

Confidence and lift

MARKET BASKET ANALYSIS IN PYTHON



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When support is misleading

TID	Transaction
1	Coffee, Milk
2	Bread, Milk, Orange
3	Bread, Milk
4	Bread, Milk, Sugar
5	Bread, Jam, Milk
...	...

1. **Milk and bread frequently purchased together.**
 - Support: $\{\text{Milk}\} \rightarrow \{\text{Bread}\}$
2. **Rule is not informative for marketing.**
 - Milk and bread are both popular items.

The confidence metric

1. Can improve over **support** with additional metrics.
2. Adding **confidence** provides a more complete picture.

$$\frac{Support(X \& Y)}{Support(X)}$$

Interpreting the confidence metric

TID	Transaction
1	Coffee, Milk
2	Bread, Milk, Orange
3	Bread, Milk
4	Bread, Milk, Sugar
5	Bread, Jam, Milk

$$\text{Support}(\text{Milk} \& \text{Coffee}) = 0.20$$

TID	Transaction
1	Coffee, Milk
2	Bread, Milk, Orange
3	Bread, Milk
4	Bread, Milk, Sugar
5	Bread, Jam, Milk

$$\text{Support}(\text{Milk}) = 1.00$$

Interpreting the confidence metric

$$\frac{\textit{Support}(\textit{Milk\&Coffee})}{\textit{Support}(\textit{Milk})} = \frac{0.20}{1.00} = 0.20$$

$$\frac{\textit{Support}(\textit{Milk\&Coffee})}{\textit{Support}(\textit{Milk})} = \frac{0.20}{0.80} = 0.25$$

$$\frac{\textit{Support}(\textit{Milk\&Coffee})}{\textit{Support}(\textit{Milk})} = \frac{0.20}{0.20} = 1.00$$

The lift metric

- **Lift provides another metric for evaluating the relationship between items.**
 - **Numerator:** Proportion of transactions that contain X and Y.
 - **Denominator:** Proportion if X and Y assigned randomly and independently.

$$\frac{\textit{Support}(X \& Y)}{\textit{Support}(X)\textit{Support}(Y)}$$

Preparing the data

```
from mlxtend.preprocessing import TransactionEncoder
import pandas as pd

# Split library strings into lists
libraries = data['Library'].apply(lambda t: t.split(','))

# Convert to list of lists
libraries = list(libraries)

# One-hot encode books
books = TransactionEncoder().fit(libraries).transform(libraries)

# Convert one-hot encoded data to DataFrame
books = pd.DataFrame(books, columns = encoder.columns_)
```

Computing confidence and lift

```
# Print first five items  
print(books.head())
```

	Hunger	Gatsby
0	False	True
1	False	True
2	False	False
3	False	True
4	False	True

Dataset: GoodBooks-10K.

Computing confidence and lift

```
# Computing support.  
supportHG = np.logical_and(books['Hunger'], books['Gatsby']).mean()  
supportH = books['Hunger'].mean()  
supportG = books['Gatsby'].mean()
```

```
# Compute and print confidence and lift.  
confidence = supportHG / supportH  
lift = supportHG / (supportH * supportG)
```

```
# Print results.  
print(supportG, confidence, lift)
```

```
(0.30, 0.16, 0.53)
```

Let's practice!

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Leverage and conviction

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Building on simpler metrics

$$\textit{Support}(X) = \frac{\textit{Frequency}(X)}{N}$$

$$\textit{Support}(X \rightarrow Y) = \frac{\textit{Frequency}(X \& Y)}{N}$$

$$\textit{Confidence}(X \rightarrow Y) = \frac{\textit{Support}(X \rightarrow Y)}{\textit{Support}(X)}$$

$$\textit{Lift}(X \rightarrow Y) = \frac{\textit{Support}(X \rightarrow Y)}{\textit{Support}(X)\textit{Support}(Y)}$$

The leverage metric

- Leverage also builds on **support**.

$$\text{Leverage}(X \rightarrow Y) =$$

$$\text{Support}(X \& Y) - \text{Support}(X)\text{Support}(Y)$$

- Leverage is similar to lift, but **easier to interpret**.
- Leverage **lies in -1 and +1 range**.
 - **Lift** ranges from 0 to infinity.

Computing leverage

```
# Compute support for Twilight and Harry Potter
supportTP = np.logical_and(books['Twilight'], books['Potter']).mean()

# Compute support for Twilight
supportT = books['Twilight'].mean()

# Compute support for Harry Potter
supportP = books['Potter'].mean()

# Compute and print leverage
leverage = supportTP - supportP * supportT
print(leverage)
```

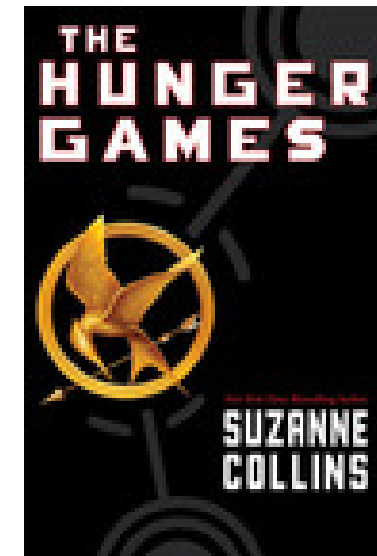
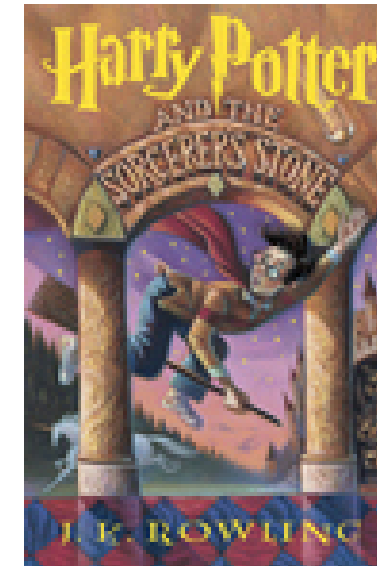
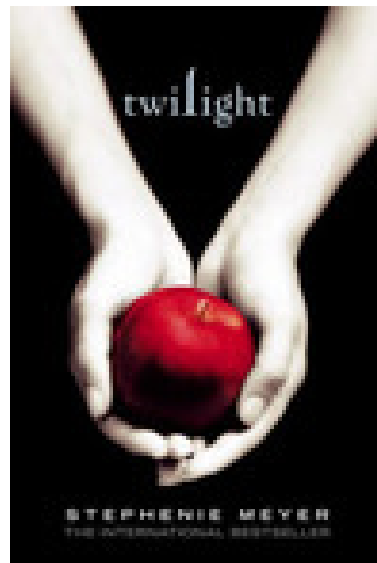
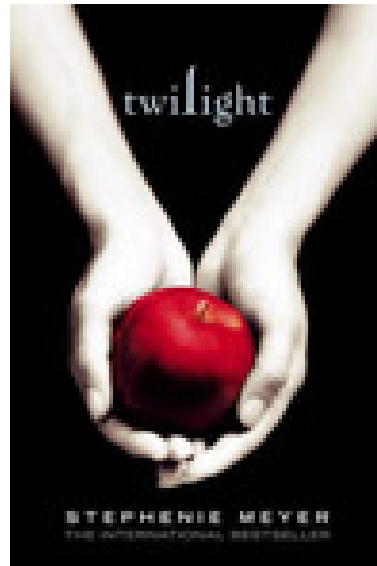
```
0.018
```

The conviction metric

1. **Conviction** is also built using support.
2. More complicated and less intuitive than **leverage**.

$$\text{Conviction}(X \rightarrow Y) = \frac{\text{Support}(X) \text{Support}(\bar{Y})}{\text{Support}(X \& \bar{Y})}$$

Interpreting conviction



¹ Images taken from goodreads.com.

Computing conviction

```
# Compute support for Twilight and Harry Potter and Twilight
supportTP = np.logical_and(books['Twilight'], books['Potter']).mean()
supportT = books['Twilight'].mean()
```

```
# Compute support for NOT Harry Potter
supportnP = 1.0 - books['Potter'].mean()
```

```
# Compute support for Twilight and NOT Harry Potter
supportTnP = supportT - supportTP
```

```
# Compute conviction
conviction = supportT*supportnP / supportTnP
print(conviction)
```

1.16

Let's practice!

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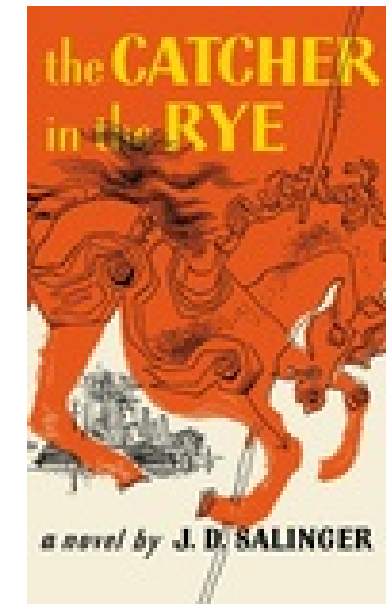
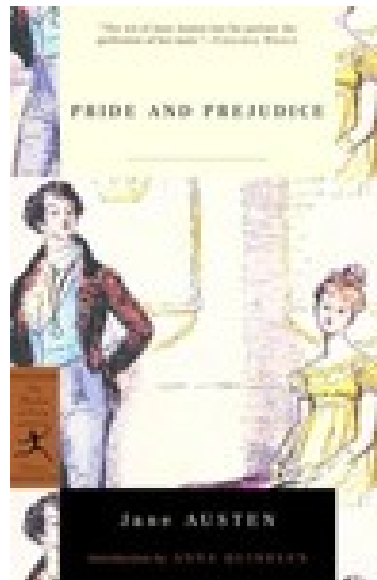
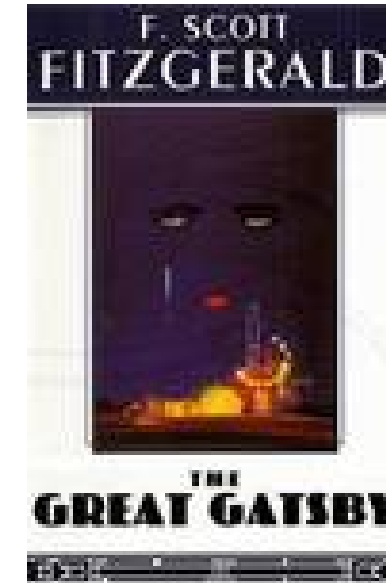
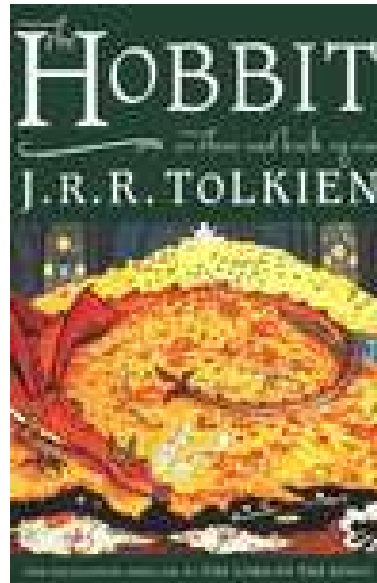
Association and dissociation

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Using dissociation to pair ebooks



¹ Images taken from goodreads.com.

Introduction to Zhang's metric

1. Introduced by Zhang (2000)

- Takes values between -1 and +1
- Value of +1 indicates perfect association
- Value of -1 indicates perfect dissociation

2. Comprehensive and interpretable

3. Constructed using support

¹ Zhang, T. (2000). Association Rules. Proceedings of the 4th Pacific-Asia conference, PADKK, pp.245-256. Kyoto, Japan.

Defining Zhang's metric

$$Zhang(A \rightarrow B) = \frac{Confidence(A \rightarrow B) - Confidence(\bar{A} \rightarrow B)}{Max[Confidence(A \rightarrow B), Confidence(\bar{A} \rightarrow B)]}$$

$$Confidence = \frac{Support(A \& B)}{Support(A)}$$

Constructing Zhang's metric using support

$$Zhang(A \rightarrow B) =$$

$$\frac{Support(A \& B) - Support(A)Support(B)}{Max[Support(AB)(1 - Support(A)), Support(A)(Support(B) - Support(AB))]}$$

Computing Zhang's metric

```
# Compute the support of each book
```

```
supportH = hobbit.mean()
```

```
supportP = pride.mean()
```

```
# Compute the support of both books
```

```
supportHP = np.logical_and(hobbit, pride).mean()
```


Computing Zhang's metric

```
# Compute the numerator
```

```
num = supportHP - supportH*supportP
```

```
# Compute the denominator
```

```
denom = max(supportHP*(1-supportH), supportH*(supportP-supportHP))
```

```
# Compute Zhang's metric
```

```
zhang = num / denom
```

```
print(zhang)
```

```
0.08903
```

Let's practice!

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Advanced rules

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Overview of market basket analysis

- **Standard procedure for market basket analysis.**
 1. Generate large set of rules.
 2. Filter rules using metrics.
 3. Apply intuition and common sense.

Generating rules

- **Number of rules grows exponentially in number of items.**
 - Most rules are not useful.
- **Must apply initial round of filtering.**
 - Covered in chapter 3 using Apriori algorithm

How does filtering work?

ID	antecedents	consequents	support	Lift
1	Harry Potter	The Hunger Games	0.001	1.01
2	Hunger Games	Twilight	0.020	1.23
3	Pride and Prejudice	The Hobbit	0.030	1.05
4	The Hobbit	Twilight	0.015	0.85
5	Harry Potter	The Hobbit	0.010	1.07

Multi-metric filtering

ID	antecedents	consequents	support	zhang
1	Harry Potter	The Hunger Games	0.001	-0.05
2	Hunger Games	Twilight	0.020	0.17
3	Pride and Prejudice	The Hobbit	0.030	0.06
4	The Hobbit	Twilight	0.015	-0.04
5	Harry Potter	The Hobbit	0.010	0.34

Performing multi-metric filtering

```
print(rules.head())
```

	antecedents	consequents	antecedent support	...	support	confidence	...	conviction
0	Potter	Hunger	0.48	...	0.12	0.26	...	0.92
1	Potter	Hunger	0.32	...	0.12	0.26	...	0.92
2	Twilight	Hunger	0.26	...	0.09	0.35	...	1.04
3	Hunger	Twilight	0.32	...	0.09	0.28	...	1.03
4	Mockingbird	Hunger	0.48	...	0.10	0.20	...	0.85

Performing multi-metric filtering

```
# Select subset of rules with low consequent support.  
rules = rules[rules['consequent support'] < 0.05]  
print(len(rules))
```

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```
# Select subset of rules with lift > 1.5.  
rules = rules[rules['lift'] > 1.5]  
print(len(rules))
```

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Let's practice!

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