## MIT Intro to solid state chem

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# 1 Introduction

## **Proposition 1**

All matter is made of atoms and such atoms can combne in fixed ratios to form molecules

## **Definition 2** (the 4 quantum numbers)

The principal quantum number n tells us the **shell** that a particular orbital is in and the angular momentum number  $\ell$  tell us the **sub-shell**. Finally the magnetic quantum number m tell us the particular **orbital** of our hydrogen atom state.

The last one will be mentioned shortly below

The total number of orbitals for a given n is

$$1+3+5+\ldots+(2n-1)=n^2$$

It tells us that if we have a *one-eletcron* system with some nucleus of Z protons then there are  $n^2$  degenerate(same energy) orbitals at energy

$$E = -\frac{RZ^2}{n^2}$$

where R is the Rydberg constant

### Fact 3 (Aufbau principle)

Electrons occupy the lowest energy states vailable and there can be at most two electrons per orbital(one of **spin up** and **spin down**. Furthermore **Hund's rule** must be obeyed which states that we always put only one electron in each available orbital if there are multiple at the same energy

The 4th quantum number is the spin magnetic quantum number  $m_s$  which is dictates the spin state of the electron  $(\frac{1}{2} \text{ or } -\frac{1}{2})$ 

### **Proposition 4**

No orbital can have more than 2 electrons and if it has two electrons then they must have opposite spins

## **Definition 5**

The **core electrons** are the electrons cloest to the nucleus and the **valence electrons** are those farthest from the nucleus.

# 2 periodic trends(atoms)

Remark 6. We often use shorthand known as the noble gas configuration for example

$$Si: [Ne]3s^2p^2$$

To understand the order that we fill our orbitals in we downward left diagonal lines across the table and fill the orbitals from top to bottom. For example we will fill in the order 1s,2s,2p,3s,3p,4s...

### Fact 7 (Exception to the Aufbau principle)

The electron configruations for K, Ca, Sc, Ti, V, Cr respectively are  $[Ar]4s^2$ ,  $[Ar]4s^2$ ,  $[Ar]4s^23d$  and  $[Ar]4s^24d^2$ ,  $[Ar]4s^23d^2$ ,  $[Ar]4s^13d^5$  respectively. Basically the 4s orbital turns out to have lower energy than the 3d orbital unlike the rule we mentioned above. The reason has got to do with atoms like have half-full or full orbitals.

#### **Definition 8**

An electronic configuration is **diamagnetic** if all electrons are paired up and is **paramagnetic** if there are unpaired electrons

Consider the following periodic trends

1. **ionization energy**(the energy required to remove an electron from its orbital in an atom). Ionization energy is given by

$$\frac{R(Z_{\rm eff})^2}{n^2}$$

- As we move across the periodic table the effective nuclear charge increases because were adding more protons and the corrrespoding electrons only partially shield the nucleus.
- As we move down the periodic table the value of *n* goes up and that makes more of an impact than the increase in effective nuclear charge. (i.e shielding overcompensates for increase in effective nuclear charge)

So in general the inoization increases to the right and decreases downward except elements such as those with half filled shells like those discussed above

- electron affinity is the amount of energy required to remove an electron from an anion of that element or equivalently the amount of energy by which the system becomes more stable when we add an electron. The trends are basically the same as the above.
- 3. **electronegativeity**(how much a system wants another electron). The trend is basically the same as the above again
- 4. **atomic radius** We generally say that the atomic radius increases down the periodic table and decreases to the right because again the electrons are more tightly bound(so think about it should be the direct opposite of ionization energy trend)

In summary ionization energy, electron affinity, electronegativity

increases right across row and decreases down the column

this is opposite of atomic radius which

decreases right across row and increases down the column

# 3 periodic trends(ions)

The reactivity and periodic trends of *anions* and *cations* compared to their neutral atoms are governed by several key periodic properties, including *electronegativity*, *atomic size*, and *ionization energy*. Understanding how these properties change when atoms gain or lose electrons provides insight into the reactivity of ions.

## 3.1 Reactivity of Anions and Cations vs. Neutral Atoms

### Cations (Positively Charged Ions)

- Formation: A cation forms when an atom loses one or more electrons, typically from its valence shell. This usually occurs for metals, which have relatively low ionization energies.
- Reactivity:
  - Cations are typically electron-deficient, which makes them electrophilic (electron-seeking). Their reactivity
    often involves accepting electrons or forming bonds with nucleophiles (electron-rich species).
  - Cations are more reactive than their neutral atoms in many cases, especially in polar reactions where they
    attract negatively charged species (like anions) or nucleophiles.
  - For example, the  $Na^+$  ion is more reactive in polar solvents like water than neutral sodium (Na), which is relatively stable as a solid metal.

### **Anions (Negatively Charged Ions)**

- Formation: An anion forms when an atom gains one or more electrons. This occurs more readily for nonmetals, which have high electronegativities and strong tendencies to accept electrons.
- Reactivity:
  - Anions are electron-rich, making them nucleophilic (donating electrons to electrophiles). They tend to react with positively charged or electron-deficient species.
  - Anions are generally more reactive than their neutral atoms, especially in reactions that involve donating electrons or forming bonds with electrophiles.
  - For instance,  $Cl^-$  is more reactive as a nucleophile than neutral chlorine  $(Cl_2)$ , which exists as a diatomic molecule.

## 3.2 Periodic Trends in Anions and Cations vs. Neutral Atoms

#### **Electronegativity**

- Definition: Electronegativity is the tendency of an atom to attract shared electrons in a bond.
- Trend in the Periodic Table:
  - Electronegativity increases across a period (left to right) as atoms become smaller and the nuclear charge increases.
  - Electronegativity *decreases down a group* (top to bottom) as the atomic size increases and the effective nuclear charge experienced by the valence electrons decreases.

## · Impact on lons:

Cations: When an atom becomes a cation (loses electrons), it typically becomes more electronegative
compared to its neutral form because the remaining electrons are held more tightly by the nucleus. The
higher positive charge pulls the electron cloud closer, increasing the atom's tendency to attract electrons
in future bonds.

- Example:  $Na^+$  is more electronegative than neutral sodium (Na) because of its smaller size and stronger nuclear attraction to the remaining electrons.
- Anions: When an atom becomes an anion (gains electrons), its effective electronegativity decreases slightly.
   This is because the additional electron(s) increase repulsion within the electron cloud, spreading the charge over a larger space and weakening the attraction of the nucleus for additional electrons.
- Example:  $CI^-$  is less electronegative than neutral chlorine (CI) due to the electron-electron repulsion after gaining an electron.

## **Atomic Size (Atomic Radius)**

- Definition: Atomic size is the distance from the nucleus to the outermost electron shell (valence shell).
- Trend in the Periodic Table:
  - Atomic size decreases across a period as nuclear charge increases, pulling the electron cloud closer to the nucleus.
  - Atomic size increases down a group as new electron shells are added, increasing the distance between the nucleus and the outermost electrons.

#### Impact on lons:

- Cations: Cations are always smaller than their neutral atoms because the loss of electrons reduces electronelectron repulsion and allows the remaining electrons to be pulled closer to the nucleus. Additionally, the
  loss of a valence shell (in many cases) significantly decreases the size.
- Example:  $Na^+$  is much smaller than neutral sodium (Na) because it loses its outermost electron and the remaining electron cloud is pulled inward by the nucleus.
- *Anions*: Anions are always *larger* than their neutral atoms because gaining electrons increases electron-electron repulsion in the outer shell, causing the electron cloud to expand.
- Example:  $Cl^-$  is larger than neutral chlorine (Cl) because the extra electron increases repulsion, spreading out the electron cloud.

## **Ionization Energy**

- *Definition*: Ionization energy is the amount of energy required to remove an electron from a neutral atom in its gaseous state.
- Trend in the Periodic Table:
  - lonization energy increases across a period as nuclear charge increases and the electrons are held more tightly to the nucleus.
  - lonization energy decreases down a group as the outermost electrons are farther from the nucleus and easier to remove.

#### · Impact on lons:

- Cations: The ionization energy for forming a cation (removing an electron) is generally high, but after a cation is formed, subsequent ionization energies are even higher due to the stronger pull of the nucleus on the remaining electrons. Cations, once formed, typically have higher ionization energies than their neutral counterparts because of the increased effective nuclear charge.

- Example:  $Na^+$  has a much higher ionization energy than neutral sodium (Na), making it difficult to remove further electrons from  $Na^+$ .
- Anions: Since anions are formed by gaining electrons, they do not have ionization energies directly related
  to their formation. However, if you were to remove an electron from an anion, it would generally have *lower*ionization energy than the corresponding neutral atom because the added electron weakens the effective
  nuclear charge experienced by the outermost electrons.
- Example: Removing an electron from  $Cl^-$  to revert to neutral chlorine is easier (lower ionization energy) than removing an electron from neutral Cl.

## 3.3 Summary of Reactivity and Periodic Trends

Property	Cations	Anions	Neutral Atoms	
Reactivity	Highly reactive (electrophilic)	Highly reactive (nucleophilic)	Varies by element	
Electronegativity	Higher than neutral atom	Lower than neutral atom	Follows periodic trend	
Atomic Size	Smaller than neutral atom	Larger than neutral atom	Follows periodic trend	
Ionization Energy	Higher than neutral atom	Lower than neutral atom	Increases across period, decreases down grou	

# 4 molecular orbital theory

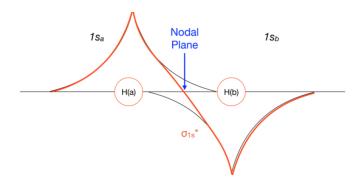


Figure 1: Antionding orbital

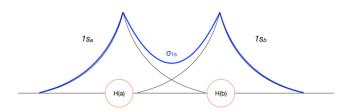
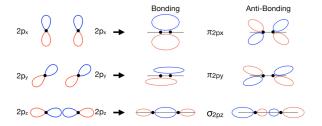


Figure 2: Bonding orbital

**Remark 9.** Note that the middle is a plane view, the  $\pi$  orbitals are overlapping side on



#### **Definition 10**

The bond order calculates the number of bonds formed between two atoms and it is given by

 $BO = \frac{1}{2}$  (number of electrons in bonding molecular orbitals - number in anti-bonding molecular orbitals)

## Example 11

Consider the following molecular orbital diagram

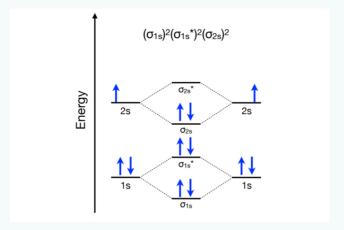


Figure 3: Dilithium

Note that we only needed to look at valence electrons because core electrons always have the same number of bonding and anti bonding orbitals and electrons in those orbitals

Note the it matters whether the orbitals are aligned in th direction of the bond axis or not

## **Definition 12**

**HOMO** highest occupied molecular orbital is the one highest energy with electrons and **LUMO**(lowest unoccupied molecular orbital) is the one lowest energy without electrons

# 5 hybridization

the act of combining orbitals in different ways

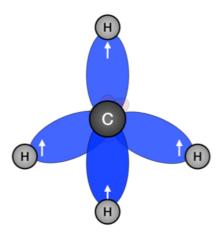


Figure 4: Methane

Carbon  $1s^22s^22p^2$  has 4 valence electrons so it promotes one its electrons into the  $2p_z$  orbitals to form 4  $2sp^3$  orbitals(named as such because this 4 orbitals are made from one s and three p orbitals) where we have formed 4  $\sigma(C2sp^3, H1s)$  bonds

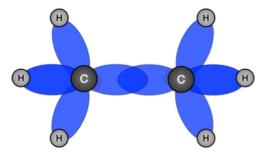


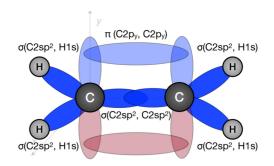
Figure 5: Ethane

Formed by a single  $\sigma(C2sp^3, C2sp^3)$  as well as size  $\sigma(C2sp^3, H1s)$  bond. See that now the electronic configuration becomes



Figure 6: Hybridization: get spin pairing during bonding

Note that we can't twist the hydorgen atoms bonded to the carbon atoms speartey without the snapping the pi bond.



## 6 VSEPR and lewis

Consider

Formula	SN	Structure	Hybridization	Angle	Example
AX <sub>2</sub>	2	Linear	sp	180°	CO <sub>2</sub>
$AX_3$	3	Trigonal planar	$sp^2$	120°	BH <sub>3</sub>
$AX_4$	4	Tetrahedral	sp <sup>3</sup>	109.5°	CH <sub>4</sub>
$AX_5$	5	Trigonal bipyramidal	sp <sup>3</sup> d	$90^{\circ}$ and $120^{\circ}$	PF <sub>5</sub>
$AX_6$	6	Octahedral	$sp^3d^2$	90°	$SF_6$

Formula	SN	Structure	Hybridization	Angle	Example
$AX_3E_2$	5	T-shaped	< 90°	CIF <sub>3</sub>	
$AX_2E_3$	5	Linear	180°	$I_3^-$	
$AX_5E$	6	Square pyramidal	< 90°	$\mathrm{BrF}_5$	
$AX_4E_2$	6	Square planar	90°	$XeF_4$	

Formula	SN	Structure	Hybridization	Angle	Example
$AX_2E$	3	Bent	< 120°	$SO_2$	
$AX_3E$	4	Trigonal pyramid	$< 109.5^{\circ}$	$NH_3$	
$AX_2E_2$	4	Bent	$< 109.5^{\circ}$	$H_2O$	
$AX_4E$	5	See-saw	$< 90^{\circ}$ , $< 120^{\circ}$	$SF_4$	

Consider expanded octet

## Example 13

The anion  $CrO_4^{2-}$  does not have normal octet(maxmimum 8 valence) since it has extra orbitals to accommodate  $Cr: [Ar]4s^13d^5$  It is said to have an **expanded octet** 

See that in total it has 32 valence electrons. But this gives us a +2 formal charge on chromium and -1 formal charge on the oxygen. But it could be made more stable with the following rearrangment

where now we ave two -1 formal charges on two oxygens and 0s everywhere else for a total of -2 formal charge which is the lowest and hence most stable you can get.

# 7 solubility, acids and bases

#### **Definition 14**

A solution s a homogenous mixture(of solids, liquids and gases)

We call the base liquid the solvent and the other materials dissolved in it the solute

#### Fact 15

Solvation(dissolving a solute into a solvent) occurs spontaneously if the solvent-solute attraction is stronger than the solute-solute and solvent-solvent interactions

### Fact 16

In general "like dissolves like" polar liquids like water are good solvents for inonic and polar compounds while nonpolar liquids like hexane are good solvents for nonpolar compounds

#### **Definition 17**

We say a solution is **satruated** when there is undissolved solute remaining because the solvent has dissolved all that it can

## **Definition 18**

The **molar solubility** is the molar ocncentarion(in moles per liter also denoted M) of a solute in a saturated solution

#### **Definition 19**

An **arrhenius acid** is a substance that increases the  $H^+$  concentration in water an **arrhenius base** is a substance that increases the  $H^-$  concentration

### **Definition 20**

A bronsted-lowry acid denotes a proton  $H^+$  while a bronsted-lowry base accepts a proton  $H^+$ 

#### **Definition 21**

Acids and bases also have conjugate bases and acids repsectively corrresponding to rmeoving or adding a  $H^+$  ion repsectively

## Example 22

$$CH_3COOH(aq) + H_2O(\ell) \rightleftharpoons H_3O^+(aq) + CH_3COO^-(aq)$$

we can think  $CH_3COO^-$  as the **conjugate base** of the original acid  $CH_3COOH$  and  $H_3O^+$  as the **conjugate acid** of  $H_2O$ 

## Example 23

This is an example of an amphoteric moelcule which can either be an acid or base

$$HCO_3^-(aq) + H_2O(\ell) \rightleftharpoons H_3O^+(aq) + CO_3^{2-}(aq)$$

$$HCO_3^-(aq) + H_2O(\ell) \rightleftharpoons H_2CO_3(aq) + OH^-(aq)$$

#### **Definition 24**

A lewis acid is a psecies that accepts lone pair electrons and a lewis base is one that donates lone pair electrons

#### **Definition 25**

The pH and pOH of a water based solution are given by

$$pH - = \log[H_3O^+], \quad pOH - = \log[OH^-]$$

and

$$pH + pOH = 14.0$$

Recall from organic chemistry that we know for hydrogen halides in general down the group means stronger acid Acidity rank

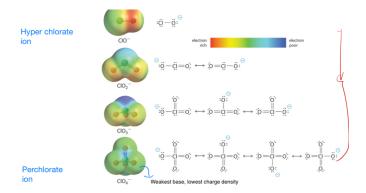
and that bascity rank

$$I^{-} < Br^{-} < CI^{-} < F^{-}$$

where the weaker the base the better its stabilizes a negative charge. However this it not true for hypohalous acids(HOX) with X representing a halogen. Acid rank

this is due to **inductive effects** where the electronegativity of X increases the distribution of electron density withint the molecule shifts away from the O-H bond making it weakeer as easier to lose proton  $H^+$ 

Another factor to consider is electron delocalization in the conjugate base



Clearly the weakest conjugate base(the most stable) as seen here has the most resonance structures which means its acid is more acidic(it wants to achieve this more stable end result more badly). This is also covered in organic chemistry

## 8 redox

#### **Definition 26**

oxidation is the term for a compound "losing electrons" and reduction is the term for "gaining electrons"

oxidation numbers increases when an atom loses electrons and decrease when an atom gains electrons

#### **Definition 27**

The **oxidinzing agent** in a reaction is the reactant that is reduced(gaining electrons) and the reducing agent is the reactant that is being oxidized(losing electrons)

### Example 28

$$2AI(\ell) + Cr_2O_3(s) \rightleftharpoons AI_2O_3(s) + 2Cr(\ell)$$

where Chromium(III) is the oxidizing agent(reduced from +3 to 0) and aluminum is the reducing agent(oxidized to a number of +3)

## 9 covalent bonding

in general the higher the bond order and the stronger the covalent bond. But size matters too

Remark 29. note the strenght of bond is similar ranked in decreasing order for

$$I-I>Br-Br-Br$$
,  $CI-CI>F-F$ 

and

$$H-I > H-Br-Br, H-CI > H-F$$

the size of atom increases more than proportionately compared volume of orbital overlap resulting in decreasing bond strength(see saylor page 146 chapter 8.8)