

Data Exploration and Networks

Topics covered so far



- 1. Data Exploration and Visualization
 - a. Hypothesis Testing
 - b. PCA
 - c. t-SNE
- 2. Graphs & Networks
 - a. Adjacency matrix
 - b. Connected components
 - c. Centrality measures

Discussion questions



- 1. What are multiple testing issues and why do they occur?
- 2. Why do we need to do dimensionality reduction?
- 3. How is PCA different from t-SNE algorithm?

Multiple testing issue and their corrections



Multiple testing problem

- This problem arises when multiple hypothesis are tested simultaneously.
- The number of false positives increases as you test more number of hypotheses

Following are the correction methods that can be used to deal with this problem:

- Bonferroni correction
 - o It states that the corrected significance level for all the test combined is α/m . where m is the total number of hypothesis tests performed
 - Reject null hypothesis H0 when p-value $\leq \alpha/m$ or m*p-value $\leq \alpha$
- Holm-Bonferroni correction
 - Sort p-values in increasing order: $p(1) \le \cdots \le p(m)$, The corrected significance level for the ith test is a/(m-i-1).
 - Reject null hypothesis H0 $p(i) \le \alpha/(m-i-1)$ or $(m-i+1)*p(i) \le \alpha$
- Benjamini-Hochberg correction:
 - Sort p-values in increasing order: $p(1) \le \cdots \le p(m)$, The corrected significance level for the ith test is $\alpha^*i/(m)$.
 - Reject null hypothesis H0 p(i) $\leq \alpha^*i/(m)$ or m*p(i)/i $\leq \alpha$





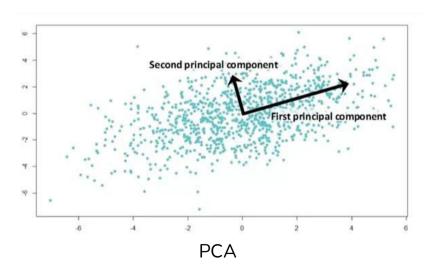
- Dimensionality reduction is the process to reduce the number of dimensions in the feature space.
- In the machine learning, we tend to add many features to get more accurate results. However, after a certain point the performance and robustness of the model starts decreasing and computational complexity starts increasing as we increase the number of features. This is called curse of dimensionality where the sample density decrease exponentially with the increase of dimensionality.
 - We use dimensionality reduction to transform the data into low dimensions while keeping most of the information intact.
 - It also helps us to visualize the high dimensional data to 2D & 3D.
- There are the following techniques we can use for dimensionality reduction:
 - o PCA
 - t-SNE

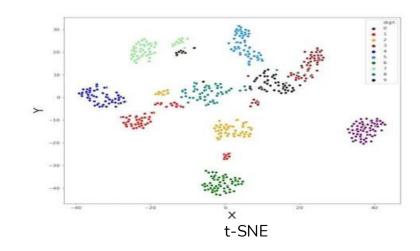
PCA and t-SNE



Principal component analysis (PCA) is a dimensionality reduction technique used for identification of a smaller number of uncorrelated variables known as principal components from a larger dataset. The technique is widely used to emphasize variation and capture strong patterns in a dataset.

t-Distributed Stochastic Neighbor Embedding (t-SNE) is a technique for dimensionality reduction that is particularly well suited for the visualization of high-dimensional datasets.









PCA	t-SNE
It tries to capture linear structure in the data.	It tries to capture non-linear structure in the data.
It focuses to preserve the global structure of the data	It focuses to preserve the local structure (i.e. clusters) of the data
There are no hyperparameters involved in PCA	There are some hyperparameters like perplexity, no. of dimensions etc. in t-SNE
PCA works by separating points as far as possible based on the highest variance	t-SNE works by grouping points as close as possible based on the characteristics of the point
It might easily get affected by outliers	It can handle outliers as well



Case Study - PCA & t-SNE

Discussion questions



- 1. Why do we study Graphs & Networks?
- 2. What is an adjacency matrix and How do we interpret it?
- 3. What do you mean by degree and How do we calculate it in a network?
- 4. What are the different types of centrality measures in a network?
- 5. Give a real life example of a network and what are the centrality measures in that network?





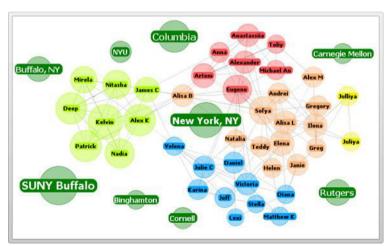
Graph is basically the study of relationships. It has certain nodes (vertices) and links (edges) that creates these relationships.

It can be used to model create many types of relations and processes in physical, social, biological and information system, and has a wide range of applications:

- Community networks (through social media)
- Google maps
- DNA/RNA sequencing
- Search engine rankings

Example: This friendship network shows us a bunch of friends, the networks they belong to, and the social cliques they are part of.



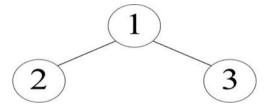


Adjacency matrix



We can represent the graph as an adjacency matrix, where the row and column indices represent the nodes, and the entries in the matrix represent the absence or presence of an edge between the nodes.

Example: For a graph 2-1-3, the adjacency matrix will be- $\begin{bmatrix} 0,1,1\\1,0,0\\1,0,0 \end{bmatrix}$



Adjacency matrix is the best representation of a graph into a mathematical form that tells us whether there are any edges between all sets of nodes. The diagonal of this matrix will always be zero if there are no self loops in the network.

Degree and its calculation



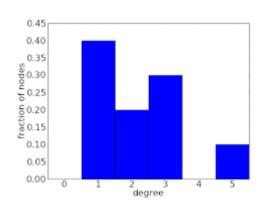
The degree of a node refers to the number of edges that are connected to it. In a directed graph, you can calculate the in-degree and out-degree which means incoming and outgoing connections of a node.

In simple words, it is a popularity measure. The higher the degree, more central the node is.

We can calculate the average degree of a network by using the formula 2m/n, where m is the number of edges and n is the number of nodes.

Degree distribution: It is a probability that the random chosen node has k number of connections.

Here in this graph you can how the degree is varying with the fraction of nodes.



Centrality measures



Centrality measures capture the importance of a node's position in a network. There are the following types of centrality measures:

- 1. Degree centrality: It is a measure of popularity of a node in a network. It does not capture the quality vs quantity.
- 2. Propagated degree (eigenvector) centrality: It measures the importance of a node in a graph with respect to the importance of its neighbors. If a node is connected to highly important nodes, it will have a higher score as compared to a node which is connected to less important nodes.
- 3. Closeness centrality: It tracks how close a node is to another by measuring the distance between them. In other words, it measures the node efficiency in terms of connection to other nodes.
- **4. Betweenness centrality:** It measures the importance of a node in a network based upon how many times it occurs in the shortest path between all pairs of nodes in a graph. Basically, It measures the extent to which a node lies on paths between other nodes.

Real life example of a network and its centrality measures



In a social network

- High degree centrality most popular person who can quickly connect with the wider network
- High eigenvector centrality most popular person who has good social network with other popular person
- High closeness centrality person who can influence the whole network most quickly
- High betweenness centrality person who influence the flow around the network i.e. removal of those person can break the network



Case Study - Caviar



Happy Learning!

