Korea University - Powered by Zigui

Team Note of Powered by Zigui

@evenharder(Sangheon Lee), @SoulTch(JEONGJIN LEE), @djkim0613(kim do jae)

Compiled on October 29, 2019

Co	ontents	Heavy-Light Decomposition				
0	Quotes and Prerequisites	2		4.8	Dominator Tree	9
	Math 1.1 Basic Mathematics 1.2 Number Theory 1.3 FFT 1.4 Miller-Rabin + Pollard-Rho Geometry 2.1 struct Point 2.2 Intersections 2.3 Projection, Reflection 2.4 Convex Hull 2.5 Rotating Calipers 2.6 Smallest Enclosing Circle 2.7 Polygon Area	2 2 3 4 4 5 5 5 5 6 6 6	5	Netw 5.1 5.2 5.3 5.4 5.5 Optin 6.1 6.2 6.3	Tree Compress vork Flow Theorems Dinic's Algorithm MCMF with SPFA Hungarian Method Hopcroft-Karp Algorithm mization Tricks Knuth Optimization Divide and Conquer Optimization Convex Hull Trick Centroid Decomposition	9 9 9 10 11 11 11 11 12
3	Strings 3.1 Aho-Corasick Algorithm 3.2 Suffix Array 3.3 Manacher's Algorithm 3.4 Manacher's Algorithm 3.5 Z Algorithm 3.6 Lexicographically Smallest String Rotation	6 6 7 7 7 8	7	7.1 7.2 7.3 7.4 7.5 7.6	Persistent Segment Tree	13 14 14 14 15
4	Graph Theory 4.1 Strongly Connected Component	8 8 8 8 8	8	8.1 8.2 8.3	cellaneous Misc Formulae and Algorithms	16 16

Korea University - Powered by Zigui
Page 2 of 17

ALL BELOW HERE ARE USELESS IF YOU READ THE STATEMENT WRONG

0 Quotes and Prerequisites

```
evenharder : Mental Abuse To Humans
djkim0613 : 열심히 응원하겠습니다.
SoulTch : How much is this bus ticket?
* This template is brought from that of 'Deobureo Minkyu Party'
```

Run script

```
#!/bin/bash
g++ -fsanitize=undefined -std=c++14 -02 -o /tmp/pow $1.cpp
time /tmp/pow < $1.in
# export PATH=~:$PATH</pre>
```

Debug Code

```
#define sz(x) ((int)(x).size())
#define rep(i, e) for (int i = 0, _##i = (e); i < _##i; i++)
#define repp(i, s, e) for (int i = (s), _##i = (e); i < _##i; i++)
#define repr(i, s, e) for (int i = (s)-1, _##i = (e); i \ge _{\#}i; i--)
#define repi(i, x) for (auto &i : (x))
// using namespace std;
using 11 = long long;
using pii = pair<int, int>;
using pll = pair<11, 11>;
template<typename T>
ostream &operator<<(ostream &os, const vector<T>& v) {
    cout << "[":
    for (auto p : v) cout << p << ",";</pre>
    cout << "]";
    return os:
}
#ifndef __SOULTCH
#define debug(...) 0
#define endl '\n'
#else
#define debug(...) cout << " [-] ", _dbg(#__VA_ARGS__, __VA_ARGS__)</pre>
template < class TH> void _dbg(const char *sdbg, TH h){ cout << sdbg << '=' << h <<
template<class TH, class... TA> void _dbg(const char *sdbg, TH h, TA... a) {
    while(*sdbg != ',') cout << *sdbg++;</pre>
    cout << '=' << (h) << ',';
    _dbg(sdbg+1, a...);
}
#endif
```

Reminders

Should be added.

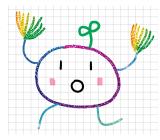


Figure 1: 풀다가 막힐 때는 이 그림을 봅시다. 아자아자 화이팅!

1 Math

1.1 Basic Mathematics

1.1.1 Trigonometry

- $\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$
- $\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$
- $\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$
- $\sin 2\theta = 2\sin\theta\cos\theta$
- $c^2 = a^2 + b^2 2ab\cos\gamma$

1.1.2 Generating Function

- $\sum_{n} (pn+q)x^{n} = \frac{p}{1-x} + \frac{q}{(1-x)^{2}}$ (Arithmetic progression)
- $\sum_{n} (rx)^n = (1 rx)^{-1}$ (Geometric progression)
- $\sum_{n} {m \choose n} x^n = (1+x)^m$ (Binomial coefficient)
- $\sum_{n} {m+n-1 \choose n} x^n = (1-x)^{-m}$ (Multiset coefficient)

1.1.3 Calculus

- $\int_a^b f(x) dx = \frac{b-a}{6} \left[f(a) + 4f(\frac{a+b}{2}) + f(b) \right]$ (Simpson's Rule)
- $\int u'v \ dx = uv \int uv' \ dx$ (Integration by parts)

1.1.4 Gaussian Elimination

Should be **added**....?

Korea University - Powered by Zigui
Page 3 of 17

1.2 Number Theory

1.2.1 Lattice Points under Line

for(ll j=0;j<m;j++) {</pre>

```
// 0 \le x \le n, 0 \le y \le (a/c)x+(b/c)
11 calc(l1 a,l1 b,l1 c,l1 n){
    if(!n)return 0;
    11 tmp=a/c*n*(n-1)/2;
    tmp+=b/c*n:
    return tmp+calc(c,(a*n+b)%c,a%c,((a%c)*n+b%c)/c);
}
1.2.2 Shanks' Baby-step Giant-step
  Should be revised.
11 mexp(ll x, ll y, ll p) {
    if(!v) return 1:
    if(v & 1) return x * mexp(x*x%p, y>>1, p) % p;
    return mexp(x*x\%p, y>>1, p);
}
vector<ll> get_factor(ll n) {
    vector<ll> v;
    for(ll i=2:i*i<=n:i++) {
        if(n \% i == 0) {
            v.push_back(i);
            while(n \% i == 0) n /= i:
        }
    }
    if(n > 1) v.push_back(n);
    return v:
}
ll get_primitive(ll n) {
    11 phi = n-1; // assume n is prime
    vector<ll> fact = get_factor(phi);
    for(11 x=2;x<=n;x++) {
        int ves = 1:
        for(ll y : fact) {
            yes &= (mexp(x, phi / y, n) != 1);
        if(yes) return x;
    }
    return -1;
// find x s.t. x^k \mod n = a \rightarrow (g^k)^y \mod n = a, where x = g^y
11 bsgs(ll k, ll a, ll n) {
    11 g = get_primitive(n);
    11 phi = n-1; // assume n is prime
    if(g == -1) return -1;
    ll m = ceil(sqrt(n) + 1e-9);
    vector<pl> prec(m);
```

```
prec[j] = {mexp(g, j * k % phi, n), j};
   }
   sort(prec.begin(), prec.end());
   ll cur = a, ncur = mexp(g, (phi - m) * k % phi, n);
   for(ll i=0:i<m:i++) {
        auto it = lower_bound(prec.begin(), prec.end(), pl(cur, 0));
        if(it->first == cur) {
            ll ans = mexp(g, (i*m + it->second) \% phi, n);
            assert(mexp(ans, k, n) == a);
            return ans:
        }
        cur = cur * ncur % n;
   }
   return 0;
}
1.2.3 Extended Euclidean Algorithm
// ax + by = gcd(a,b) \Rightarrow x ? y ?
typedef long long int 11
pair<11,11> ext_gcd(11 a,11 b) {
   if(b) {
        auto tmp = ext_gcd(b, a%b);
        return {tmp.second, tmp.first - (a/b) * tmp.second};
   }
    else return {1, 0};
// ax = 1 mod M, x?
ll mod inv(ll a, ll M) {
   return (ext_gcd(a, M).first + M) % M;
1.2.4 Chinese Remainder Theorem
typedef long long int 11;
11 CRT(vector<ll> rem. vector<ll> mod. int k) {
    11 m = 1:
   for(auto i : mod) m *= i;
   11 \text{ ret} = 0:
   for(int i = 0 ; i < k ; i++) {
        11 tmp = (m / mod[i]) % mod[i];
        11 si = mod inv(tmp, mod[i]):
        ret += (rem[i] * si % m) * (m / mod[i]) % m;
        ret %= m:
   }
    return ret;
x \equiv a \pmod{m}, x \equiv b \pmod{n}일 경우 해가 존재하려면 a \equiv b \pmod{\gcd(m,n)}이여야 함.
 q = \gcd(n, m) = um + vn이라 할 때 x \equiv (avn + bum)/q \pmod{lcm(n, m)}. Should be added.
```

Korea University - Powered by Zigui
Page 4 of 17

1.2.5 Möbius Inversion Formula

```
\forall n \in \mathbb{N} \ g(n) = \sum_{d \mid n} f(d) \implies f(n) = \sum_{d \mid n} \mu(d)g(n/d)
```

1.3 FFT

```
FFT: (a_0, a_1, \dots, a_{n-1}) \mapsto (\sum_{j=0}^{n-1} a_0(\omega^0)^j, \sum_{j=0}^{n-1} a_1(\omega^1)^j, \dots, \sum_{j=0}^{n-1} a_{n-1}(\omega^{n-1})^j)
void fft(vector<base>& a, bool inv) {
    int n = a.size(), i = 0:
    vector<ll> roots(n/2);
    for(int i=1:i<n:i++) {
        int bit = (n >> 1);
        while(j >= bit) {
             j -= bit;
             bit >>= 1;
        j += bit;
        if(i < j) swap(a[i], a[j]);</pre>
    }
    double ang = 2 * acos(-1) / n * (inv ? -1 : 1);
    for(int i=0:i<n/2:i++) {
        roots[i] = base(cos(ang * i), sin(ang * i));
    }
    /* In NTT, let prr = primitive root. Then,
    int ang = mexp(prr, (mod - 1) / n);
    if(inv) ang = mexp(ang, mod - 2);
    for(int i=0; i< n/2; i++){
        roots[i] = (i ? (111 * roots[i-1] * ang % mod) : 1);
    also, make sure to apply modulus under here
    for(int i=2;i<=n;i<<=1) {</pre>
        int step = n / i:
        for(int j=0;j<n;j+=i) {</pre>
             for(int k=0; k<i/2; k++) {
                 ll u = a[i+k], v = a[i+k+i/2] * roots[step * k]:
                 a[j+k] = u+v;
                 a[j+k+i/2] = u-v;
             }
        }
    }
    if(inv) for(int i=0;i<n;i++) a[i] /= n;</pre>
void conv(vector<base>& x, vector<base>& y) {
    int n = 2; while (n < max(x.size(), y.size())) n <<= 1;
    n <<= 1:
    x.resize(n); y.resize(n);
```

```
fft(x, false); fft(y, false);
   for(int i=0;i<n;i++) x[i] *= y[i];</pre>
   fft(x, true): // access (ll)round(x[i].real())
1.4 Miller-Rabin + Pollard-Rho
//Prove By Solving - https://www.acmicpc.net/problem/4149
namespace miller_rabin{
   lint mul(lint x, lint y, lint mod){ return (__int128) x * y % mod; }
 lint ipow(lint x, lint y, lint p){
   lint ret = 1, piv = x \% p:
   while(v){
     if(v&1) ret = mul(ret, piv, p);
     piv = mul(piv, piv, p);
     y >>= 1;
   return ret;
 bool miller_rabin(lint x, lint a){
   if(x % a == 0) return 0;
   lint d = x - 1;
   while(1){
     lint tmp = ipow(a, d, x);
     if(d&1) return (tmp != 1 && tmp != x-1);
     else if(tmp == x-1) return 0;
     d >>= 1;
   }
 }
 bool isprime(lint x){
   for(auto &i : {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}){
     if(x == i) return 1;
     if (x > 40 \&\& miller rabin(x, i)) return 0:
   if(x <= 40) return 0;
   return 1:
 }
namespace pollard_rho{
 lint f(lint x, lint n, lint c){
   return (c + miller_rabin::mul(x, x, n)) % n;
 void rec(lint n, vector<lint> &v){
   if(n == 1) return;
   if(n \% 2 == 0){
     v.push back(2):
     rec(n/2, v);
     return;
   }
   if(miller_rabin::isprime(n)){
```

Korea University - Powered by Zigui
Page 5 of 17

};

```
v.push_back(n);
      return:
    }
    lint a, b, c;
    while(1){
     a = rand() \% (n-2) + 2;
      b = a;
      c = rand() \% 20 + 1;
       a = f(a, n, c);
       b = f(f(b, n, c), n, c);
      }while(gcd(abs(a-b), n) == 1);
      if(a != b) break:
    lint x = gcd(abs(a-b), n);
    rec(x, v):
    rec(n/x, v);
  vector<lint> factorize(lint n){
    vector<lint> ret;
    rec(n. ret):
    sort(ret.begin(), ret.end());
    return ret;
 }
};
```

2 Geometry

2.1 struct Point

```
template <class T>
struct point{
   typedef point P;
   T x, y;
   point(T x=0, T y=0) : x(x), y(y) {}
   bool operator< (P a) const { return x != a.x ? x < a.x : y < a.y;}
    bool operator== (P a) const {return x == a.x and y == a.y;}
    P operator+ (P a) const {return P(x+a.x, y+a.y);}
   P operator- (P a) const {return P(x-a.x, y-a.y);}
   P operator- () const {return P(-x, -y);};
    T operator* (P a) const {return x*a.x + y*a.y;} // inner prod
    T operator/ (P a) const {return x*a.y - y*a.x;} // outer prod
   T dist2() const {return x*x + y*y;}
    double dist() const {return sqrt(double(dist2()));}
   P perp() const {return P(-y, x);}; // rotate 90 deg ccw
   P mult(T t) const {return P(x*t, v*t);}
   P unit() const {return P(x/dist(), y/dist());}
   P rotate(double a){
        return P(x*cos(a)-y*sin(a), x*sin(a)+y*cos(a));
    }
```

```
2.1.1 Sorting Points by Angle
// credit : http://koosaga.com/97
auto angle_sort = [&](const point &a, const point &b){
   if((a > point(0, 0)) ^ (b > point(0, 0))) return a > b;
   if(a / b != 0) return a / b > 0;
```

return a.dist() < b.dist(); // norm</pre>

2.2 Intersections

}: // clockwise sort

벡터 내적 외적 이용하면 생각보다 간단 / 선분은 예외처리가 좀 많음 Should be added.

- 2.2.1 Line-Line intersection
- 2.2.2 Line-Segment intersection
- 2.2.3 Segment-Segment Intersection
- 2.2.4 Circle-Line Intersection

2.3 Projection, Reflection

Should be added.

2.4 Convex Hull

```
vector<pll> get_CV(vector<pll> V){
    sort(V.begin(), V.end());
   sort(V.begin() + 1, V.end(), [&](pll x, pll y){
        pll xx = x - V[0];
        pll yy = y - V[0];
        11 \text{ res} = xx / vv:
        if(res != 0) return res > 0;
        if(xx.first != yy.first) return xx.first < yy.first;</pre>
        return xx.second < yy.second;</pre>
   });
   vector<pll> ret;
   for(auto val : V){
        while(ret.size() > 1){
            pll xx = ret[ret.size() - 2] - val;
            pll yy = ret[ret.size() - 1] - val;
            if(xx / yy <= 0) ret.pop_back();</pre>
            else break:
        ret.push_back(val);
   }
```

Korea University - Powered by Zigui
Page 6 of 17

```
return ret;
}
      Rotating Calipers
void rotating_calipers(vector<pll> CV){
    int pos = 0;
    for(int i = 0 ; i < CV.size() ; i++) if(CV[pos] < CV[i]) pos = i;</pre>
    int ind1 = 0, ind2 = pos;
    11 dist = (CV[ind1] - CV[ind2]) * (CV[ind1] - CV[ind2]);
    auto get_v = [\&](int x) { return CV[(x + 1) \% CV.size()] - <math>CV[x];};
    for(int i = 0 ; i < CV.size() ; i++){</pre>
        pll v = get_v(i);
        while((-v) / get_v(pos) < 0) pos = (pos + 1) % CV.size();
        11 tmp_dist = (CV[pos] - CV[i]) * (CV[pos] - CV[i]);
        if(dist < tmp_dist) {</pre>
            dist = tmp_dist;
            ind1 = i; ind2 = pos;
        }
    }
    printf("%lld %lld %lld %lld\n", CV[ind1].first, CV[ind1].second, CV[ind2].first,
    CV[ind2].second);
}
2.6 Smallest Enclosing Circle
//Prove By Solving - https://www.acmicpc.net/problem/11930
int main(){
    scanf("%d", &N);
    for(int i = 1; i \le N; i++) scanf("%lf%lf", &A[i].x, &A[i].y, &A[i].z);
    int t = 70000:
    double rate = 1.0;
    point cur = (point)\{0, 0, 0\};
    for(int i = 1 : i \le t: i++){}
        int ind = 1;
        for(int j = 1; j \le N; j++) if((A[j] - cur) * (A[j] - cur) > (A[ind] -
        cur) * (A[ind] - cur)) ind = j;
        cur = cur + (A[ind] - cur) * rate;
        rate *= 0.99:
    }
```

for(int i = 1; $i \le N$; i++) r = max(r, (A[i] - cur) * (A[i] - cur));

double r = 0:

}

cout << sqrt(r);
return 0;</pre>

2.7 Polygon Area

Should be **added**.

- 2.7.1 Polygon Area
- 2.7.2 Polygon Overlapping
- 3 Strings

3.1 Aho-Corasick Algorithm

```
namespace aho corasick {
   const int MAXN = 100000, MAXC = 26;
   int trans[MAXN+1][MAXC];
   int fail[MAXN+1];
   bool term[MAXN+1];
   void build(const vector<string> &v) {
        setz(trans), setz(fail), setz(term);
       int cnode = 1:
       repi(s, v) {
           int p = 0;
           repi(j, s) {
                char c = j-'a';
               if (!trans[p][c]) trans[p][c] = cnode++;
               p = trans[p][c];
           }
            term[p] = true;
       }
       queue<int> q; rep(i, MAXC) if (trans[0][i]) q.push(trans[0][i]);
        while(!q.empty()) {
           int t = q.front(); q.pop();
           rep(i, MAXC) {
               if (trans[t][i]) {
                    int p = fail[t];
                    while(p and not trans[p][i]) p = fail[p];
                   p = trans[p][i]:
                   fail[trans[t][i]] = p;
                   if (term[p]) term[trans[t][i]] = true;
                    q.push(trans[t][i]);
           }
       }
   bool query(string &t) {
       int p = 0;
       repi(i, t) {
            char c = i-'a';
```

Korea University - Powered by Zigui
Page 7 of 17

```
while(p and not trans[p][c]) p = fail[p];
            p = trans[p][c];
            if (term[p]) return true;
        }
        return false;
    }
}
      Suffix Array
// str : abracadabra
// SA : 10 7 0 3 5 8 1 4 6 9 2
// LCP : 1 4 1 1 0 3 0 0 0 2
vector<int> make_sa(const string& s) {
    int n = s.length();
    int \lim = \max(128, n+1):
    vector<int> sa(n), g(n+1), ng(n+1), cnt(lim), ind(lim+1);
    for(int i=0;i<n;i++) {</pre>
        sa[i] = i; g[i] = s[i];
    g[n] = 0;
    for(int t=1:t<s.length():t<<=1)</pre>
        auto cmp = [&] (int a, int b) {
            return g[a] != g[b] ? g[a] < g[b] : g[a+t] < g[b+t];
        for(int i=0;i<n;i++) cnt[g[min(i+t, n)]]++;</pre>
        for(int i=1;i<lim;i++) cnt[i] += cnt[i-1];</pre>
        for(int i=n-1; i>=0; i--) ind[--cnt[g[min(i+t, n)]]] = i;
        for(int i=0;i<lim;i++) cnt[i] = 0;</pre>
        for(int i=0; i < n; i++) cnt[g[i]]++; // same as cnt[g[ind[i]]]++
        for(int i=1;i<lim;i++) cnt[i] += cnt[i-1];</pre>
        for(int i=n-1:i>=0:i--) sa[--cnt[g[ind[i]]]] = ind[i]:
        ng[sa[0]] = 1;
        for(int i=1:i<n:i++) {</pre>
            ng[sa[i]] = ng[sa[i-1]] + cmp(sa[i-1], sa[i]);
        g = ng;
        fill(cnt.begin(), cnt.end(), 0);
        fill(ind.begin(), ind.end(), 0);
    }
    return sa;
}
vector<int> make lcp(const string& s. const vector<int>& sa) {
    int n = s.length();
    vector<int> lcp(n-1), rank(n);
    for(int i=0;i<n;i++)</pre>
        rank[sa[i]] = i;
```

```
int len = 0;
   for(int i=0;i<n;i++) {</pre>
       if(rank[i]) {
           int j = sa[rank[i]-1];
           int lc = n - max(i,i):
           while(len < lc && s[i+len] == s[j+len]) len++;</pre>
           lcp[rank[i]-1] = len;
        if(len) len--;
   }
    return lcp;
3.3 Manacher's Algorithm
//s = #h#e#l#l#o#
// ret = 0 1 0 1 0 1 2 1 0 1 0
vector<int> manacher(const string& s) {
    int n = s.size(), r = -1, k = -1;
    vector<int> p(n);
   for (int i=0; i<n; i++) {
       if (i<=r) p[i] = min(r-i, p[2*k-i]);</pre>
        while (i-p[i]-1>=0 and i+p[i]+1< n and s[i-p[i]-1] == s[i+p[i]+1]) p[i]++;
        if (r < i+p[i]) r = i+p[i], k = i;
   }
    return p;
3.4 Manacher's Algorithm
// 0-based
//s = #h#e#l#l#o#
// ret = 0 1 0 1 0 1 2 1 0 1 0
vector<int> manacher(const string& s) {
    int n = s.size(), r = -1, k = -1;
   vector<int> p(n):
   for (int i=0; i<n; i++) {
        if (i<=r) p[i] = min(r-i, p[2*k-i]);</pre>
        while (i-p[i]-1>=0 and i+p[i]+1< n and s[i-p[i]-1] == s[i+p[i]+1]) p[i]++;
        if (r < i+p[i]) r = i+p[i], k = i;
   }
   return p;
3.5 Z Algorithm
// 0-based
// s = a b c a b a b c a
```

Korea University - Powered by Zigui

Page 8 of 17

```
// ret = 9 0 0 2 0 4 0 0 1
vector<int> z_algo(const string &s) {
    int 1 = 0, r = 0, N = sz(s);
    vector<int> Z(N):
    Z[0] = N;
    repp(i, 1, N) {
       if (i > r) {
           1 = r = i;
            while(r < N and s[r] == s[r-1]) r++;
            Z[i] = r-1+1;
       } else {
            int k = i-1;
            if (Z[k] < r-i+1) Z[i] = Z[k];
            else {
               1 = i;
               while(r < N and s[r] == s[r-1]) r++;
               r--:
               Z[i] = r-1+1;
            }
       }
    }
    return Z;
}
```

3.6 Lexicographically Smallest String Rotation

```
// rotate(v.begin(), v.begin()+min_rotation(v), v.end());
int min_rotation(string s) {
   int a=0, N=sz(s); s += s;
   rep(b,0,N) rep(i,0,N) {
      if (a+i == b || s[a+i] < s[b+i]) {b += max(0, i-1); break;}
      if (s[a+i] > s[b+i]) { a = b; break; }
   }
   return a;
}
```

4 Graph Theory

4.1 Strongly Connected Component

```
vector<int> adj[MAX_V];
int finished[MAX];
int dfsn[MAX_V];
int cnt = 1;
vector<vector<int>> SCC;
stack<int> s;
int dfs(int cur) {
    dfsn[cur] = cnt++;
```

```
s.push(cur);
   int res = dfsn[cur];
   for (int n : adj[cur]) {
       if (!dfsn[n]) res = min(res, dfs(n));
       else if (!finished[n]) res = min(res, dfsn[n]);
   }
   if (res == dfsn[cur]) {
       vector<int> sub:
       int t = -1;
       do {
           t = s.top(); s.pop();
           finished[t] = 1;
           sub.push_back(t);
       } while (t != cur);
       SCC.push_back(sub);
   }
   return res;
4.2 2-SAT
 Should be added.
4.3 Biconnected Component
 Should be added.
4.4 Euler Tour
struct Edge{
   int to, cnt; // to: 인접한 정점, cnt: 남은 사용 횟수
   Edge *dual; // dual: 역방향 간선을 가리키는 포인터
   Edge(): Edge(-1, 0){}
   Edge(int to1, int cnt1): to(to1), cnt(cnt1), dual(nullptr){}
void Eulerian(int curr){
   for(Edge *e: adj[curr]){
       if(e->cnt > 0){
           e->cnt--:
           e->dual->cnt--;
           Eulerian(e->to); // dfs
   }
   cout << curr << '\n';
```

4.5 Offline Dynamic Connectivity

Should be added.

Korea University - Powered by Zigui
Page 9 of 17

4.6 Heavy-Light Decomposition

Should be added.

4.7 Dominator Tree

Should be added.

4.8 Negative Cycle Detection

Should be added.

4.9 Tree Compress

Should be added.

5 Network Flow

5.1 Theorems

Should be added.LR-flow and bunch of theories?

5.2 Dinic's Algorithm

```
const int INF = 1e9;
struct Dinic{
    int N;
    struct edge{
       int index, cap, rev;
       edge() : index(0), cap(0), rev(0) {}
        edge(int index, int cap, int rev) : index(index), cap(cap), rev(rev) {}
   };
    vector<vector<edge>> ADJ;
    vector<int> R, W;
   Dinic() {}
   Dinic(int N) : N(N){
        ADJ.resize(N); R.resize(N);
                                        W.resize(N):
   }
   void CE(int node1, int node2, int cap){
        ADJ[node1].push_back(edge(node2, cap, ADJ[node2].size()));
        ADJ[node2].push_back(edge(node1, 0, ADJ[node1].size() - 1));
   }
   bool bfs(int src, int sink){
       for(int i = 0; i < R.size(); i++) R[i] = -1;
       R[src] = 0;
       queue<int> Q; Q.push(src);
        while(Q.size()){
```

```
int here = Q.front(); Q.pop();
           for(auto e : ADJ[here]){
                if(e.cap > 0 \&\& R[e.index] == -1) R[e.index] = R[here] + 1,
                Q.push(e.index);
           }
       }
        return R[sink] != -1;
   }
   int dfs(int here, int sink, int f){
        if(here == sink) return f;
       for(int &i = W[here] ; i < ADJ[here].size() ; i++){</pre>
           auto &e = ADJ[here][i]:
           if(e.cap > 0 && R[here] < R[e.index]){</pre>
                int res = dfs(e.index, sink, min(f, e.cap));
                if(res) {
                    e.cap -= res;
                    ADJ[e.index][e.rev].cap += res;
                    return res;
               }
           }
        }
        return 0;
   }
   int solve(int src, int sink){
        int ret = 0:
        while(bfs(src, sink)){
           for(int i = 0 : i < N : i++) W[i] = 0:
            while((res = dfs(src, sink, INF))) ret += res;
       }
        return ret;
   }
};
5.3 MCMF with SPFA
const int INF = 1e9:
struct MCMF {
 struct EDGE {
   int there, cap, cost, rev;
   EDGE() : there(0), cap(0), cost(0), rev(0) {}
   EDGE(int there, int cap, int cost, int rev) : there(there), cap(cap),
   cost(cost), rev(rev) {}
 };
 int N;
 vector<vector<EDGE>> ADJ:
 vector<int> R, INQ, C, I;
```

Korea University - Powered by Zigui Page 10 of 17

```
MCMF(): N(0) {}
  MCMF(int N) : N(N) { ADJ.resize(N + 1); R.resize(N + 1); INQ.resize(N + 1);
  C.resize(N + 1); I.resize(N + 1); }
  void connect_edge(int i, int j, int cap, int cost) {
    ADJ[i].push_back(EDGE(j, cap, cost, ADJ[j].size()));
    ADJ[i].push_back(EDGE(i, 0, -cost, ADJ[i].size() - 1));
  bool SPFA(int src, int sink) {
    queue<int> Q; Q.push(src);
    fill(R.begin(), R.end(), -1); R[src] = 0;
   fill(C.begin(), C.end(), -1); C[src] = 0;
    fill(INQ.begin(), INQ.end(), 0); INQ[src] = 1;
    while (Q.size()) {
     int here = Q.front(); Q.pop();
      INQ[here] = 0;
     for (int i = 0; i < ADJ[here].size(); i++) {</pre>
       auto e = ADJ[here][i]:
       if (e.cap > 0 \&\& (C[e.there] == -1 || C[e.there] > C[here] + e.cost)) {}
          C[e.there] = C[here] + e.cost; R[e.there] = here; I[e.there] = i;
          if (!INQ[e.there]) INQ[e.there] = 1, Q.push(e.there);
       }
     }
    if (C[sink] == -1) return false:
    return true:
  }
  pii mcmf(int src, int sink) {
   pii ret = { 0, 0 };
    while (SPFA(src, sink)) {
      int flow = INF, cost = 0;
      for (int here = sink: here != src: here = R[here]) flow = min(flow.
      ADJ[R[here]][I[here]].cap):
      for (int here = sink; here != src; here = R[here]) {
       auto &e = ADJ[R[here]][I[here]];
       cost += e.cost * flow;
       e.cap -= flow;
       ADJ[e.there][e.rev].cap += flow:
      ret.first += flow, ret.second += cost;
    }
    return ret;
 }
};
5.4 Hungarian Method
```

```
namespace Hung {
   const int MX = 2000;
```

```
// IMPORTANT : n <= m, 1-based
using T = long double;
T \max v = 1e200:
T a[MX][MX], n, m:
void init(int nn, int mm) { n = nn; m = mm; }
void set_value(int x, int y, T val) { a[x][y] = val; }
T solve(vector <int> &ans) {
    vector<T> v(m+1), u(n+1):
    vector\langle int \rangle p (m+1), way (m+1);
    for (int i=1; i<=n; ++i) {
        \mathfrak{p}[0] = \mathfrak{i}:
        int j0 = 0;
        vector<T> minv (m+1, maxv);
        vector<char> used (m+1, false):
        do ſ
             used[j0] = true;
             T delta = maxv:
             int i0 = p[j0], j1;
             for (int j=1; j<=m; ++j) if (!used[j]) {</pre>
                 T cur = a[i0][j]-u[i0]-v[j];
                 if (cur < minv[j]) {</pre>
                     minv[j] = cur, way[j] = j0;
                 if (minv[i] < delta) {</pre>
                     delta = minv[i]. i1 = i:
                 }
            }
             for (int j=0; j<=m; ++j) {
                 if (used[i]) {
                     u[p[j]] += delta, v[j] -= delta;
                 }
                 else {
                     minv[j] -= delta;
                 }
            }
             i0 = i1;
        } while (p[j0] != 0);
        do {
             int j1 = way[j0];
             p[j0] = p[j1];
             j0 = j1;
        } while (i0);
    }
    ans.resize(n + 1);
    for(int j=1; j<=m;++j) {</pre>
        ans[p[j]] = j;
    return -v[0];
```

Korea University - Powered by Zigui
Page 11 of 17

```
.
```

5.5 Hopcroft-Karp Algorithm

```
struct hopcroft_karp{
    int N:
    vector<vector<int>> ADJ;
    vector<int> L, rev, used;
   hopcroft_karp() {}
   hopcroft_karp(int N) : N(N) {
       ADJ.resize(N);
       L.resize(N), rev.resize(N, -1), used.resize(N, 0);
   }
    void CE(int here, int there){
        ADJ[here].push_back(there);
   }
    void bfs(){
        queue<int> Q;
       for(int i = 0; i < N; i++) {
           if(used[i]) L[i] = -1;
            else L[i] = 0, Q.push(i);
       }
        while(Q.size()){
           int here = Q.front(); Q.pop();
           for(int there : ADJ[here]){
                if(rev[there] != -1 && L[rev[there]] == -1) {
                   L[rev[there]] = L[here] + 1;
                    Q.push(rev[there]);
               }
           }
       }
   }
    bool dfs(int here){
       for(int there : ADJ[here]){
            if(rev[there] == -1 || (L[here] < L[rev[there]] && dfs(rev[there]))){
               rev[there] = here;
                used[here] = 1;
               return true;
           }
       }
       return false:
   }
    int solve(){
       int ret = 0;
```

```
while(1){
    bfs();
    int res = 0;
    for(int i = 0 ; i < N ; i++) {
        if(used[i]) continue;
        res += dfs(i);
    }
    if(res == 0) break;
    ret += res;
    }
    return ret;
}</pre>
```

6 Optimization Tricks

6.1 Knuth Optimization

- Recurrence : $D[i][j] = \min_{i < k < j} (D[i][k] + D[k][j]) + C[i][j]$
- Quadrangle Inequality : $C[a][c] + C[b][d] \le C[a][d] + C[b][c], \ a \le b \le c \le d$
- Monotonicity : $C[b][c] \le C[a][d], \ a \le b \le c \le d$
- $A[i][j] = (\min k \text{ s.t. } D[i][j] \text{ is min.}).$ Then $A[i][j-1] \le A[i][j] \le A[i+1][j]$
- $O(N^2)$ time complexity

```
// opt[i-1][i] = i
for(int d=2;d<=n;d++) {
    for(int i=1;i+d<=n+1;i++) {
        for(int k=opt[i][j-1], j=i+d; k<=opt[i+1][j]; k++) {
            int v = dp[i][k] + dp[k][j] + c[i][j];
            if(dp[i][j] > v) dp[i][j] = v, opt[i][j] = k;
        }
    }
}
```

6.2 Divide and Conquer Optimization

- Recurrence : $D[t][i] = \min_{k < i} (D[t-1][k] + C[k][i])$
- Min index : $A[t][i] \le A[t][i+1]$ $(A[t][i] = (\min. k \ s.t. \ D[t][i] \ is \ min.))$ [-] Quadrangle Inequality : $C[a][c] + C[b][d] \le C[a][d] + C[b][c], \ a \le b \le c \le d$
- \bullet Able to Divide and Conquer base on calculating D[t][i]
- $O(TN \lg N)$ time complexity

Korea University - Powered by Zigui
Page 12 of 17

```
// range of index : [1,r]
// range of dp : [s,e]
void dnc(int t, int 1, int r, int s, int e)
{
    if(s > e) return;
    int m = (s+e)/2;
    D[t][m] = 2e9;
    for(int k=1;k<m&&k<=r;k++)
    {
        int tmp = D[t-1][k] + C[k][m];
        if(D[t][m] > tmp)
            D[t][m] = tmp, A[t][m] = k;
    }
    dnc(t, 1, A[t][m], s, D[t][m]-1);
    dnc(t, A[t][m], r, D[t][m]+1, e);
}
```

6.3 Convex Hull Trick

- Recurrence : $dp[i] = \min_{j < i} (dp[j] + a[i]b[j]), \ b[i-1] \le b[i]$
- Think as $dp[x = a[i]] = \min_{j < i} (b[j] \cdot x + dp[j])$
- Thus push lines and find minimum (by binary search)
- If $a[i] \le a[i+1]$ sweeping is possible
- Intersection of $y = a_i x + b_i$ and $y = a_{i+1} x + b_{i+1}$: $x = \frac{b_{i+1} b_i}{a_i a_{i+1}}$

6.4 Centroid Decomposition

```
// credit : https://gist.github.com/igorcarpanese/75162f3253bd230abd0f32f9950bf384
int dfs(int u, int p) {
    sub[u] = 1;
    for (auto v : tree[u])
        if (v != p) sub[u] += dfs(v, u);
    return sub[u] + 1;
}
int centroid(int u, int p, int r) { // r : root
    for (auto v : tree[u])
        if (v != p and sub[v] > sub[r]/2) return centroid(v, u);
    return u;
}
```

7 Data Structure

7.1 Persistent Segment Tree

```
const MAXN = 1e5 + 10;
struct node{
```

```
node *1, *r;
   int cnt;
   node () {}
} pool[(1 << 17) * 17], *tree_head[MAXN];</pre>
int tcnt;
node* alloc(){
   memset(pool + tcnt, 0, sizeof(node));
    return pool + tcnt++;
node * init(int 1, int r){
   node *ret = alloc();
   if(1 != r) {
        int mid = (1 + r) / 2;
        ret->l = init(l, mid);
        ret->r = init(mid + 1, r);
   }
    return ret;
void update(node * here, node *par, int 1, int r, int val){
   if(1 == r) {
        here->cnt = par->cnt + 1;
        return;
   }
    int mid = (1 + r) / 2;
    if(val <= mid){</pre>
        here->1 = alloc();
        here->r = par->r;
        update(here->1, par->1, 1, mid, val);
   }
   else {
        here > 1 = par > 1;
        here->r = alloc();
        update(here->r, par->r, mid + 1, r, val);
    here->cnt = here->l->cnt + here->r->cnt;
int query(node *node1, node *node2, int 1, int r, int k){
    if(1 == r) return 1:
    int ccc = node1->l->cnt - node2->l->cnt;
   int mid = (1 + r) / 2:
   if(k <= ccc) return query(node1->1, node2->1, 1, mid, k);
    else return query(node1->r, node2->r, mid + 1, r, k - ccc);
```

Korea University - Powered by Zigui
Page 13 of 17

7.2 Link-Cut Tree

```
struct node{
    node *pp, *p, *1, *r;
    int val;
    node(){p = 0, 1 = 0, r = 0;}
    node(int val) : val(val) \{ p = 0, 1 = 0, r = 0; \}
};
void push(node *x){}
void pull(node *x){}
void rotate(node *x){
  if(!x->p) return;
  push(x->p); // if there's lazy stuff
  push(x);
  node *p = x->p;
  bool is_left = (p->1 == x);
  node *b = (is_left ? x->r : x->1);
  x->p = p->p;
  if(x-p \&\& x-p->1 == p) x-p->1 = x;
  if(x->p \&\& x->p->r == p) x->p->r = x;
  if(is_left){
    if(b) b \rightarrow p = p;
    p->1 = b;
    p->p = x;
    x->r = p;
  else{
    if(b) b \rightarrow p = p;
   p->r = b;
   p->p = x;
    x->1 = p;
  pull(p); // if there's something to pull up
  pull(x);
  //if(!x->p) root = x; // IF YOU ARE SPLAY TREE
  if(p->pp){ // IF YOU ARE LINK CUT TREE
    x->pp = p->pp;
    p->pp = nullptr;
}
void splay(node *x){
  while(x->p){
    node *p = x->p;
    node *g = p->p;
    if(g){
      if((p\rightarrow l == x) ^ (g\rightarrow l == p)) rotate(x);
      else rotate(p);
    }
    rotate(x);
```

```
void access(node *x){
 splay(x);
 push(x):
 if(x->r){
   x->r->pp = x;
   x->r->p = nullptr;
   x->r = nullptr;
 pull(x);
 while(x->pp){
   node *nxt = x->pp;
   splay(nxt);
   push(nxt);
   if(nxt->r){
     nxt->r->pp = nxt;
     nxt->r->p = nullptr;
     nxt->r = nullptr;
   }
   nxt->r = x;
   x->p = nxt;
   x->pp = nullptr;
   pull(nxt);
   splay(x);
 }
node *root(node *x){
 access(x):
 while(x->1){
   push(x);
   x = x->1;
 access(x);
 return x;
node *par(node *x){
 access(x);
 if(!x->1) return nullptr;
 push(x):
 x = x \rightarrow 1;
 while(x->r){
   push(x);
   x = x->r;
 }
 access(x);
 return x;
node *lca(node *s, node *t){
 access(s);
```

Korea University - Powered by Zigui
Page 14 of 17

```
access(t);
 splay(s);
 if(s->pp == nullptr) return s;
 return s->pp;
void link(node *par, node *son){
 access(par);
 access(son):
 //son->rev ^= 1; // remove if needed
 push(son):
 son->1 = par;
 par->p = son;
 pull(son);
void cut(node *p){
 access(p);
 push(p);
 if(p->1){
   p->1->p = nullptr;
   p->l = nullptr;
 pull(p);
```

7.3 Li-Chao Tree

Should be added....?

7.4 Dynamic Convex Hull

```
// https://github.com/niklasb/contest-algos/blob/master/convex_hull/dynamic.cpp
const ll is_query = -(1LL<<62);</pre>
struct Line {
    11 m. b:
    mutable function<const Line*()> succ;
    bool operator<(const Line& rhs) const {</pre>
        if (rhs.b != is_query) return m < rhs.m;</pre>
        const Line* s = succ();
        if (!s) return 0:
        11 x = rhs.m;
        return b - s->b < (s->m - m) * x:
    }
};
struct HullDynamic : public multiset<Line> { // will maintain upper hull for maximum
    bool bad(iterator y) {
        auto z = next(y);
        if (v == begin()) {
            if (z == end()) return 0;
            return y->m == z->m && y->b <= z->b;
        }
        auto x = prev(y);
```

```
if (z == end()) return y > m == x - m && y - b <= x - b;
       return (x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m);
   }
   void insert_line(ll m, ll b) {
        auto v = insert({ m, b }):
       y->succ = [=] { return next(y) == end() ? 0 : &*next(y); };
        if (bad(y)) { erase(y); return; }
        while (next(y) != end() && bad(next(y))) erase(next(y));
        while (y != begin() && bad(prev(y))) erase(prev(y));
   }
   11 eval(ll x) {
        auto 1 = *lower_bound((Line) { x, is_query });
       return 1.m * x + 1.b:
   }
};
7.5 Stern-Brocot Tree
// __int128 is recommended
bool test(11 a, 11 b) { // for testing directions, vary by prob
   // return true if (true value) >= a/b
   11 n = 0, m = 1;
   rep(i, N) {
        if (n < m*A[i].fi) n = A[i].fi, m = 1;
       11 c = b*n+m*a, d = m*b;
       11 g = gcd(c, d);
       n = c/g;
       m = d/g;
       if (n > m*A[i].se) return false;
   }
   return true:
}
pair<11, 11> stern_brocot(11 M, 11 N) {
   // M : max value
   // N : max divisor
   // if result is a/b, return as {a, b}
   11 a = 0, b = 1; // 1
   11 c = 1, d = 0; // r
    int 1. r:
   bool chg = true;
    while(chg) {
        chg = false:
        // to left
       1 = 0, r = (N-d-1)/b+1:
        while(1 < r)  {
```

Korea University - Powered by Zigui
Page 15 of 17

```
int mid = (1+r+1)/2;
        if (test(a*mid+c, b*mid+d)) r = mid-1;
        else 1 = mid:
   c += a*1;
   d += b*1;
   chg |= (1 > 0);
   // to right
   1 = 0, r = (d?(N-b-1)/d+1:M);
   while(1 < r) {
       int mid = (1+r+1)/2;
       if (test(a+mid*c, b+mid*d)) l = mid;
        else r = mid-1;
   }
   a += c*1;
   b += d*l:
   chg |= (1 > 0);
return {a, b};
```

7.6 Rope

}

Should be added.

7.7 Policy Based Data Structure

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
using namespace std;
using namespace __gnu_pbds;
typedef tree<
int,
null_type,
less<int>,
rb_tree_tag,
tree_order_statistics_node_update >
ordered_set;
// less<int> : not allow for duplicate
// less_equal<int> : allow for duplicate
// use upper_bound when you erase from set used less_equal
```

```
int N;
int main(void) {
    iostream::sync_with_stdio(false);
    cin.tie(nullptr);
    ordered_set X;
   X.insert(1);
   X.insert(2);
   X.insert(4);
   X.insert(8);
   X.insert(16);
    cout<<*X.find_by_order(1)<<endl; // 2</pre>
    cout<<*X.find_by_order(2)<<endl; // 4</pre>
    cout<<*X.find_by_order(4)<<endl; // 16</pre>
    cout<<(end(X)==X.find_by_order(6))<<endl; // true</pre>
    cout<<X.order_of_key(-5)<<endl; // 0</pre>
    cout<<X.order_of_key(1)<<endl; // 0</pre>
    cout<<X.order_of_key(3)<<endl; // 2</pre>
    cout<<X.order_of_key(4)<<endl; // 2</pre>
    cout<<X.order_of_key(400)<<endl; // 5</pre>
```

8 Miscellaneous

8.1 Misc Formulae and Algorithms

8.1.1 Faulhaber's Formula

$$T(n,k) = \sum_{i=1}^{n} i^{k} = \frac{(n+1)^{k+1} - 1^{k+1} - \sum_{j=0}^{k-1} {k+1 \choose j} T(n,j)}{{k+1 \choose k}}$$

Also use

$$(x+1)^d - x^d = 1 + {d \choose 1}x + {d \choose 2}x^2 + \dots + {d \choose d-1}x^{d-1}$$

to get each coef.

8.1.2 Maximum Clique

Should be added....?

8.1.3 De Brujin Sequence

Should be added....?

Korea University - Powered by Zigui Page 16 of 17

8.2 Highly Composite Numbers, Large Prime

< 10	`k number	divisors	2 3 5 71113171923293137
1	6	4	1 1
2	60	12	2 1 1
3	840	32	3 1 1 1
4	7560	64	3 3 1 1
5	83160	128	3 3 1 1 1
6	720720	240	4 2 1 1 1 1
7	8648640	448	6 3 1 1 1 1
8	73513440	768	5 3 1 1 1 1 1
9	735134400	1344	6 3 2 1 1 1 1
10	6983776800	2304	5 3 2 1 1 1 1 1
11	97772875200	4032	6 3 2 2 1 1 1 1
12	963761198400	6720	6 4 2 1 1 1 1 1 1
13	9316358251200	10752	6 3 2 1 1 1 1 1 1 1
14	97821761637600	17280	5 4 2 2 1 1 1 1 1 1
15	866421317361600	26880	6 4 2 1 1 1 1 1 1 1 1
16	8086598962041600	41472	8 3 2 2 1 1 1 1 1 1 1
17	74801040398884800	64512	6 3 2 2 1 1 1 1 1 1 1 1
18	397612484786617600	103680	8 4 2 2 1 1 1 1 1 1 1 1
	_		

< 10^]	k prime	# of prime	< 10^	k prime
1	7	4	10	999999967
2	97	25	11	9999999977
3	997	168	12	99999999999
4	9973	1229	13	999999999971
5	99991	9592	14	9999999999973
6	999983	78498	15	99999999999989
7	9999991	664579	16	99999999999937
8	99999989	5761455	17	999999999999997
9	99999937	50847534	18	9999999999999999

NTT Prime:

```
\begin{array}{l} 469762049=7\times 2^{26}+1. \ {\rm Primitive\ root}:3.\\ 998244353=119\times 2^{23}+1. \ {\rm Primitive\ root}:3.\\ 985661441=235\times 2^{22}+1. \ {\rm Primitive\ root}:3.\\ 1012924417=483\times 2^{21}+1. \ {\rm Primitive\ root}:5. \end{array}
```

8.3 Fast Integer IO

```
// credit : https://github.com/koosaga/DeobureoMinkyuParty/blob/master/teamnote.tex
static char buf[1 << 19]; // size : any number geq than 1024
static int idx = 0;
static int bytes = 0;
static inline int _read() {
  if (!bytes || idx == bytes) {
    bytes = (int)fread(buf, sizeof(buf[0]), sizeof(buf), stdin);
    idx = 0;</pre>
```

```
return buf[idx++];
static inline int _readInt() {
 int x = 0, s = 1:
 int c = _read();
 while (c \leq 32) c = _read();
 if (c == '-') s = -1, c = read():
 while (c > 32) x = 10 * x + (c - '0'), c = _read();
 if (s < 0) x = -x:
 return x;
8.4 C++ Tips / Environments
 Should be revised.(with random, chrono)
#include <bits/stdc++.h> // magic header
using namespace std; // magic namespace
struct StupidGCCCantEvenCompileThisSimpleCode{
 pair<int, int> array[1000000];
}; // https://gcc.gnu.org/bugzilla/show_bug.cgi?id=68203
// how to use rand (in 2017)
mt19937 rng(Oxdeadbeef):
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
int randint(int lb, int ub){ return uniform_int_distribution<int>(lb, ub)(rng); }
shuffle(permutation.begin(), permutation.end(), rng);
mt19937_64 _R(chrono::steady_clock::now().time_since_epoch().count()); // _R()
// comparator overload
auto cmp = [](seg a, seg b){return a.func() < b.func(); };</pre>
set<seg. decltvpe(cmp)> s(cmp):
map<seg, int, decltype(cmp)> mp(cmp);
priority_queue<seg, vector<seg>, decltype(cmp)> pq(cmp); // max heap
// hash func overload
struct point{
int x, y;
bool operator==(const point &p)const{ return x == p.x && y == p.y; }
struct hasher {
size_t operator()(const point &p)const{ return p.x * 2 + p.y * 3; }
unordered_map<point, int, hasher> hsh;
// c++ setprecision example
#include <iostream>
                       // std::cout, std::fixed
#include <iomanip>
                       // std::setprecision
```

Korea University - Powered by Zigui
Page 17 of 17

```
int main () {
   double f =3.14159;
   std::cout << std::setprecision(5) << f << '\n'; // 3.1416
   std::cout << std::setprecision(9) << f << '\n'; // 3.14159
   std::cout << std::fixed;
   std::cout << std::setprecision(5) << f << '\n'; // 3.14159
   std::cout << std::setprecision(9) << f << '\n'; // 3.141590000
   return 0;
}</pre>
```