

## 1 Moving to $\mathbb{R}^3$

In  $\mathbb{R}^3$ , we often have that  $y$  is facing towards us. However, in this course,  $y$  will be facing upwards while  $z$  is facing towards us.

Let  $f(\mathbf{x}) = M\mathbf{x}$ , where  $M$  is a  $3 \times 3$  matrix. Here,  $M$  is denoted by

$$\begin{bmatrix} f(\mathbf{i}) & f(\mathbf{j}) & f(\mathbf{k}) \end{bmatrix}.$$

Additionally, note that the unit vectors in  $\mathbb{R}^3$  are given by

$$\mathbf{i} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \mathbf{j} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \mathbf{k} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}.$$

### 1.1 Scaling

For  $\alpha \in \mathbb{R}$ , we say that  $S_\alpha(\mathbf{x}) = \alpha\mathbf{x}$  is known as *uniform scaling*.

Now, for  $a, b, c \in \mathbb{R}$ , we say that  $S_{\langle a, b, c \rangle}(\langle x_1, x_2, x_3 \rangle) = \langle ax_1, bx_2, cx_3 \rangle$  is known as *non-uniform scaling*.

(Example.) Suppose we have  $S = S_{\langle 1/2, 1, 1 \rangle}$  and  $R = R_{90^\circ, \mathbf{j}}$ . Find the following:

- $S \circ R$ .
- $R \circ S$ .