

(and)  $\wedge$  of  $\cup$  &

①

$\pi$  is hyper 3 and  $\pi$  less than 3.2

$\pi > 3 \wedge \pi < 3.2$  to illustrate

$3 < \pi < 3.2$

$\phi, \psi$  :  $\phi, \psi$  :  $\phi \wedge \psi$  means they both true

Conjunction

~~$\phi$  and  $\psi$~~   $\phi, \psi$  are called ~~Conjunction~~

$\phi, \psi$  individually true, then  $\phi \wedge \psi$  are true

$\phi \rightarrow$  called "phi"

$\psi$  called "psi"

~~$\phi, \psi$~~

Conjunction

$\phi \wedge \psi$  means same as  $\psi \wedge \phi$   $\psi \wedge \phi$  same as  $\phi \wedge \psi$

Conjunction is commutative?  $\leftarrow$  independent of order

in normal English and is not commutative.

- X - I picked up glass and it fell out of my hand
- X - it fell out of my hand and I picked up glass



Propositional Truth table

| $\Phi$ | $\Psi$ | $\Phi \wedge \Psi$ |
|--------|--------|--------------------|
| T      | T      | T                  |
| T      | F      | F                  |
| F      | T      | F                  |
| F      | F      | F                  |

OR

$\wedge$  and  $\vee$   
(OR)

$a > 0$  or the equation  $x^2 + a = 0$  has real root (excluded)

$ab = 0$  if  $a = 0$  or  $b = 0$

in maths, "or" means inclusive (X)

(Inclusive) (X)

use  $\vee$  symbol (disjunction)

$\Phi, \Psi$  :  $\Phi \vee \Psi$ ,  $\Phi$  or  $\Psi$  or both.

$\Phi, \Psi$  are called disjuncts, with at least one can be true

$(3 < 5)$  or  $(1 = 0)$  (true)

if even though this is false

| $\Phi$ | $\Psi$ | $\Phi \vee \Psi$ |
|--------|--------|------------------|
| T      | T      | T                |
| T      | F      | T                |
| F      | T      | T                |
| F      | F      | F                |



not  $\Psi$ , not  $\Psi$   $\neg \Psi$   $\vee \sim \Psi$

(3)

$\neg(x=y)$  or  $\neg(a < b)$  ✓ Better.  
and not  $\neg(x \neq y)$  or  $(a \neq x \neq b) \Leftarrow$  avoid

$\neg(\pi < 3)$ , mean  $\pi \geq 3$ . (easy)

"all foreign cars are badly made"

$\Rightarrow$  How negate?

(a) all foreign cars are well made

(b) all bad cars are badly made

(c) one foreign car is well made

? (c) at least one foreign car is well made  
? (d) at least one foreign car is not badly made  
two possibilities

Truth table

| $\Phi$ | $\neg \Phi$ |
|--------|-------------|
| T      | F           |
| F      | T           |

Answer is dependent  
on our knowledge  
of everyday world  
 $\Rightarrow$  in many cases is  
not the case!

for