

# Electric Circuits I

## Laboratory 1: Vectors and Matrices MATLAB

### Objective:

- In this laboratory you will learn how to represent and use vectors and matrices in MATLAB.

### Background notes:

In MATLAB an  $M \times N$  matrix is a rectangular array of numbers with  $M$  rows and  $N$  columns. It can be defined by typing the matrix elements between square brackets. Elements along a row are separated by commas, and rows are separated by semi colons.

In Lab 0 you used row vectors for values of the angle and time variable. A row vector is a matrix with  $M=1$ .

In MATLAB Help, go to the Mathematics chapter. The second section is “Matrices in MATLAB.” Read the first four sections about creating, adding, and multiplying matrices.

### Matrix Multiplication:

Create 2 x 2 matrices A and B as follows:

$A = \begin{bmatrix} 2,1; 3,2 \end{bmatrix}$  and  $B = \begin{bmatrix} 3,1; 2,2 \end{bmatrix}$

Print  $A'$  and  $B'$ , the transposes of these two matrices.

Compute the following 4 matrix products and print them. Are any the same? Which ones?

$A1 = A * B$ ,  $A2 = B * A$ ,  $A3 = (A' * B')'$ ,  $A4 = (B' * A')'$

### Matrix Inverses:

Use “inv” to compute the following matrix inverses.

$A1 = \text{inv}(A * B)$ ,  $A2 = \text{inv}(A) * \text{inv}(B)$ ,  $A3 = \text{inv}(B * A)$ ,  $A4 = \text{inv}(B) * \text{inv}(A)$ .

Check the inverse values. Multiply  $A1 * (A * B)$  and also multiply  $(A * B) * A1$ . What are the two products?

### Solving Circuits with MATLAB:

The result of a KVL/KCL analysis of a circuit is the set of simultaneous equations:

$$\begin{aligned} V1 + V3 &= 10 \\ 3V1 + 3V2 + 4V3 &= 12 \\ 2V1 + 2V2 + 3V3 &= 5 \end{aligned}$$

which can be written using matrices as follows:

$$\begin{bmatrix} 1 & 0 & 1 \\ 3 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \cdot \begin{bmatrix} V1 \\ V2 \\ V3 \end{bmatrix} = \begin{bmatrix} 10 \\ 12 \\ 5 \end{bmatrix} = C \cdot V = S$$

$$C = \begin{bmatrix} 1 & 0 & 1 \\ 3 & 3 & 4 \\ 2 & 2 & 3 \end{bmatrix} \quad V = \begin{bmatrix} V1 \\ V2 \\ V3 \end{bmatrix} \quad S = \begin{bmatrix} 10 \\ 12 \\ 5 \end{bmatrix}$$

To solve this 3x3 system of equations we invert the coefficients matrix C and multiply it by the source matrix S.

Invert the matrix C and solve the system for the voltage matrix V. Then verify that the result is correct by multiplying C\*V and compare the result with S.

## More About Matrix Inverses:

Find the inverse of the matrix D shown below:

$$D = \begin{bmatrix} 2 & 4 \\ 1 & 2 \end{bmatrix}$$

- Is there an inverse of D ?
- If the answer is 'NO' then why not?

## Products of Time Functions:

Given the following functions,

$$p(t) = 5\cos(2\pi \cdot 3 \cdot t) \text{ and } v(t) = 5\exp(-0.5 \cdot t)$$

plot p(t) and v(t) from t = 0 to t=10 using time steps of 0.01.

Create the point by point product function b(t) = p(t)v(t) using b=p.\*v and plot it. Note that the .\* operation multiplies the two vectors point by point rather than computing a matrix product.

Note: Please show all your work.