

## MATLAB assignment 7

Introduction to Linear Algebra (Week 11)

Fall, 2020

1. A common problem in experimental work is to find a curve  $y = f(x)$  of a specified form corresponding to experimentally determined values of  $x$  and  $y$ , say

$$(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n).$$

The followings are the three important models in applications.

- **Linear line model** ( $y = ax + b$ )
- **Exponential model** ( $y = ae^{bx}$ )
- **Logarithmic model** ( $y = a + b \ln x$ )

A function file `LS_solver.m` fits given experimental data to the proper mathematical model using least squares method.

If you execute the following MATLAB commands:

```
>> x = [2, 3, 4, 5, 6, 7, 8, 9];  
>> y = [1.75, 1.91, 2.03, 2.13, 2.22, 2.30, 2.37, 2.43];  
>> [a, b] = LS_solver(x, y, 1)
```

Then, you may obtain the following results with the figure (See Figure 1 below):

Linear model

a =  
0.0948

b =  
1.6213

### **Problem.**

- (a) Download the function file `LS_solver_guide.m` on KLMS and complete the missing parts. Save completed file as `LS_solver.m`. (25 points)
- (b) Use `LS_solver.m` to fit an exponential model to the following data (Table 1), graph the curve and data points in the same figure and check that the code works.

Table 1: Data points of Problem 1-ii (exponential model)

<b>x</b>	0	1	2	3	4	5	6	7
<b>y</b>	3.9	5.3	7.2	9.6	12	17	23	31

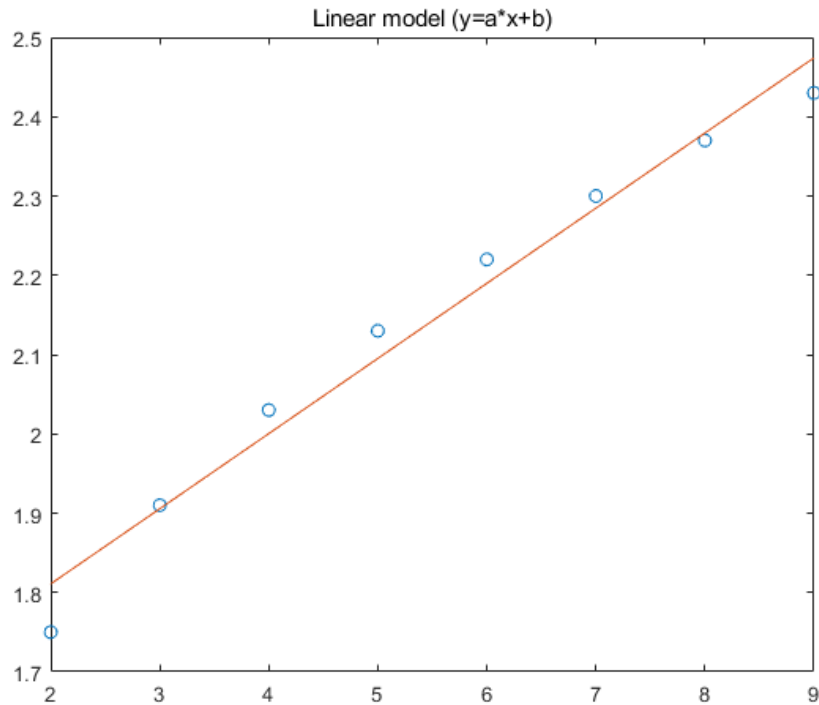


Figure 1: Execution result

- (c) Use `LS_solver.m` to fit a logarithmic model to the following data (Table 2), graph the curve and data points in the same figure and check that the code works.
- (d) Replace the `if-else if-else` command of the `LS_solver.m` with the `switch-case` command. Save this version of the file as `LS_solver_cs.m`. (25 points)

Table 2: Data points of Problem 1-iii (logarithmic model)

<b>x</b>	2	3	4	5	6	7	8	9
<b>y</b>	4.07	5.30	6.21	6.79	7.32	7.91	8.23	8.51

You may use the backslash operator in MATLAB (syntax :  $A \setminus \mathbf{b}$  for a linear system  $A\mathbf{x} = \mathbf{b}$ ) and refer to the T5 and T7 in Section 7.8 of the textbook.

[Who those use the built-in MATLAB command to get the least square solution **at once** will got zero points.]

- Read the section in the '*MATLAB basic (Lee, Jeon)*' that corresponds to the this week class and practice by your self.

### *Submission guide*

- Submit your `LS_solver.m` and `LS_solver_cs.m` files to 'Homework box for MATLAB assignment 7' on the KLMS.

- Incorrect file names and incorrect file format will cause a disadvantage in the scoring process.

[Your file should work properly as a 'function' and this means that it makes outputs **related** with given inputs. Double check if the file **works** or not, before upload.]

- `LS_solver.m` file only: maximum (25 points)  
`LS_solver_cs.m` file only: (0 points)  
Both files: maximum (50 points)

**Due date : Nov 19 (Thu) 23:59**

**Late submission will not be allowed.**