

# Exercise 9

## Ultrasound Signal Processing

TTK 4165 MEDICAL SIGNAL PROCESSING

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## Part 1: Theory

Even Florenas MTEL

a)

Received frequency is the remaining of the transmitted after doppler shift:

$$f_r = f_0 - 2f_0 \frac{v \cos \phi}{c}$$
$$= \underline{\underline{f_0 (1 - 2 \frac{v \cos \phi}{c})}}$$

b)

The doppler shift:

$$f_d = \underline{\underline{f_0 \frac{2v \cos \phi}{c}}}$$

c)

$$f_0 = 2.5 \text{ MHz}, c = 1540 \text{ m/s}, v = 1 \text{ m/s}$$

$$1) \phi = 90^\circ: f_r = f_0 (1 - 2 \frac{v \cos 90^\circ}{c})$$
$$= f_0 = \underline{\underline{2.5 \text{ MHz}}}$$

$$f_d = f_0 \frac{2v \cos 90^\circ}{c} = \underline{\underline{0}}$$

$$2) \phi = 45^\circ$$

$$\begin{aligned} f_r &= f_0 \left( 1 - \frac{2v \cos 45^\circ}{c} \right) \\ &= f_0 \left( 1 - \frac{v}{c} \sqrt{2} \right) = f_0 \left( 1 - \frac{v}{c} \sqrt{2} \right) \\ &= \underline{\underline{2.4977 \text{ MHz}}} \end{aligned}$$

$$\begin{aligned} f_d &= f_0 \frac{v}{c} \sqrt{2} = 2295.8 \text{ Hz} \\ &= \underline{\underline{2.3 \text{ kHz}}} \end{aligned}$$

$$d) r = 7.7 \text{ cm}$$

$$\phi = 45^\circ$$

$$v_{\max} = 1.5 \text{ m/s}$$

1) Time per measurement:

$$\Delta t_{\min} = \frac{2r}{c} = \underline{10^{-4} \text{ s}}$$

$$\text{PRF}_{\max} = \frac{1}{\Delta t_{\min}} = 10^4 \text{ Hz} = \underline{\underline{10 \text{ kHz}}}$$

2)

$$\text{PRF}_{\max} = \frac{4f_0}{c} v_{\max} \cos 45^\circ$$

$$\begin{aligned} f_0 &= \frac{c \cdot \text{PRF}_{\max}}{4v_{\max} \cdot \cos 45^\circ} = \underline{\underline{24.5 \text{ MHz}}} \\ &= \underline{\underline{3.63 \text{ MHz}}} \end{aligned}$$

3)  $\phi = 30^\circ$

Even Florences TTTEL

Need to find phase-shift for this case:

(From Ex. 8):

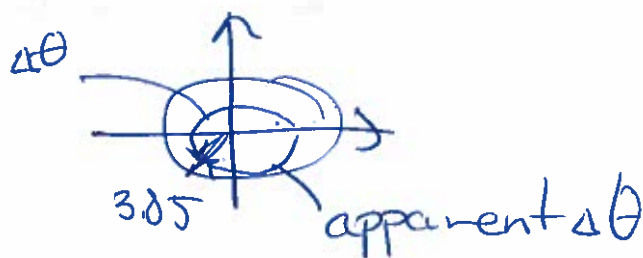
$$\Delta\theta = 4\pi \frac{v}{\text{PRF} \cdot \lambda} = 4\pi \frac{v \cdot f_0}{c \cdot \text{PRF}}$$

$$= 4\pi \frac{v_{\max} f_0 \cos(\phi)}{c \cdot \text{PRF}}$$

$$= 4\pi \frac{3.63 \cdot 10^6 \frac{1}{s} \cdot 1.5 \frac{m}{s} \cdot \cos(30^\circ)}{1540 \text{ m/s} \cdot 10^4 \text{ Hz}}$$

$$= \underline{3.85 \text{ rad}}$$

$\Delta\theta$  will not be the apparent  $\Delta\theta$ :



$\Delta\theta_{\text{apparent}} = \text{Apparent } \Delta\theta$

$$\Delta\theta_{\text{apparent}} = -(2\pi - 3.85) = \underline{-2.43 \text{ rad}}$$

$$\Delta\theta_{\text{apparent}} = 4\pi \frac{v_{\text{apparent}} \cdot f_0}{c \cdot \text{PRF}}$$

$$v_{\text{apparent}} = \Delta\theta_{\text{apparent}} \frac{c \cdot \text{PRF}}{4\pi \cdot f_0} = \underline{\underline{-0.82 \text{ m/s}}}$$

$$V_{\text{apparent}} = V_{\text{Max apparent}} \cdot \cos(30^\circ)$$

$$V_{\text{max apparent}} = \frac{V_{\text{apparent}}}{\cos 30^\circ} = \underline{\underline{-0.95 \text{ m/s}}}$$

Doppler shift:

$$\begin{aligned} f_d &= f_0 \frac{2 V_{\text{apparent}}}{c} = -3865.7 \text{ Hz} \\ &= \underline{\underline{-3.9 \text{ kHz}}} \end{aligned}$$

e)

Even Floren as 1-172

1) CW Doppler have no depth resolution

True, CW Doppler have continuous transmission of waves which will give no resolution along the beam. The results of transmission will all flow along the line-of-sight add together and mix.

2) Maximum velocity with PW (Measurable) is inversely proportional to the distance.

If this is true:  $v_{\max} = \frac{k}{r}$  where

$k$  - const. and  $r$  - distance to sample volume

Relation between  $PRF_{\max}$  and  $v_{\max}$ :

$$PRF_{\max} = \frac{4f_0}{c} v_{\max} \cos \theta \quad (1)$$

Find  $PRF_{\max}$ :

$$t_{\min} = \frac{2r}{c} \Rightarrow PRF_{\max} = \frac{1}{t_{\min}} = \frac{c}{2r} \quad (2)$$

(2)  $\rightarrow$  (1):

$$\frac{c}{2r} = \frac{4f_0}{c} v_{\max} \cos \theta$$

$$v_{\max} = \frac{c^2}{2 \cdot 4 f_0 \cos \theta} \cdot \frac{1}{r} \quad \text{if } f_0 = \text{const.}$$

$$= \frac{1}{k} \cdot \frac{1}{r}$$

$$k = \frac{c^2}{8 f_0 \cos \theta}$$

statement is true

f) Increasing transmit frequency implies a better velocity resolution in PW doppler when the PRF is kept constant.

Velocity (max) in PW Doppler is explained by:

$$V_{max} = \frac{c^2}{8f_0 \cos \theta} \cdot \frac{1}{r} = \frac{c \cdot PRF_{max}}{4f_0 \cos \theta}$$

If  $f_0$  is increased (with PRF kept const.) the resolution in velocity will decrease.

Statement is not true (untrue)

g)

In many practices Color flow replaces PW and CW. Color flow can easily be used for measuring size and direction for imaged organs. Timing information is more complicated in 2D-color flow display. For measuring velocity PW and CW would be a better choice. Statement is untrue.

h)

Formula for speed resolution:

$$V = \frac{c \cdot PRF}{f_0 \cdot 4 \cos \theta}$$

A shorter pulse will not effect the speed resolution as it will change the spread of frequency (bandwidth), but not the PRF or  $f_0$ . It will give better lateral resolution. Statement untrue.