537.
$$\lim_{h\to 0} \frac{\log (x+h) + \log (x-h) - 2 \log x}{h^2} (x>0).$$

538.
$$\lim_{x\to 0} \frac{\ln \operatorname{tg}\left(\frac{\pi}{4} + ax\right)}{\sin bx}$$
. 539.
$$\lim_{x\to 0} \frac{\ln \cos ax}{\ln \cos bx}$$
.

540.
$$\lim_{x\to 0} \left(\ln \frac{nx + \sqrt{1 - n^2x^2}}{x + \sqrt{1 - x^2}} \right)$$
.

540.1.
$$\lim_{x\to 0} \frac{\ln(nx+\sqrt{1-n^2x^2})}{\ln(x+\sqrt{1-x^2})}$$
.

541.
$$\lim_{x\to 0} \frac{a^x-1}{x}$$
 (a>0). 542. $\lim_{x\to a} \frac{a^x-x^a}{x-a}$ (a>0).

543.
$$\lim_{x\to a} \frac{x^x-a^a}{x-a} (a>0)$$
. 544. $\lim_{x\to a} (x+e^x)^{1/x}$.

545.
$$\lim_{x\to 0} \left(\frac{1+x\cdot 2^x}{1+x\cdot 3^x}\right)^{1/x^2}$$
.

545.1.
$$\lim_{x\to 0} \left(\frac{1+\sin x\cos\alpha x}{1+\sin x\cos\beta x}\right)^{\operatorname{ctg}^3 x}.$$

545.2.
$$\lim_{x\to 1} \frac{\sin(\pi x^{\alpha})}{\sin(\pi x^{\beta})}$$
. **545.3.** $\lim_{x\to 1} \frac{\sin^2(\pi \cdot 2^x)}{\ln[\cos(\pi \cdot 2^x)]}$.

546.
$$\lim_{n\to\infty} \operatorname{tg}^n\left(\frac{\pi}{4} + \frac{1}{n}\right)$$
. 547. $\lim_{x\to 0} \frac{e^{\alpha x} - e^{\beta x}}{\sin \alpha x - \sin \beta x}$.

548.
$$\lim_{x\to a} \frac{x^{2}-a^{\alpha}}{x^{\beta}-a^{\beta}}$$
 (a>0). **549.** $\lim_{x\to b} \frac{a^{x}-a^{b}}{x-b}$ (a>0).

550.
$$\lim_{h\to 0} \frac{a^{x+h} + a^{x-h} - 2a^x}{h^2}$$
 (a>0).

551.
$$\lim_{x\to\infty} \frac{(x+a)^{x+a}(x+b)^{x+b}}{(x+a+b)^{2x+a+b}}$$
.

552.
$$\lim_{n\to\infty} n(\sqrt[n]{x}-1)$$
 (x>0).

553.
$$\lim_{n\to\infty} n^2 \left(\sqrt[n]{x} - \sqrt[n+1]{x} \right) \quad (x>0).$$

554.
$$\lim_{n\to\infty} \left(\frac{a-1+\sqrt[n]{b}}{a}\right)^n \quad (a>0, b>0).$$

555.
$$\lim_{n\to\infty} \left(\frac{\sqrt[n]{a} + \sqrt[n]{b}}{2} \right)^n$$
 (a>0, b>0).