

# 2014 CURRICULUM SUMMARY

## FURTHER MATHEMATICS

TYLER FERNANDO  
YARRA VALLEY GRAMMAR

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## 1.2 Organising and displaying categorical data

## 1.3 Organising and displaying numerical data

## 1.4 What to look for in a histogram

## 1.5 Stem-and-leaf plots and dot plots

## 2 Summarising numerical data: the median, range, IQR and box plots

- 2.1 Will less than the whole picture do?
- 2.2 The median, range and interquartile range (IQR)
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