<u>3.1</u>

#	Algorithm	Running time	Best Case	Worst Case
1	Bubble Sort (Non-Recursive)	O(n ²)	O(n) when array is sorted	O(n²)
2	Bubble Sort (Recursive)	O(n ²)	O(n) when array is sorted	O(n²)
3	Selection Sort (Non-Recursive)	O(n²)	O(n²)	O(n ²⁾
4	Insertion Sort (Non-Recursive)	O(n ²)	O(n) when array is sorted	O(n²)
5	Merge Sort (Recursive)	O(n·log(n))	O(n·log(n))	O(n·log(n))

3.2

Bubble Sort

,	77	00	20	20	50	77	20	40	٥	
4	77	98	30	20	50	77	22	49	2	
i= 0, j < 9. After 1st pass:										
4	77	30	20	50	77	22	49	2	98	
i = 1, j < 8. After 2nd pass:										
4	30	20	50	77	22	49	2	77	98	
i = 2, j < 7	i = 2, j < 7. After 3rd pass:									
4	20	30	50	22	49	2	77	77	98	
i = 3, j < 6	6. After 4th	n pass:								
4	20	30	22	49	2	50	77	77	98	
i = 4, j < 5	5. After 5th	n pass:								
4	20	22	30	2	49	50	77	77	98	
i = 5, j < 4	4. After 6th	n pass:								
4	20	22	2	30	49	50	77	77	98	
i = 6, j < 3	3. After 7th	n pass:								
4	20	2	22	30	49	50	77	77	98	
i = 7, j < 2. After 8th pass:										
4	2	20	22	30	49	50	77	77	98	
i = 8, j <1. After 9th pass:										
2	4	20	22	30	49	50	77	77	98	
i = 9 > length -1, return.										

Bubble Sort Recursive Stack Trace: bubbleSort(int[] arr, int end)

 $arr = \{4, 77, 98, 30, 20, 50, 77, 22, 49, 2\}, end = arr.length -1 = 9$



Top of Stack

Return: arr = {2, 4, 20, 22, 30, 49, 50, 77, 77, 98}

Selection Sort:

Select the smallest in the array and swap it with i th element in the front:

• black-boxed: to-be-swapped

• green-boxed: min in the "non-swapped" part
Swap black-boxed with green-boxed:

4	77	98	30	20	50	77	22	49	2	
i = 0, min = 9, swap arr[0], arr[9]										
2	77	98	30	20	50	77	22	49	4	
i = 1, min	= 9, swap	arr[1], arr	[9]							
2	4	98	30	20	50	77	22	49	77	
i = 2, min	i = 2, min = 4, swqp arr[2], arr[4]									
2	4	20	30	98	50	77	22	49	77	
i = 3, min	= 7, swap	arr[3], arr	[7]		•					
2	4	20	22	98	50	77	30	49	77	
i = 4, min	= 7, swap	arr[4], arr	[7]							
2	4	20	22	30	50	77	98	49	77	
i = 5, min	= 8, swap	arr[5], arr	[8]							
2	4	20	22	30	49	77	98	50	77	
i = 6, min	= 8, swap	arr[6], arr	[8]							
2	4	20	22	30	49	50	98	77	77	
i = 7, min = 8, swap arr[7], arr[8]										
2	4	20	22	30	49	50	77	98	77	
i = 8, min = 9, swap arr[8], arr[9]										
2	4	20	22	30	49	50	77	77	98	
i = 9 !< le	i = 9!< length -1, return.									

Insertion Sort:

Look at following element and decide its place on the "sorted part" based on its value. Right shifting is important.

• orange-boxed: sorted part

• blue-boxed: unsorted part

• text-in-blue-and-bold: the following term to be placed in the sorted part.

4 77 98 30 20 50 77 22 49 2 i = 2 = j, look at arr[2], 98 >= 77 so it is placed after 77. 4 77 98 30 20 50 77 22 49 2 i = 3 = j, look at arr[3], 30 < 98; 30<77; 30 >= 4 so it is placed after 4. 4 30 77 98 20 50 77 22 49 2 i = 4 = j, look at arr[4], 20 < 98; 20 < 77; 20 < 30; 20 >= 4 so it is placed after 4. 4 20 30 77 98 50 77 22 49 2 i = 5 = j, look at arr[5], 50 < 98; 50 < 77; 50 >= 30 so it is placed after 30. 4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 >= 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 49 2										
4 77 98 30 20 50 77 22 49 2 i = 2 = j, look at arr[2], 98 >= 77 so it is placed after 77. 4 77 98 30 20 50 77 22 49 2 i = 3 = j, look at arr[3], 30 < 98; 30	4	77	98	30	20	50	77	22	49	2
i = 2 = j, look at arr[2], 98 >= 77 so it is placed after 77. 4	i = 1 = j, look at arr[1], 77 >= 4 so it is placed after 4.									
4 77 98 30 20 50 77 22 49 2 i = 3 = j, look at arr[3], 30 < 98; 30<77; 30 >= 4 so it is placed after 4. 4 30 77 98 20 50 77 22 49 2 i = 4 = j, look at arr[4], 20 < 98; 20 < 77; 20 < 30; 20 >= 4 so it is placed after 4. 4 20 30 77 98 50 77 22 49 2 i = 5 = j, look at arr[5], 50 < 98; 50 < 77; 50 >= 30 so it is placed after 30. 4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 >= 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	77	98	30	20	50	77	22	49	2
i = 3 = j, look at arr[3], 30 < 98; 30<77; 30 >=4 so it is placed after 4. 4 30 77 98 20 50 77 22 49 2 i = 4 = j, look at arr[4], 20 < 98; 20 < 77; 20 < 30; 20 >= 4 so it is placed after 4. 4 20 30 77 98 50 77 22 49 2 i = 5 = j, look at arr[5], 50 < 98; 50 < 77; 50 >= 30 so it is placed after 30. 4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 >= 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	i = 2 = j, l	ook at arr[[2], 98 >= [77 so it is	placed afte	er 77.				
4 30 77 98 20 50 77 22 49 2 i = 4 = j, look at arr[4], 20 < 98; 20 < 77; 20 < 30; 20 >= 4 so it is placed after 4. 4 20 30 77 98 50 77 22 49 2 i = 5 = j, look at arr[5], 50 < 98; 50 < 77; 50 >= 30 so it is placed after 30. 4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 >= 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	77	98	30	20	50	77	22	49	2
i = 4 = j, look at arr[4], $20 < 98$; $20 < 77$; $20 < 30$; $20 >= 4$ so it is placed after 4. 4 20 30 77 98 50 77 22 49 2 i = 5 = j, look at arr[5], $50 < 98$; $50 < 77$; $50 >= 30$ so it is placed after 30. 4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], $77 < 98$; $77 >= 77$ so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], $22 < 98$; $22 < 77$; $22 < 77$; $22 < 50$; $22 < 30$; $22 >= 20$, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], $49 < 98$; $49 < 77$ 77 50 ; $49 >= 30$ so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], $2 < 98$ 77 77 50 49 30 22 20 4 , it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	i = 3 = j, l	ook at arr[[3], 30 < 98	3; 30<77; 3	30 >=4 so	it is place	d after 4.			
4 20 30 77 98 50 77 22 49 2 i = 5 = j, look at arr[5], 50 < 98; 50 < 77; 50 >= 30 so it is placed after 30. 4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 >= 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	30	77	98	20	50	77	22	49	2
i = 5 = j, look at arr[5], 50 < 98; 50 < 77; 50 >= 30 so it is placed after 30. 4	i = 4 = j, l	ook at arr[[4], 20 < 98	3; 20 < 77;	20 < 30; 2	20 >= 4 sc	it is place	ed after 4.		
4 20 30 50 77 98 77 22 49 2 i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 > = 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	20	30	77	98	50	77	22	49	2
i = 6 = j, look at arr[6], 77 < 98; 77 >= 77 so it is placed after 77. 4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22 >= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 > = 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	i = 5 = j, l	ook at arr[[5], 50 < 98	3; 50 < 77;	50 >= 30	so it is pla	ced after	30.		
4 20 30 50 77 77 98 22 49 2 i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22>= 20, placed after 20. 4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 > = 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	20	30	50	77	98	77	22	49	2
i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22>= 20, placed after 20. 4	i = 6 = j, l	ook at arr[[6], 77 < 98	3; 77 >= 7	7 so it is p	laced afte	r 77.			
4 20 22 30 50 77 77 98 49 2 i = 8 = j, look at arr[8], 49 < 98; 49 < 777750; 49 > = 30 so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	20	30	50	77	77	98	22	49	2
i = 8 = j, look at arr[8], $49 < 98$; $49 < 777750$; $49 > = 30$ so it is placed after 30. 4 20 22 30 49 50 77 77 98 2 $i = 9 = j$, look at arr[9], $2 < 98777750493022204$, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	i = 7 = j, look at arr[7], 22 < 98; 22 < 77; 22 < 77; 22 < 50; 22 < 30; 22>= 20, placed after 20.									
4 20 22 30 49 50 77 77 98 2 i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2 4 20 22 30 49 50 77 77 98	4	20	22	30	50	77	77	98	49	2
i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4. 2	i = 8 = j, look at arr[8], $49 < 98$; $49 < 777750$; $49 > = 30$ so it is placed after 30.									
2 4 20 22 30 49 50 77 77 98	4	20	22	30	49	50	77	77	98	2
	i = 9 = j, look at arr[9], 2 < 98777750493022204, it is placed j-1 = 0, before 4.									
i = 10 >= size, return.	2	4	20	22	30	49	50	77	77	98

Merge Sort (Recursive):

