

# Project report – Calcul scientifique

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# 1 Limitations of the power method

We test with matrices of the following shapes

$$\mathbf{1} \begin{pmatrix}
1 & & & & (0) \\
 & 2 & & & \\
 & & 3 & & \\
 & & & \ddots & \\
 & & & & n
\end{pmatrix}$$

2 diag(random(1e-10, 1))

**3** diag 
$$\left( (10^5)^{-\frac{i-1}{n-1}} \right)_{i \in [\![1,n]\!]}$$

4 diag 
$$\left(1 - (1 - 10^{-2})\frac{i-1}{n-1}\right)_{i \in [\![1,n]\!]}$$

| Type / Alg | 1                | 2               | 3               | 4                |
|------------|------------------|-----------------|-----------------|------------------|
| eig(10)    | $20\mathrm{ms}$  | $0\mathrm{ms}$  | $10\mathrm{ms}$ | $10\mathrm{ms}$  |
| power(11)  | $1.77\mathrm{s}$ | $40\mathrm{ms}$ | $60\mathrm{ms}$ | $1.81\mathrm{s}$ |
| power(12)  | $0.9\mathrm{s}$  | $60\mathrm{ms}$ | $60\mathrm{ms}$ | $0.93\mathrm{s}$ |
| v0 (0)     |                  |                 |                 |                  |

Table 1: Computation time comparisons

#### 1.1 Main computing time drawback of the improved deflation method

power\_v12 is slower than power\_v11 on matrices of type 2 (diagonal matrices of random floating point values close to zero). It is twice as fast on matrices of type 1 or 4.