

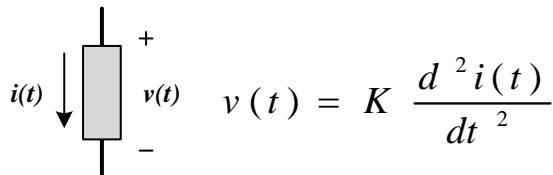
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Quiz #1 [50pts]

Problem Sets

1. If the input and output is current and voltage, is the following element linear? [5pts]

Ans: (Yes, No, Depends on situation) (3 points deducted if incorrect. No need to provide proof.)

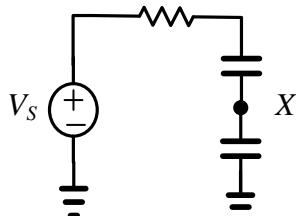


Sol)

Yes.

2. Is it possible for the net charge on node X to change if you can provide ANY voltage source at the input Vs?

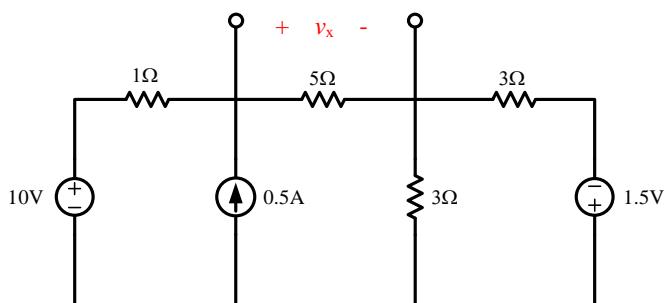
Ans: (Yes, No, Depends on the input) (3 points deducted if incorrect, No need to provide any explanation.) [5pts]



Sol)

No.

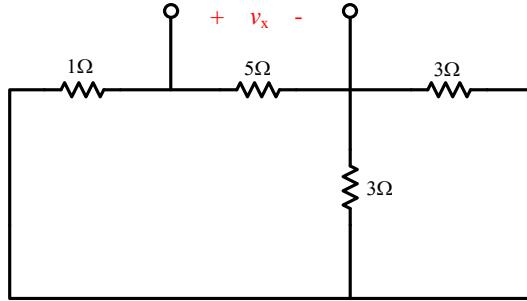
3. Determine the Thévenin equivalent of the network shown as below as seen looking into v_x . [10pts]



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Sol)

$$R_{th} = 5 \parallel (1 + 3 \parallel 3) = \frac{5}{3} \Omega$$

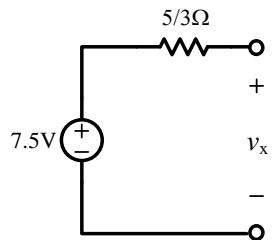
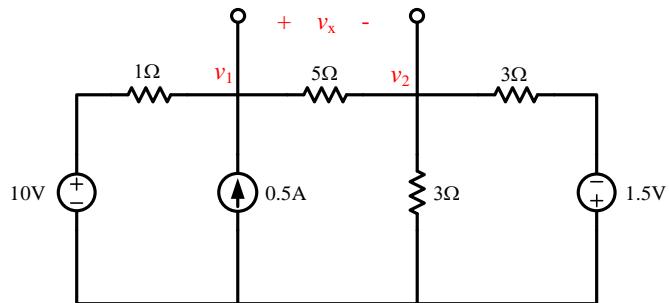


Use KCL

$$\frac{v_1 - 10}{1} - 0.5 + \frac{v_1 - v_2}{5} = 0$$

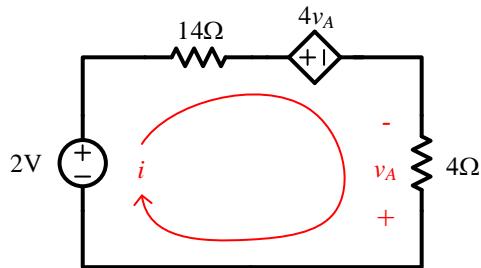
$$\frac{v_2 - v_1}{5} + \frac{v_2}{3} + \frac{v_2 - (-1.5)}{3} = 0$$

$$v_1 = 9V, v_2 = 1.5V, v_x = 7.5V$$



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4. What is the power absorbed by the 4 ohm resistor in the circuit shown below? [10pts]



Sol)

Use KVL

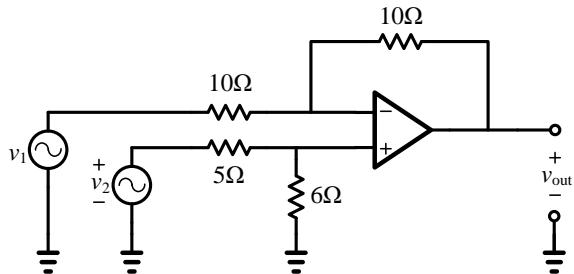
$$-2 + 14i + 4v_A + 4i = 0, \quad i = \frac{-v_A}{4}$$

$$-2 + 14i + 4 \times (-4i) + 4i = -2 + 14i - 16i + 4i = 2 + 2i = 0$$

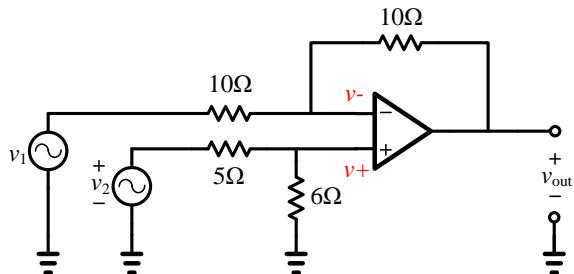
$$i = 1A$$

$$P = I^2 R = 1^2 \times 4 = 4W$$

5. Derive an expression for v_{out} as a function of v_1 and v_2 for the circuit represented as below. [10pts]



Sol)



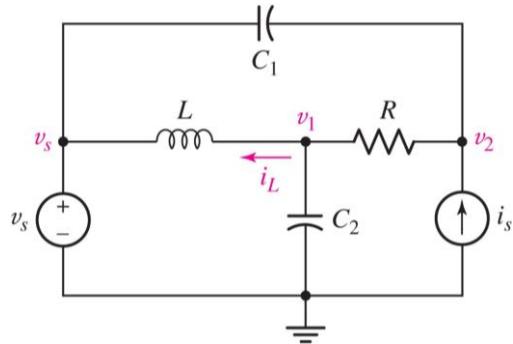
$$v_+ = v_- = \frac{6}{5+6} v_2 = \frac{6}{11} v_2$$

$$\frac{v_- - v_1}{10} + \frac{v_- - v_{out}}{10} = 0, \quad 2v_- - v_1 - v_{out} = 0$$

$$v_{out} = 2v_- - v_1 = \frac{12}{11} v_2 - v_1$$

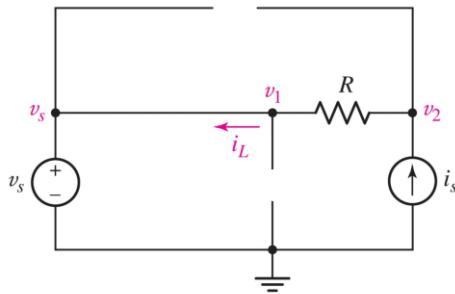
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6. Find the final steady-state output voltage of v_1 and v_2 in the below circuit. Assume $v_s = 2V$, $i_s=2A$, $R = 2\Omega$, $L=1nH$, $C_1=1uF$, $C_2 = 5uF$. Assume initial conditions of all elements are zero. [10pts]



Sol)

At final steady-state, capacitor acts as an open circuit. Inductor acts as a short circuit.



$$v_s = v_1 = 2V$$

$$v_2 - v_1 = R \times i_s = 2 \times 2 = 4V$$

$$v_1 = 2V, v_2 = 6V$$