

Gathered notes from:

- Haskell Programming from First Principles [1]

1 Monoid

todo

2 Functor

todo

3 Applicative

todo

4 Monad

todo

5 Arrow operator as Functor and Applicative

5.1 Functor

$((\rightarrow) r) = (r \rightarrow)$ as a functor
 $(r \rightarrow) *$ expects a type as argument
 instances of $(\rightarrow) r *$ as a type class
 examples of other functors: $[] *$, $Maybe *$
 functor as a type constructor

fmap:

```
<$> :: (a -> b) -> F a -> F b
let F = (\->) r
<$> :: (a -> b) -> ((->) r) a -> ((->) r) b
<$> :: (a -> b) -> (r -> a) -> (r -> b)
<$> :: (a -> b) -> (r -> a) -> r -> b
```

composition operator:

```
(.) :: (b -> c) -> (a -> b) -> a -> c
```

therefore,

$<$> = (.)$ where $F = (\rightarrow) r$ for functor

5.1.1 example

```
(+) <$> (*2)
(+) . (*2)
\ x -> (+) ((*2) x)
\ x -> (+) (x*2)
\ x -> x*2 :: a -> a
(\ x -> (+) (x*2)) :: a -> (a -> a)
(\ x -> (+) (x*2)) :: a -> a -> a
(\ x -> ((x*2)+)) :: a -> a -> a
(\ x -> (\ y -> (x*2) + y)) :: a -> a -> a
```

5.2 Applicative

apply:

```
<*> :: F (a -> b) -> F a -> F b
let F = (\->) r = r ->, then
<*> :: ((->) r) (a -> b) -> ((->) r) a -> ((->) r) b
<*> :: (r -> a -> b) -> (r -> a) -> (r -> b)
```

$\text{pure} :: a \rightarrow F a$

$\text{pure } x = ((\rightarrow) r) x = r \rightarrow x :: F a$

5.2.1 example

```
(+) <$> (*2) <*> (+10)
(+) . (*2) <*> (+10)
(\ x -> (+) (x*2)) <*> (\ x -> x + 10)
\ x -> (+) (x*2) (x+10)
```

types:

```
\ x -> :: (\->) r
(+) (x*2) :: a -> b where x is fixed
\ x -> (+) (x*2) :: ((->) r) a -> b
```

```
\ x -> x + 10 :: r -> a = ((->) r) a
```

```
(+) (x*2) (x+10) :: b where x is fixed
\ x -> (+) (x*2) (x+10) :: ((->) r) b
```

```
<*> :: (((->) r) a -> b) -> (((->) r) a) -> (((->) r) b)
```

thus types are as expected for applicative

References

- [1] Allen & Moronuki. Haskell programming from first principles, 2016.