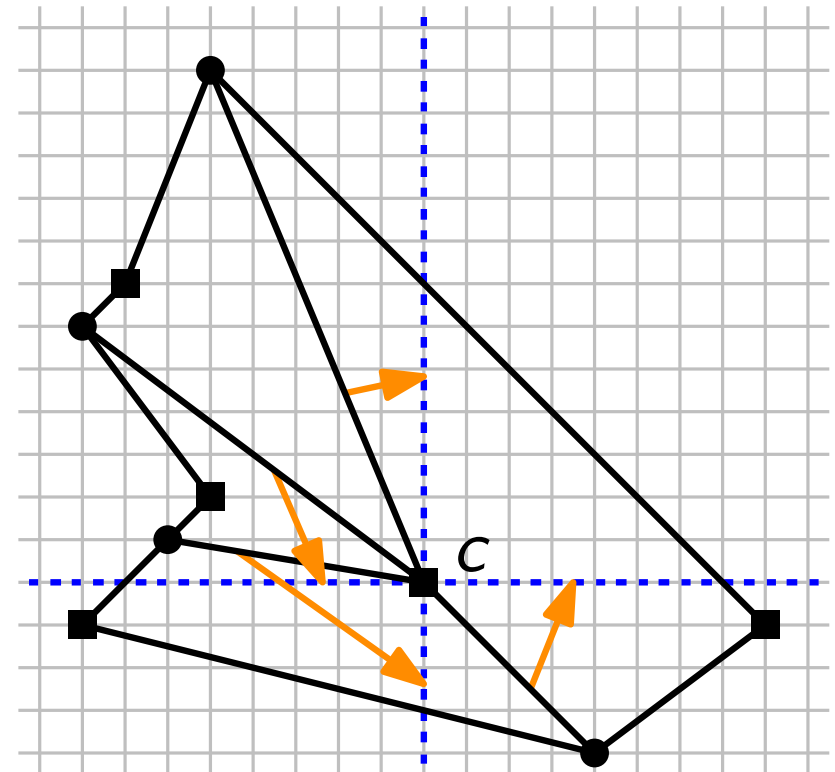
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Postprocessing (obtaining crossings at right angles):

- Consider the four axis-parallel half-lines originating at c
- Assign the four edges being incident to c to these half-lines
- Bend these edges at their assigned half-lines:
 - 1. Refine the grid by $\tilde{n} \in O(n)$

grid size:
 $O(n) \times O(n)$



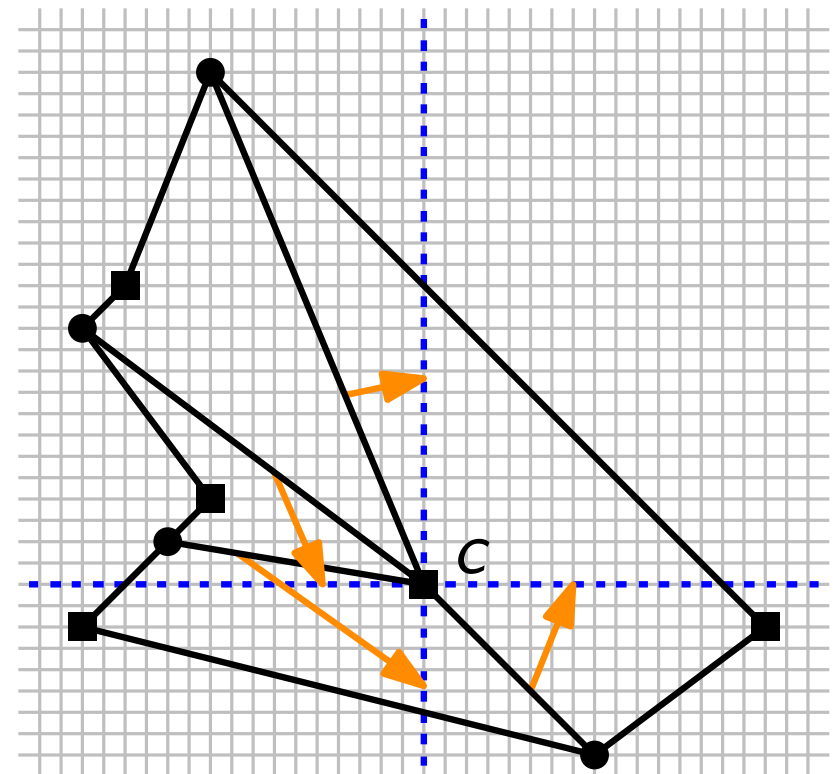
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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 - 1. Refine the grid by $\tilde{n} \in O(n)$

grid size:
 $O(n^2) \times O(n^2)$



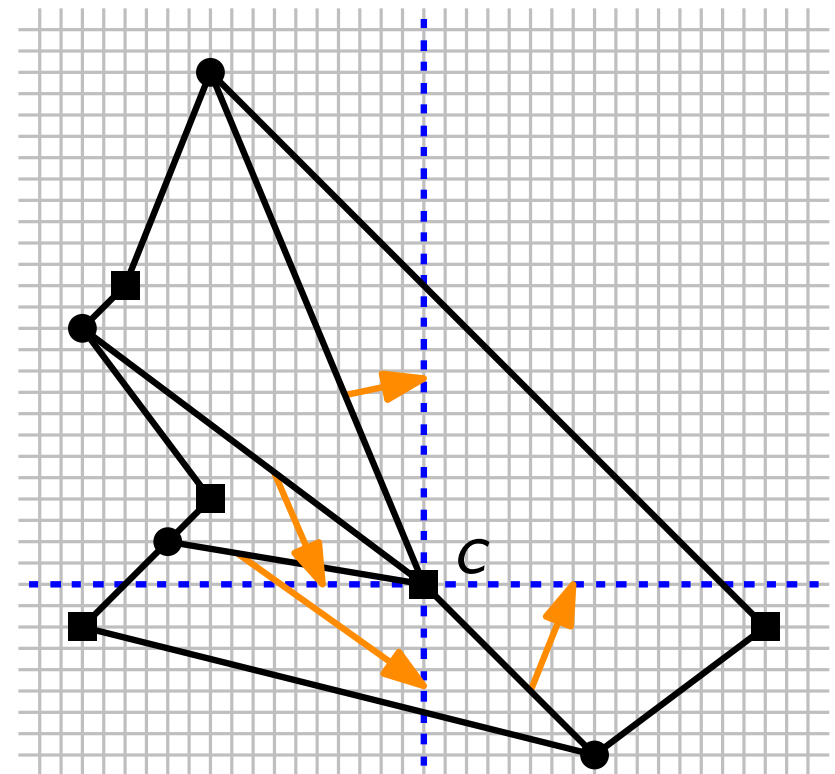
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 - 1. Refine the grid by $\tilde{n} \in O(n)$
 - 2. Re-draw independent edges

grid size:
 $O(n^2) \times O(n^2)$



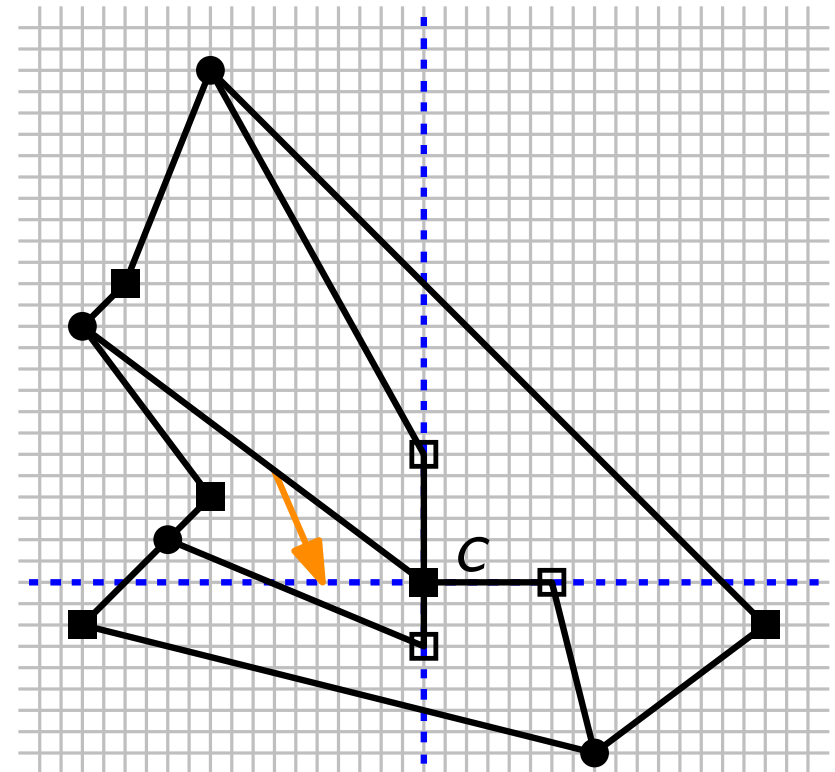
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 - 2. Re-draw independent edges

grid size:
 $O(n^2) \times O(n^2)$

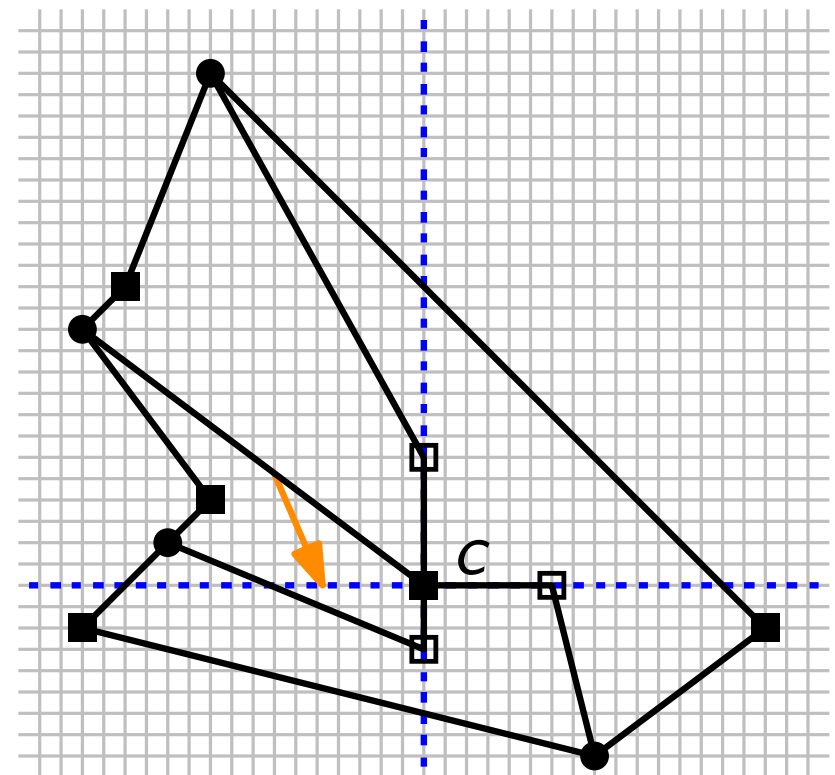


Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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- Assign the four edges being incident to c to these half-lines
- Bend these edges at their assigned half-lines:
grid size: $O(n^2) \times O(n^2)$
 1. Refine the grid by $\tilde{n} \in O(n)$
 2. Re-draw independent edges
 3. Refine the grid by \tilde{n} again



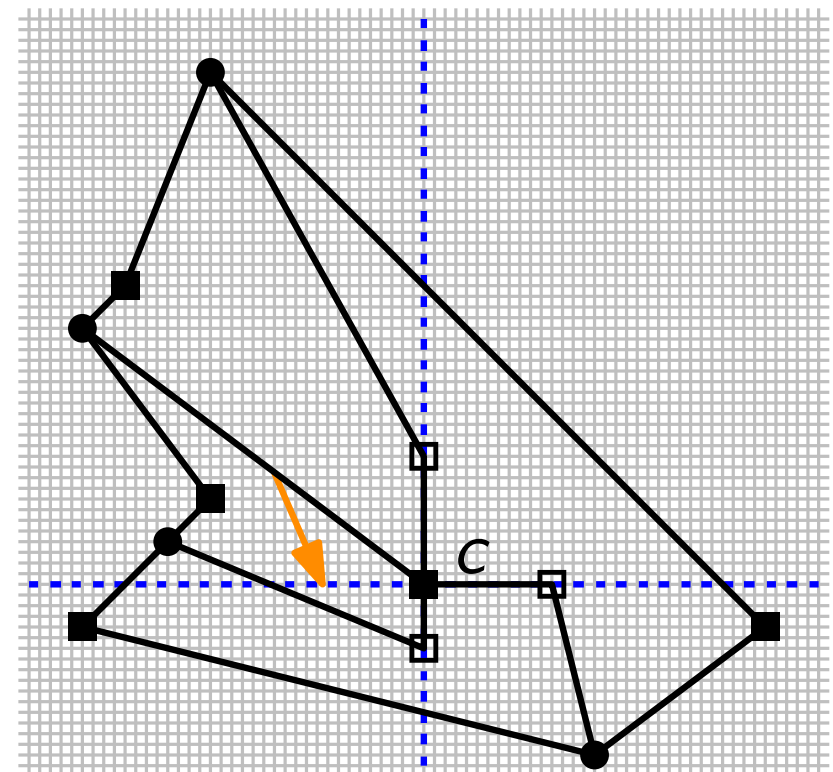
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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 - 1. Refine the grid by $\tilde{n} \in O(n)$
 - 2. Re-draw independent edges
 - 3. Refine the grid by \tilde{n} again

grid size:
 $O(n^3) \times O(n^3)$



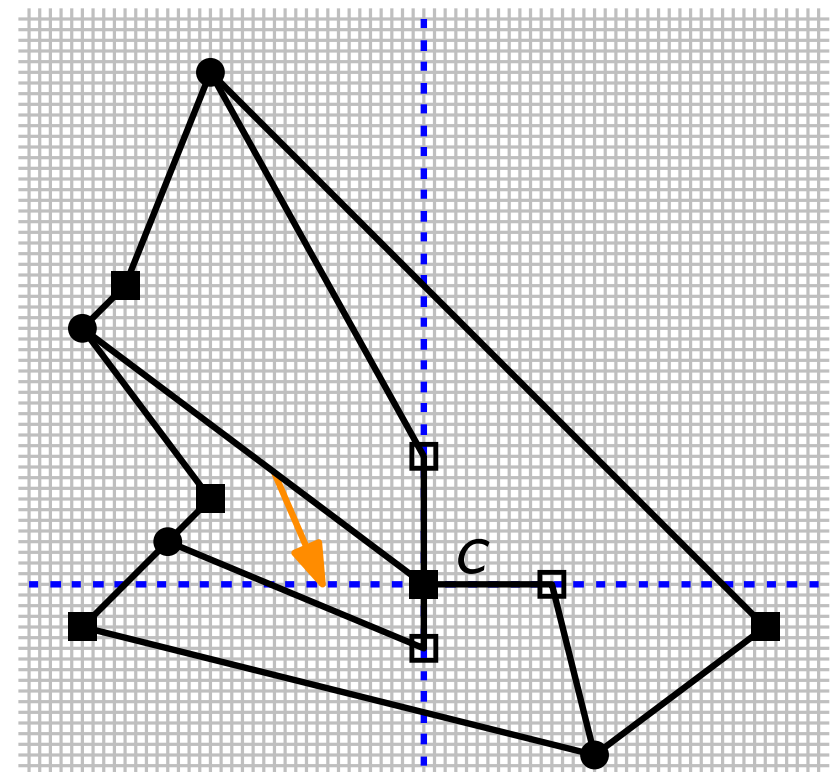
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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 - 2. Re-draw independent edges
 - 3. Refine the grid by \tilde{n} again
 - 4. Re-draw dependent edges

grid size:
 $O(n^3) \times O(n^3)$



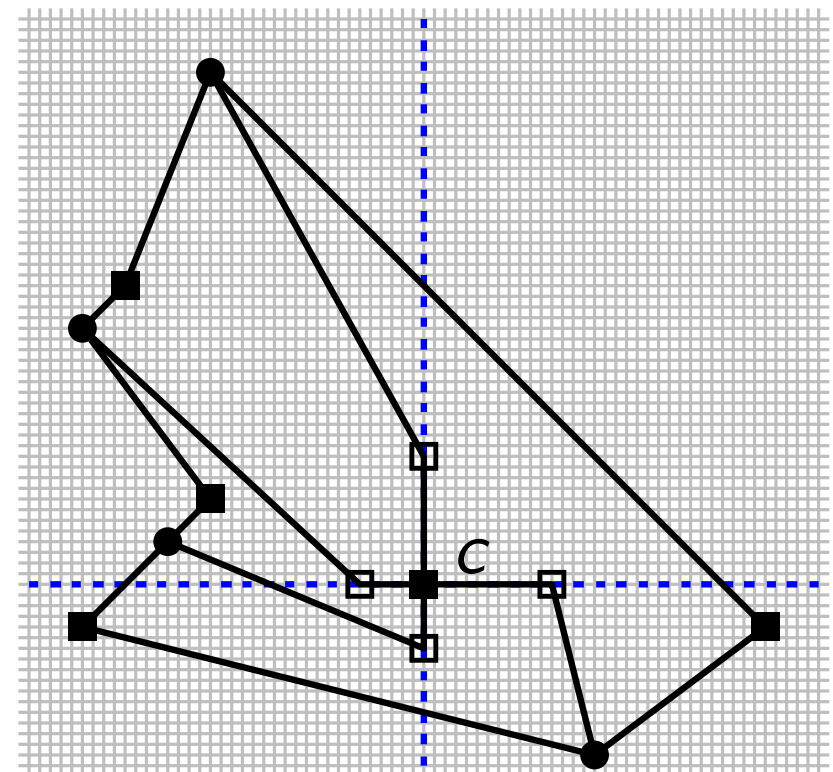
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 - 3. Refine the grid by \tilde{n} again
 - 4. Re-draw dependent edges

grid size:
 $O(n^3) \times O(n^3)$



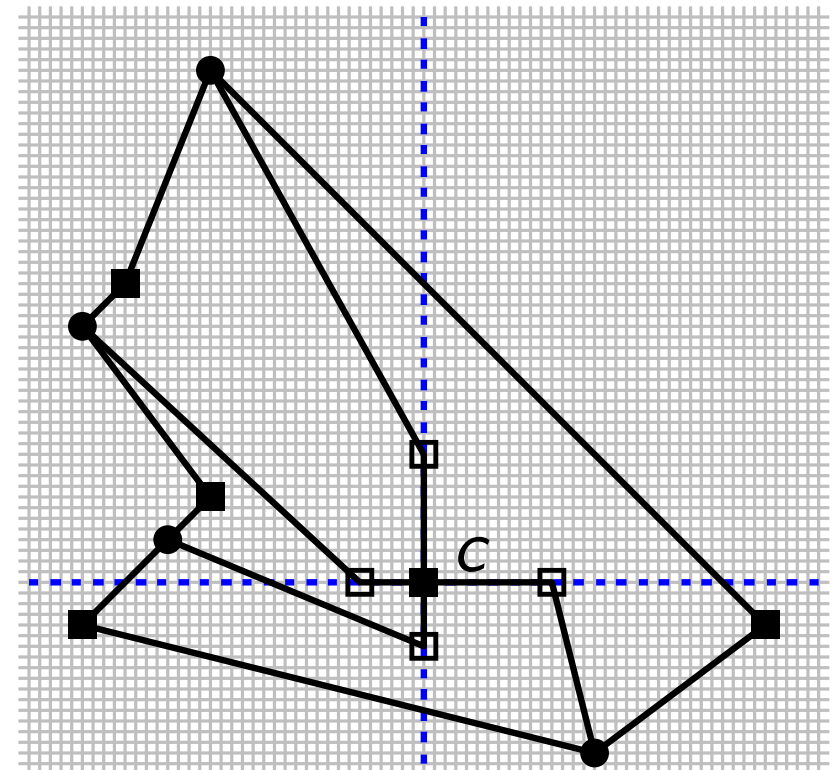
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

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- Bend these edges at their assigned half-lines:
 - 1. Refine the grid by $\tilde{n} \in O(n)$
 - 2. Re-draw independent edges
 - 3. Refine the grid by \tilde{n} again
 - 4. Re-draw dependent edges
- Remove the dummy objects

grid size:
 $O(n^3) \times O(n^3)$



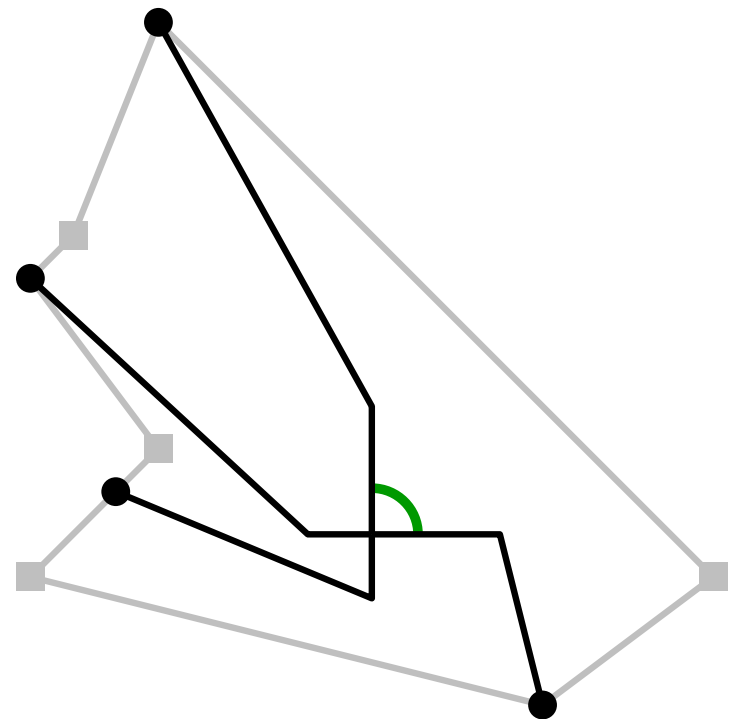
Result 2: 1-Plane Graphs $\subseteq \text{RAC}_2^{\text{poly}}$

11

Postprocessing (obtaining crossings at right angles):

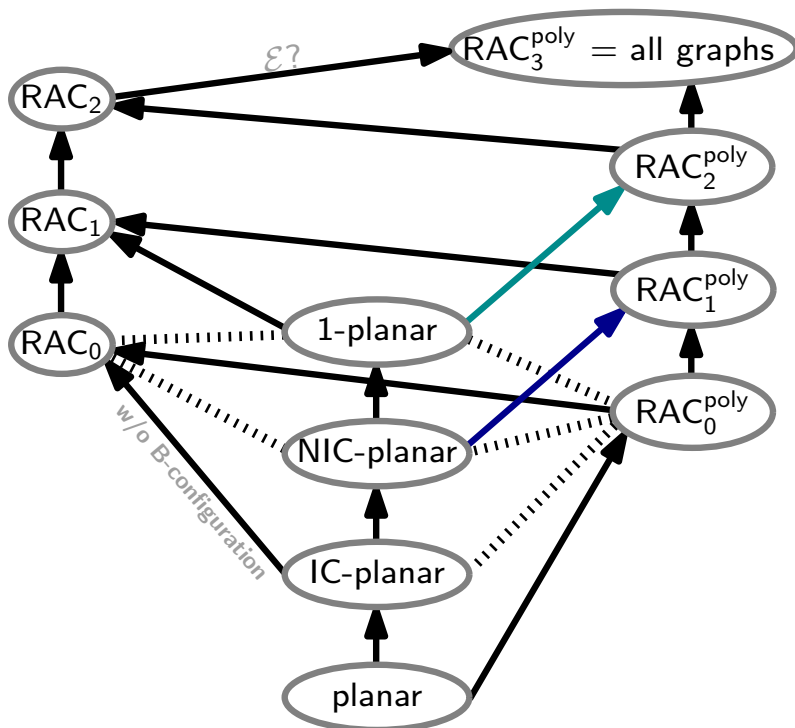
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 - 3. Refine the grid by \tilde{n} again
 - 4. Re-draw dependent edges
- Remove the dummy objects

grid size:
 $O(n^3) \times O(n^3)$



Summary and Open Questions

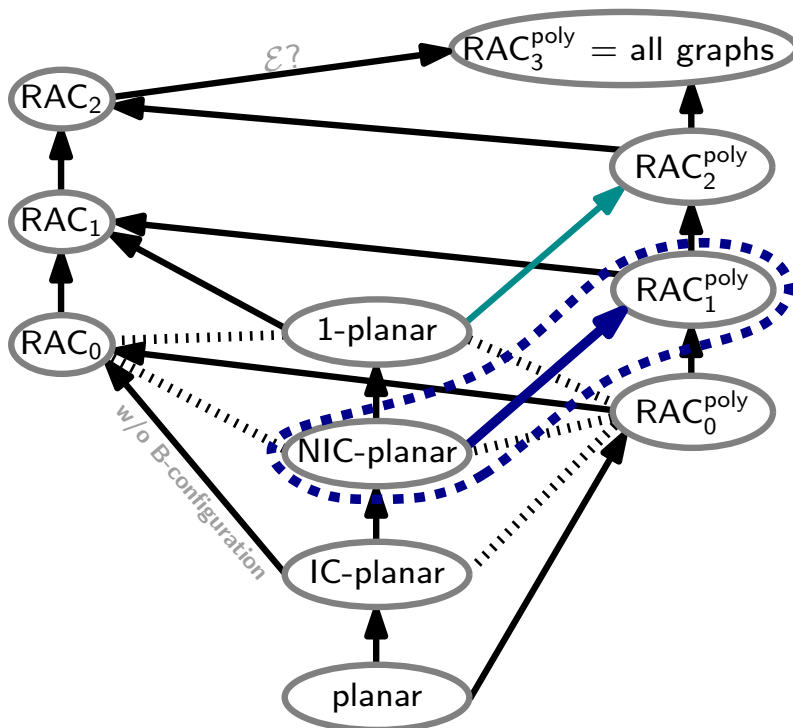
12



Summary and Open Questions

12

NIC-plane
 $\subseteq \text{RAC}_1^{\text{poly}}$

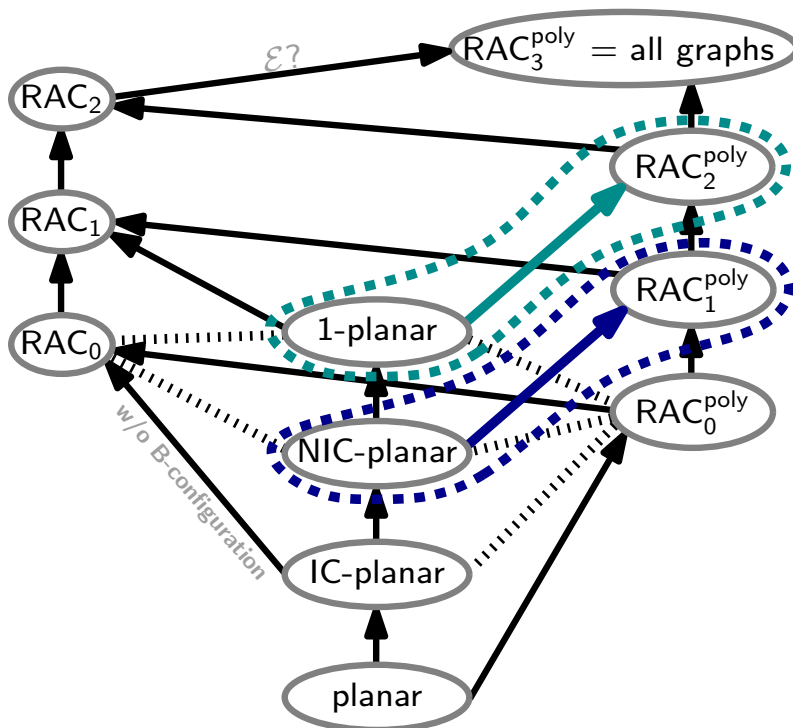


Summary and Open Questions

12

NIC-plane
 $\subseteq \text{RAC}_1^{\text{poly}}$

1-plane
 $\subseteq \text{RAC}_2^{\text{poly}}$



Summary and Open Questions

12

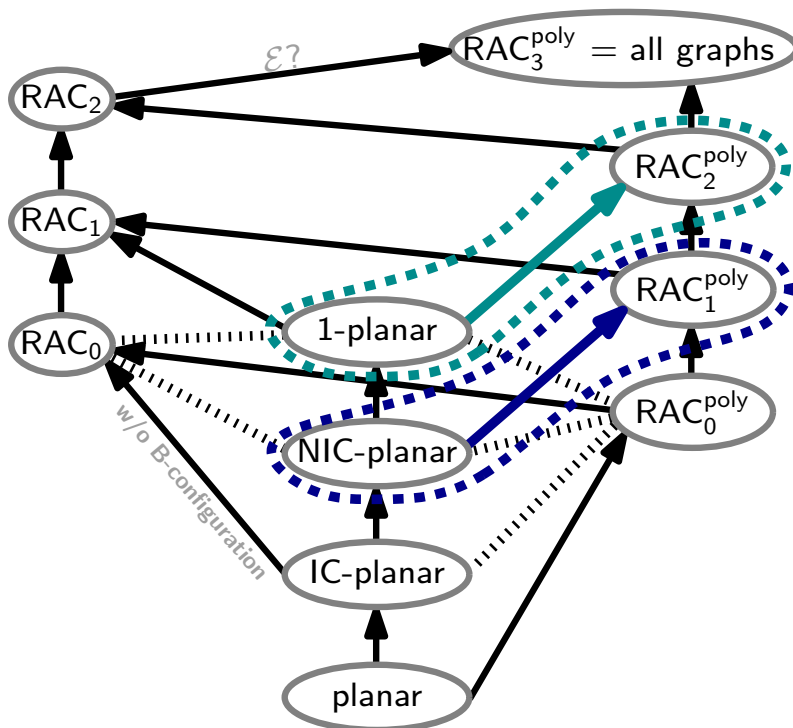
NIC-plane
 $\subseteq \text{RAC}_1^{\text{poly}}$

1-plane
 $\subseteq \text{RAC}_2^{\text{poly}}$

Preserves embedding

Yes

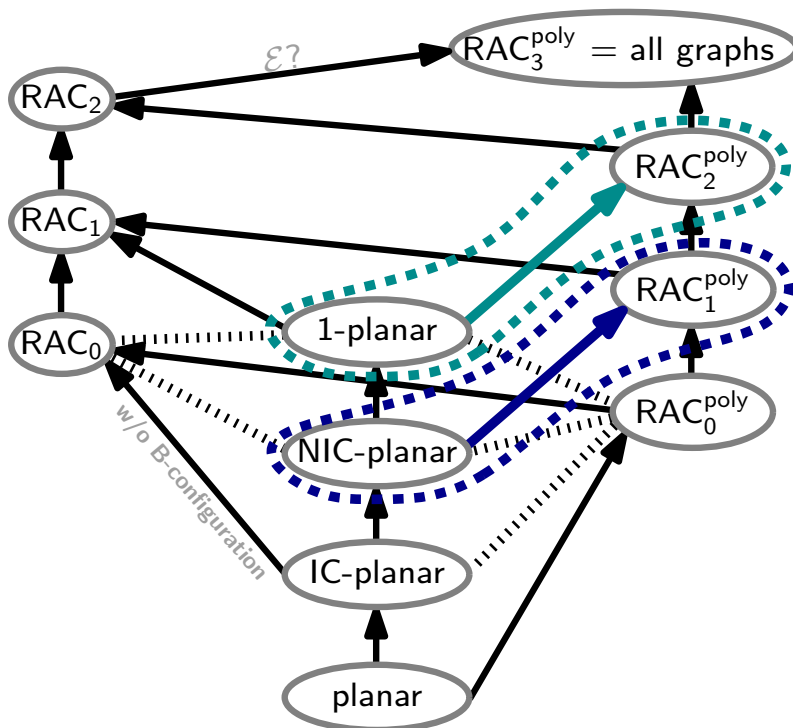
Yes



Summary and Open Questions

12

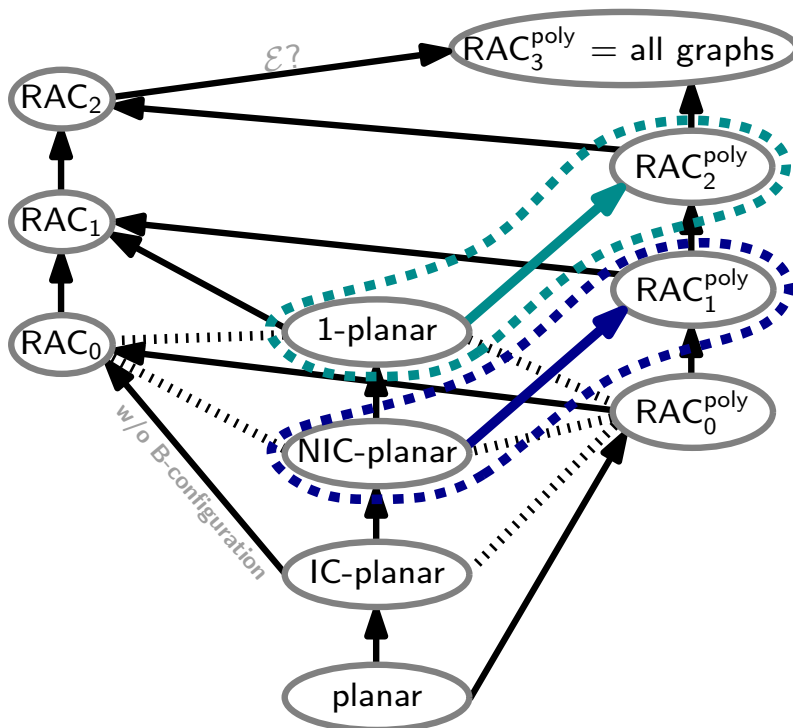
	NIC-plane $\subseteq \text{RAC}_1^{\text{poly}}$	1-plane $\subseteq \text{RAC}_2^{\text{poly}}$
Preserves embedding	Yes	Yes
Runtime	$O(n)$	$O(n)$



Summary and Open Questions

12

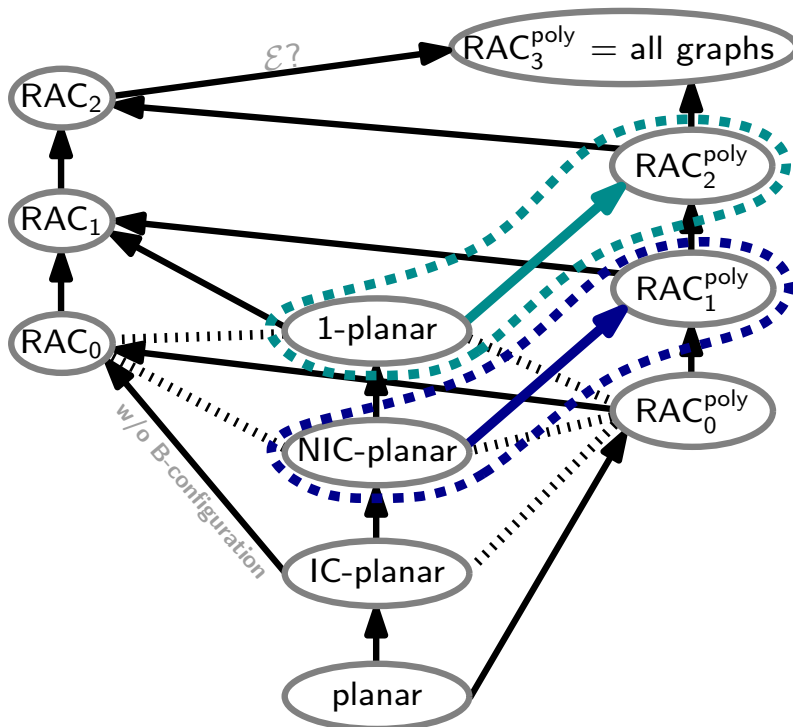
	NIC-plane $\subseteq \text{RAC}_1^{\text{poly}}$	1-plane $\subseteq \text{RAC}_2^{\text{poly}}$
Preserves embedding	Yes	Yes
Runtime	$O(n)$	$O(n)$
Bends per edge	≤ 1	≤ 2



Summary and Open Questions

12

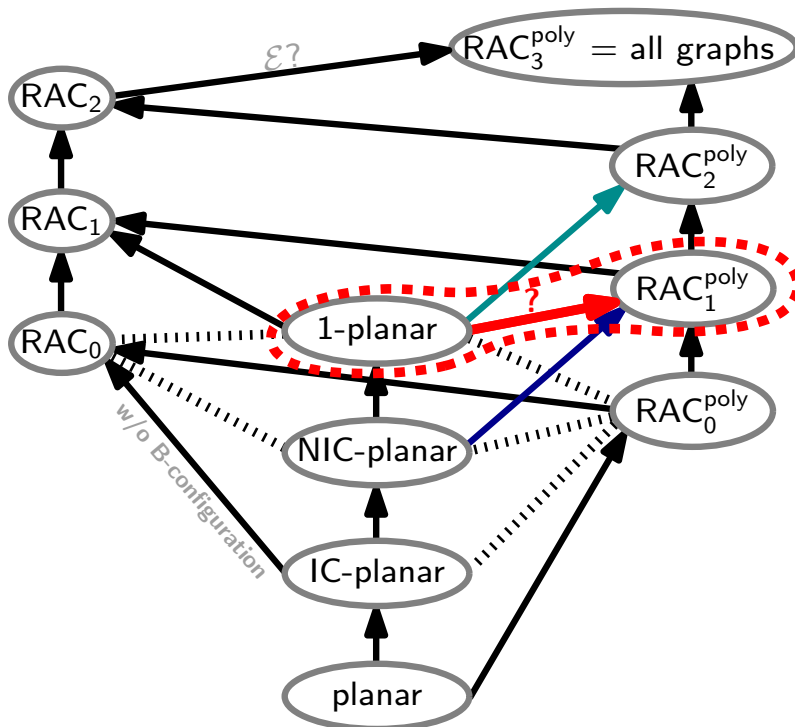
	NIC-plane $\subseteq \text{RAC}_1^{\text{poly}}$	1-plane $\subseteq \text{RAC}_2^{\text{poly}}$
Preserves embedding	Yes	Yes
Runtime	$O(n)$	$O(n)$
Bends per edge	≤ 1	≤ 2
Grid size	$O(n) \times O(n)$	$O(n^3) \times O(n^3)$



Summary and Open Questions

12

	NIC-plane $\subseteq \text{RAC}_1^{\text{poly}}$	1-plane $\subseteq \text{RAC}_2^{\text{poly}}$
Preserves embedding	Yes	Yes
Runtime	$O(n)$	$O(n)$
Bends per edge	≤ 1	≤ 2
Grid size	$O(n) \times O(n)$	$O(n^3) \times O(n^3)$

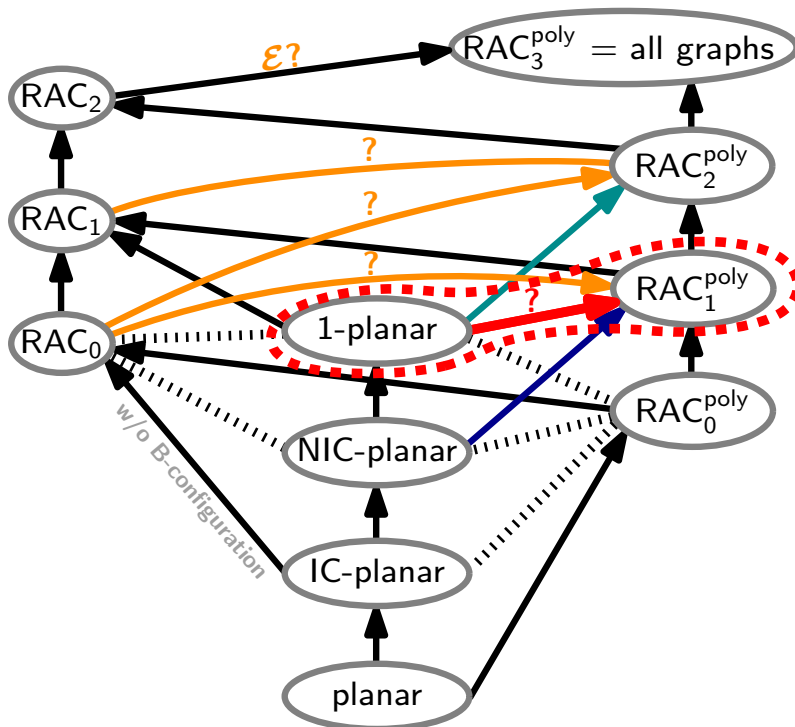


Open question:
1-planar $\subseteq \text{RAC}_1^{\text{poly}}$?

Summary and Open Questions

12

	NIC-plane $\subseteq \text{RAC}_1^{\text{poly}}$	1-plane $\subseteq \text{RAC}_2^{\text{poly}}$
Preserves embedding	Yes	Yes
Runtime	$O(n)$	$O(n)$
Bends per edge	≤ 1	≤ 2
Grid size	$O(n) \times O(n)$	$O(n^3) \times O(n^3)$



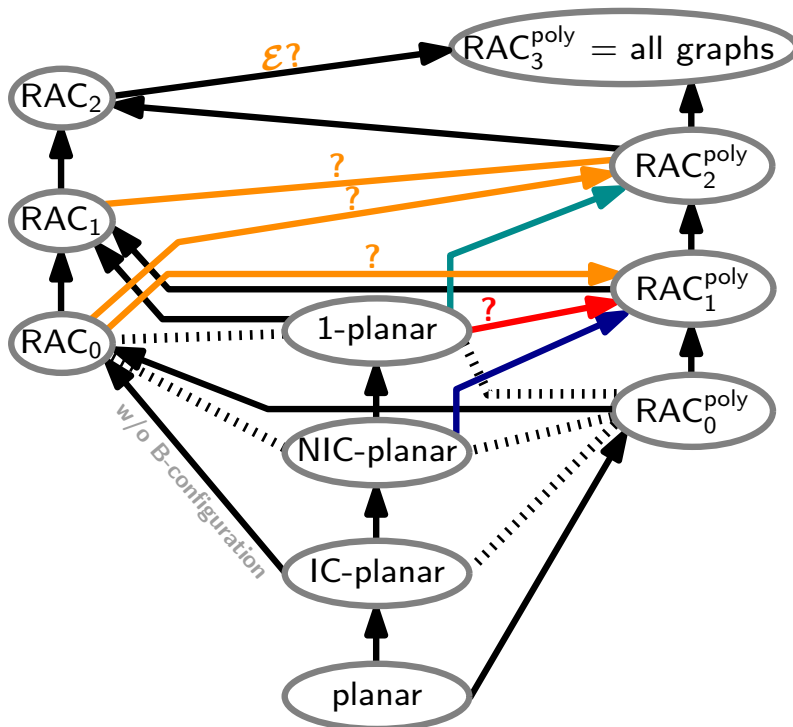
More open questions

Open question:
 $1\text{-planar} \subseteq \text{RAC}_1^{\text{poly}} ?$

Summary and Open Questions

12

	NIC-plane $\subseteq \text{RAC}_1^{\text{poly}}$	1-plane $\subseteq \text{RAC}_2^{\text{poly}}$
Preserves embedding	Yes	Yes
Runtime	$O(n)$	$O(n)$
Bends per edge	≤ 1	≤ 2
Grid size	$O(n) \times O(n)$	$O(n^3) \times O(n^3)$



More open questions

Open question:
 $1\text{-planar} \subseteq \text{RAC}_1^{\text{poly}} ?$