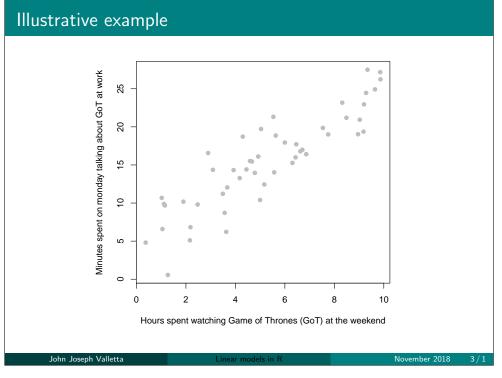
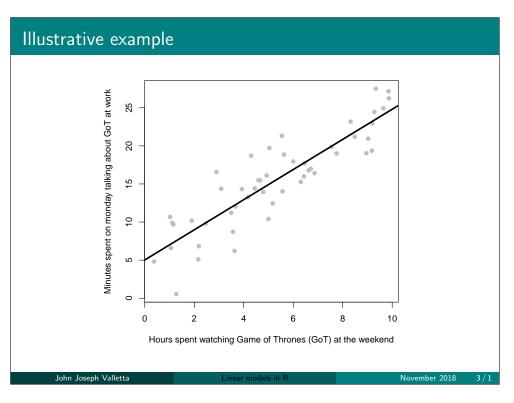
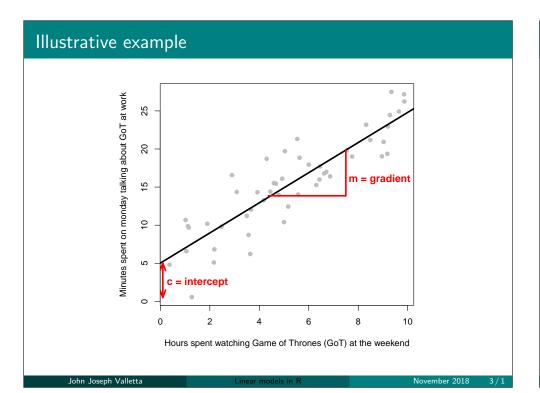
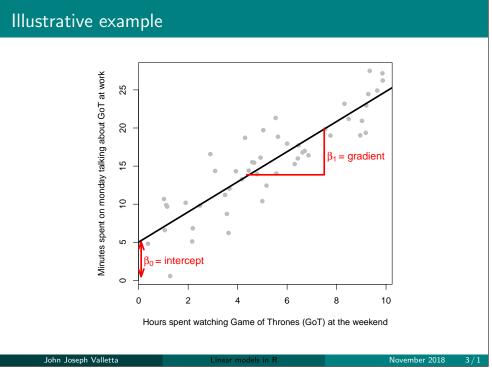


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Formal definition

$$y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$
$$\epsilon_i \sim \mathcal{N}(0, \sigma^2)$$

Observed data

- ullet y (outcome/response): minutes spent talking about GoT
- ullet x (explanatory): hours spent watching Game of Thrones (GoT)

Parameters to infer

- β_0 : intercept
- β_1 : gradient wrt minutes talking about GoT

Linear models in R

- Use the lm() function
- Requires a formula object outcome ~ explanatory variable

```
# talk: minutes spent talking about GoT (outcome/response variable)
# watch: hours spent watching GoT (explanatory variable)

fit <- lm(talk ~ watch)

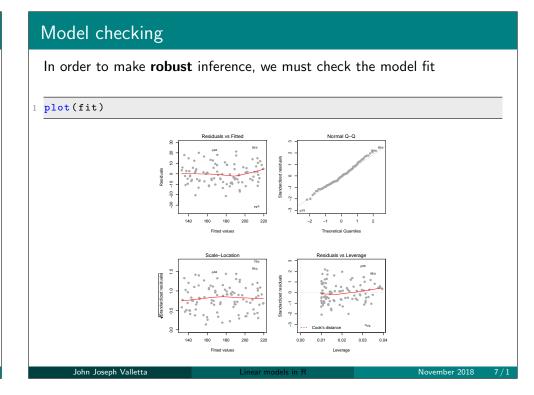
# If data is in a data frame called "df"

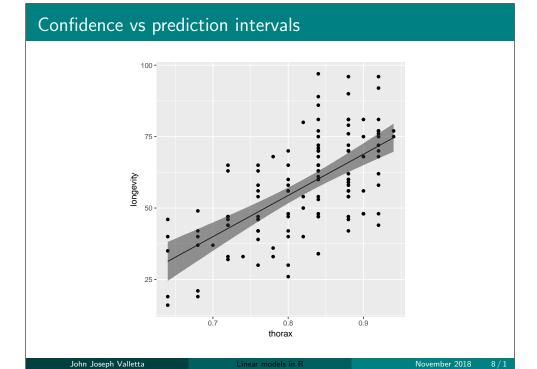
fit <- lm(talk ~ watch, df)</pre>
```

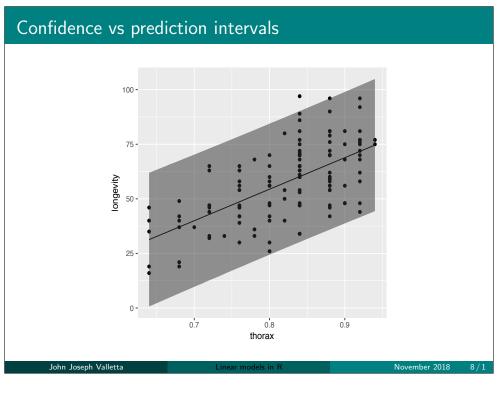
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Summary of fitted model

```
summary(fit)
 ##
 ## lm(formula = height ~ weight, data = df)
 ## Residuals:
        Min
                 1Q Median
                                 ЗQ
                                        Max
 ## -31.089 -6.926 -0.689
                             6.057 24.967
 ##
 ## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
 ## (Intercept) 2.35229
                           7.11668 0.331
                                              0.742
                            0.08782 24.762
                                            <2e-16 ***
 ## weight
                 2.17446
 ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 ## Residual standard error: 10.31 on 98 degrees of freedom
 ## Multiple R-squared: 0.8622, Adjusted R-squared: 0.8608
 ## F-statistic: 613.1 on 1 and 98 DF, p-value: < 2.2e-16
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```



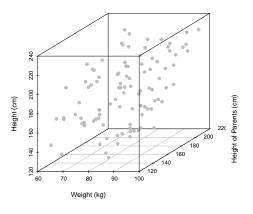




Multiple linear regression

$$y_i = \beta_0 + \beta_1 x_{1i} + \ldots + \beta_p x_{pi} + \epsilon_i$$

$$\epsilon_i \sim \mathcal{N}(0, \sigma^2)$$



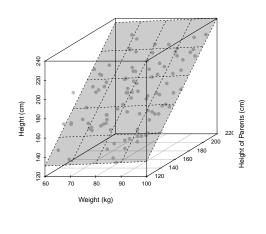
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Multiple linear regression

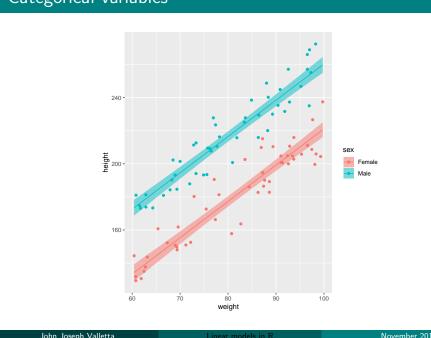
$$y_i = \beta_0 + \beta_1 x_{1i} + \ldots + \beta_p x_{pi} + \epsilon_i$$

$$\epsilon_i \sim \mathcal{N}(0, \sigma^2)$$



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Categorical variables



Categorical variables

We need dummy variables

$$S_i = \left\{ \begin{array}{ll} 1 & \text{if } i \text{ is male,} \\ 0 & \text{otherwise} \end{array} \right.$$

Here, female is known as the baseline/reference level The regression is:

$$y_i = \beta_0 + \beta_1 S_i + \beta_2 x_i + \epsilon_i$$

Or in English:

$$height_i = \beta_0 + \beta_1 sex_i + \beta_2 weight_i + \epsilon_i$$

Categorical variables

The mean regression lines for male and female are:

• Female (sex=0)

$$\begin{aligned} \text{height}_i &= \beta_0 + (\beta_1 \times 0) + \beta_2 \text{weight}_i \\ \text{height}_i &= \beta_0 + \beta_2 \text{weight}_i \end{aligned}$$

• Male (sex=1)

$$\begin{aligned} \text{height}_i &= \beta_0 + (\beta_1 \times 1) + \beta_2 \text{weight}_i \\ \text{height}_i &= (\beta_0 + \beta_1) + \beta_2 \text{weight}_i \end{aligned}$$

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