



**FINAL
EXAMINATION
FALL 2006**

Student Number: _____

Question 1: Recursion (10 marks)

Recursively define the following types of binary trees, based on the non-recursive definitions used in class:

- 1) Full binary tree
- 2) Complete binary tree
- 3) Balanced binary tree

Question 2: Linked List (10 marks)

- 1) The last node of a linear linked list _____.
a) has the value `null`
b) has a `next` reference whose value is `null`
c) has a `next` reference which references the first node of the list
d) cannot store any data

Answer:

- 2) Which of the following will be true when the reference variable `curr` references the last node in a linear linked list?
a) `curr == null`
b) `head == null`
c) `curr.getNext() == null`
d) `head.getNext() == null`

Answer:

- 3) If a linked list is empty, the statement `head.getNext()` will throw a(n) _____.
a) `IllegalArgumentException`
b) `ArithmeticException`
c) `IndexOutOfBoundsException`
d) `NullPointerException`

Answer:

- 4) What are two advantages of using a reference-based implementation of the ADT list instead of an array-based implementation?

- 5) Write the code fragment to delete the node that the reference variable `curr` references in a circular doubly linked list? Each node supports the methods `setNext()`, `getNext()`, `getPrecede()` and `setPrecede()`.

- 6) Write the code fragment to insert a new node that the reference variable `newNode` references before the node referenced by the reference variable `curr` in a doubly linked list, using the methods listed in part 5).

Question 3: Algorithm Complexity (5 marks)

- 1) Assuming a linked list of n nodes, the code fragment:

```
Node curr = head;
while (curr != null) {
    System.out.println(curr.getItem());
    curr.setNext(curr.getNext());
} // end while
```

requires _____ assignments.

- a) n
- b) $n - 1$
- c) $n + 1$
- d) 1

Answer:

- 2) Assuming a linked list of n nodes, the above code fragment (in part 1))

requires _____ comparisons.

- a) n
- b) $n - 1$
- c) $n + 1$
- d) 1

Answer:

- 3) Assuming a linked list of n nodes, the above code fragment (in part 1))

requires _____ write operations.

- a) n
- b) $n - 1$
- c) $n + 1$
- d) 1

Answer:

- 4) Consider an algorithm that contains loops of the form:

```
for (x = 1 through n) {
    for (y = 1 through x) {
        for (z = 1 through 10) {
            Task T
        } // end for
    } // end for
} // end for
```

If task T requires t time units, the innermost loop on z requires _____ time units.

- a) y
- b) 10
- c) $z * t$
- d) $10 * t$

Answer:

- 5) Consider the above algorithm (part 4) again.

If task T requires t time units, the loop on y requires _____ time units.

- a) $10 * t$
- b) $(10 * t) + x$
- c) $10 * t * x$
- d) $t * x$

Answer:

Question 4: Binary Trees (10 marks)

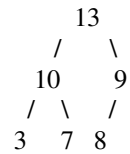
- 1) Beginning with an empty binary search tree, what binary search tree is formed when you insert the following values in the order given?
 - a. W, T, N, J, E, B, A
 - b. W, T, N, A B, E, J
 - c. A, B, W, J, N, T, E

- 2) Write pseudocode for a method that performs a range query for a binary search tree. That is, `RangeQuery(tree, low, high)` should visit all items/nodes in `tree` that have a search key `k` with $low \leq k \leq high$. To indicate the a specific node `x` is being visited (printed, modified, ...), simply use the pseudocode instruction `visit(x)`.

- 3) Proof by induction that a binary tree with n nodes has exactly $n+1$ empty subtrees (or, in Java terms, $n+1$ *null* references in a reference-based implementation)

Question 5: Heaps/Priority Queues (10 marks)

- 1) Given the following `maxheap h`, show what the heap would look like after each of the following pseudocode operations:

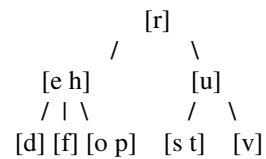


- a) `h.heapInsert(16)`
 - b) `h.heapInsert(14)`
 - c) `h.heapDelete()`
- 2) Does the order in which you insert items into a heap affect the heap that results? Explain.
- 3) Suppose that after you have placed several items into a priority queue, you need to adjust one of the priority values. For example, a particular task in a priority queue of tasks could become more or less urgent. How can you adjust the heap if a single priority value changes? Note: your solution should be better than “remove the item and re-insert it” as we have no operation to delete arbitrary items from a heap.

Question 6: Balanced Trees/Tables (10 marks)

- 1) What are the advantages of implementing the ADT table with a 2-3 tree instead of a binary search tree? Why do you not, in general, maintain a completely balanced binary search tree?

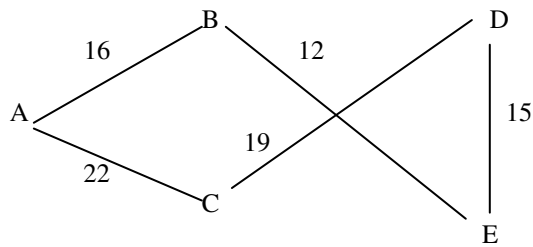
- 2) Given the 2-3 tree below, draw the tree that results after inserting k, b, c, y, and w into the tree.



- 3) Write pseudocode for the *tableDelete* operation when the implementation uses hashing and linear probing to resolve collisions.

Question 7: Graphs (10 marks)

- 1) Use both the depth-first and the breadth-first strategy to traverse the graph below, beginning with vertex A. List the vertices in the order in which each traversal visits them. If a node has multiple neighbors, assume that they are visited in alphabetical order



- 2) By modifying the DFS traversal algorithm, write pseudocode for an algorithm that determines whether a graph contains a cycle.
- 3) For the graph above, draw all possible spanning trees. Which one is the minimum spanning tree?