

# HW 8

## A

Compute the closure of the following set F of functional dependencies for relation schema R=(A,B,C,D,E)

$$A \rightarrow BC \quad CD \rightarrow E \quad B \rightarrow D \quad E \rightarrow A$$

List the candidate keys for R. (2 points)

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### Answer:

the candidate keys for R is **A, E, CD, BC**

## B

Using the functional dependencies of Question A, compute the canonical cover  $F_c$ .

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### Answer:

$F_c$  equals to  $F$ , so  $F_c = \{A \rightarrow BC, \quad CD \rightarrow E, \quad B \rightarrow D, \quad E \rightarrow A\}$

## C

Suppose that we decompose the schema R=(A,B,C,D,E) into

$$(A, B, C) \text{ and } (A, D, E)$$

Show that this decomposition is a lossless-join decomposition if the following set F of functional dependencies holds:(1 point)

$$A \rightarrow BC \quad CD \rightarrow E \quad B \rightarrow D \quad E \rightarrow A$$

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### Answer:

combine  $A \rightarrow BC$  and  $B \rightarrow D$  as  $A \rightarrow CD$

combine  $A \rightarrow CD$  and  $CD \rightarrow E$  as  $A \rightarrow E$

decompose  $A \rightarrow CD$  into  $A \rightarrow C$  and  $A \rightarrow D$

combine  $A \rightarrow CD$  and  $CD \rightarrow E$  as  $A \rightarrow E$

combine  $A \rightarrow BC$  and  $A \rightarrow C$  as  $A \rightarrow BC$

dependency  $A \rightarrow BC$  can be verified in tabel  $(A, B, C)$

dependency  $A \rightarrow DE$  can be verified in tabel  $(A, B, C)$

dependency  $E \rightarrow A$  can be verified in tabel  $(A, B, C)$

so the decomposition of R  $(A, B, C)$  and  $(A, D, E)$  is a lossless-join decomposition.