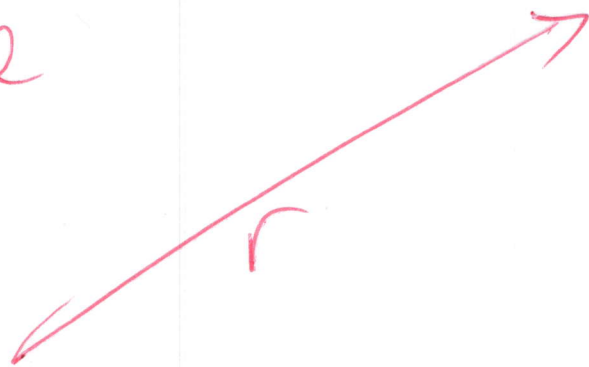


But what makes a vector a vector?  
— What operations can we do  
on  $\vec{v}$  vectors, and what  
then defines what they are

①

we can think of vector as an  
object that moves us about in  
space



— It can be a physical space or  
space of data.

in data science, we think of vector  
as list of attributes of object

Eg take have, with attributes

②

120 Sqn

2 beds

1 Bathroom

\$150k.

This can then be written as a list  
(120, 2, 1, 150 000) or as a

vector

$$\begin{bmatrix} 120 \\ 2 \\ 1 \\ 150 \end{bmatrix}$$

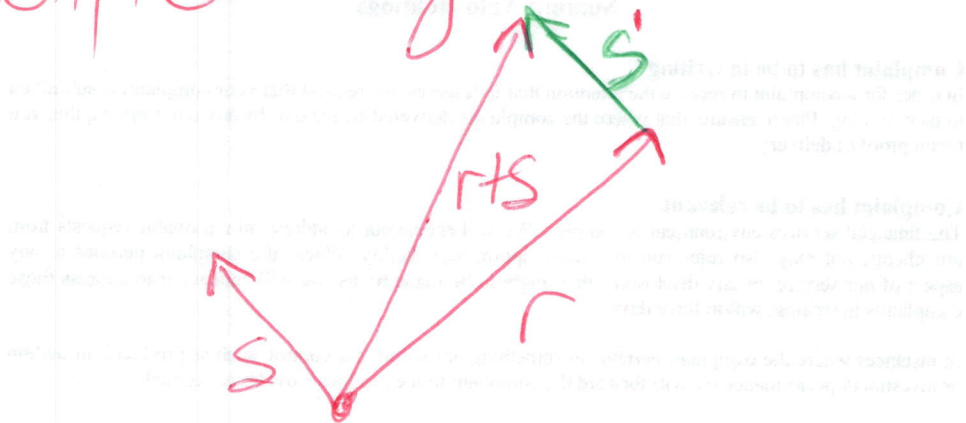
So in physics its thought of as something  
that moves us about in space,

In DS, its thought of as attribute  
of object!  
or description of attribute of object

Vector is based on 2 (two) rules ③

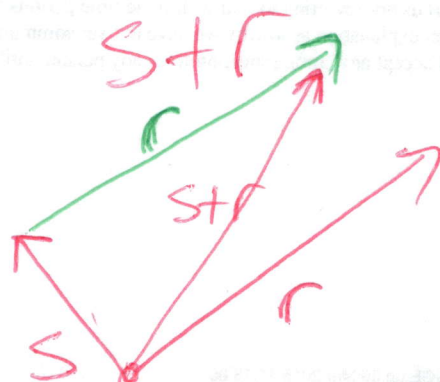
⇒ Addition

② multiplication by scalar number.



— we have two vectors S and R and  
we need to add to 'R',  
⇒ we put S at end (tail of R)  
and we draw diagonal to end  
of S', and that is sum  
of S', and that is sum  
of S, and that is sum  
of R + S

we can also



and gives us the same answer!



④

$$\therefore r + s = s + r$$

Same Thing (Commutative Rule)

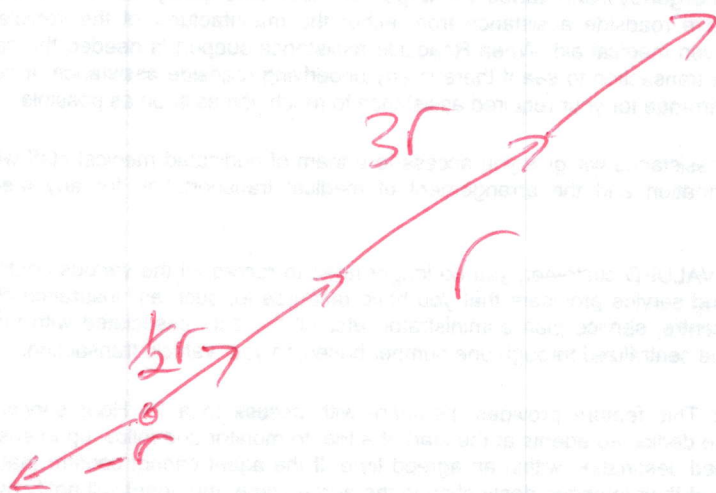
Next things to do scalar multiplication

(ar)

where  
 $a=3$

or  $\frac{1}{2}r$

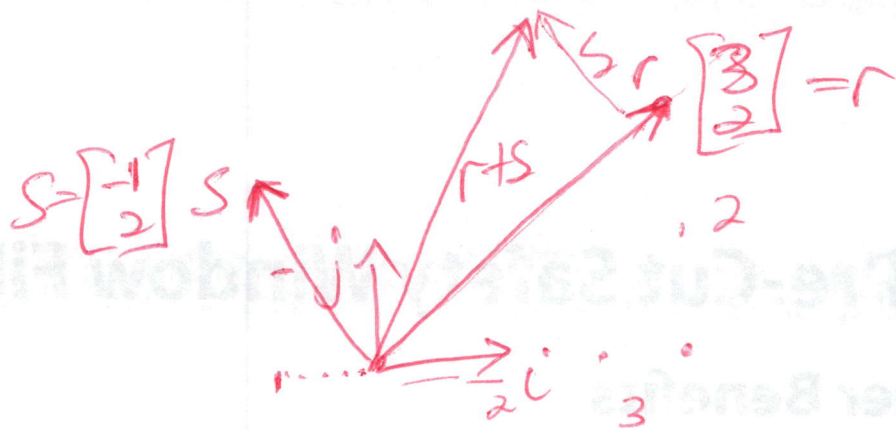
$$\underline{3 \times r}$$



or minus  $r$ ,  $-r$ , we  
go back other way

Now let's define a  $\mathbb{R}^2$  Coordinate System  
of length 1





⑤

lets now have vector  $r = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$

that mean 3 of  $i$   
2 of  $j$

Scalar number 3 of  $i$

and Scalar number 2 of  $j$

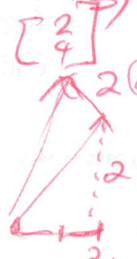
lets say we have another vector  $s$   
 $s = \begin{bmatrix} -1 \\ 2 \end{bmatrix} \rightarrow i$   
 $\quad \quad \quad \rightarrow j$

$$r + s = \begin{bmatrix} 3 \\ 2 \end{bmatrix} + \begin{bmatrix} -1 \\ 2 \end{bmatrix} = \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

Associative

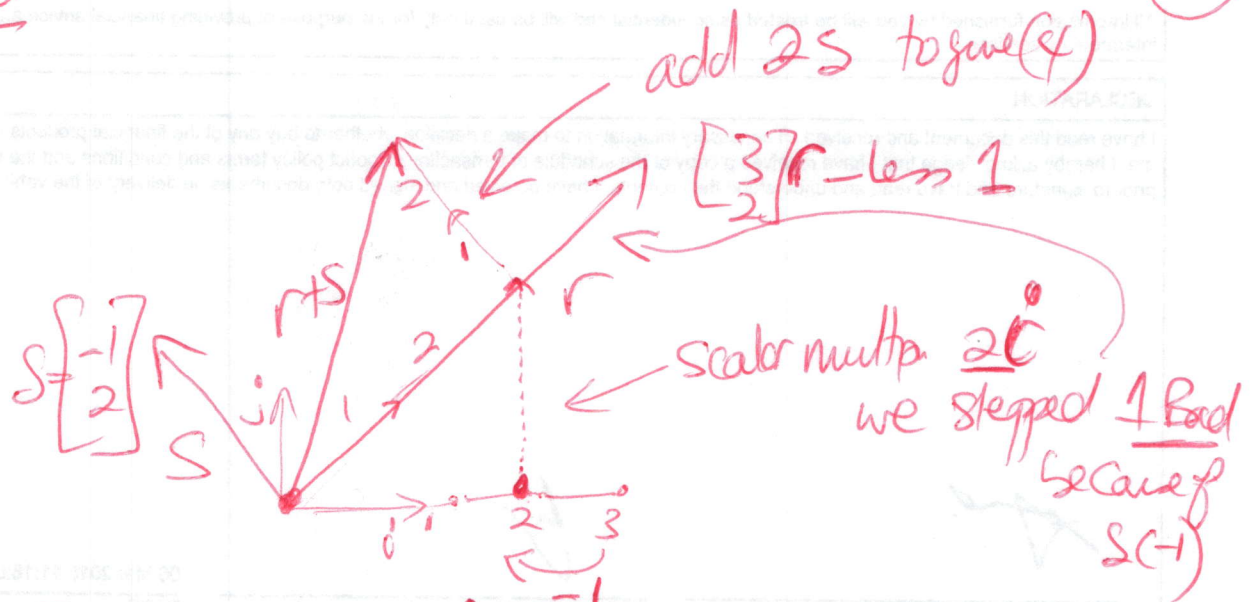
$$r + s = s + r$$

on diagram we go back 2 for  $i$   
and add 2 of  $j$



Again

6



$$\begin{bmatrix} 3 \\ 2 \end{bmatrix} + \begin{bmatrix} -1 \\ 2 \end{bmatrix} = \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

$$\therefore 3 - 1 = 2$$

~~array~~

$\rightarrow \begin{bmatrix} 2 \\ 4 \end{bmatrix}$

$$2 + 2 = 4 (s)$$



help lost at scalar multiplication: ✓

⑦

$\vec{e}_i$  } Basis vectors that define the  
Coordinate System.

But don't have to work with vectors  
Geometrically, Can use list

