# Aol-Guaranteed Incentive Mechanism for Mobile Crowdsensing With Freshness Concerns

Yin Xu, Mingjun Xiao, Yu Zhu, Jie Wu, Sheng Zhang, Jinrui Zhou Published in: IEEE Transactions on Mobile Computing, 2024

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# **Agenda**

- 1. Overview
- 2. System Model
- 3. Problem Formulation
- 4. Characterizing AoI of Data
- 5. Bayesian Game
- 6. AoI guaranteed Incentive Mechanism (AIM)
- 7. DRL-based Incentive Mechanism (DIM)
- 8. Performance Evaluation
- 9. Conclusion
- 10. My Contribution

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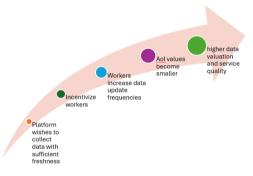
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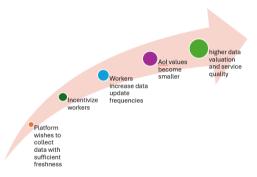
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  - Workers share their collected data with their social neighbors to obtain extra social benefits (i.e., additional utility from data sharing among workers).

# **Incentive Mechanism Challenges**

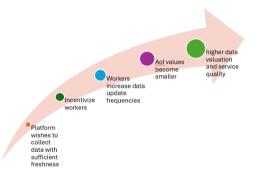


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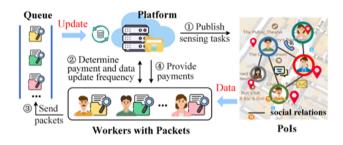
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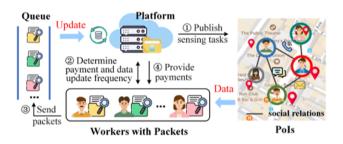
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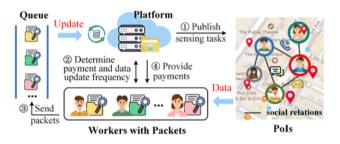
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- Demonstrate effectiveness of the proposed AIM and DIM mechanisms' performance using real-world traces simulation.

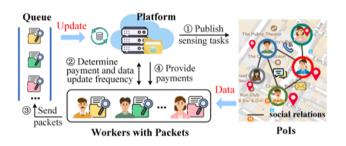




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Platform Utility Function:

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• Two-stage Stackelberg game,  $SG(p_i, R_i; \varphi)$ , where  $\varphi = \{s_i, a_i, b_i \mid \forall i \in \mathcal{N}\} \cup \{\eta, c, d\}$  is the set of all participants' parameters, with public (SPP) and unknown parameters (SUP).

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• Subject to:

$$\delta_i(p_i, P_{-i}) \leq \varepsilon, \quad \forall i \in N$$

$$\sum_{i=1}^n p_i \leq \hat{p}.$$

## AoI of Data for a Single Worker

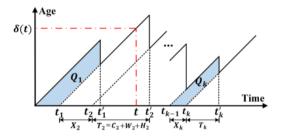
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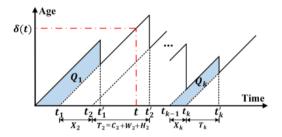
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$$\overline{\delta}^{\, au} = rac{1}{T} \left( Q_1 + \sum_{k=2}^{I(\mathcal{T})} Q_k + rac{\mathcal{T}_{I(\mathcal{T})}^2}{2} 
ight)$$

## Aol of Data for a Single Worker (continue)

$$(12) \overline{\delta}^T = \frac{1}{T} \left( Q_1 + \sum_{k=2}^{I(T)} Q_k + \frac{T_{I(T)}^2}{2} \right) = \frac{Q_1 + \frac{T_{I(T)}^2}{2}}{T} + \frac{I(T) - 1}{T} \cdot \frac{1}{I(T) - 1} \sum_{k=2}^{I(T)} Q_k$$

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 $p = \lim_{T \to \infty} \frac{I(T)}{T}$ , indicate the data update frequency in the steady state.

(14) 
$$\overline{\delta} = \lim_{T \to T} \overline{\delta}^T = p(\mathbb{E}[XT] + \mathbb{E}[X^2/2]).$$

# AoI of Data for a Single Worker (Plugging M/M/1)

For an M/M/1, FCFS queue with arrival rate p and service rate  $\mu$ , plus an added constant "collection time"  $\beta$  each time a service occurs:

- Effective service-time distribution has mean  $\beta + 1/\mu$ .
- Offered load:  $\rho = p(\beta + 1/\mu)$ .
- Mean system time (waiting + service):  $\mathbb{E}[T] = \frac{\beta + 1/\mu}{1-\rho}$ .
- Each update arrives after an exponentially distributed interarrival time X,  $\mathbb{E}[X] = \frac{1}{p}$ ,  $\mathbb{E}[X^2] = \frac{2}{p^2}$

$$\overline{\delta} = rac{(
ho-1)ig(
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where 
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$$\bar{\delta}_i = \frac{\alpha \beta_i}{\sum_{j \in \mathcal{N}_i} \mathsf{v}_{i,j}} + \frac{\mathsf{p}_i}{\mu^2 (1 - \rho_{-i})} \left[ \frac{\rho_i \rho_{-i}}{(1 - \rho_{-i})^2} + \frac{\rho_i / (1 - \rho)}{1 - \rho_{-i}} + \frac{\rho_{-i}}{\rho_i} \right] + \frac{1}{\mu} + \frac{1}{\mathsf{p}_i}$$

where 
$$\rho = \sum_{i=1}^N \rho_i, \quad \rho_i = \frac{p_i}{\mu}, \quad \text{and } \rho_{-i} = \sum_{i \neq i} \rho_j.$$

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N workers compete for the data update through an M/M/1 FCFS queue, in which each worker i's data update frequency, collection time, serving rate, and offered loads are  $p_i, \beta_i, \mu$ , and  $\rho_i$ , respectively. Then, the average AoI  $\bar{\delta}_i$  of worker i's data satisfies

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- A Bayesian Nash equilibrium is a strategy profile where each player's strategy maximizes their expected utility, given their beliefs about the other players' types and strategies.

## AoI guaranteed Incentive Mechanism (AIM)

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- 2. Solve the platform, leader (stage-1) game, to derive the optimal unit-remuneration  $R_i^*$  paid by the platform.

(3) 
$$\Omega_i(p_i, P_{-i}; s_i, a_i, b_i) = R(p_i) + \Psi_i(p_i, P_{-i}) - \Theta_i(p_i; s_i, a_i, b_i) = R_i p_i + \sum_{i \in N_i} \nu_{ij} p_i p_j - s_i \left(a_i p_i^2 + b_i p_i\right)$$

• Set social network influence  $\nu_{ij} = \nu$  for all i, j ( $i \neq j$ ).

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- Thus utility of the worker with degree f can be represented as follows:

$$\overline{\Omega}_f(p(f),P_{-f}) = R(f)p(f) + vp(f)f\overline{P_{-f}} - \left(ap^2(f) + bp(f)\right)s.$$

## Worker's (Follower) Optimal Strategy

#### Definition (Bayesian Nash Equilibrium (BNE))

A BNE is defined as a strategy profile that maximizes the expected payoff of each player for the given types and strategies performed by other players.

A strategy vector  $\Gamma = (\Gamma_1(\psi_1), \Gamma_2(\psi_2), \dots, \Gamma_N(\psi_N))$  is a Bayesian Nash Equilibrium if and only if the following condition is satisfied for each player i:

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#### Theorem (Follower's Optimal Strategy)

Given any unit remuneration R(f), the closed-form expression of the action (i.e., data update frequency) of the follower game is:

$$p(f) = \frac{1}{2as}R(f) - \frac{b}{2a} + \frac{vf(\overline{R} - bs)}{2as(2as - v\overline{f})},$$

where 
$$\overline{R} = \sum_{f \in G} \overline{F}(f) R(f)$$
 and  $\overline{f} = \sum_{f \in G} \overline{F}(f) f$ .

• Platform utility function when applying the configuration model:

$$\overline{\Phi} = \mathbb{E}[\Phi] = \mathbb{E}\left[\eta \sum_{i=1}^{N} \left(c p_i - d p_i^2\right) - \sum_{i=1}^{N} R_i p_i
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$$g(R(f)) = \delta_f(R(f)) - \epsilon \le 0,$$
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Finding optimal solution, using Lagrangian function:

$$\mathcal{L}(R(f),\zeta) = \overline{\Phi}(R(f)) + \zeta_1 g(R(f)) + \zeta_2 \widetilde{g}'(R(f)),$$
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- Since it is a convex optimization problem, the optimal solution must satisfy the Karush-Kuhn-Tucker (KKT) optimality conditions:

$$\begin{split} \frac{\partial \mathcal{L}}{\partial R(f)} \bigg|_{R(f) = R^*(f)} &= 0, \quad \zeta_1 g(R(f)) = 0, \quad \zeta_2 \tilde{g}'(R(f)) = 0, \\ g(R(f)) &\leq 0, \quad g'(R(f)) \leq 0, \quad \zeta_1 \geq 0, \quad \zeta_2 \geq 0. \end{split}$$

## Platform (Leader) Game With Constraints (continue)

Case 1:  $\zeta_1 = 0, \zeta_2 = 0$ , both constraints are inactive. Plus the sum over all  $l \neq f$ : the first-order derivative of  $\overline{\Phi}(R(f))$  be equal to zero:

$$\frac{\partial \overline{R}}{\partial R(f)} = \overline{F}(f), \quad \frac{\partial p(I)}{\partial R(f)} = \frac{\nu_I \overline{F}(f)}{2as(2as - \nu f)} = \Delta \overline{F}(f)I \quad (I \neq f),$$

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$$\frac{\partial \bar{\Phi}}{\partial R(f)} = NF(f) \left[ -p(f) + (\eta c - R(f) - 2\eta dp(f)) \left( \frac{1}{2as} + \Delta \overline{F}(f)f \right) \right] + N \sum_{l \neq f} F(l) \left[ (\eta c - R(l) - 2\eta dp(l)) \Delta \overline{F}(f)f \right] = 0.$$

#### Maximum Platform and Worker Utilities

Considering social network is seen as a configuration model with large numbers of workers, optimal unit remuneration:

$$R^*(f) = \frac{2a^2\tilde{s}^2}{(2as\Delta\overline{F}(f)f+1)(as+\eta d)+as} \left[\frac{b}{2a} - \Delta f(\overline{R}^*-bs)\right] + \left(\Delta\overline{F}(f)f + \frac{1}{2as}\right)$$
$$\left(\eta c + \frac{b\eta d}{a} - 2\Delta f \eta d(\overline{R}^*-bs)\right) + \Delta f\left[-\left(1 + \frac{\eta d}{as}\right)\frac{\Lambda^*}{f} + \frac{\eta(ac+bd)}{a} - 2\Delta \eta d(\overline{R}^*-bs)\overline{f}\right].$$

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The optimal data update frequency of worker i:

$$p_i^*(f) = \frac{1}{2\mathsf{a}\mathsf{s}}R^*(f) - \frac{\mathsf{b}}{2\mathsf{a}} + \frac{\nu f(\overline{R}^* - \mathsf{b}\mathsf{s})}{2\mathsf{a}\mathsf{s}(2\mathsf{a}\mathsf{s} - \nu \overline{f})}$$

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Maximum Platform and Worker Utilities:

$$\Phi^* = N \sum_{f \in C} F(f) \left[ (\eta c - R^*(f)) p^*(f) - \eta d(p^*(f))^2 \right].$$

$$\Omega_i^* = R^*(f)p^*(f) + \nu p^*(f)fP_{-f} - \left(a(p^*(f))^2 + bp^*(f)\right)s.$$

#### **AoL Constraint Active**

Case 2:  $\zeta_1 \neq 0, \zeta_2 = 0$ , AoI constraint  $g(R(f)) = \delta_f(R(f)) - \epsilon \leq 0$  is active.

$$g(R(f)) = \frac{\alpha\beta}{f\nu} + \frac{p^2(f)}{\mu^2\check{\rho}} \left( \frac{\rho_{-i}(f)}{\mu(\check{\rho})^2} + \frac{1}{\check{\rho}\mu(1-\rho(f))} + \frac{\rho_{-i}(f)\mu}{p^2(f)} \right) + \frac{1}{\mu} + \frac{1}{p(f)} - \epsilon = 0,$$

where:

- $\breve{\rho} = 1 \rho_{-i}(f)$  represents the remaining service capacity.
- $\rho(f) = \frac{\sum_{f} p(f)}{\mu}$  is the total offered load.
- $\rho_{-i}(f) = \frac{\sum_f \rho(f) \rho(f)}{\mu}$  represents the load from other workers.

Since g(R(f)) depends on p(f), and p(f) is determined by R(f), combine the derivative of the utility function with the derivative of the AoI constraint to ensure both are met:

$$\frac{\partial \bar{\Phi}}{\partial R(f)} + \frac{\partial g}{\partial R(f)} = 0.$$

### **Total Data Update Frequency Constraint Active**

Case 3:  $\zeta_1 = 0, \zeta_2 \neq 0$ , total data update frequency constraint  $g'(R(f)) = \sum_f F(f)p(f) - \hat{p} \leq 0$  is active,

and the system needs to adjust R(f) and p(f) to bring it back within bounds.

$$L(R(f),\zeta_2) = \bar{\Phi}(R(f)) + \zeta_2 g'(R(f)), \text{ where } g'(R(f)) = \sum_f F(f) p(f) - \hat{p}.$$

For optimal  $R^*(f)$  derivative the Lagrangian with respect to R(f) and set it to zero:

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$$\frac{\partial \bar{\Phi}}{\partial R(f)} + \zeta_2 \frac{\partial g'}{\partial R(f)} = 0.$$

$$R^*(f) = rac{as(\eta c - bs + \zeta_2)}{2as + \eta d} \left(1 - rac{f}{f}
ight) + rac{2asf \hat{p}}{Nf} + bs - 2as\Delta f(\overline{R} - bs),$$

where:

- $\bar{f} = \sum_{f} F(f)f$  is the average degree,
- $\hat{p}$  is the threshold for total update frequency.
- $\zeta_2$  is determined by solving g'(R(f)) = 0.

#### **Activating Both Constraints**

**Case 4:**  $\zeta_1 \neq 0, \zeta_2 \neq 0$ , AoL and total data update frequency constraints are active.

$$\frac{\partial \bar{\Phi}}{\partial R(f)} + \zeta_1 \frac{\partial g}{\partial R(f)} + \zeta_2 \frac{\partial g'}{\partial R(f)} = 0,$$

along with: g(R(f)) = 0, g'(R(f)) = 0.

- Solving this system is complex because of nonlinearity of functions and the interdependencies between constraints and the utility function.
- Numerical methods (e.g., Bisection, Newton's, etc.) are employed to approximate.
- Iterative Process.

#### The Aol-Guaranteed Incentive Mechanism (AIM)

12 else

13

14

15

if  $\sum_{i=1}^{N} p_i \leq \hat{p}$  then

else Solving Eq. (43)  $\Rightarrow R^*(f)$ ;

#### Algorithm 1: The AoI-Guaranteed Incentive Mechanism. **Input**: degree distribution F(f), worker i's degree f, and some public parameters a, b, c, d, n, s: **Output:** $R^*(f)$ , $p^*(f)$ , $\Phi^*$ , and $\Omega_i^*$ ; 1 Platform: Determine its tentative optimal strategy (i.e., the unit-remuneration $R^*(f)$ ) according to Eq. (37); 2 for each worker $i, i \in \mathcal{N}$ do Determine its tentative optimal strategy (i.e., the data update frequency $p_i^*(f)$ based on $R^*(f)$ and Eq. (38); 4 if $\delta_i(p_i, P_{-i}) < \varepsilon$ for $\forall i$ then if $\sum_{i=1}^{N} p_i \leq \hat{p}$ then Platform: Obtain $\Phi^*$ according to Eq. (39); Worker i: Obtain $\Omega_i^*$ according to Eq. (40); else Solving Eq. (42) and $g'(R(f)) = 0 \Rightarrow R^*(f)$ ; Platform: Update its strategy as $R^*(f)$ ; Worker i: Update $p_i^*(f)$ based on $R^*(f)$ ; 10 Calculate $\Phi^*$ and $\Omega^*$ based on Eqs. (39) and (40): 11

Solving Eq. (41) and  $\partial \mathcal{L}/\partial R(f) = 0 \Rightarrow R^*(f)$ ;

Platform and Workers: Update  $p_i^*(f), R^*(f), \Phi^*, \Omega_i^*$ ;

#### The BNE Analysis

#### Lemma 1: The follower game has at least one pure Bayesian Nash Equilibrium (BNE).

Proof: if the Bayesian sub-game satisfies the (Milgrom-Shannon) Single Crossing Property of Incremental Returns (SCP-IR), the Bayesian subgame has at least one pure BNE.

 The partial derivative of the follower's payoff function with respect to their strategy p<sub>i</sub> and others' strategies P<sub>-i</sub> is:

$$\frac{\partial^2 \bar{\Omega}_i(p_i, P_{-i}, R)}{\partial p_i \partial P_{-i}} = \nu f > 0.$$

This indicates that the payoff increases with others' strategies.

• The second-order partial derivative with respect to  $p_i^2$  is:

$$\frac{\partial^2 \bar{\Omega}_i(p_i, P_{-i}, R)}{\partial p_i^2} = -2as < 0,$$

confirming concavity of the payoff with respect to  $p_i$ , which satisfies the SCP-IR.

### The BNE Analysis (continue)

#### Lemma 2: Uniqueness of the Bayesian Nash Equilibrium

The Bayesian sub-game has at most one BNE if the following condition is satisfied:

$$\left|\left(\frac{\partial^2 \overline{\Omega}_i \big(p_i, P_{-i}, \mathcal{R}\big)}{\partial p_i \, \partial P_{-i}}\right) / \left(\frac{\partial^2 \overline{\Omega}_i \big(p_i, P_{-i}, \mathcal{R}\big)}{\partial p_i^2}\right)\right| < 1, \quad \forall \, i \in \mathcal{N}.$$

The left-hand side represents the interaction between the strategies of player i and others.

If the interaction is sufficiently weak, the uniqueness of the equilibrium is guaranteed.

Result: When the condition  $\nu f_{\text{max}} - 2as < 0$  is met, the uniqueness of the BNE is ensured.

## The BNE Analysis (continue)

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The Bayesian sub-game has at most one BNE if the following condition is satisfied:

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Result: When the condition  $\nu f_{\text{max}} - 2as < 0$  is met, the uniqueness of the BNE is ensured.

Stackelberg Game Equilibrium: The leader in the Stackelberg game can optimize their strategy with the certainty that the followers' response is unique and predictable (as derived from Lemmas 1 and 2).

#### **Unique Stackelberg Equilibrium**

#### Theorem (Unique Stackelberg Equilibrium)

The optimal incentive strategy  $\langle p^*(f), R^*(f) \rangle$  determined by AIM constitutes the unique Stackelberg equilibrium while satisfying AoI constraints.

#### Uniqueness of Equilibrium

- In Stage I,  $R^*(f)$  is derived as the unique optimal solution for the platform's utility maximization.
- In Stage II,  $p^*(f)$  forms a unique Bayesian Nash Equilibrium (BNE), as shown in the equilibrium analysis.

Together, these ensure that the entire Stackelberg game has a unique equilibrium.

#### Aol Constraints

The AoI constraint,  $g(R(f)) = \delta_f(R(f)) - \epsilon \le 0$ , ensures that the age of information for workers' data is below a specified threshold. This constraint is satisfied as part of the incentive mechanism design, ensuring that all workers' data meet the freshness requirement.

• DRL-based Incentive Mechanism (DIM) with AoI guarantees to address the SUP problem, where the platform and workers have no prior knowledge of the Stackelberg game.

- DRL-based Incentive Mechanism (DIM) with AoI guarantees to address the SUP problem, where the platform and workers have no prior knowledge of the Stackelberg game.
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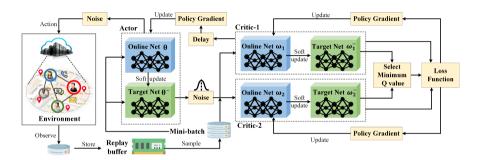
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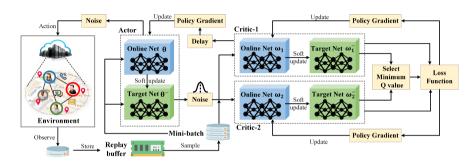
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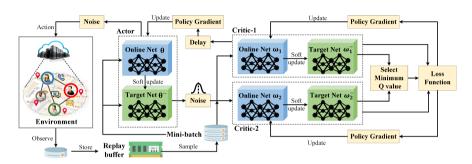
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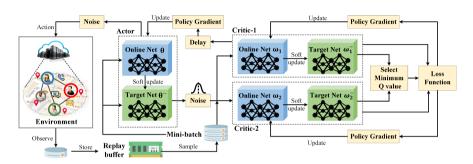




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- Random noise promotes more diverse exploration and reduces the tendency to exploit a single action.

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- The experience (i.e., current state, action, reward, and next state) is saved in the finite-size replay buffer, which used for the network update.

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- Reward Function:

$$\Upsilon(\mathbf{s}^t, \mathcal{R}^t) = \varrho_1 \Phi(P^t, \mathcal{R}^t) - \varrho_2 \left[ \frac{\sum_{i=1}^N \rho_i^t - \hat{\rho}}{\hat{\rho}} \right]^+ - \varrho_3 \sum_{i=1}^N \left[ \frac{\delta_i^t - \epsilon}{\epsilon} \right]^+,$$

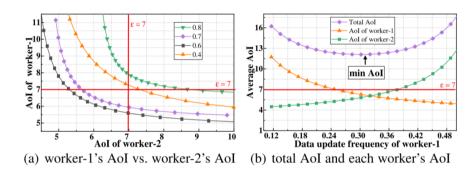
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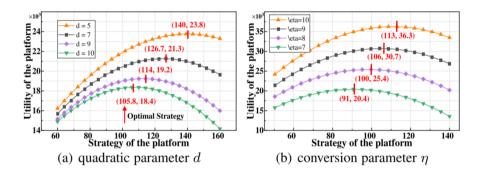
#### **Evaluation of Aol**



**Evaluating AoI**: two workers, fixed total load  $\rho_1 + \rho_2 = \hat{\rho}$ .

- (a) AoI value of worker-1 decreases with the increase of worker-2's AoI value.
- (b) AoI optimization problem depends on both the total load  $\hat{\rho}$  and the allocation of data update frequency among workers.

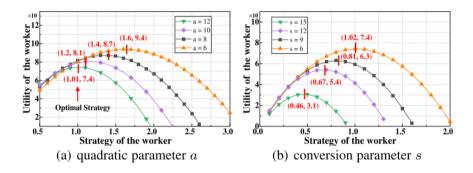
## **Evaluation of AIM - Platform**



Evaluating AIM: Platform Strategy Vs. Utility with different parameters.

- PU will always find a maximum point.
- A small d or a larger  $\eta$  will result in the growth of the optimal PS and the optimal PU.

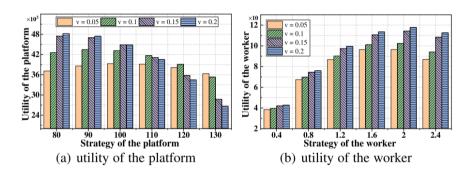
## **Evaluation of AIM - Worker**



**Evaluating AIM**: Worker Strategy Vs. Utility with different parameters.

- WU find a maximum point.
- worker's utility increase when applying a smaller a or s since the cost of the worker becomes smaller.

## **Evaluation of Social Network Effect**

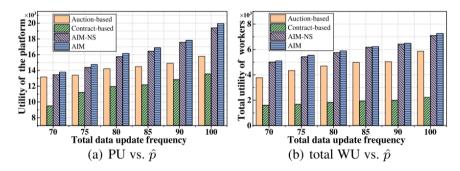


#### **Evaluating Influence of social network effects:**

• Enlarging social network effect coefficient v from 0.05 to 0.2, enables both the worker and platform to achieve higher utility.

## **Evaluation of Different Incentive Mechanisms**

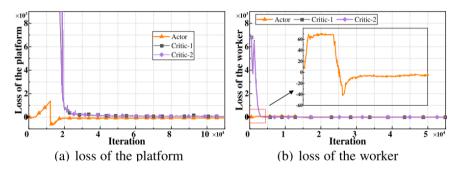
#### **Evaluation of Different Incentive Mechanisms:**



• When  $\hat{p} = 100$ , the achieved PU of AIM is about 47.3% and 26.4% higher than those of the contract-based and auction-based algorithms on average, respectively.

## **Evaluation of DIM Conversion**

### **Evaluation of DIM Conversion via training loss:**



 Both the actor network and two critic networks of the platform tend to a stable state as the training time increases.

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#### **Performance Evaluation:**

- Experiments with real-world data validate the efficacy of AIM and DIM.
- Both mechanisms outperform baseline methods in utility optimization and AoI guarantee.

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