

MATLAB assignment 7

Introduction to Linear Algebra (Week 11)

Fall, 2020

1. A common problem in experimental work is to find a curve $y = f(x)$ of a specified form corresponding to experimentally determined values of x and y , say

$$(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n).$$

The followings are the three important models in applications.

- **Linear line model** ($y = ax + b$)
- **Exponential model** ($y = ae^{bx}$)
- **Logarithmic model** ($y = a + b \ln x$)

A function file `LS_solver.m` fits given experimental data to the proper mathematical model using least squares method.

If you execute the following MATLAB commands:

```
>> x = [2, 3, 4, 5, 6, 7, 8, 9];
>> y = [1.75, 1.91, 2.03, 2.13, 2.22, 2.30, 2.37, 2.43];
>> [a, b] = LS_solver(x, y, 1)
```

Then, you may obtain the following results with the figure (See Figure 1 below):

```
Linear model
```

```
a =  
0.0948
```

```
b =  
1.6213
```

Problem.

- Download the function file `LS_solver_guide.m` on KLMS and complete the missing parts. Save completed file as `LS_solver.m`. (25 points)
- Use `LS_solver.m` to fit an exponential model to the following data (Table 1), graph the curve and data points in the same figure and check that the code works.

Table 1: Data points of Problem 1-ii (exponential model)

| | | | | | | | | |
|---|-----|-----|-----|-----|----|----|----|----|
| x | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| y | 3.9 | 5.3 | 7.2 | 9.6 | 12 | 17 | 23 | 31 |

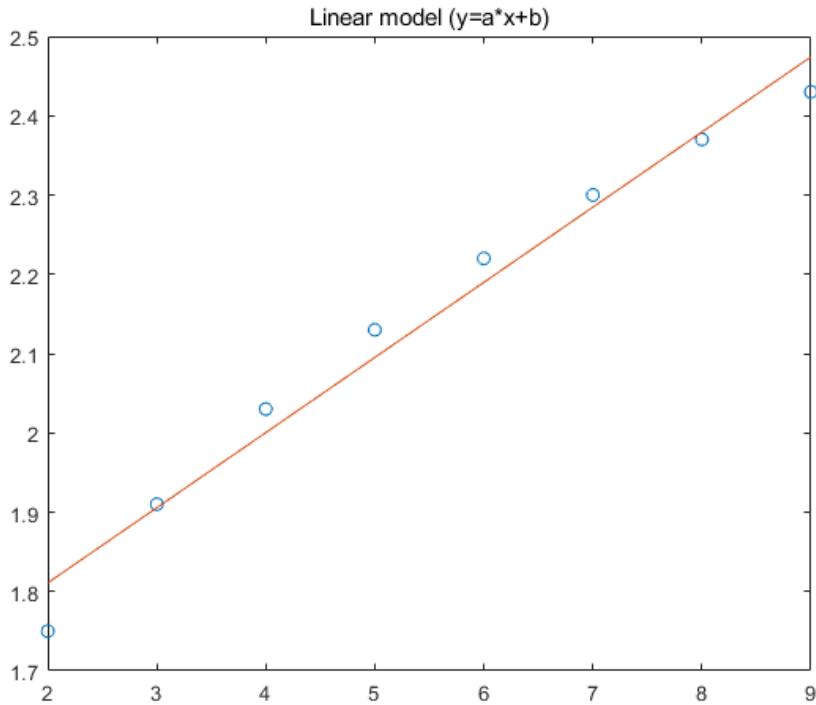


Figure 1: Execution result

- (c) Use `LS_solver.m` to fit a logarithmic model to the following data (Table 2), graph the curve and data points in the same figure and check that the code works.
- (d) Replace the `if-else if-else` command of the `LS_solver.m` with the `switch-case` command. Save this version of the file as `LS_solver_cs.m`. (25 points)

Table 2: Data points of Problem 1-iii (logarithmic model)

| x | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|------|------|------|------|------|------|------|------|
| y | 4.07 | 5.30 | 6.21 | 6.79 | 7.32 | 7.91 | 8.23 | 8.51 |

You may use the backslash operator in MATLAB (syntax : $A \setminus b$ for a linear system $Ax = b$) and refer to the T5 and T7 in Section 7.8 of the textbook.

[Who those use the built-in MATLAB command to get the least square solution **at once** will got zero points.]

2. Read the section in the ‘MATLAB basic (Lee, Jeon)’ that corresponds to the this week class and practice by your self.

Submission guide

- Submit your `LS_solver.m` and `LS_solver_cs.m` files to ‘Homework box for MATLAB assignment 7’ on the KLMS.
- Incorrect file names and incorrect file format will cause a disadvantage in the scoring process.
[Your file should work properly as a ‘function’ and this means that it makes outputs **related** with given inputs. Double check if the file **works** or not, before upload.]
- `LS_solver.m` file only: maximum (25 points)
`LS_solver_cs.m` file only: (0 points)
Both files: maximum (50 points)

Due date : Nov 19 (Thu) 23:59
Late submission will not be allowed.