

1. (1) 消去 G_1 左递归如下: $G_1: S \rightarrow a | \wedge | (T)$ $T \rightarrow ST'$ $T' \rightarrow , ST' | \epsilon$

, 求出每个非终结符的 First 集与 Follow 集

 $First(S) = \{a, \wedge, (\}$ $Follow(S) = \{\#, , ,)\}$ $First(T) = \{a, \wedge, (\}$ $Follow(T) = \{) \}$ $First(T') = \{ , , \epsilon \}$ $Follow(T') = \{) \}$

递归子程序如下:

procedure T:

begin.

 $S;$ $T;$

end.

procedure T'

begin.

if sym = "," then

begin.

Advance;

 $S;$ $T';$

end.

else if sym = ")" then

return;

else. ERROR;

procedure S

begin.

if sym = 'a' or sym = '\wedge'

then Advance;

else if sym = '(' then

begin.

Advance;

 $T;$

if sym = ',' then

Advance

else. ERROR;

else

ERROR;

(2) 首先经改写的文法满足左递归, 其次对于任一非终结符的产生式:

 $First(a) = \{a\} \neq First(\wedge) = \{\wedge\} \neq First((T)) = \{($ $First(ST') = \{a, \wedge, (\}$ $First(,ST') = \{ , \} \neq First(\epsilon) = \{\epsilon\},$ 其次对于 $T' \rightarrow \epsilon$, $First(T') \cap Follow(T') = \emptyset$ 所以 G_1 为 LL(1) 的, 预测分析表如下:

	a	\wedge	()	,	#
S	$S \rightarrow a$	$S \rightarrow \wedge$	$S \rightarrow (T)$			
T	$T \rightarrow ST'$	$T \rightarrow ST'$	$T \rightarrow ST'$			
T'				$T' \rightarrow \epsilon$	$T' \rightarrow ,ST'$	

2. (1) 计算非终结符的 First 集与 Follow 集如下:

 $First(E) = \{ (, a, b, \wedge \}$ $Follow(E) = \{ \#,) \}$ $First(E') = \{ +, \epsilon \}$ $Follow(E') = \{ \#,) \}$ $First(T) = \{ (, a, b, \wedge \}$ $Follow(T) = \{ +, \#,) \}$ $First(T') = \{ \epsilon, (, a, b, \wedge \}$ $Follow(T') = \{ +, \#,) \}$ $First(F) = \{ (, a, b, \wedge \}$ $Follow(F) = \{ (, a, b, \wedge, +, \#,) \}$ $First(F') = \{ *, \epsilon \}$ $Follow(F') = \{ (, a, b, \wedge, +, \#,) \}$ $First(P) = \{ (, a, b, \wedge \}$ $Follow(P) = \{ *, \epsilon, (, a, b, \wedge, +, \#,) \}$ 

(2) 首先观察到该文法没有左递归,

对于非终结符产生式:

$\text{First}(+E) = \{+\}$, $\text{First}(\epsilon) = \{\epsilon\}$, 交集为 \emptyset .

$\text{First}(T) = \{(\text{, } a, b, \wedge)\}$, $\text{First}(\epsilon) = \{\epsilon\}$, 交集为 \emptyset .

$\text{First}(*F') = \{*\}$, $\text{First}(\epsilon) = \{\epsilon\}$, 交集为 \emptyset .

$\text{First}(\epsilon E) = \{\epsilon\}$, $\text{First}(a) = \{a\}$, $\text{First}(b) = \{b\}$, $\text{First}(\wedge) = \{\wedge\}$, 交集两两为 \emptyset .

其次对于 $\epsilon \in \text{First}(E')$, 有 $\text{First}(E') \cap \text{Follow}(E') = \emptyset$.

$\epsilon \in \text{First}(T')$, 有 $\text{First}(T') \cap \text{Follow}(T') = \emptyset$.

$\epsilon \in \text{First}(F')$, 有 $\text{First}(F') \cap \text{Follow}(F') = \emptyset$.

所以文法是 LL(1) 的

(3).

	+	*	ϵ	a	b	\wedge)	#	(
E			$E \rightarrow TE'$	$E \rightarrow TE'$	$E \rightarrow TE'$	$E \rightarrow TE'$			$E \rightarrow TE'$
E'	$E' \rightarrow +E$						$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$	
T				$T \rightarrow FT'$	$T \rightarrow FT'$	$T \rightarrow FT'$			$T \rightarrow FT'$
T'	$T' \rightarrow \epsilon$			$T' \rightarrow T$	$T' \rightarrow T$	$T' \rightarrow T$	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$	$T' \rightarrow T$
F				$F \rightarrow PF'$	$F \rightarrow PF'$	$F \rightarrow PF'$			$F \rightarrow PF'$
F'	$F' \rightarrow \epsilon$	$F' \rightarrow *F'$		$F' \rightarrow \epsilon$	$F' \rightarrow \epsilon$	$F' \rightarrow \epsilon$	$F' \rightarrow \epsilon$	$F' \rightarrow \epsilon$	$F' \rightarrow \epsilon$
P				$P \rightarrow a$	$P \rightarrow b$	$P \rightarrow \wedge$			$P \rightarrow (E)$

procedure E
begin
 T;
 E';
end.

procedure E'
begin
 if sym = '+' then
 Advance;
 E;
 else if sym = '#' or sym = ')' then
 return;
 else ERROR;

procedure T
begin
 F;
 T';
end.

procedure T'
begin
 if sym = '+' or sym = '#' or sym = ')' then
 return;
 else
 T
 end.
end.

procedure P
begin
 if sym = '(' then
 Advance;
 E;
 if sym = ')' then Advance
 also ERROR

else if sym = 'a' then Advance;
else if sym = 'b' then Advance;
else if sym = ' \wedge ' then Advance;

procedure F
begin
 P;
 F';
end.

procedure F'
begin
 if sym = '*' then
 begin
 Advance;
 F';
 end.
 else if sym = '(' or
 sym = 'a' or sym = 'b' or
 sym = ' \wedge ' or sym = '+' or
 sym = '#' or sym = ')' then
 return
 else ERROR;



$(1) \text{First}(S) = \{a, b, c\}$ $\text{Follow}(S) = \{\#\}$
 $\text{First}(A) = \{a, \epsilon\}$ $\text{Follow}(A) = \{b, c\}$
 $\text{First}(B) = \{b, \epsilon\}$ $\text{Follow}(B) = \{c\}$

① 文法不含左递归

② $\text{First}(a) \cap \text{First}(\epsilon) = \emptyset$,

$\text{First}(b) \cap \text{First}(\epsilon) = \emptyset$

③ $\text{First}(A) \cap \text{Follow}(A) = \emptyset$, $\text{First}(B) \cap \text{Follow}(B) = \emptyset$

为 LL(1) 文法

$(2) \text{First}(S) = \{a, b\}$ $\text{Follow}(S) = \{\#\}$
 $\text{First}(A) = \{a, b, \epsilon\}$ $\text{Follow}(A) = \{b\}$
 $\text{First}(B) = \{b, \epsilon\}$ $\text{Follow}(B) = \{b\}$

因为 $\epsilon \in \text{First}(B)$ 且 $\text{First}(B) \cap \text{Follow}(B) \neq \emptyset$
所以该文法不属于 LL(1)

4. 解: 首先求出各非终结符的 First 集与 Follow 集

$\text{First}(\text{Expr}) = \{-, (, \text{id}\}$, $\text{Follow}(\text{Expr}) = \{\#,)\}$

$\text{First}(\text{ExprTail}) = \{-, \epsilon\}$ $\text{Follow}(\text{ExprTail}) = \{\#,)\}$

$\text{First}(\text{Var}) = \{\text{id}\}$ $\text{Follow}(\text{Var}) = \{-, \#,)\}$

$\text{First}(\text{VarTail}) = \{\epsilon, (\}$ $\text{Follow}(\text{VarTail}) = \{-, \#,)\}$

构造分析表:

	-	id	()	#
Expr	$\text{Expr} \rightarrow -\text{Expr}$	$\text{Expr} \rightarrow \text{id ExprTail}$	$\text{Expr} \rightarrow (\text{Expr})$		
ExprTail	$\text{ExprTail} \rightarrow -\text{Expr}$			$\text{ExprTail} \rightarrow \epsilon$	$\text{ExprTail} \rightarrow \epsilon$
Var		$\text{Var} \rightarrow \text{id}$ VarTail			
VarTail	$\text{VarTail} \rightarrow \epsilon$		$\text{VarTail} \rightarrow (\text{Expr})$	$\text{VarTail} \rightarrow \epsilon$	$\text{VarTail} \rightarrow \epsilon$

