

Basic for loop

- ▶ Print 0 through N

```
1  
2  
-  
for i = 0 to N  
  print i
```

- ▶ Runtime?

- $O(N)$

Nested loops

► Print pairs

```
1 for i = 0 to N
2   for j = 0 to N:
3     print i + ", " + j
```

► Runtime?

- $O(N^2)$

More loops

Drop constants, $2N$ is the same as N (does it scale linearly?)

► Print evens

```
1  for i = 0 to N
2      if i % 2 == 0:
3          print i
```

► Runtime?

- $O(N)$

Two loops

► Print evens, then odds

```
1 for i = 0 to N
2     if i % 2 == 0:
3         print i
4
5 for i = 0 to N
6     if i % 2 != 0:
7         print i
```

► Runtime?

- $O(N)$

Basic for loop

► Print ordered pairs

```
1 for i = 0 to N
2   for j = i to N:
3     print i + ", " + j
```

► Runtime?

- $O(N^2)$

| | $j: 0 \rightarrow N$ | | | | | |
|-------------------|----------------------|---|---|---|---|---|
| $i: 0 \uparrow N$ | x | x | x | x | x | x |
| | | x | x | x | x | x |
| | | | x | x | x | x |
| | | | | x | x | x |
| | | | | | x | x |
| | | | | | | x |

Basic for loop

► Print ordered pairs

```
1 for i = 0 to A.length  
2   for j = 0 to B.length  
3     print A[i] + ", " + B[j]
```

► Runtime?

- $O(A * B)$

Okay now things are getting tougher!

```
1  int last_death = Integer.Min
2
3  /* step 1: get last death */
4  for (Person person : people) {
5      last_death = max(last_death, person.death)
6  }
7
8  /* step 2: increment counter for each year someone died */
9  int[] counter = new int[last_death]
10 for (Person person : people) {
11     for (int year = person.birth; year < person.death; year++)
12         counter[year]++;
13 }
14
15
16 /* step 3: find population peak */
17 int highest_population = 0
18 for (int year = 0; year < counter.length; year++)
19     highest_population = max(highest_population, counter[year])
20 }
```

► Step 1: $O(P)$

- P = number of people

► Step 2: $O(P * L)$

- L = max life span

► Step 3: $O(Y)$

- Y = total # years

► $O(P + P * L + Y) \rightarrow O(P * L + Y)$

Week. Recursion?

► Fibonacci

```
1 int fib(int n) {  
2     if (n == 0 || n == 1) {  
3         return 1;  
4     } else {  
5         return fib(n - 1) + fib(n - 2);  
6     }  
7 }
```

► Runtime?

fib(6)
fib(5) fib(4)
fib(4) fib(3) fib(3) fib(2)
...

- Height of K
- Each level doubles # nodes
- $\rightarrow O(2^k)$ ***

Actually slightly less for complex math reasons.

Week. Recursion?

► Fibonacci, part 2

```
1 int fib(int n, int[] memo) {  
2     if (n == 0 || n == 1) {  
3         return 1;  
4     } else if (memo[n] == 0)  
5         memo[n] = fib(n - 1) + fib(n - 2);  
6     }  
7     return memo[n];  
8 }
```

► Runtime?

fib(6)
fib(5) x
fib(4) x
fib(3)
...

- Height of K
- Each level has ONE node
- $\rightarrow O(k)$