Spatial transformations

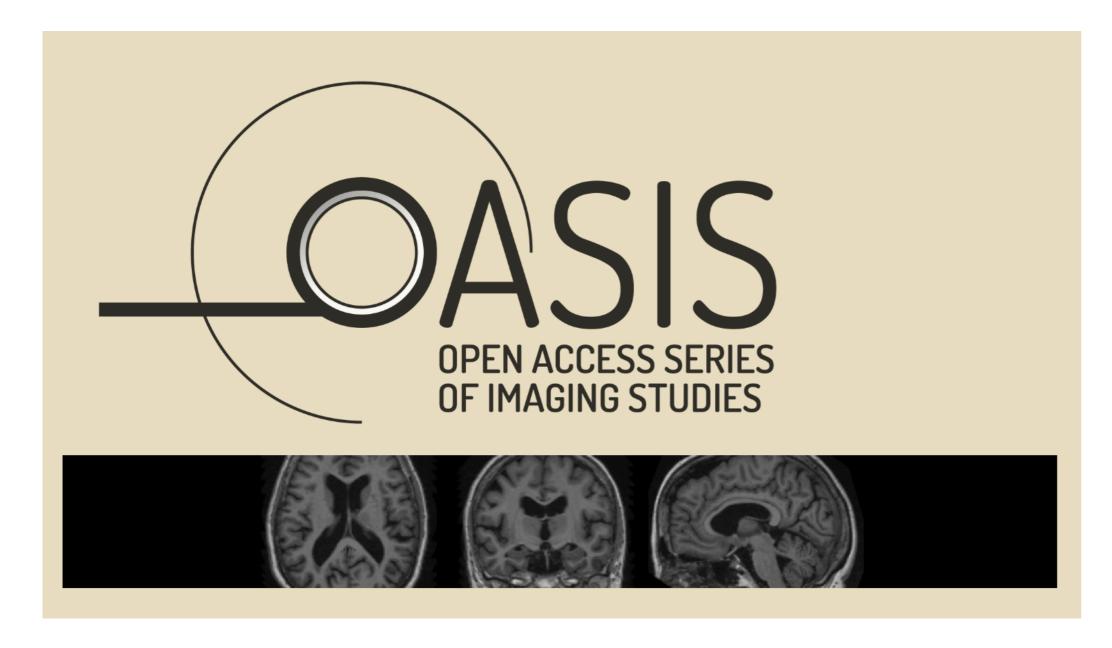
BIOMEDICAL IMAGE ANALYSIS IN PYTHON



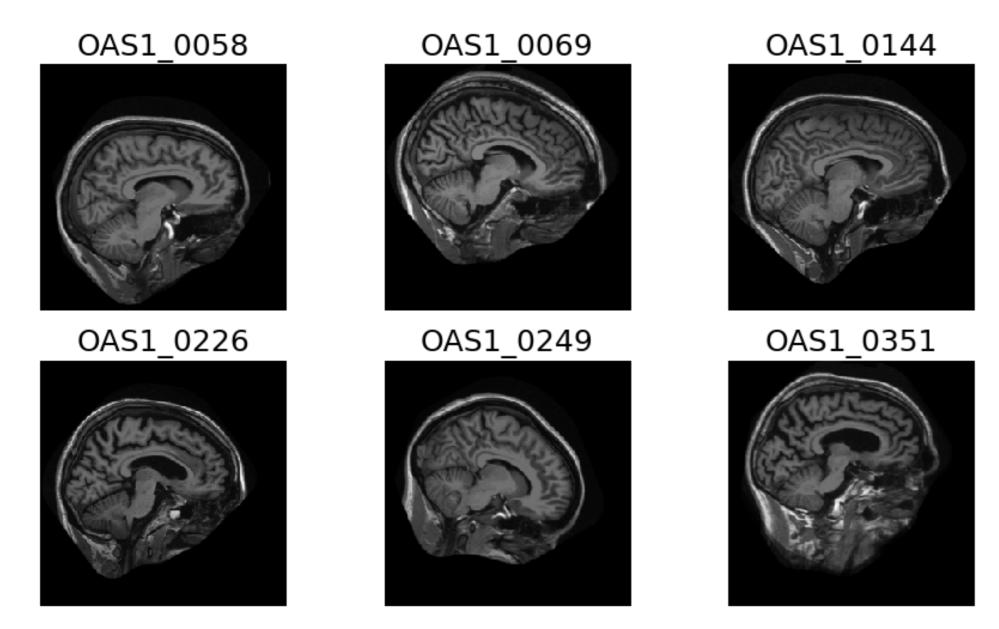
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Instructor



OASIS Database

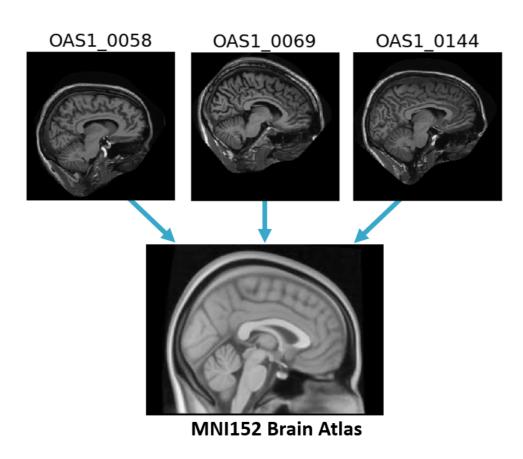


Significant variability

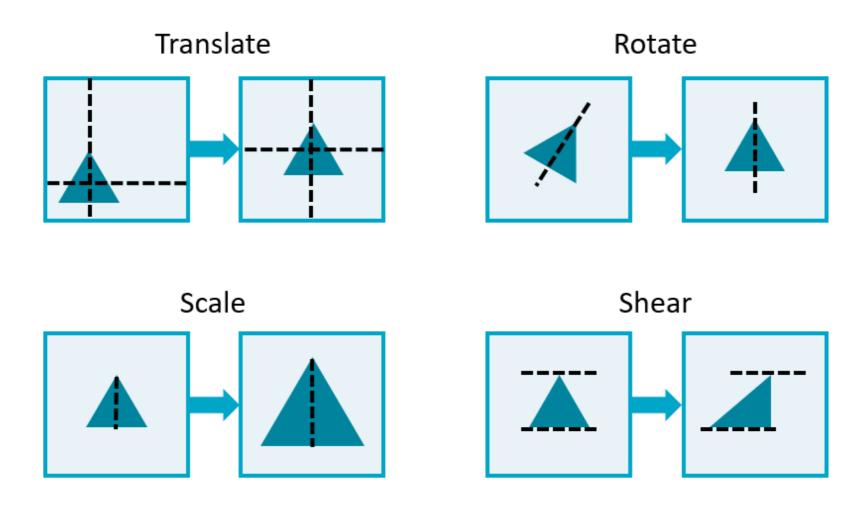


Registration

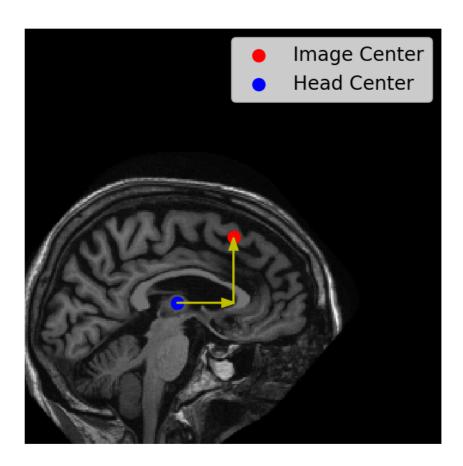
- Align images to template
- Minimize spatial variability
- Templates:
 - may represent multiple subjects
 - may be an "average" image
- Entails many spatial transformations



Affine transformations preserve points, lines, and planes



Translation



```
import imageio
import scipy.ndimage as ndi
im=imageio.imread('OAS1036-2d.dcm')
im.shape
```

(256, 256)

Rotation

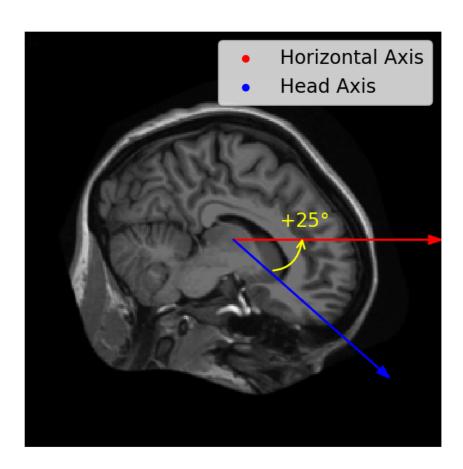


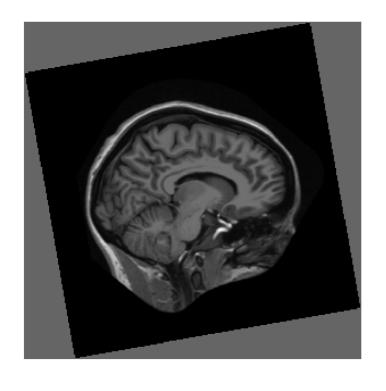
Image rotation

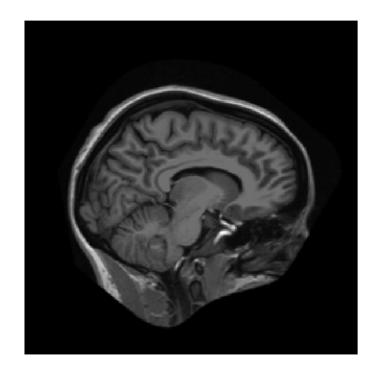
xfm = ndi.rotate(im, angle=25)

xfm.shape

(297, 297)

(256, 256)

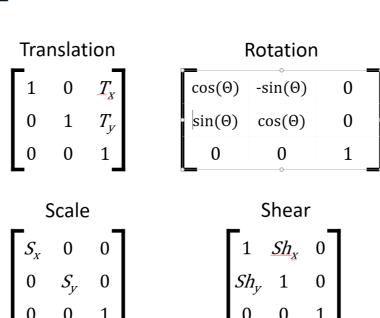




Transformation matrix

Transformation matrix: applied to one image for registration.

Elements of the matrix encode "instructions" for different affine transformations.



Applying a transformation matrix

Translate

Rotate

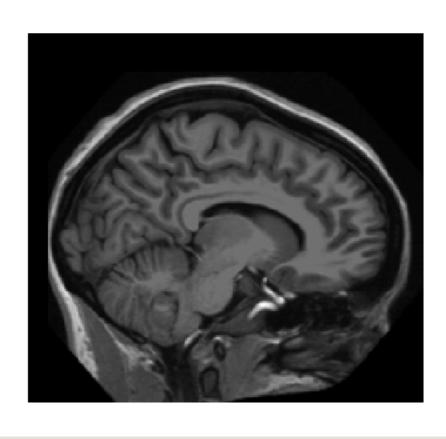
$$\begin{array}{cccc} \cos(\Theta) & -\sin(\Theta) & & 0 \\ \sin(\Theta) & \cos(\Theta) & & 0 \\ & 0 & & 0 & & 1 \end{array}$$

Scale

$$egin{array}{cccc} S_{_{\! X}} & 0 & 0 \ 0 & S_{_{\! Y}} & 0 \ 0 & 0 & 1 \ \end{array}$$

Shear

$$\begin{bmatrix}
 1 & Sh_x & 0 \\
 Sh_y & 1 & 0 \\
 0 & 0 & 1
 \end{bmatrix}$$



Let's practice!

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Resampling and interpolation

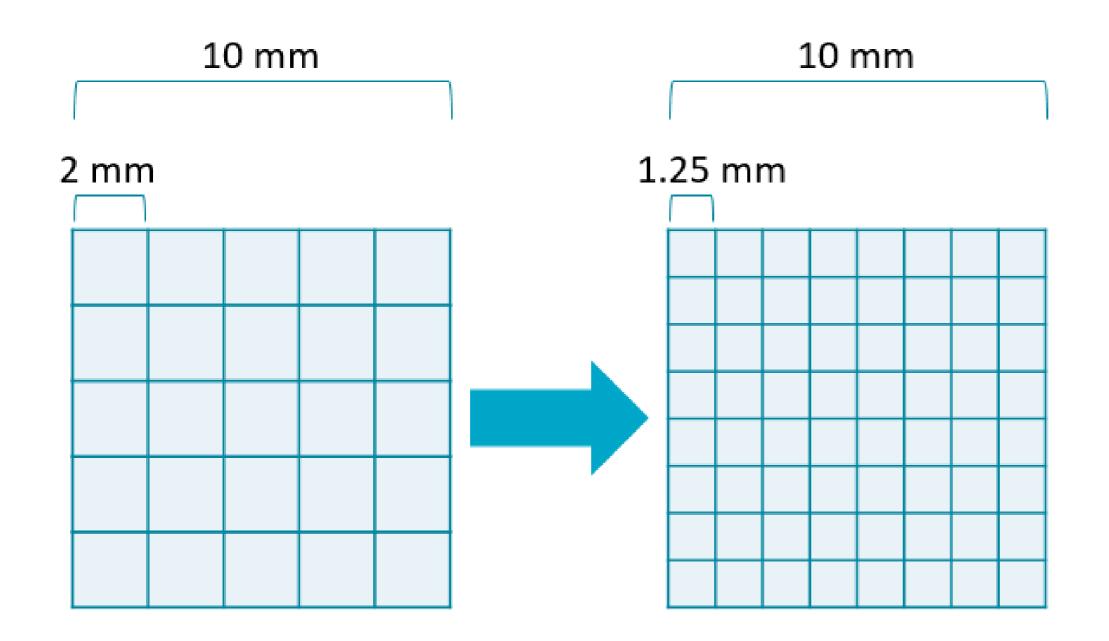
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Resampling changes the array shape



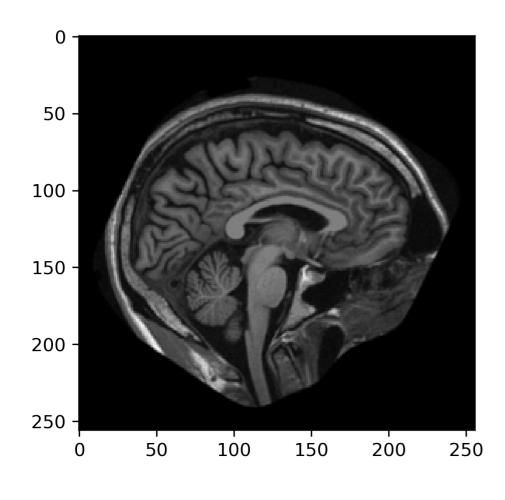
Downsampling

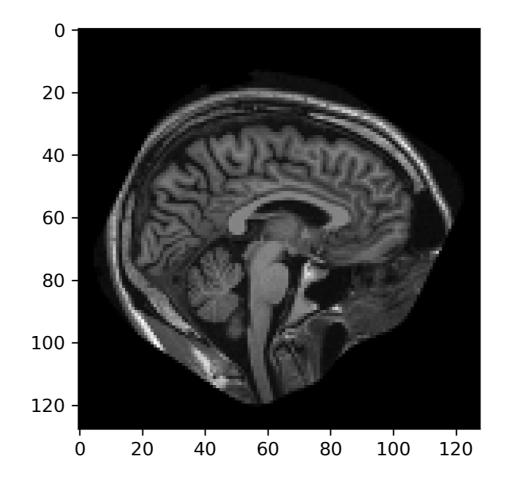
vol = imageio.volread('OAS1_0255')
vol.shape

vol_dn = ndi.zoom(vol, zoom=0.5)
vol_dn.shape

(256, 256, 256)

(128, 128, 128)



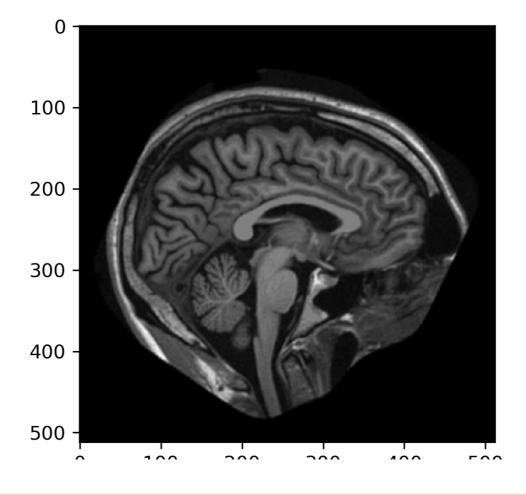


Upsampling

- Resampling to a larger grid
- Not the same as collecting higher-resolution data
- Useful for standardizing sampling rates that are unequal

```
vol_up = ndi.zoom(vol, zoom=2)
vol_up.shape
```

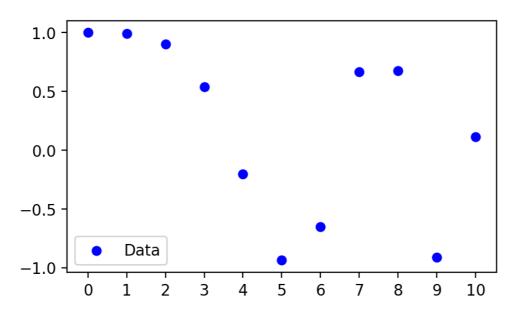
(512, 512, 512)



Interpolation

 "Stitches together" grid points to model the space between points.

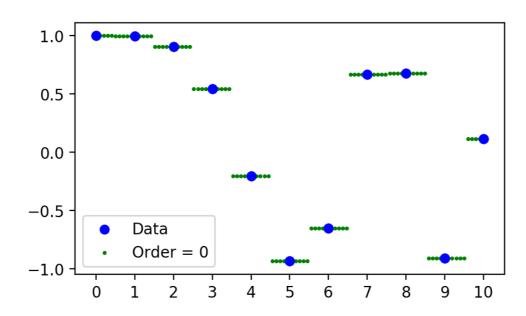
$Interpolation\ in\ 1\ D$



Interpolation

- "Stitches together" grid points to model the space between points.
- Nearest-neighbor: uses the closest measured value.

$Interpolation\ in\ 1\ D$

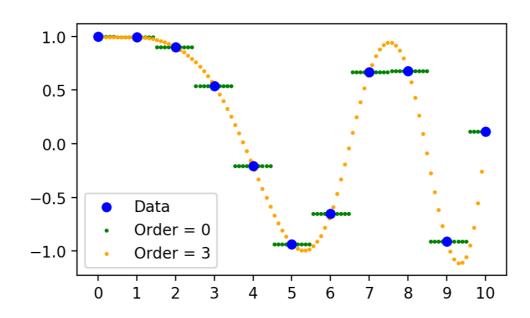




Interpolation

- "Stitches together" grid points to model the space between points.
- Nearest-neighbor: uses the closest measured value.
 - order = 0
- B-spline interpolation:
 models space between
 points with spline functions
 of a specified order.
 - order is between 1 and5

$Interpolation\ in\ 1\ D$

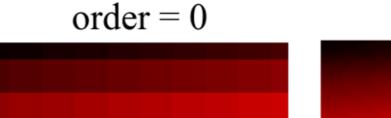


Interpolation in 2D

```
im=np.arange(100).reshape([10,10])
```



```
zm1=ndi.zoom(im, zoom=10, order=0)
zm2=ndi.zoom(im, zoom=10, order=2)
zm3=ndi.zoom(im, zoom=10, order=4)
```



Let's practice!

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Comparing images

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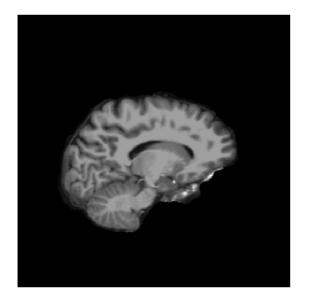


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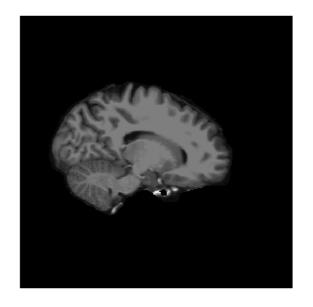


Comparing images

Visit 1



Visit 2



Mask Overlay



Summary metrics

Goal: define a metric of similarity between two images.

Cost functions produce metrics to be minimized.

Objective functions produce metrics to be maximized.



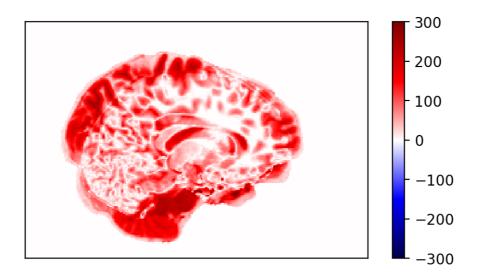
Mean absolute error

```
import imageio
import numpy as np
i1=imageio.imread('OAS1035-v1.dcm')
i2=imageio.imread('OAS1035-v2.dcm')
err = i1 - i2
plt.imshow(err)
```

```
300
- 200
- 100
- 0
- -100
- -200
- 300
```

```
abs_err = np.abs(err)
plt.imshow(abs_err)
mae = np.mean(abs_err)
mae
```

29.8570

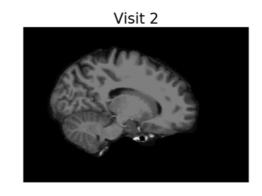


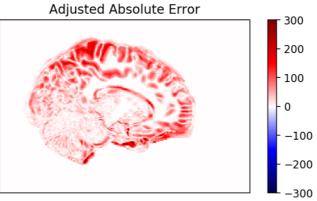
Mean absolute error

Goal: *minimize* the cost function

Visit 1 - Adjusted

Adjusted Al



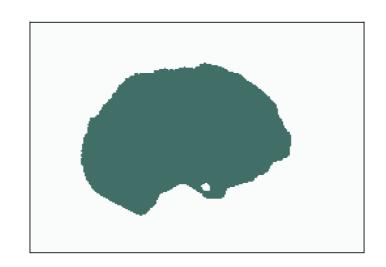


13.0376

Intersection of the union

$$IOU = rac{I_1 \cap I_2}{I_1 \cup I_2}$$

```
mask1 = im1 > 0
mask2 = im2 > 0
intsxn = mask1 & mask2
plt.imshow(intsxn)
```



```
union = mask1 | mask2
plt.imshow(union)
iou = intsxn.sum() / union.sum()
iou
```



0.68392

Let's practice!

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Normalizing measurements

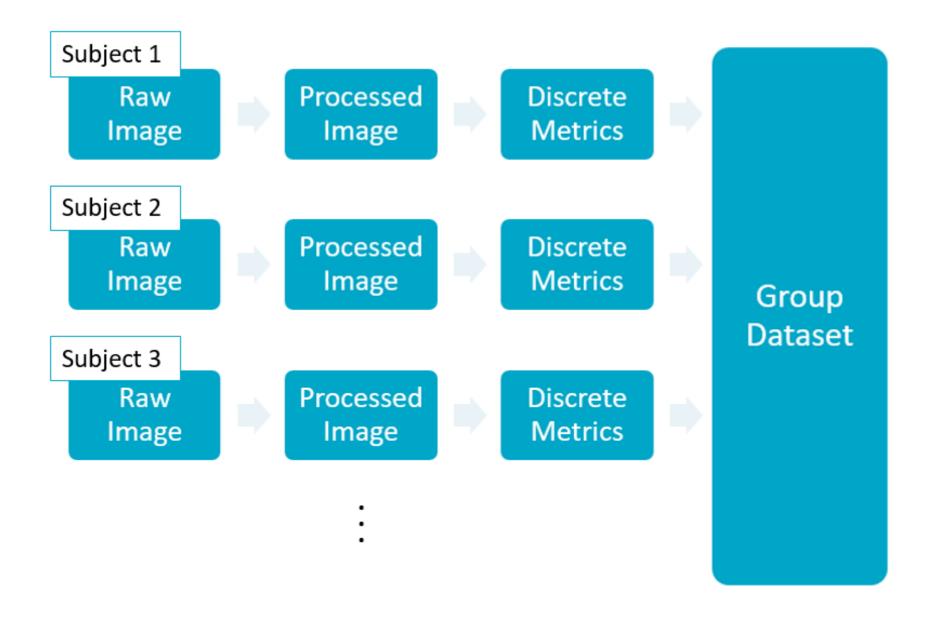
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Analysis workflow





OASIS population

```
df.shape
```

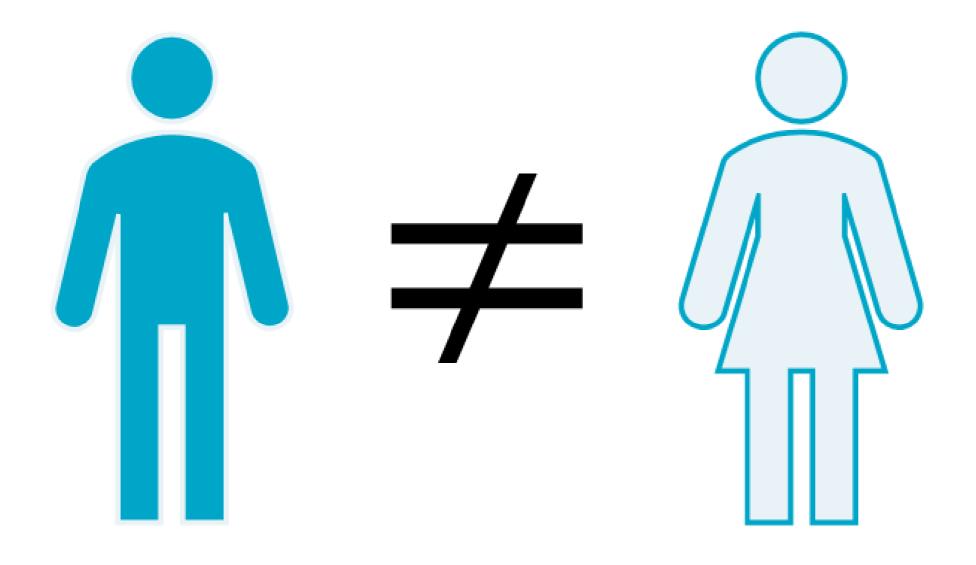
```
(400, 5)
```

```
df.sample(5)
```

	age	sex	alzheimers	brain_vol	skull_vol
ID					
0AS1_0272	75	F	True	851.451	1411.125695
0AS1_0112	69	F	False	894.801	1434.146892
0AS1_0213	48	F	False	925.859	1412.781004
0AS1_0311	22	F	False	980.163	1363.413762
0AS1_0201	85	F	False	904.104	1420.631447



Hypothesis testing



Hypothesis testing

Null hypothesis: two populations' mean brain volumes (μ_m, μ_w) are equal.

$$H_{null}: \mu_w = \mu_m$$

$$H_{alt}: \mu_w
eq \mu_m$$

$$t=rac{ar{X}-\mu}{s/\sqrt{n}}$$

Implemented in scipy.stats.ttest_ind()

Hypothesis testing

```
brain_m = df.loc[df.sex == 'M', 'brain_vol']
brain_f = df.loc[df.sex == 'F', 'brain_vol']
from scipy.stats import ttest_ind
results = ttest_ind(brain_m, brain_f)
```

```
results.statistic
results.pvalue
```

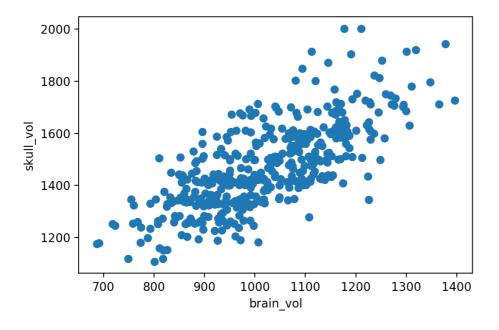
```
10.20986
5.03913e-22
```

A large t-statistic and low p-value suggests that there is a significant difference!

Correlated measurements

```
df[['brain_vol', 'skull_vol']].corr()
```

```
'brain_vol' 'skull_vol'
'brain_vol' 1.000 0.736
'skull_vol' 0.736 1.000
```





Normalization

```
df['brain_norm'] = df.brain_vol / df.skull_vol
brain_norm_m = df.loc[df.sex == 'M', 'brain_norm']
brain_norm_f = df.loc[df.sex == 'F', 'brain_norm']
results = ttest_ind(brain_norm_m, brain_norm_f)
```

```
results.statistic
results.pvalue
```

```
-0.94011
0.34769
```

Size, not gender likely drove original results.

Many potential confounds in imaging

Image acquisition

- Contrast
- Resolution
- Field of view

Context

- Hospital
- Radiologist
- Equipment

Subject / object

- Age
- Gender
- Pathology

Data Quality

- Format
- Artifacts

Congratulations!

Exploration

- Loading images
- N-D data
- Subplots

Measurement

- Labelling
- Multi-object measurement
- Morphology

Masks and Filters

- Intensity distributions
- Convolutions
- Edge detection

Image Comparison

- Transformations
- Resampling
- Cost functions
- Normalization

Good luck!

BIOMEDICAL IMAGE ANALYSIS IN PYTHON

