

$$\begin{aligned}
\theta_2 \ddot{\theta}_2 = & - \frac{2 \left( (l_1 m_1 + l_1 m_2) \cos(\phi_1(t))^4 + 2 (l_1 m_1 + l_1 m_2) \cos(\phi_1(t))^2 \sin(\phi_1(t))^2 + (l_1 m_1 + l_1 m_2) \sin(\phi_1(t))^4 \right) \cos(\theta_1(t)) \sin(\theta_1(t))^2 D[0](\phi_1)(t)^2 + \left( 2 \left( (l_2 m_1 + l_2 m_2) \cos(\phi_1(t))^4 + 2 (l_2 m_1 + l_2 m_2) \cos(\phi_1(t))^2 \sin(\phi_1(t))^2 + (l_2 m_1 + l_2 m_2) \sin(\phi_1(t))^4 \right) \cos(\theta_1(t))^2 + \left( 2 l_2 m_2 \cos(\phi_1(t)) \sin(\phi_1(t)) + (2 l_2 m_1 + l_2 m_2) \cos(\phi_1(t))^2 + (2 l_2 m_1 + l_2 m_2) \sin(\phi_1(t))^2 \right) \sin(\theta_1(t))^2 \right) \cos(\theta_2(t)) D[0](\theta_2)(t)^2 + 2 \left( (g m_1 + g m_2) \cos(\phi_1(t))^4 + 2 (g m_1 + g m_2) \cos(\phi_1(t))^2 \sin(\phi_1(t))^2 + (g m_1 + g m_2) \sin(\phi_1(t))^4 \right) \cos(\theta_1(t))^2 + 2 \left( (l_1 m_1 + l_1 m_2) \cos(\phi_1(t))^4 + 2 (l_1 m_1 + l_1 m_2) \cos(\phi_1(t))^2 \sin(\phi_1(t))^2 + (l_1 m_1 + l_1 m_2) \sin(\phi_1(t))^4 \right) \cos(\theta_1(t))^3 + \left( (l_1 m_1 + l_1 m_2) \cos(\phi_1(t))^4 + 2 (l_1 m_1 + l_1 m_2) \cos(\phi_1(t))^2 \sin(\phi_1(t))^2 + (l_1 m_1 + l_1 m_2) \sin(\phi_1(t))^4 \right) \cos(\theta_1(t)) \sin(\theta_1(t))^2 \right) D[0](\theta_1)(t)^2}{\left( 2 \left( (l_2 m_1 + l_2 m_2) \cos(\phi_1(t))^4 + 2 (l_2 m_1 + l_2 m_2) \cos(\phi_1(t))^2 \sin(\phi_1(t))^2 + (l_2 m_1 + l_2 m_2) \sin(\phi_1(t))^4 \right) \cos(\theta_1(t))^2 + \left( 2 l_2 m_2 \cos(\phi_1(t)) \sin(\phi_1(t)) + (2 l_2 m_1 + l_2 m_2) \cos(\phi_1(t))^2 + (2 l_2 m_1 + l_2 m_2) \sin(\phi_1(t))^2 \right) \sin(\theta_1(t))^2 \right) \sin(\theta_2(t))}
\end{aligned} \tag{1}$$