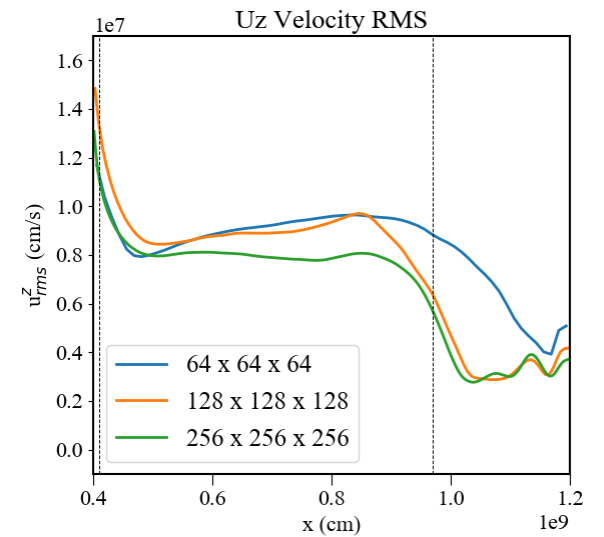
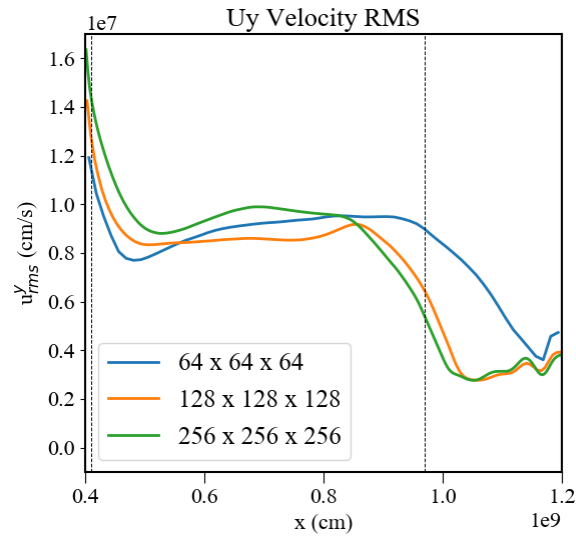
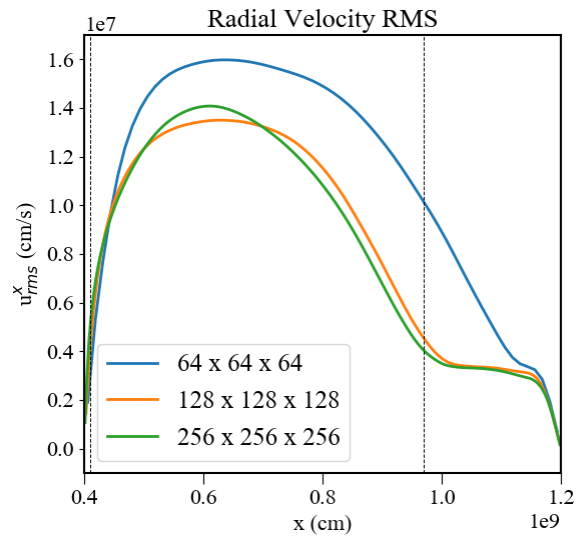
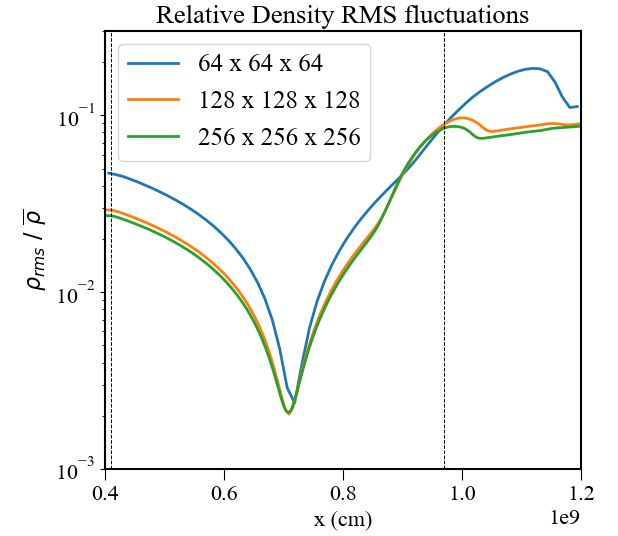
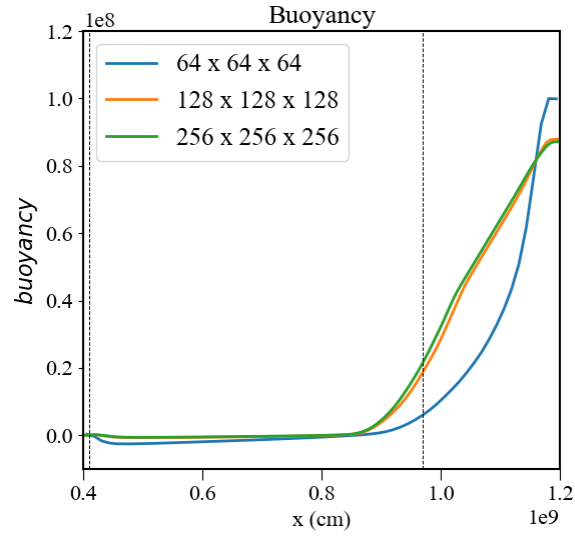
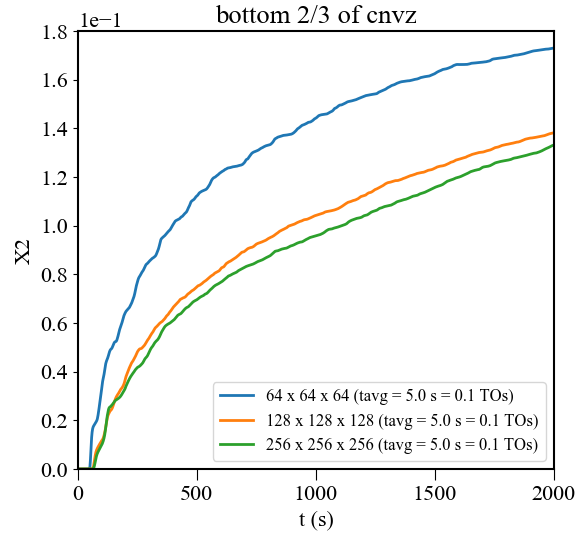


## Code Comparison Project – two-layer setup 3D simulation (RANS analysis highlights)



With increasing resolution, the entrainment rate decreases - consistent with Woodward, 2014. The strength of turbulence at convection boundary decreases (radial and horizontal rms velocity goes down, perhaps due to decreasing density fluctuations >> less buoyancy >> weaker turbulence flow). And from buoyancy jump, it looks like the bndry becoms stiffer >>  $Ri_B$  >> smaller  $E$ . What effect has averaging window  $\tau_{avg}$ ? above averaged over 1500 s.

One of the primary conclusions of these studies is that the entrainment rate depends on a Richardson number, which is a dimensionless measure of the “stiffness” of the boundary relative to the strength of the turbulence. In shear-free turbulent entrainment the bulk Richardson number,

$$Ri_B = \frac{\Delta b L}{\sigma^2}, \quad (2)$$

is most commonly studied. Here  $\Delta b$  is the buoyancy jump across the interface,  $\sigma$  is the rms turbulence velocity adjacent to the interface, and  $L$  is a length scale for the turbulent motions, which is often taken to be the horizontal integral scale of the turbulence near the interface. The relative buoyancy is defined by the integral

$$b(r) = \int_{r_i}^r N^2 dr, \quad (3)$$

where  $N$  is the buoyancy frequency defined by

$$N^2 = -g \left( \frac{\partial \ln \rho}{\partial r} - \frac{\partial \ln \rho}{\partial r} \Big|_s \right). \quad (4)$$

The entrainment coefficient  $E$  is the interface migration speed  $u_e$  normalized by the rms turbulent velocity at the interface  $E = u_e/\sigma$  and is generally found to obey a power-law dependence on  $Ri_B$ ,

$$E = A Ri_B^{-n}. \quad (5)$$

The exponent is usually found to lie in the range  $1 \lesssim n \lesssim 1.75$

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Received 2006 October 27; accepted 2007 May 21

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Submitted: July 15, 2013; Accepted: August 12, 2014

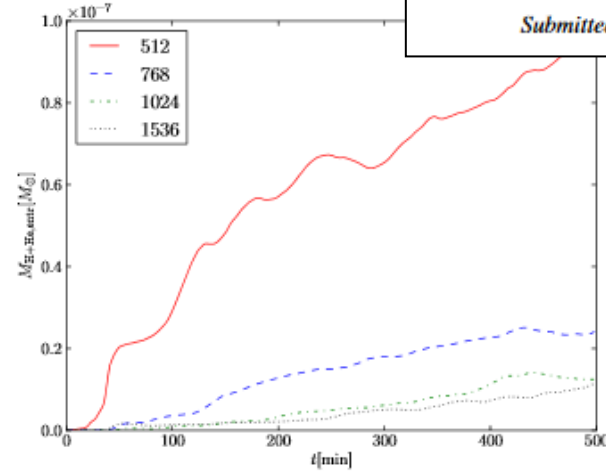


FIG. 16.— Entrained mass, integrated between the radial coordinates 10100km and 29200km, as a function of time. Simulations for different grid sized  $n^3$  are shown. The number of grid points  $n$  in one direction is shown in the legend.

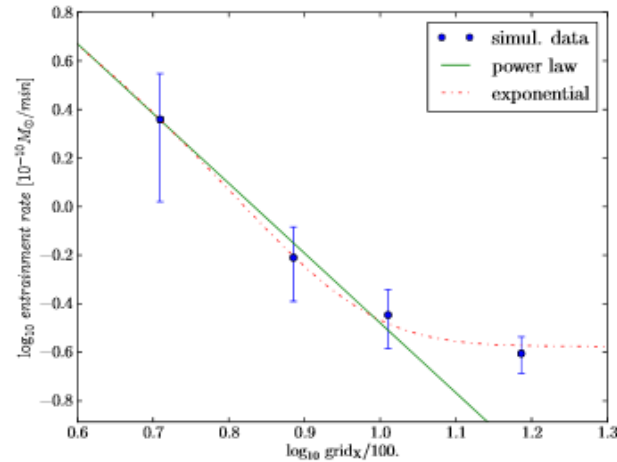
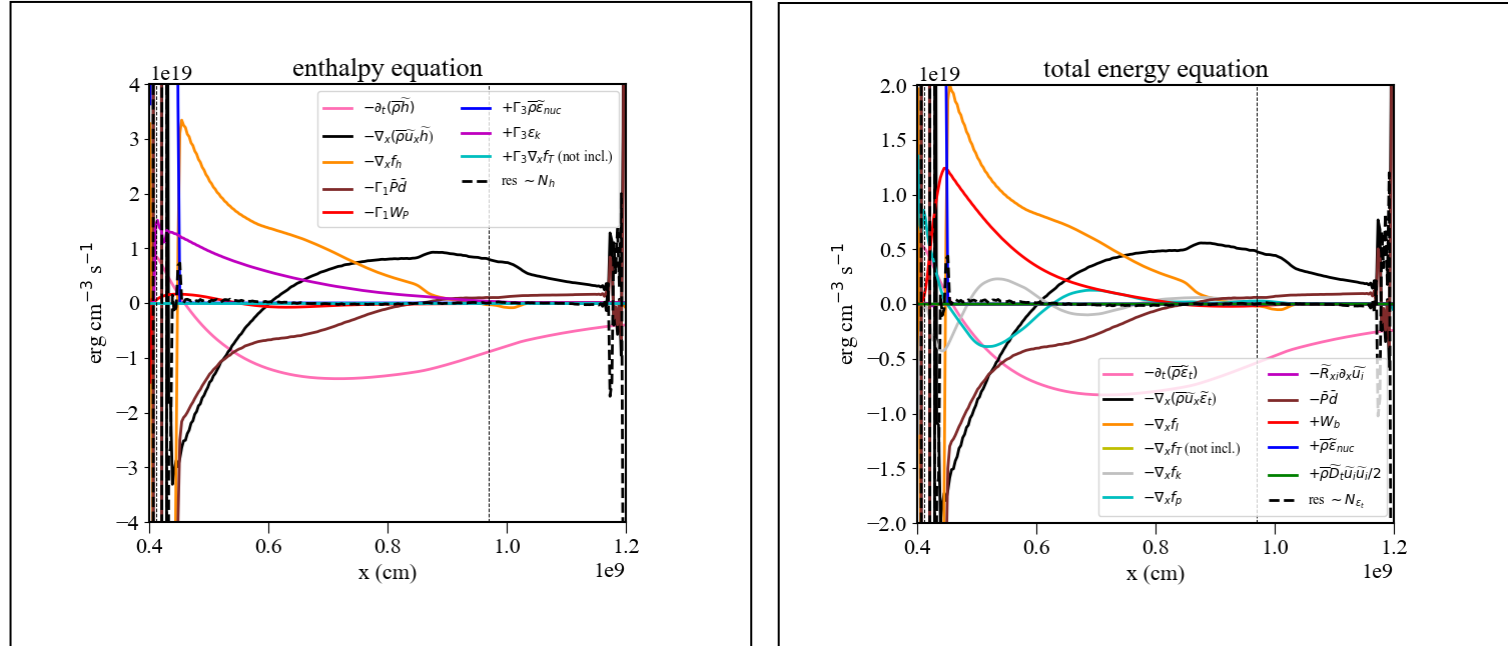
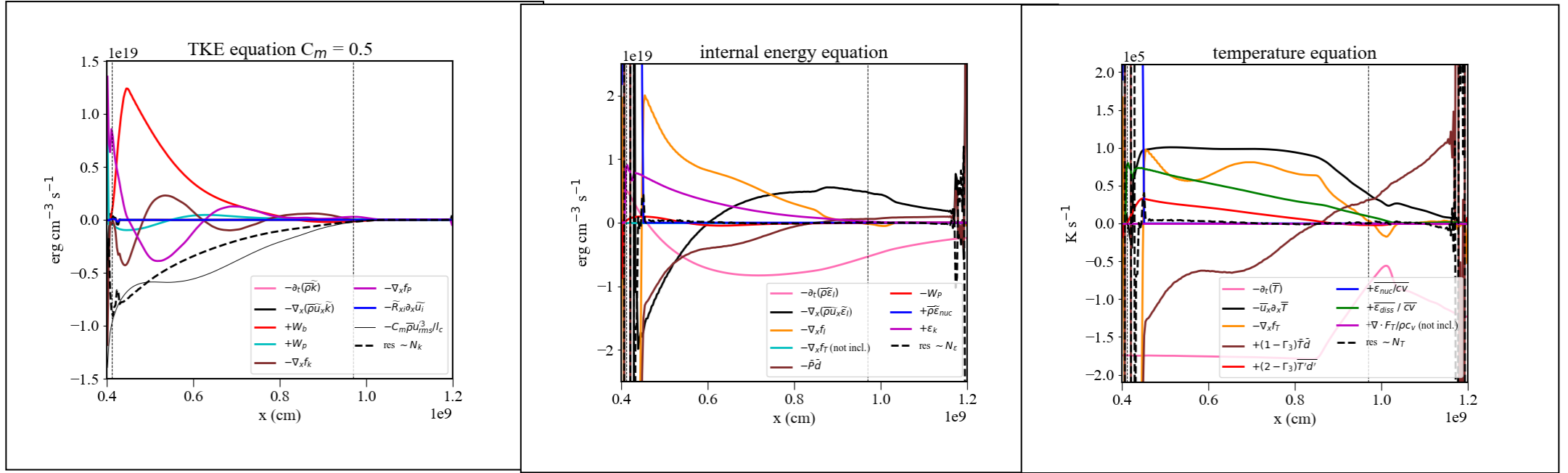
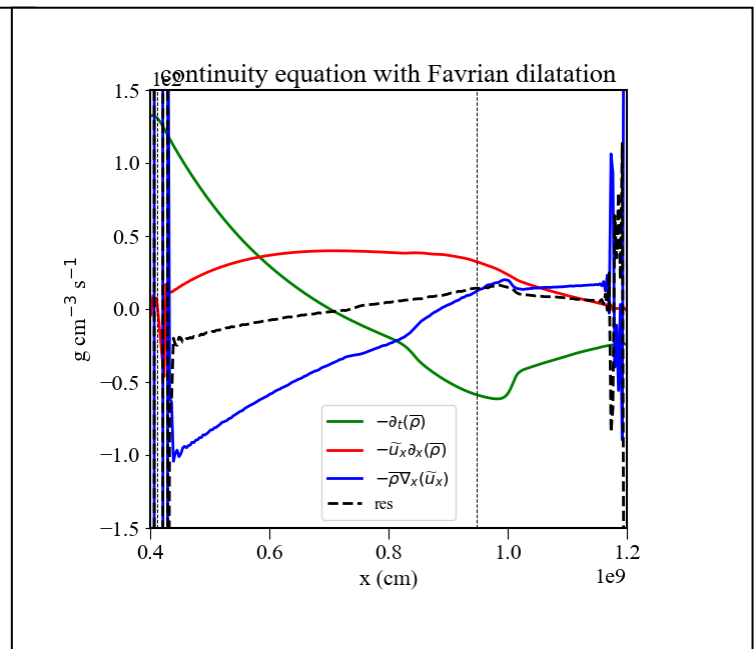
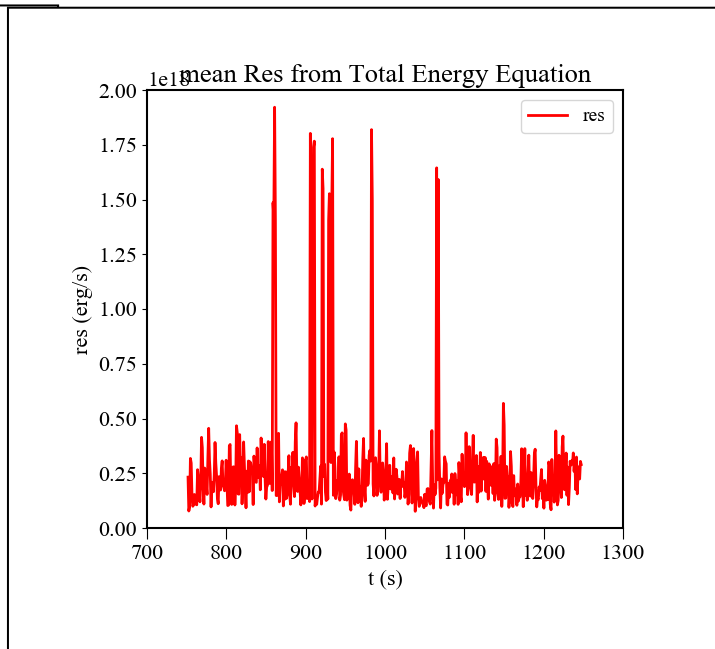
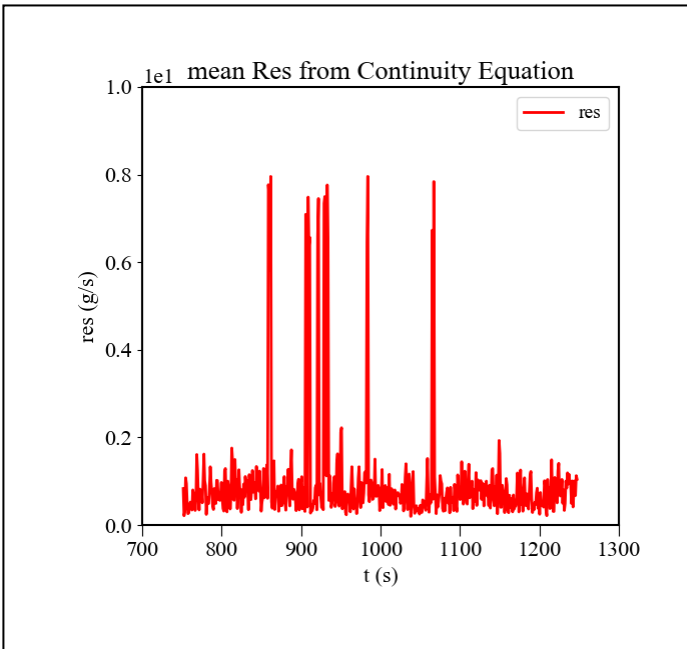
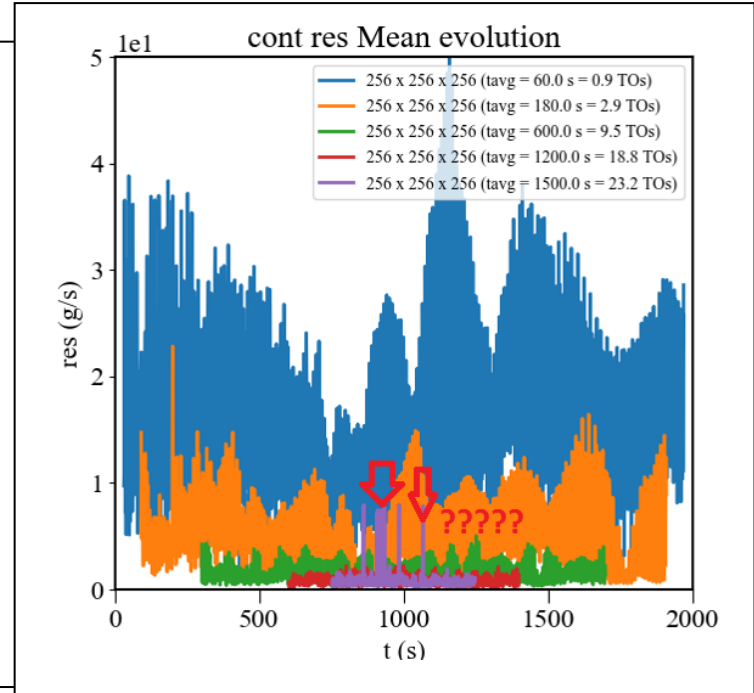
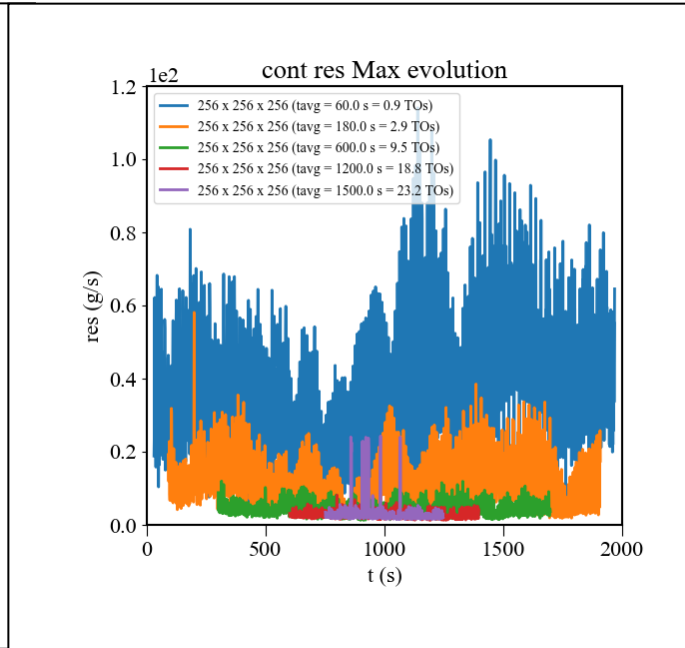
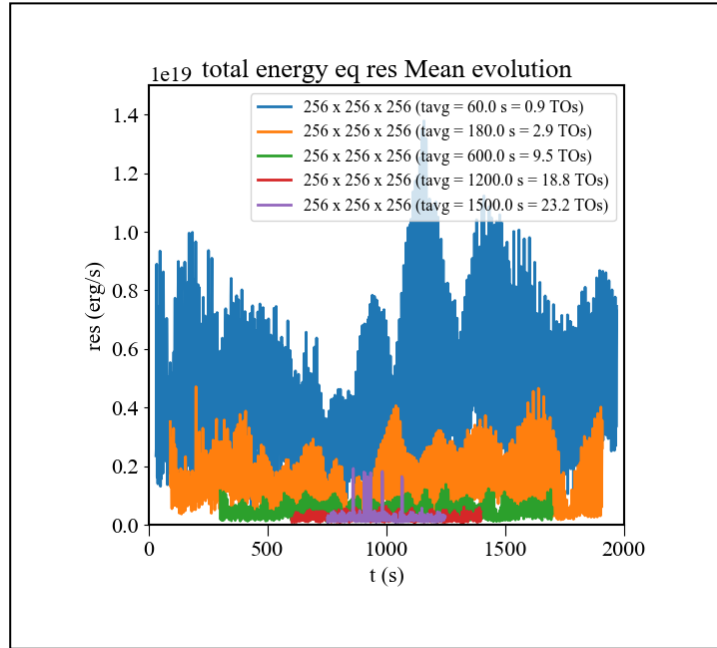


FIG. 17.— Logarithm of mean entrainment rates with error bars representing 99% confidence intervals (see text) as a function of grid size. The mean entrainment rates have been fitted with a power law and an exponential according to Eq. (7).

Turbulent kinetic energy dissipation appear to play a significant role at controlling internal energy, temperature or enthalpy evoluti. See below epsilon terms



Occasional burst of relatively large res when averaging over many TOs (down-right is the continuity eq. res256c, intc 110, having large residual, timewise it correspond to one of the first spikes in the plots)

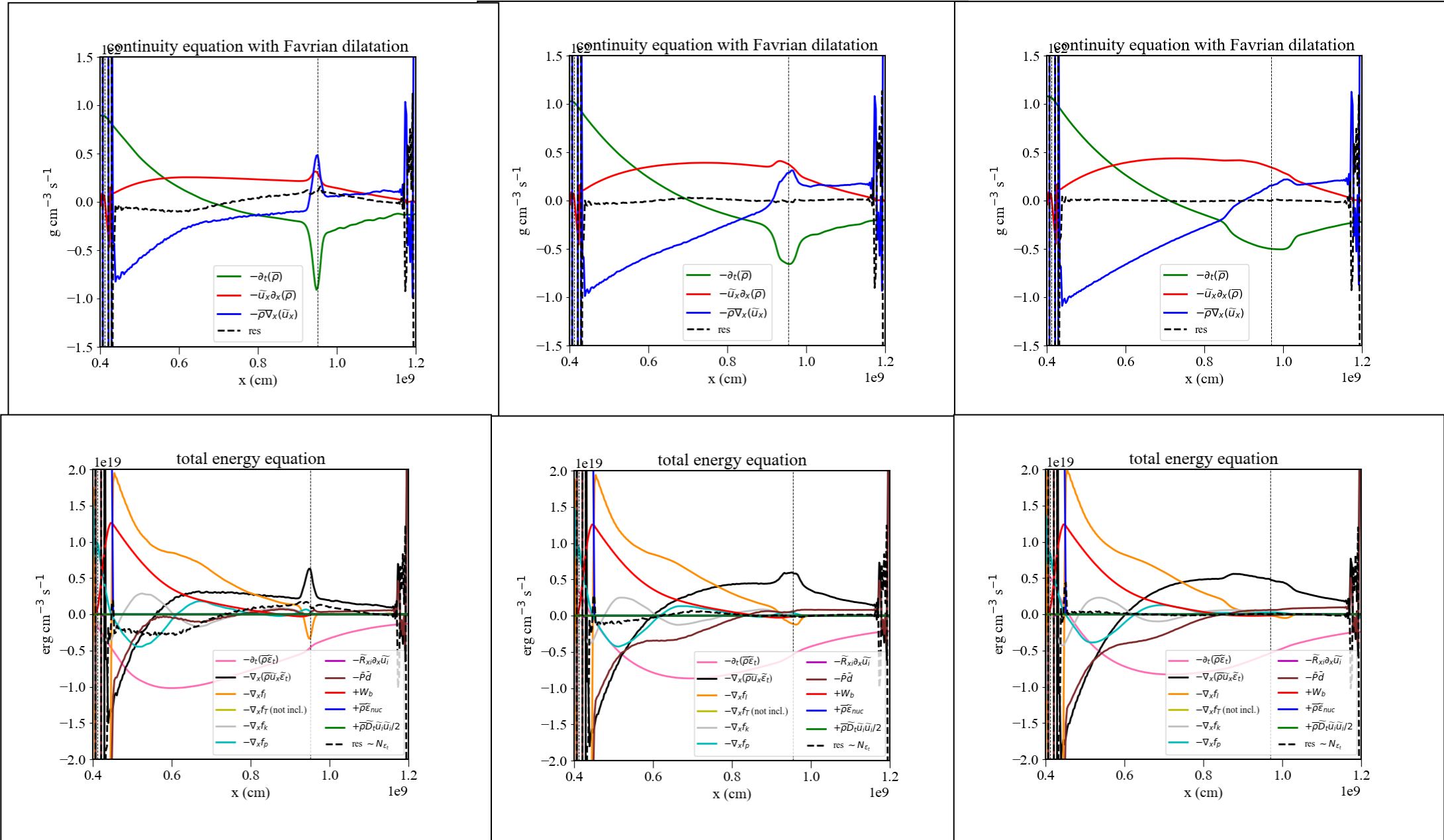


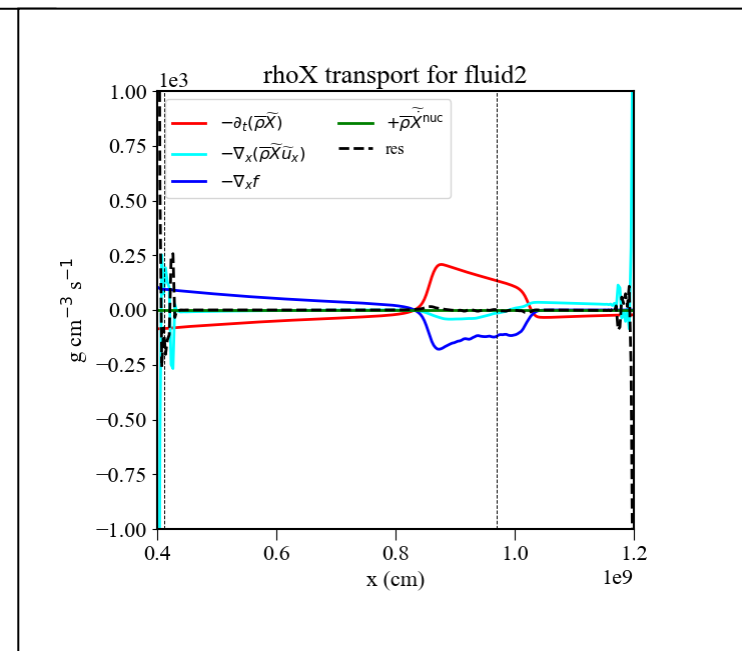
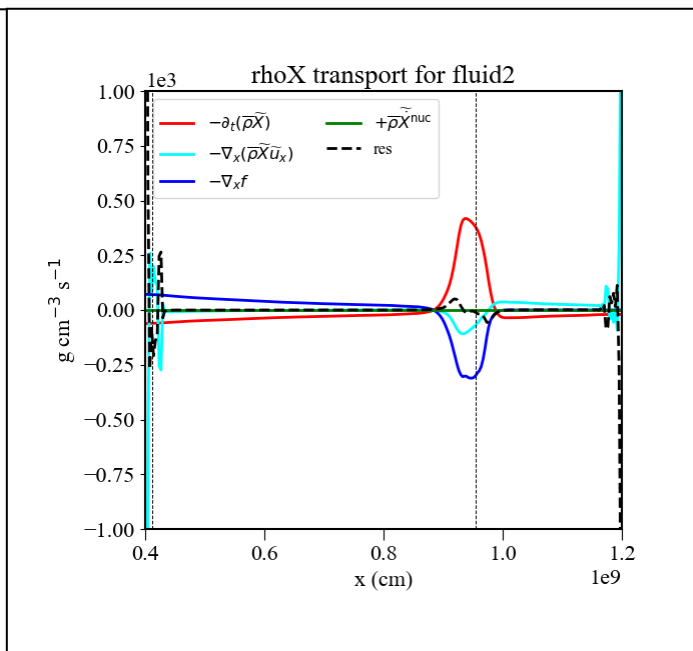
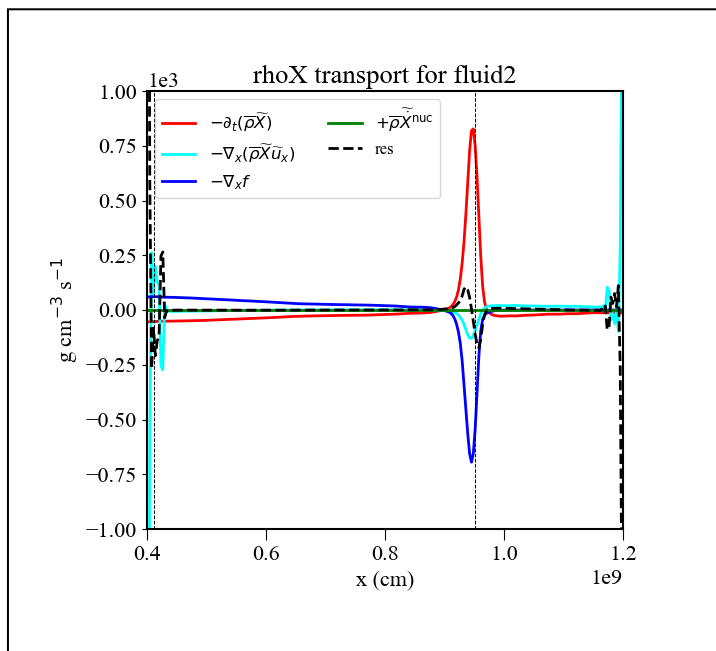
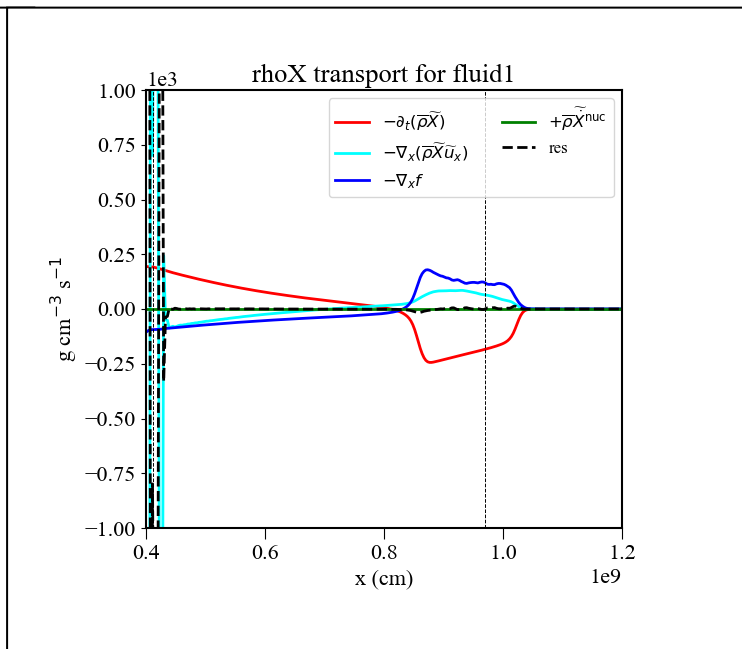
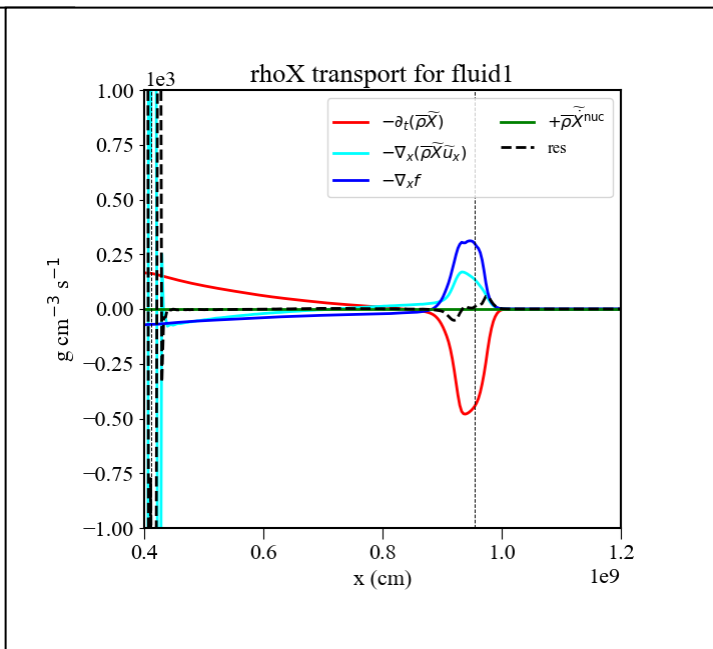
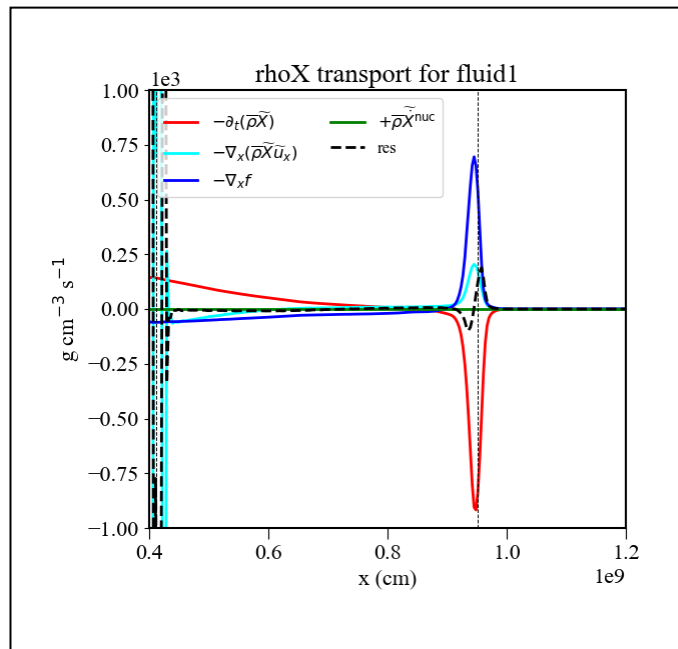
Dependence of RANS on averaging window: - (below  $\text{tavg}$  180 secs – 3 TOs, 600 secs – 10 TOs, 1500 secs – 25 TOs at  $\text{timec} = 1017$  secs) – looks like averaging over 3 TOs not enough, the 25 Tos averaging window gives best residual. The mean fields change visible at convection bndry mostly.

180 secs (3 TOs)

600 secs (10 TOs)

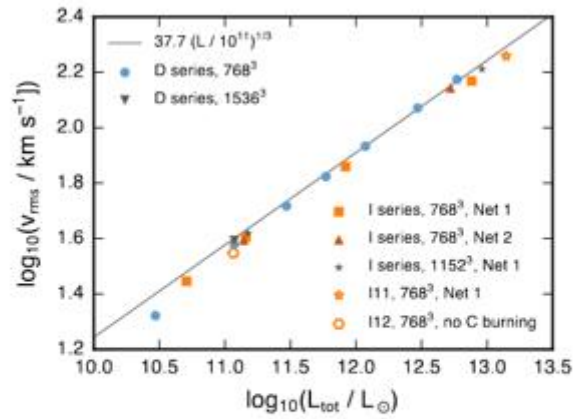
1500 secs (25 TOs)





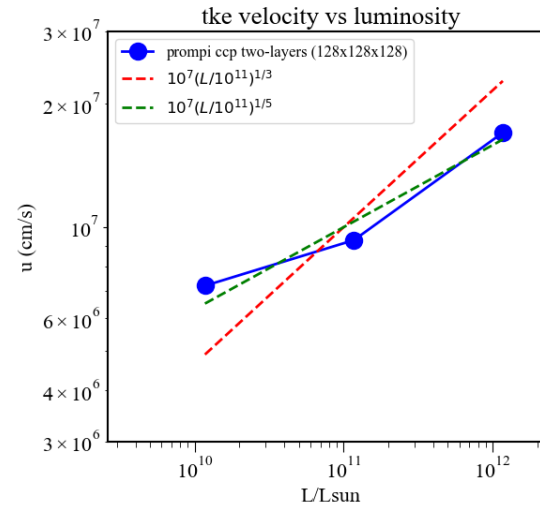
Dependence of turbulence velocities as a function of luminosity. It seems that the slope is shallower compared to what was found by Andrássy et al.

14 *R. Andrássy et al.*

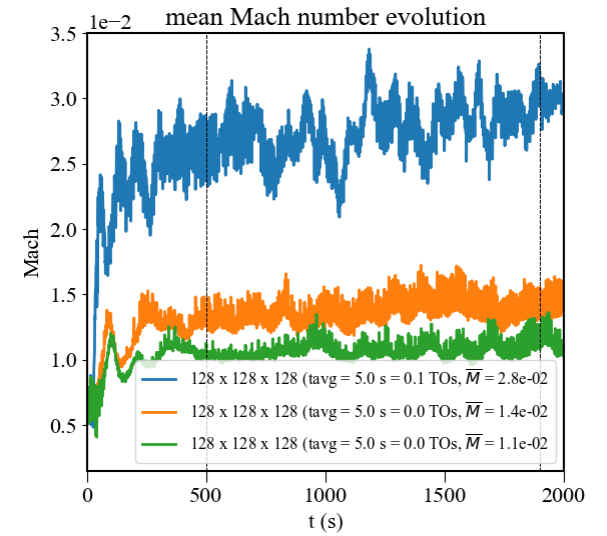
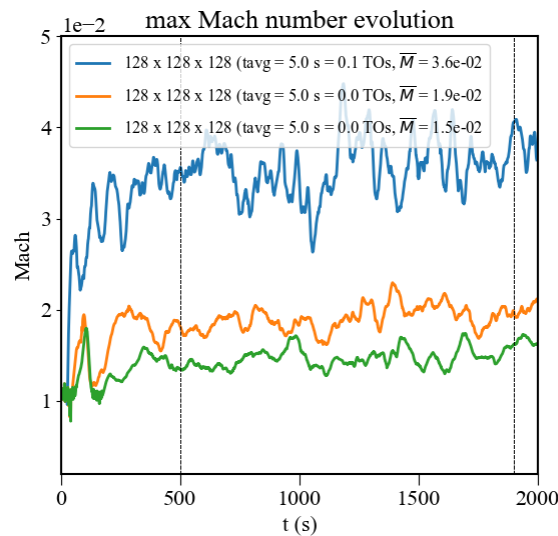
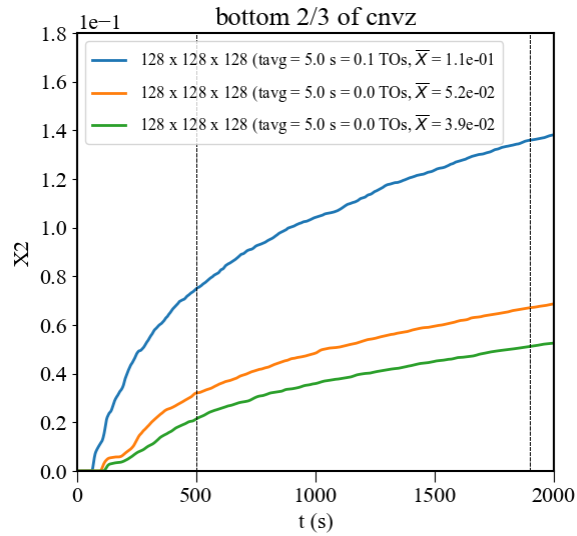
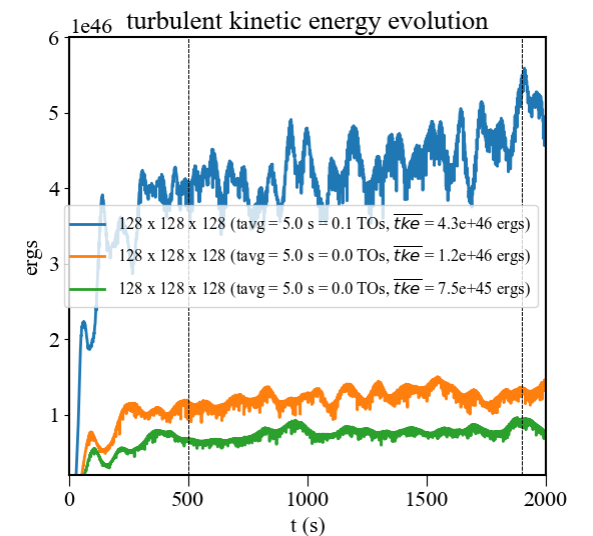
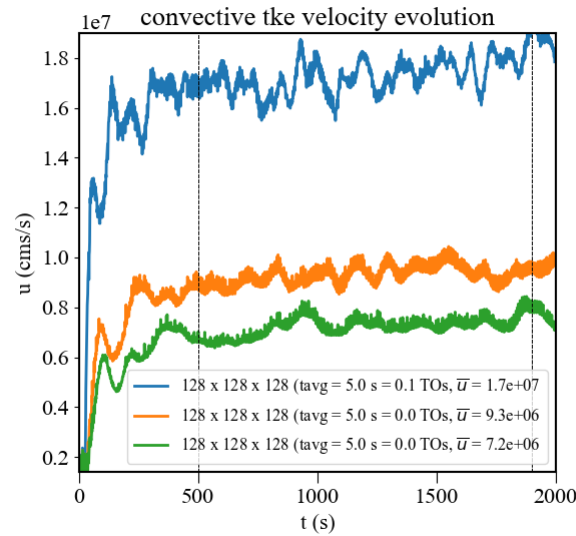
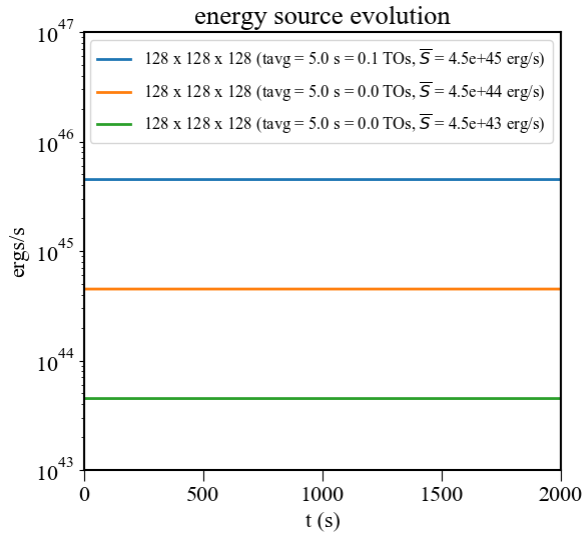


**Figure 15.** Dependence of the rms convective velocity  $v_{\text{rms}}$  on the total luminosity  $L_{\text{tot}}$  integrated over the convection zone. The expected scaling law  $v_{\text{rms}} \propto L_{\text{tot}}^{1/3}$  is shown for comparison. The last 2.2 min of run I11 are used when the instability described in Sect. 3.6 has fully developed.

3D hydrodynamic simulations of C ingestion into a convective O shell. Andrássy, 1,2,3,F, Herwig, 1,2,P, Woodward, 4,C, Ritter, 2



# Code Comparison Project – two-layer setup 3D simulation 128cubed (Luminosity Study for L=4.5e45, L/10 and L/100)





In the convection zone is pressure fluctuations depression off the density depression and temperature fluctuations have no depression. Interesting. In case of a convective roll, shouldn't all the minima be aligned?

