Housing Analysis

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Overview

This project is the second project for Flatiron School's bootcamp program in Data Science. We are being placed into a hypothetical situation as a Data Scientist and hoping to provide value to our business for the scenario we are given.

Business Problem

I have been hired by a real estate agency that helps homeowners sell homes. For this project, I am to provide expected/estimated home prices to homeowners based on the logistics of their home. This can also give insight on how home renovations might increase the estimated value of their homes, and what type of potential renovations are best.

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import statsmodels.api as sm
import scipy.stats as stats
%matplotlib inline
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import OneHotEncoder
from sklearn.impute import SimpleImputer
from sklearn.pipeline import make pipeline
from sklearn.preprocessing import PolynomialFeatures
from sklearn.linear model import LinearRegression
from statsmodels.formula.api import ols
from sklearn.preprocessing import StandardScaler
from statsmodels.stats.outliers influence import varianc
```

Data Investigation and Cleaning

To start, we have access to the King County House Sales dataset. Let's take a look at this to get a feel for what our starting point is and what raw data we have to work with.

```
df original = pd.read csv("data\kc house data.csv")
df_original.info()
 <class 'pandas.core.frame.DataFrame'>
 RangeIndex: 21597 entries, 0 to 21596
 Data columns (total 21 columns):
     Column
                 Non-Null Count Dtype
     -----
                   _____
  0
     id
                   21597 non-null int64
  1
     date
                  21597 non-null object
  2
                   21597 non-null float64
     price
  3
     bedrooms
                   21597 non-null int64
     bathrooms
                   21597 non-null float64
  4
  5
     sqft_living
                   21597 non-null int64
  6
    sqft_lot
                   21597 non-null int64
  7
                   21597 non-null float64
     floors
  8
     waterfront 19221 non-null float64
  9
     view
                   21534 non-null float64
  10 condition
                 21597 non-null int64
                  21597 non-null int64
  11 grade
  12 sqft_above
                   21597 non-null int64
  13 sqft_basement 21597 non-null object
  14 yr built
                   21597 non-null int64
  15 yr_renovated 17755 non-null float64
  16 zipcode
                   21597 non-null int64
  17 lat
                   21597 non-null float64
  18 long
                   21597 non-null float64
  19 sqft_living15 21597 non-null int64
  20 sqft lot15
                   21597 non-null int64
 dtypes: float64(8), int64(11), object(2)
 memory usage: 3.5+ MB
```

df_original.head(10)

	id	date	price	bedrooms	bathroo
0	7129300520	10/13/2014	221900.0	3	1.00
1	6414100192	12/9/2014	538000.0	3	2.25
2	5631500400	2/25/2015	180000.0	2	1.00
3	2487200875	12/9/2014	604000.0	4	3.00
4	1954400510	2/18/2015	510000.0	3	2.00
5	7237550310	5/12/2014	1230000.0	4	4.50
6	1321400060	6/27/2014	257500.0	3	2.25
7	2008000270	1/15/2015	291850.0	3	1.50
8	2414600126	4/15/2015	229500.0	3	1.00
9	3793500160	3/12/2015	323000.0	3	2.50

10 rows × 21 columns

Per the project description, I will be ignoring the following features: date, view, sqft_above, sqft_basement, yr_renovated, zipcode, lat, long, sqft_living15, sqft_lot15. For the time being, I am trying to make my modeling phase in this project as simple as possible.

df_col_drops = df_original.drop(columns=['id', 'date', '
display(df_col_drops)

	price	bedrooms	bathrooms	sqft_living	sq1		
0	221900.0	3	1.00	1180	565		
1	538000.0	3	2.25	2570	724		
2	180000.0	2	1.00	770	100		
3	604000.0	4	3.00	1960	500		
4	510000.0	3	2.00	1680	808		
			•••				
21592	360000.0	3	2.50	1530	113		
21593	400000.0	4	2.50	2310	581		
21594	402101.0	2	0.75	1020	135		
21595	400000.0	3	2.50	1600	238		
21596	325000.0	2	0.75	1020	107		
21597 rows × 10 columns							

```
df col drops.info()
 <class 'pandas.core.frame.DataFrame'>
 RangeIndex: 21597 entries, 0 to 21596
 Data columns (total 10 columns):
      Column
                  Non-Null Count Dtype
                  -----
  0
      price
                  21597 non-null float64
     bedrooms
                 21597 non-null int64
  1
  2
    bathrooms 21597 non-null float64
     sqft_living 21597 non-null int64
  3
    sqft_lot
                 21597 non-null int64
  5
    floors
                  21597 non-null float64
  6 waterfront 19221 non-null float64
  7
     condition 21597 non-null int64
  8
      grade
                  21597 non-null int64
                 21597 non-null int64
     yr built
 dtypes: float64(4), int64(6)
 memory usage: 1.6 MB
 Waterfront appears to have ~2000 null values. Let's
 investigate what values are in this column to see what we
 can do about the null values.
 Which ones are the most important features?
df_col_drops.waterfront.value_counts()
    0.0
          19075
    1.0
            146
    Name: waterfront, dtype: int64
 Only 146 have a waterfront view. Since this is a binary-filled
 column, I believe we can fill in all NaNs with a zero value.
 This makes sense, as NaNs almost certainly denotes the
 absence of a waterfront view.
df_col_drops.waterfront.fillna(0, inplace=True)
display(df_col_drops.head())
      price bedrooms bathrooms sqft_living sqft_lo
0 221900.0 3
                        1.00
                                     1180
                                                 5650
   538000.0 3
                        2.25
                                     2570
                                                 7242
   180000.0 2
                        1.00
                                     770
                                                  10000
   604000.0 4
                                                 5000
                        3.00
                                     1960
4 510000.0 3
                        2.00
                                     1680
                                                 8080
```

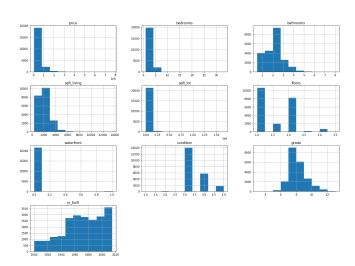
df_col_drops.describe()

	price	bedrooms	bathrooms	sqft_liv
count	2.159700e+04	21597.000000	21597.000000	21597.000
mean	5.402966e+05	3.373200	2.115826	2080.3218
std	3.673681e+05	0.926299	0.768984	918.10612
min	7.800000e+04	1.000000	0.500000	370.00000
25%	3.220000e+05	3.000000	1.750000	1430.0000
50%	4.500000e+05	3.000000	2.250000	1910.0000
75%	6.450000e+05	4.000000	2.500000	2550.0000
max	7.700000e+06	33.000000	8.000000	13540.000

df_col_drops.columns

#iterating over all columns except id to see general dis

df_col_drops.hist(figsize = (20,15));



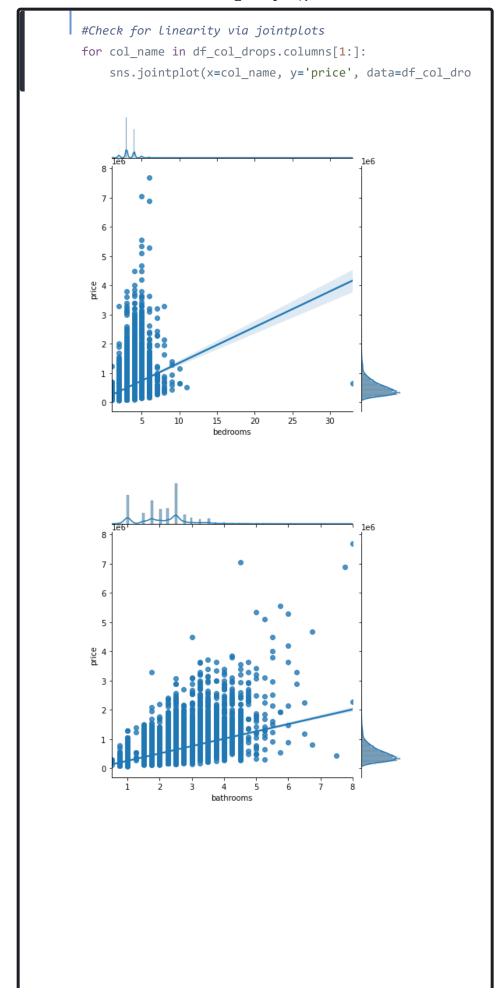
It appears that we have some outliers in this data, so it's a little difficult to get a sense for what some the distrubutions actually are.

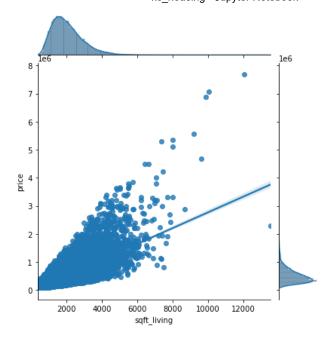
Specifically, I'm seeing a single entry priced at 7.7 million.

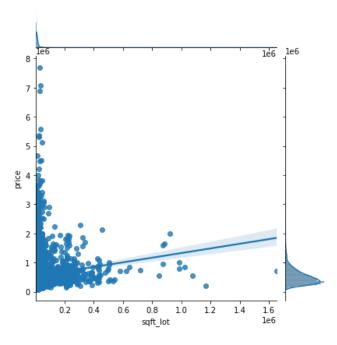
I also can't really tell what the bedroom distribution is with an outlier of 33.

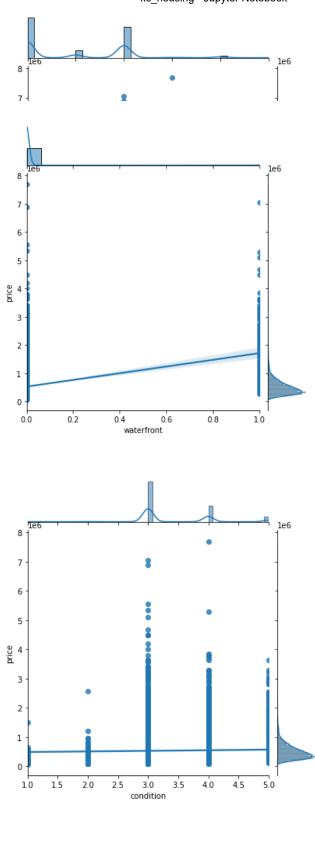
sqft_lot has only a single column in this view and the mean is vastly different from the median. We will need to take a closer look at this as well.

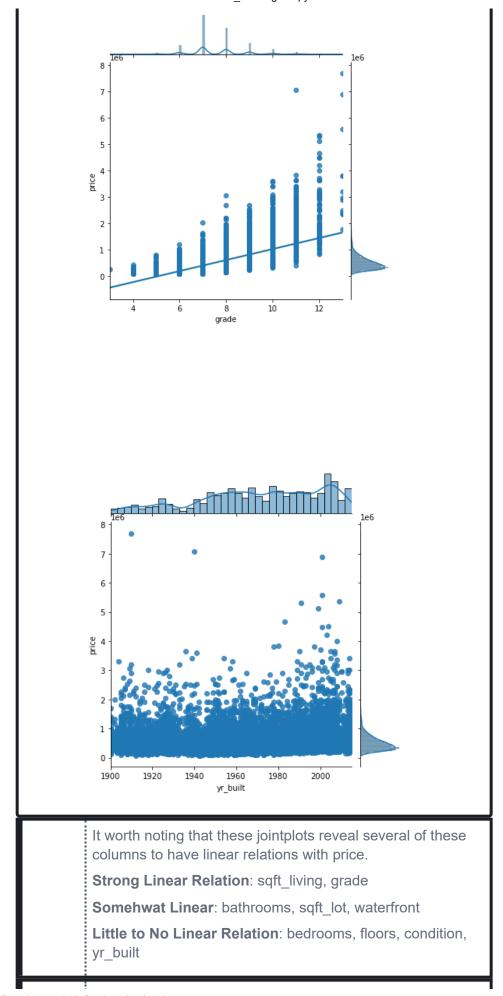
Condition and grade seem to be relatively normal.











It appears that the features that have the largest impact on the price of a home are the square footage of the home, as well as the Grade- this rating is given by the King County Housing System. I have copied this system below for more context.

- 1-3 Falls short of minimum building standards. Normally cabin or inferior structure.
- 4 Generally older, low quality construction. Does not meet code.
- 5 Low construction costs and workmanship. Small, simple design.
- 6 Lowest grade currently meeting building code. Low quality materials and simple designs.
- 7 Average grade of construction and design. Commonly seen in plats and older sub-divisions.
- 8 Just above average in construction and design. Usually better materials in both the exterior and interior finish work.
- 9 Better architectural design with extra interior and exterior design and quality.
- 10 Homes of this quality generally have high quality features. Finish work is better and more design quality is seen in the floor plans. Generally have a larger square footage.
- 11 Custom design and higher quality finish work with added amenities of solid woods, bathroom fixtures and more luxurious options.
- 12 Custom design and excellent builders. All materials are of the highest quality and all conveniences are present.
- 13 Generally custom designed and built. Mansion level. Large amount of highest quality cabinet work, wood trim, marble, entry ways etc.

Modeling

Model 1

```
outcome = 'price'
x_cols = list(df_col_drops.columns)
x_cols.remove(outcome)
print(x_cols)

['bedrooms', 'bathrooms', 'sqft_living', 'sqft_lot', 'floors', 'waterfront', 'condition', 'grade', 'yr_built']
```

```
train, test = train_test_split(df_col_drops)
```

```
for col in x_cols:
    train[col] = (train[col] - train[col].mean())/train[
display(train.head())
```

print(len(train), len(test))

<ipython-input-15-f07e438ec62e>:2: SettingWithCopyWarnin
g:

A value is trying to be set on a copy of a slice from a D $\mbox{\ensuremath{\mbox{ataFrame.}}}$

Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-vers us-a-copy (https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

train[col] = (train[col] - train[col].mean())/train[co
l].std()

	price	bedrooms	bathrooms	sqft_living	SC
12536	442500.0	-0.402234	-0.803642	0.682700	0.7
13098	381000.0	-0.402234	-0.479047	0.671829	0.0
17379	440000.0	-0.402234	-0.154452	-0.317497	0.40
14127	307300.0	-1.465211	-0.154452	-0.611033	-0.3
14618	267000.0	0.660743	-0.479047	-0.089191	-0.1

16197 5400

```
predictors = '+'.join(x_cols)
formula = outcome + '~' + predictors
model = ols(formula=formula, data=train).fit()
model.summary()
```

OLS Regression Results

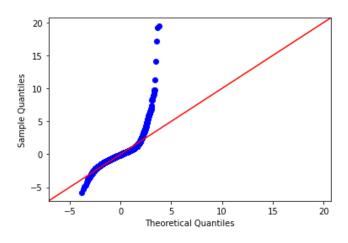
Dep. Variabl	e:	price			R-s	quared:		0.64	.6
Model:		OLS				Adj. R- squared:		0.646	
Method: Least Squares		S		F-st	tatistic:		3284	4.	
Date: Fri, 19 2021		Fri, 19 N 2021	Mar			b (F- tistic):		0.00)
Time: 10:05:27		7		Log	J- elihood:		-2.2	218e+05	
No. Observations:				AIC	:		4.44	4e+05	
Df Residuals: 16		16187			BIC	:		4.44	5e+05
Df Model: 9		9							
Covariance Type:		nonrobust							
	coe	f std e		err	•	t	P	> t	[0.025
Intercept	5.40	3e+05	1724.5		545	313.278	0.	000	5.37e+05
bedrooms	-3.6	96e+04	2185.60		606	-16.911	0.	000	-4.12e+04
bathrooms	3.90)2e+04	3084.6		654	12.650	0.	000	3.3e+04
sqft_living	1.60	9e+05	351	8.0	325	45.828	0.	000	1.54e+05
sqft_lot	-937	72.8854	176	6.1	156	-5.307	0.	000	-1.28e+04
floors	860	0.5384	216	31.0)40	3.980	0.	000	4364.661
waterfront	6.30	7e+04	174	12.8	391	36.184	0.	000	5.96e+04
condition	1.19	9e+04	187	6.5	67	6.387	0.	000	8307.926
grade	1.54	l2e+05	.2e+05 2918.8		302	52.833	0.	000	1.48e+05
yr_built	-1.1	17e+05	226	6.7	720	-49.293	0.	000	-1.16e+05
Omnibus:		12304.	793	Dı	urbii	n-Watson:		2.01	16
Prob(Omnib	us):	0.000		Ja	arqu	e-Bera (JB	3):	895	270.137
Skew:		3.055		Pı	rob(JB):		0.00)
Kurtosis:		38.906		C	ond.	No.		4.74	1

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

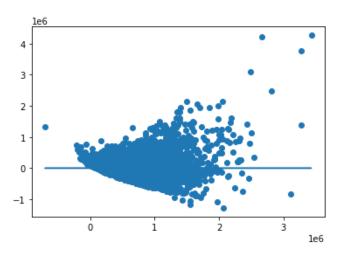
The p-values are less than 0.05 for our selected columns. Let's take a look at our residuals for normality.

fig = sm.graphics.qqplot(model.resid, dist=stats.norm, 1



plt.scatter(model.predict(train[x_cols]), model.resid)
plt.plot(model.predict(train[x_cols]), [0 for i in range

[<matplotlib.lines.Line2D at 0x1f955244820>]



This doesn't look great, as our QQ plot looks incorrect and we have a pronounced funnel shape on our check for homoscedasticity. We are going to need to make some changes.

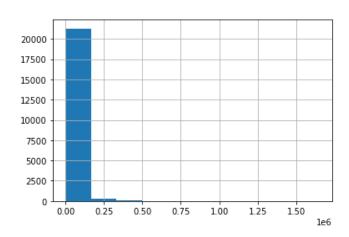
Model 2 Iterations

For this iteration, I'm going to remove some outliers. (log transformation?)

I recall having the most issues determining the normal distributions of sqft_lot and bedrooms, so I'm going to filter on both.

```
df_col_drops.sqft_lot.hist()
```

<AxesSubplot:>



```
for i in range(80,100):
    q = i/100
    print("{} percentile: {}".format(q,df_col_drops.sqft
 0.8 percentile: 12182.39999999998
 0.81 percentile: 12558.0
 0.82 percentile: 13055.43999999995
 0.83 percentile: 13503.68
 0.84 percentile: 14197.0
 0.85 percentile: 15000.0
 0.86 percentile: 15716.040000000012
 0.87 percentile: 16646.640000000003
 0.88 percentile: 18000.0
 0.89 percentile: 19550.0
 0.9 percentile: 21371.600000000006
 0.91 percentile: 24149.360000000015
 0.92 percentile: 28505.11999999999
 0.93 percentile: 34848.0
 0.94 percentile: 37643.1999999999
 0.95 percentile: 43307.200000000026
 0.96 percentile: 50655.28
 0.97 percentile: 67381.7199999999
 0.98 percentile: 107157.0
 0.99 percentile: 213008.0
```

I think filtering out homes with greater than 100k sqaure feet is acceptable here.

```
for i in range(80,100):
    q = i/100
    print("{} percentile: {}".format(q,df_col_drops.bedr
 0.8 percentile: 4.0
 0.81 percentile: 4.0
 0.82 percentile: 4.0
 0.83 percentile: 4.0
 0.84 percentile: 4.0
 0.85 percentile: 4.0
 0.86 percentile: 4.0
 0.87 percentile: 4.0
 0.88 percentile: 4.0
 0.89 percentile: 4.0
 0.9 percentile: 4.0
 0.91 percentile: 4.0
 0.92 percentile: 5.0
 0.93 percentile: 5.0
 0.94 percentile: 5.0
 0.95 percentile: 5.0
 0.96 percentile: 5.0
 0.97 percentile: 5.0
 0.98 percentile: 5.0
 0.99 percentile: 6.0
```

df_col_drops.bedrooms.value_counts()

9824

3

Name: bedrooms, dtype: int64

I will also be filtering out all houses with more than 6 bedrooms, removing about 2% of the total entries. (may overlap with sq footage)

I will also include a log transformation to the price feature, as this may help fix our QQplot from Model 1.

```
orig tot = len(df col drops)
df_outlier_filter = df_col_drops.copy()
df_outlier_filters = df_outlier_filter[df_outlier_filter
print('Percent removed:', (orig_tot -len(df_outlier_filt
df_outlier_filters = df_outlier_filters[df_outlier_filte
print('Percent removed:', (orig_tot -len(df_outlier_filt
#applying a log transformation to the price, which is ri
df_outlier_filter['price'] = np.log(df_outlier_filter['p
train2, test2 = train_test_split(df_outlier_filters)
# Refit model with subset features
predictors = '+'.join(x cols)
formula = outcome + "~" + predictors
model2 = ols(formula=formula, data=train2).fit()
model2.summary()
 Percent removed: 0.021530768162244755
 Percent removed: 0.024355234523313424
```

OLS Regression Results

Dep. Variable: price		price		R-sq	uared:	0.652	0.652	
Model:	Model: OLS				Adj. R- squared:			
Method:		Least Squares		F-sta	F-statistic:			
Date:		Fri, 19 Mar 2021			Prob (F- statistic):			
Time:		1111115178		Log- Like	lihood:	-2.160	09e+05	
No. Observations:		15803		AIC:	AIC:		4.322e+05	
Df Residuals:		15793	15793		BIC:		e+05	
Df Model:		9						
Covariance Type:	nonrohuet		st					
	CO	ef	std e	err	t	P> t	[0.025	
Intercept	6.5	39e+06	1.46	e+05	44.654	0.000	6.25e+06	
bedrooms	-4.	765e+04	2485	5.774	-19.169	0.000	-5.25e+0 ²	
bathrooms	5.4	07e+04	07e+04 3930		13.756	0.000	4.64e+04	
sqft_living	179	9.6059	3.90	6	45.984	0.000	171.950	
sqft_lot	-1.	5529	0.16	0	-9.714	0.000	-1.866	

1.155e+04 3939.660 2.932 0.003 3828.551 floors waterfront 7.974e+05 2.18e+04 36.615 0.000 7.55e+05 condition 2.005e+04 2784.624 7.201 0.000 1.46e+04 grade 1.304e+05 2446.460 53.311 0.000 1.26e+05 yr_built -3753.7342 75.323 -49.835 0.000 -3901.375

Omnibus: 10197.238 **Durbin-Watson:** 1.997

Prob(Omnibus): 0.000 **Jarque-Bera** (JB): 438980.484

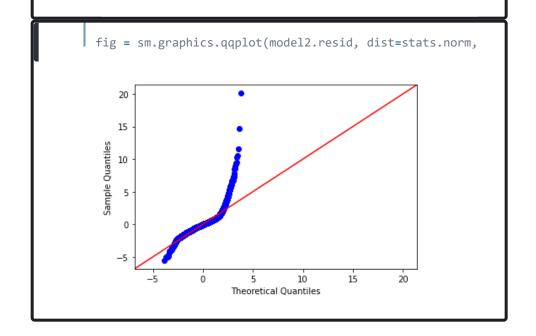
 Skew:
 2.514
 Prob(JB):
 0.00

 Kurtosis:
 28.326
 Cond. No.
 1.34e+06

Notes:

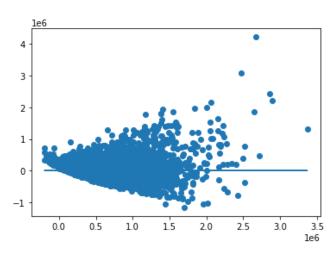
- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.34e+06. This might indicate that there are

strong multicollinearity or other numerical problems.



 $\label{lem:plt.scatter} $$ plt.scatter(model2.predict(train2[x_cols]), model2.resid $$ plt.plot(model2.predict(train2[x_cols]), [0 for i in ran) $$ and $$$

[<matplotlib.lines.Line2D at 0x1f95673ef40>]



Similar problems as last time, but our OLS has alerted us that there is strong collinearity. Let's investigate what we should remove.

```
X = df_col_drops[x_cols]
vif = [variance_inflation_factor(X.values, i) for i in r
list(zip(x_cols, vif))

[('bedrooms', 23.09608478897893),
    ('bathrooms', 24.591759875968087),
    ('sqft_living', 25.181513925621946),
    ('sqft_lot', 1.18527557276325),
    ('floors', 13.133195105016583),
    ('waterfront', 1.0252421775002192),
    ('condition', 29.533165474917077),
    ('grade', 124.69739326481557),
    ('yr_built', 124.82668596464562)]
```

Going to drop 'grade' and 'yr_built' from our model for the time being and go from there. You usually want to remove

variables with a cif of 10 or greater, incdicating that they are displaying multicollinearity with other variables in the feature set.

0.512

```
train2a, test2a = train_test_split(df_outlier_filter)

outcome = 'price'
x_cols = ['bedrooms', 'bathrooms', 'sqft_living', 'sqft_lot
predictors = '+'.join(x_cols)
formula = outcome + '~' + predictors
model2a = ols(formula=formula, data=train2a).fit()
model2a.summary()
```

Dep. Variable: price R-squared:

OLS Regression Results

Dop. variab	Dep. variable. price			11-34		luai ca.		0.012		
Model:		OLS	;		Adj. R- square			0.512		
Method:		Leas Squ		:S	F-statis	F-statistic:		2427.	2427.	
Date: Fri, 1 2021			Mar	*	Prob (F- statistic):					
Time:		10:0	5:2	28	Log- Likelih	ood:		-6739.	1	
No. Observation	No. Observations:		97		AIC:			1.349e	+04	
Df Residuals: 16		1618	39		BIC:			1.356e	+04	
Df Model:	Df Model: 7									
Covariance Type:	nonr		ob	ust						
	coe	f	s1 eı		t	P>	t	[0.025	0.975]	
Intercept	11.9	9256	0.	.022	552.526	0.0	00	11.883	11.968	
bedrooms	-0.0	612	0.004		-14.980	0.0	00	-0.069	-0.053	
bathrooms	0.0	371	0.	.006	5.888	0.0	00	0.025	0.050	
sqft_living	0.0	004	5.	.25e- 6	74.830	0.0	00	0.000	0.000	
sqft_lot	-1.6 07	69e-	6.	.85e- 8	-2.468	0.0	14	-3.03e- 07	-3.48e 08	
floors	0.0	893	0.	.006	13.983	0.0	00	0.077	0.102	
waterfront	0.5	934	0.	.035	17.050	0.0	00	0.525	0.662	
condition	0.0	875	0.	.005	18.884	0.0	00	0.078	0.097	
Omnibus:		5.73	30	Durk	oin-Watsor	ղ։	1.9	980		
Prob(Omnib	ous):	0.0	57	Jarq	ue-Bera (J	JB):	6.0	6.076		
Skew:		0.0	12	Prob	o(JB):		0.0	0.0479		
Kurtosis:		3.09	92	Con	d. No.		5.	51e+05		

Notes

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 5.51e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
train2b, test2b = train_test_split(df_outlier_filter)

x_cols = ['sqft_living','sqft_lot', 'floors','waterfront
predictors = '+'.join(x_cols)
formula = outcome + '~' + predictors
model2b = ols(formula=formula, data=train2b).fit()
model2b.summary()
```

OLS Regression Results

OLS Regress	OLS Regression Results								
Dep. Variab	le:	pric	е		R-squ	ared:	0.5	505	
Model:		OLS	8			Adj. R- squared:		0.505	
Method: Lea		Lea	st Squar	es	F-stat	istic:	33	07.	
		Fri, 202	19 Mar 1			(F- tic):	0.0	00	
Time: 10:0)5:28		Log- Likeli	hood:	-68	837.0		
No. Observations:		161	97	97		AIC:		1.369e+04	
Df Residuals: 10		161	91		BIC:		1.3	373e+04	
Df Model: 5		5							
Covariance Type:		non	robust						
	coef		std err	t		P> t	[0.025	0.975]	
Intercept	11.83	351	0.020	58	88.019	0.000	11.79	6 11.875	
sqft_living	0.000	04	3.45e- 06	10	8.001	0.000	0.000	0.000	
sqft_lot	-1.91 07	9e-	7.12e- 08	-2	.696	0.007	-3.316 07	e5.24e- 08	
floors	0.10	51	0.006	17	7.704	0.000	0.093	0.117	
waterfront	0.612	24	0.035	17	7.475	0.000	0.544	0.681	
condition	0.08	16	0.005	17	7.591	0.000	0.073	0.091	
Omnibus:		1.63	39 Dur k	oin-	Watsor	n: 2.0	028		

Notes:

Skew:

Kurtosis:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Prob(Omnibus): 0.441 Jarque-Bera (JB): 1.639

0.009 **Prob(JB)**:

2.954 **Cond. No.**

0.441

5.34e+05

[2] The condition number is large, 5.34e+05. This might

indicate that there are
strong multicollinearity or other numerical problems.

```
train2c, test2c = train_test_split(df_outlier_filter)

x_cols = ['sqft_living','sqft_lot','waterfront','conditi
predictors = '+'.join(x_cols)
formula = outcome + '~' + predictors
model2c = ols(formula=formula, data=train2c).fit()
model2c.summary()
```

OLS Regression Results

OLS Regress	DLS Regression Results									
Dep. Variab	ole:	price	Э			R-squa	red:	0.502		
Model:	Model: OL		;				Adj. R- squared:		0.502	
Method: Leas Square					F-statis	stic:	4081.			
Date:	Date: Fri, 202			lar		Prob (F		0.00		
Time:	10:0		5:29)		Log- Likelih	ood:	-7009.	4	
No. Observation	No. Observations:		97			AIC:		1.403e	+04	
Df Residua	Df Residuals: 1619		92	2 BIC :		1.407e	+04			
Df Model:	1: 4									
Covariance Type:	•	non	obu	st						
	coef	F	std	•	t		P> t	[0.025	0.975]	
Intercept	12.0	085	0.0	17	6	89.970	0.000	11.974	12.043	
sqft_living	0.00	04	3.2 06	6e-	1	22.372	0.000	0.000	0.000	
sqft_lot	-2.59 07	95e-	7.3 08	1e-	-;	3.548	0.000	-4.03e- 07	-1.16e 07	
waterfront	0.62	200	00 0.034		1	8.106	0.000	0.553	0.687	
condition	0.06	10	0.0	05	1	3.489	0.000	0.052	0.070	
Omnibus:		46.7	777	Du	rbi	in-Watso	on:	1.997		
Prob(Omnil	bus):	0.00	000 Jarqu		ıe-Bera (JB): 36		36.592	3.592		
Skew:		0.00)2	Pro	b((JB):	,	1.13e-08		

Notes:

Kurtosis:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2.767 **Cond. No.**

5.07e+05

[2] The condition number is large, 5.07e+05. This might

```
indicate that there are
   strong multicollinearity or other numerical problems.
X = df_{col_drops}[x_{cols}]
vif = [variance_inflation_factor(X.values, i) for i in r
list(zip(x_cols, vif))
    [('sqft_living', 5.2175232204298165),
     ('sqft_lot', 1.1680613101385844),
     ('waterfront', 1.0162448940537252),
     ('condition', 4.999908921746516)]
fig = sm.graphics.qqplot(model2c.resid, dist=stats.norm,
 Sample Quantiles
   -1
   -2
   -3
                      Theoretical Quantiles
plt.scatter(model2c.predict(train2c[x_cols]), model2c.re
plt.plot(model2c.predict(train2c[x_cols]), [0 for i in r
    [<matplotlib.lines.Line2D at 0x1f95685af70>]
   1.0
  0.5
  0.0
  -0.5
 -1.0
  -1.5
             13
  This is a modeling choice. There are pros and cons to this
  approach versus the first model. Removing multiple
 components has substantially diminished the model's
```

performance, as indicated by the r-squared value. However, multicollinearity between the features has been reduced.

Model 3

Going back to the drawing board, let's look at a multicolinearity heatmap to determine the columns to remove from our model.

```
first_features = ['sqft_living', 'grade', 'bathrooms', '
corr = df_col_drops[first_features].corr()
corr
```

	sqft_living	grade	bathrooms	sqft_lot
sqft_living	1.000000	0.762779	0.755758	0.173453
grade	0.762779	1.000000	0.665838	0.114731
bathrooms	0.755758	0.665838	1.000000	0.088373
sqft_lot	0.173453	0.114731	0.088373	1.000000
waterfront	0.104637	0.082818	0.063629	0.021459
floors	0.353953	0.458794	0.502582	-0.004814
condition	-0.059445	-0.146896	-0.126479	-0.008830
yr_built	0.318152	0.447865	0.507173	0.052946

sns.heatmap(corr, center=0, annot=True) <AxesSubplot:> - 1.0 0.17 0.1 0.35 -0.059 0.32 sqft_living 0.11 0.083 0.46 -0.15 0.45 grade - 0.6 0.088 0.064 0.5 bathrooms -0.76 0.67 1 -0.13 0.51 sqft_lot - 0.17 0.11 0.088 0.021-0.00480.00880.053 - 0.4 0.1 0.083 0.064 0.021 1 0.021 0.017 -0.024 waterfront -- 0.2 0.35 0.46 0.5 -0.00480.021 -0.26 0.49 - 0.0 -0.059 -0.15 -0.13 -0.00880.017 -0.26 condition -0.20.32 0.45 0.51 0.053 -0.024 0.49 -0.36 yr_built

> sqft_living and grade = 0.76 sqft_living and bathrooms = 0.76 grade and bathrooms = 0.67

Let's remove grade and bathrooms for this model. We will also use our previous outlier filter, as this seems to be a step in the right direction.

```
train3, test3 = train_test_split(df_outlier_filter)
x_cols = ['sqft_living', 'sqft_lot', 'waterfront', 'floo
predictors = '+'.join(x_cols)
formula = outcome + '~' + predictors
model3 = ols(formula=formula, data=train3).fit()
model3.summary()
```

OLS Regress	OLS Regression Results								
Dep. Variab	le:	price)		R-squa	red:	0.537		
Model:		OLS	;		Adj. R- square		0.537	0.537	
Mothod		Leas Squ			F-statis	stic:	3126.		
Date:	Date: Fri		19 Ma 1	ar	Prob (F statisti		0.00		
Time:	Time: 10:0		5:30		Log- Likelih	ood:	-6355.	8	
No. Observations:		1619	97		AIC:		1.273e	+04	
Df Residuals: 1		1619	90		BIC:		1.278e	+04	
Df Model:	Model: 6								
Covariance Type:	ļ	nonrok		t					
	coe	f	std err		t	P> t	[0.025	0.975]	
Intercept	19.1	667	0.23	1	83.101	0.000	18.715	19.619	
sqft_living	0.00	04	3.42 06	e-	115.938	0.000	0.000	0.000	
sqft_lot	-1.6 07	51e-	7.15 08	e-	-2.310	0.021	-3.05e- 07	-2.5e- 08	
waterfront	0.59	72	0.03	5	16.833	0.000	0.528	0.667	
floors	0.17	24	0.00	6	27.550	0.000	0.160	0.185	
condition	0.03	880	0.00	5	8.137	0.000	0.029	0.047	
yr_built	-0.0	037	0.00	0	-31.884	0.000	-0.004	-0.003	
Omnibus:		115	.168	Du	rbin-Wats	son:	2.011		
Prob(Omnil	bus):	0.00	00	Ja	rque-Bera	(JB):	141.348		
Skew:		-0.1	33	Pro	ob(JB):	2.03e-31			
Kurtosis:			Co	nd. No.		3.52e+06			

Notes:

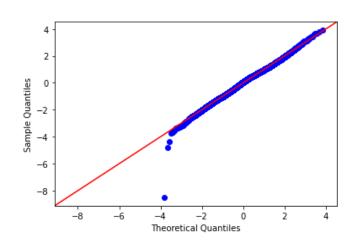
[1] Standard Errors assume that the covariance matrix of

the errors is correctly specified.

[2] The condition number is large, 3.52e+06. This might indicate that there are

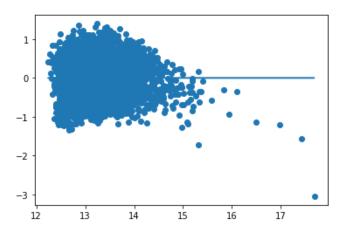
strong multicollinearity or other numerical problems.

fig = sm.graphics.qqplot(model3.resid, dist=stats.norm,



 $\label{lem:plt.scatter} $$ plt.scatter(model3.predict(train3[x_cols]), model3.resid $$ plt.plot(model3.predict(train3[x_cols]), [0 for i in ran transformation of the color of the color$

[<matplotlib.lines.Line2D at 0x1f94f8e4790>]

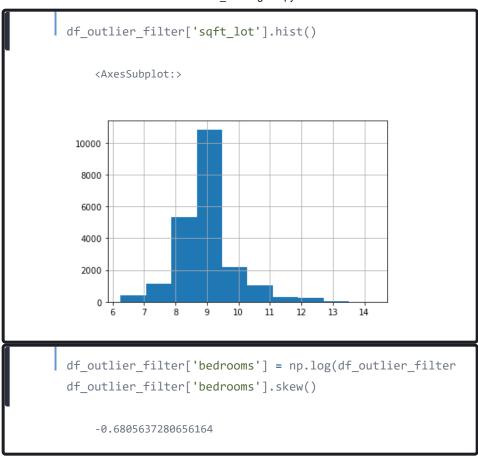


Model 4

Our QQ plots are less than ideal in previous models. Let's see if we can fix that by using a transform on the appropriate features.

```
for col_name in df_outlier_filter.columns[1:]:
    print(col_name)
    print(df_outlier_filter[col_name].skew())
 bedrooms
 2.023641235344595
 bathrooms
 0.5197092816403838
 sqft_living
 1.473215455425834
 sqft_lot
 13.072603567136046
 floors
 0.6144969756263127
 waterfront
 12.039584643829357
 condition
 1.0360374245132955
 grade
 0.7882366363846076
 yr_built
 -0.4694499764949978
```

'sqft_lot' seems to be the main issue with the highest skew coefficient. I'm not sure if I should apply this to waterfront. We may need to use another method here, or look elsewhere for model improvements.



```
x_cols = list(df_outlier_filter.columns)
x_cols.remove(outcome)

train4, test4 = train_test_split(df_outlier_filter)

predictors = '+'.join(x_cols)
formula = outcome + '~' + predictors
model4 = ols(formula=formula, data=train4).fit()
model4.summary()
```

OLS Regression Results

Dep. Variable:	price	R-squared:	0.646
Model:	OLS	Adj. R-squared:	0.645
Method:	Least Squares	F-statistic:	3275.
Date:	Fri, 19 Mar 2021	Prob (F- statistic):	0.00
Time:	10:05:31	Log-Likelihood:	-4151.9
No. Observations:	16197	AIC:	8324.
Df Residuals:	16187	BIC:	8401.
Df Model:	0		
	9		

Covariance

Type:

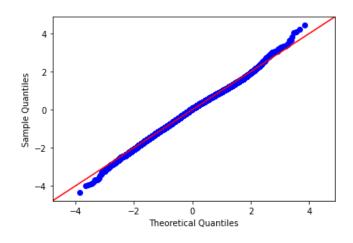
nonrobust

. 7 1								
	coef		std err		t	P> t	[0.025	0.975]
Intercept	22.0160		0.2	14	102.848	0.000	21.596	22.436
bedrooms	-0.1065		0.0	11	-9.635	0.000	-0.128	-0.085
bathrooms	0.0808		0.006		14.091	0.000	0.070	0.092
sqft_living	0.0002		5.7e- 06		36.097	0.000	0.000	0.000
sqft_lot	-0.0470		0.003		-14.600	0.000	-0.053	-0.041
floors	0.0520		0.006		8.578	0.000	0.040	0.064
waterfront	0.4809		0.031		15.731	0.000	0.421	0.541
condition	0.0458		0.004		11.110	0.000	0.038	0.054
grade	0.2273		0.004		63.858	0.000	0.220	0.234
yr_built	-0.0	-0.0056		000	-50.456	0.000	-0.006	-0.005
Omnibus:	Omnibus:		219 D u		rbin-Watson:		2.038	
Prob(Omnib	0.000		Ja	rque-Bera	(JB):	77.043		
Skew:		-0.1	-0.100		ob(JB):		1.86e-17	
Kurtosis:		3.273		Со	nd. No.		2.57e+05	

Notes:

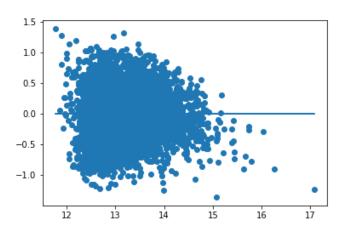
- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 2.57e+05. This might indicate that there are strong multicollinearity or other numerical problems.

fig = sm.graphics.qqplot(model4.resid, dist=stats.norm,



plt.scatter(model4.predict(train4[x_cols]), model4.resid
plt.plot(model4.predict(train4[x_cols]), [0 for i in ran

[<matplotlib.lines.Line2D at 0x1f95378cdc0>]



This is a nice improvement. This is our best model thus far. It passes the normality check from looking at the QQ plot and it is homoscedastic.

Interpreting this model:

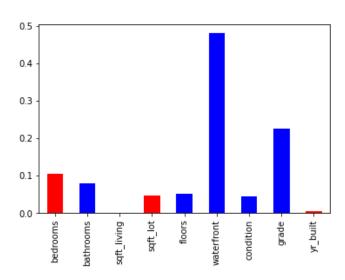
R-squared: 64.6% variation in the price can be explained by 'sqft_living', 'grade', 'bathrooms', 'sqft_lot', 'waterfront', 'floors', 'condition', 'yr built', and 'bedrooms'

Durbin-waton: A value preferred between 1-2 implies that the regression results are reliable from the side of homoscedasticity.

The highest coefficients belong to Grade and Waterfront: namely, what grade the home has been given by the King County Housing System. Additionally, having a waterfront view as a part of your home largely impacts the price.

When needed, we can now use this model to give us prediction values for an estimated price, given the values for the features of a home we are trying to sell. Obviously, someone would be unable to renovate their home to suddenly have a waterfront view, but doing something like adding a bathroom (the 3rd highest coefficient) seems to also have a significant impact of the expected price of a home for this model as well.

model4.params[1:].abs().plot.bar(color=['red','blue','bl



This is a visualization of our coefficients. To compare, I have taken the absolute value of each in the series, but made sure to indicate negative coefficients in red columns.

Conclusion

I believe the best model is Model 4, where the outliers have been filtered out and none of the features are removed . Although this suffers from multicollinearity, it has an r-squared value of ~0.647, which is the most accurate model in our analysis.

I believe this is acceptable within the context of this scenario. It affects the coefficients and p-values, but it does not influence the predictions, precision of the predictions, and the statistics determining goodness of fit. Our primary goal is to have a model to make predictions for us.

To further improve this, I would use more of the columns included in the original dataset to try to increase my r-squared value and hopefully fix the QQplot issues I was having for all of my models.