# Linear models in R

Richard Sherley

University of Exeter, Penryn Campus, UK

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Researcher Development



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Februrary 2020

1 / 13

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#### The Team

- Dr Beth Clark
- Dr Dan Padfield
- Dr Matt Silk
- Dr Richard Inger

Richard Sherley Linear models in R Februrary 2020 2 / 13

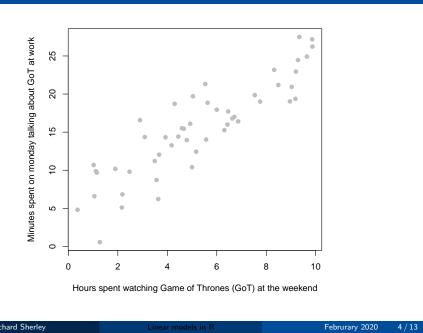
## What is a model and why do we need one?

A **model** is a human construct/abstraction that tries to approximate the **data generating process** in some useful manner

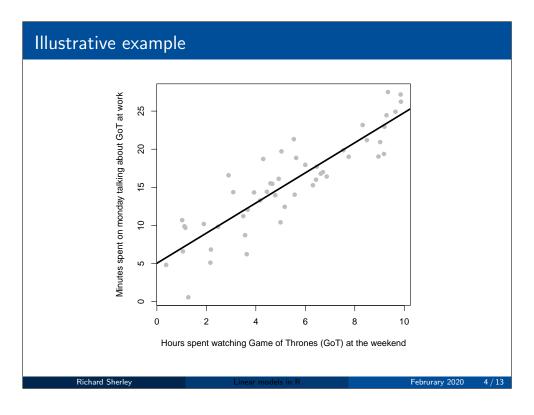
#### Models are built for

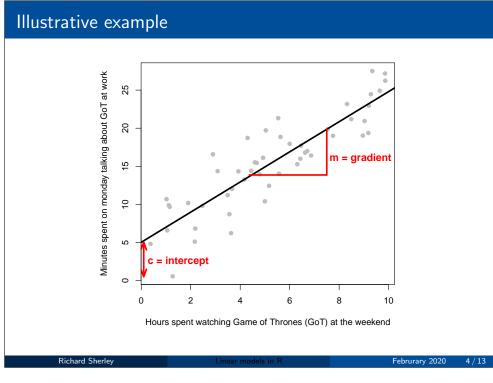
- enhancing our understanding of a complex phenomenon
- executing "what if" scenarios
- predicting/forecasting an outcome
- controlling a system

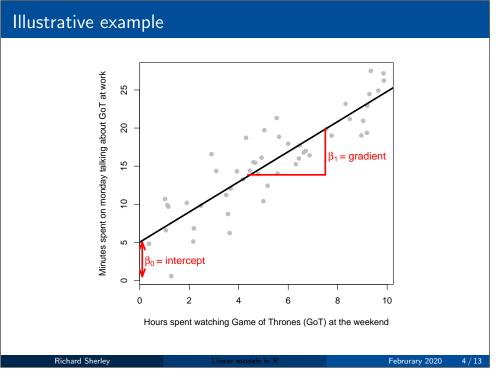
# Illustrative example



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## Formal definition

$$y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$
$$\epsilon_i \sim \mathcal{N}(0, \sigma^2)$$

#### Observed data

- ullet y (outcome/response): minutes spent talking about GoT
- x (explanatory): hours spent watching Game of Thrones (GoT)

#### Parameters to infer

- $\beta_0$ : intercept
- $\beta_1$ : gradient wrt minutes talking about GoT

Richard Sherley Linear models in R Februrary 2020 5/13

#### Linear models in R

- Use the lm() function
- Requires a **formula** object outcome  $\sim$  explanatory variable

```
1 # talk: minutes spent talking about GoT (outcome/response variable)
2 # watch: hours spent watching GoT (explanatory variable)
4 fit <- lm(talk ~ watch)
6 # If data is in a data frame called "df"
7 fit <- lm(talk ~ watch, df)</pre>
```

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Februrary 2020 6 / 13

### Summary of fitted model

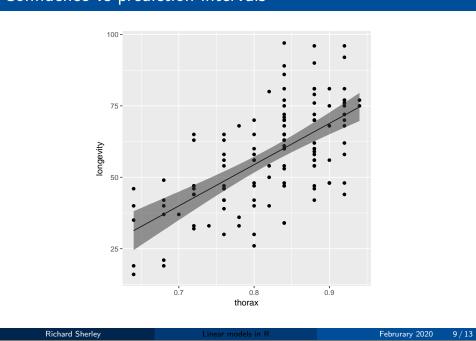
```
summary(fit)
## Call:
## lm(formula = height ~ weight, data = df)
## Residuals:
      Min
               1Q Median
## -31.089 -6.926 -0.689 6.057 24.967
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.35229
                       7.11668 0.331
              ## weight
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 10.31 on 98 degrees of freedom
## Multiple R-squared: 0.8622, Adjusted R-squared: 0.8608
## F-statistic: 613.1 on 1 and 98 DF, p-value: < 2.2e-16
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                                                           Februrary 2020 7 / 13
```

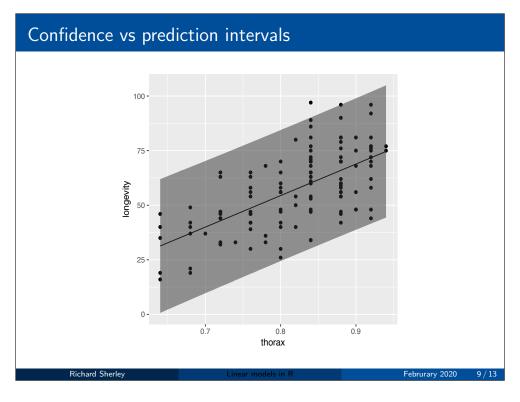
## Model checking

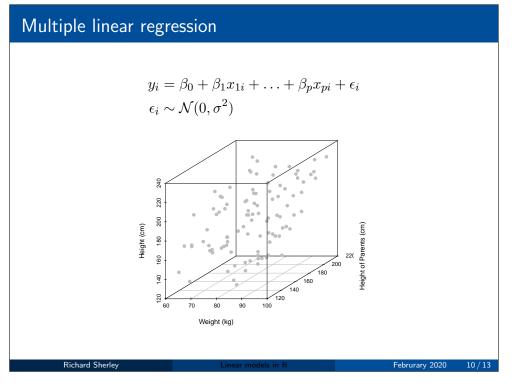
In order to make robust inference, we must check the model fit

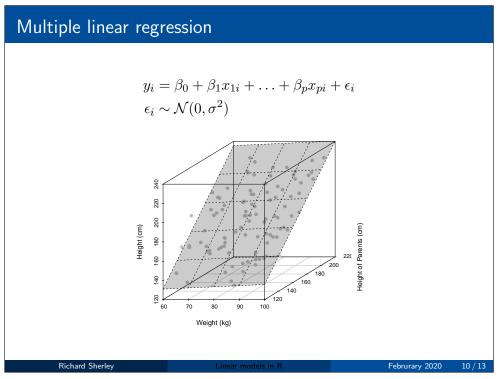
```
plot(fit)
```

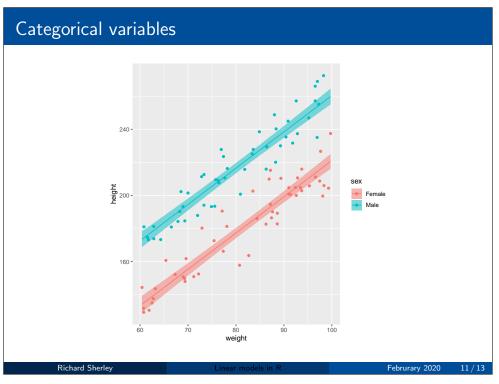
## Confidence vs prediction intervals











# Categorical variables

We need **dummy** variables

$$S_i = \begin{cases} 1 & \text{if } i \text{ is male,} \\ 0 & \text{otherwise} \end{cases}$$

Here, female is known as the **baseline/reference level** The regression is:

$$y_i = \beta_0 + \beta_1 S_i + \beta_2 x_i + \epsilon_i$$

Or in English:

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$$height_i = \beta_0 + \beta_1 sex_i + \beta_2 weight_i + \epsilon_i$$

Februrary 2020

12 / 13

Categorical variables

The mean regression lines for male and female are:

• Female (sex=0)

$$\begin{aligned} \text{height}_i &= \beta_0 + (\beta_1 \times 0) + \beta_2 \text{weight}_i \\ \text{height}_i &= \beta_0 + \beta_2 \text{weight}_i \end{aligned}$$

• Male (sex=1)

height<sub>i</sub> = 
$$\beta_0 + (\beta_1 \times 1) + \beta_2$$
weight<sub>i</sub>  
height<sub>i</sub> =  $(\beta_0 + \beta_1) + \beta_2$ weight<sub>i</sub>

Richard Sherley Linear models in R Februrary 2020 13/13