Exercise 7:

Foundations of Mathematical, WS24

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This is **exercise** 7 for Foundations of Mathematical, WS24. Generated on 2024-11-04 with 10 problems per section.

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1. Introduction

! Practice makes perfect.

We need many exercises to master the skill of mathmatical. However, it's not easy to find the exercise which just fit for you.

So, I create this repo to generate the exercise for you.

Just enjoy it!

The syntax of this document is Quarto syntax, which is a markdown-based language. It is designed to be human-readable and easy to write, while also being powerful enough to support complex document structures.

You can check the syllabus of this course in the following link: Syllabus°.

2. Exercise

2.1. Vector Arithmetic

2.1.1. Addition

1. Let $\mathbf{u} = \begin{bmatrix} -7 \\ 5 \\ 2 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 9 \\ -8 \\ 2 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
2. Let $\mathbf{u} = \begin{bmatrix} 8 \\ 4 \\ 9 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -9 \\ 10 \\ -7 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
3. Let $\mathbf{u} = \begin{bmatrix} -10 \\ -9 \\ -7 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -8 \\ 8 \\ 10 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
4. Let $\mathbf{u} = \begin{bmatrix} 10 \\ -4 \\ -3 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 7 \\ 8 \\ -6 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
5. Let $\mathbf{u} = \begin{bmatrix} 3 \\ 1 \\ 10 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -9 \\ -10 \\ 10 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
6. Let $\mathbf{u} = \begin{bmatrix} 2 \\ -5 \\ -2 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -4 \\ -10 \\ 5 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
7. Let $\mathbf{u} = \begin{bmatrix} 8 \\ -5 \\ -4 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -6 \\ 4 \\ 10 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
8. Let $\mathbf{u} = \begin{bmatrix} -2 \\ -5 \\ -8 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 1 \\ -4 \\ 8 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
9. Let $\mathbf{u} = \begin{bmatrix} -10 \\ 7 \\ -9 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -9 \\ 0 \\ -7 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.
10. Let $\mathbf{u} = \begin{bmatrix} 0 \\ -2 \\ -7 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 4 \\ 10 \\ -10 \end{bmatrix}$. Compute $\mathbf{u} + \mathbf{v}$.

2.1.2. Subtraction

1. Let $\mathbf{u} = \begin{bmatrix} -6 \\ 5 \\ -1 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 5 \\ -4 \\ -7 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
2. Let $\mathbf{u} = \begin{bmatrix} 5 \\ 0 \\ -9 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 2 \\ -7 \\ -9 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
3. Let $\mathbf{u} = \begin{bmatrix} 10 \\ 9 \\ 5 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 4 \\ 0 \\ -6 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
4. Let $\mathbf{u} = \begin{bmatrix} 3 \\ 7 \\ 1 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 2 \\ 9 \\ 8 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
5. Let $\mathbf{u} = \begin{bmatrix} -7 \\ -10 \\ 3 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -10 \\ 1 \\ 4 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
6. Let $\mathbf{u} = \begin{bmatrix} 8 \\ 3 \\ -9 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -10 \\ -4 \\ -7 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.

7. Let $\mathbf{u} = \begin{bmatrix} -1 \\ 4 \\ -10 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -10 \\ 2 \\ -6 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
8. Let $\mathbf{u} = \begin{bmatrix} -9 \\ 0 \\ -3 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 5 \\ 10 \\ 9 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
9. Let $\mathbf{u} = \begin{bmatrix} 10 \\ 8 \\ 10 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} 0 \\ 3 \\ 5 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.
10. Let $\mathbf{u} = \begin{bmatrix} -3 \\ -10 \\ 6 \end{bmatrix}$ and $\mathbf{v} = \begin{bmatrix} -2 \\ 8 \\ -9 \end{bmatrix}$. Compute $\mathbf{u} - \mathbf{v}$.

2.1.3. Scalar Multiplication

1. Let $\mathbf{u} = \begin{bmatrix} -5 \\ 1 \\ -4 \end{bmatrix}$. Compute $0\mathbf{v}$.
2. Let $\mathbf{u} = \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$. Compute $-10\mathbf{v}$.
3. Let $\mathbf{u} = \begin{bmatrix} 3 \\ 5 \\ 5 \end{bmatrix}$. Compute $6\mathbf{v}$.
4. Let $\mathbf{u} = \begin{bmatrix} 2 \\ 5 \\ -4 \end{bmatrix}$. Compute $7\mathbf{v}$.
5. Let $\mathbf{u} = \begin{bmatrix} -1 \\ 9 \\ 0 \end{bmatrix}$. Compute $-4\mathbf{v}$.
6. Let $\mathbf{u} = \begin{bmatrix} -9 \\ -1 \\ -10 \end{bmatrix}$. Compute $2\mathbf{v}$.
7. Let $\mathbf{u} = \begin{bmatrix} 7 \\ 10 \\ -2 \end{bmatrix}$. Compute $3\mathbf{v}$.
8. Let $\mathbf{u} = \begin{bmatrix} 10 \\ 2 \\ 4 \end{bmatrix}$. Compute $1\mathbf{v}$.
9. Let $\mathbf{u} = \begin{bmatrix} 5 \\ 7 \\ -5 \end{bmatrix}$. Compute $2\mathbf{v}$.
10. Let $\mathbf{u} = \begin{bmatrix} -3 \\ 9 \\ -2 \end{bmatrix}$. Compute $-6\mathbf{v}$.

2.2. Matrix Arithmetic

2.2.1. Addition

1. Let $A = \begin{bmatrix} -1 & -5 & -4 \\ -2 & 6 & 5 \\ -10 & -5 & -1 \end{bmatrix}$ and $B = \begin{bmatrix} 6 & 2 & -2 \\ -4 & -8 & -4 \\ -3 & 7 & -10 \end{bmatrix}$. Compute $A + B$.
2. Let $A = \begin{bmatrix} -6 & 3 & 6 \\ 1 & -3 & 1 \\ -3 & 9 & -1 \end{bmatrix}$ and $B = \begin{bmatrix} 7 & -5 & -1 \\ -7 & -7 & 5 \\ 7 & 8 & -5 \end{bmatrix}$. Compute $A + B$.
3. Let $A = \begin{bmatrix} -5 & 5 & -3 \\ -9 & 9 & 5 \\ -3 & 9 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 8 & 1 & -10 \\ 1 & 5 & 7 \\ 7 & -9 & 0 \end{bmatrix}$. Compute $A + B$.

4. Let $A = \begin{bmatrix} 8 & 6 & -10 \\ 3 & 8 & -5 \\ 1 & 1 & -8 \end{bmatrix}$ and $B = \begin{bmatrix} 4 & -2 & -3 \\ -6 & -6 & 5 \\ -4 & -3 & -3 \end{bmatrix}$. Compute $A + B$.
5. Let $A = \begin{bmatrix} -10 & 6 & 5 \\ 1 & 8 & -9 \\ -10 & 0 & 6 \end{bmatrix}$ and $B = \begin{bmatrix} -6 & 0 & -2 \\ -9 & 1 & 4 \\ -4 & -8 & -2 \end{bmatrix}$. Compute $A + B$.
6. Let $A = \begin{bmatrix} 6 & -7 & 2 \\ 3 & -3 & -4 \\ -4 & 8 & -2 \end{bmatrix}$ and $B = \begin{bmatrix} 5 & 1 & 1 \\ 0 & -5 & 5 \\ -3 & 2 & 0 \end{bmatrix}$. Compute $A + B$.
7. Let $A = \begin{bmatrix} 4 & 5 & 0 \\ -4 & -2 & -5 \\ -6 & 5 & -7 \end{bmatrix}$ and $B = \begin{bmatrix} 5 & -5 & 7 \\ 2 & -1 & 2 \\ -10 & 0 & -10 \end{bmatrix}$. Compute $A + B$.
8. Let $A = \begin{bmatrix} 9 & 5 & -2 \\ -5 & -6 & -3 \\ 0 & 6 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 4 & -2 & 2 \\ -3 & -5 & 7 \\ -10 & 1 & -3 \end{bmatrix}$. Compute $A + B$.
9. Let $A = \begin{bmatrix} 3 & -1 & -3 \\ -9 & 3 & -8 \\ -5 & 3 & 6 \end{bmatrix}$ and $B = \begin{bmatrix} 6 & -10 & 6 \\ -6 & -9 & -6 \\ -5 & 0 & 5 \end{bmatrix}$. Compute $A + B$.
10. Let $A = \begin{bmatrix} 8 & -8 & 9 \\ -1 & 6 & 3 \\ 7 & 5 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} -3 & 3 & -7 \\ 7 & -8 & -7 \\ -10 & -6 & 5 \end{bmatrix}$. Compute $A + B$.

2.2.2. Subtraction

1. Let $A = \begin{bmatrix} 3 & -10 & 8 \\ -10 & -4 & -8 \\ 9 & 0 & -10 \end{bmatrix}$ and $B = \begin{bmatrix} -1 & -3 & 4 \\ -5 & -9 & 5 \\ -6 & 1 & 2 \end{bmatrix}$. Compute $A - B$.
2. Let $A = \begin{bmatrix} 0 & -9 & 6 \\ -9 & -7 & 8 \\ -8 & 4 & -2 \end{bmatrix}$ and $B = \begin{bmatrix} -9 & 9 & -7 \\ -4 & 5 & -9 \\ 2 & 3 & 6 \end{bmatrix}$. Compute $A - B$.
3. Let $A = \begin{bmatrix} -1 & 1 & -10 \\ 2 & 7 & 8 \\ 1 & -6 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 5 & 4 & -9 \\ -8 & 1 & 9 \\ 4 & 6 & -10 \end{bmatrix}$. Compute $A - B$.
4. Let $A = \begin{bmatrix} 9 & -7 & 6 \\ 7 & 6 & -8 \\ 0 & -2 & -5 \end{bmatrix}$ and $B = \begin{bmatrix} -4 & -3 & -3 \\ 6 & -8 & 1 \\ -1 & -8 & -6 \end{bmatrix}$. Compute $A - B$.
5. Let $A = \begin{bmatrix} -9 & -6 & -6 \\ -2 & 1 & -5 \\ 3 & -8 & 7 \end{bmatrix}$ and $B = \begin{bmatrix} 9 & -10 & 4 \\ 1 & -4 & -4 \\ -9 & -3 & 5 \end{bmatrix}$. Compute $A - B$.
6. Let $A = \begin{bmatrix} -1 & -9 & 2 \\ 2 & -1 & -2 \\ -7 & -1 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} -5 & 0 & -8 \\ -7 & 0 & 5 \\ 5 & -3 & -4 \end{bmatrix}$. Compute $A - B$.
7. Let $A = \begin{bmatrix} -9 & 5 & 0 \\ -5 & 9 & 6 \\ -4 & 0 & -8 \end{bmatrix}$ and $B = \begin{bmatrix} 4 & 1 & -6 \\ 4 & 3 & 4 \\ -8 & -6 & -10 \end{bmatrix}$. Compute $A - B$.
8. Let $A = \begin{bmatrix} 7 & 7 & 3 \\ 0 & -9 & 4 \\ -8 & 5 & -7 \end{bmatrix}$ and $B = \begin{bmatrix} -9 & -7 & -4 \\ 4 & -9 & -6 \\ 3 & 6 & -9 \end{bmatrix}$. Compute $A - B$.
9. Let $A = \begin{bmatrix} 3 & -10 & -4 \\ -10 & 1 & 6 \\ 2 & -8 & 6 \end{bmatrix}$ and $B = \begin{bmatrix} -4 & 3 & 9 \\ -7 & -3 & 6 \\ 3 & 4 & -4 \end{bmatrix}$. Compute $A - B$.
10. Let $A = \begin{bmatrix} -2 & 7 & -7 \\ -5 & -4 & -6 \\ -10 & 3 & 3 \end{bmatrix}$ and $B = \begin{bmatrix} -9 & -8 & -1 \\ 6 & 3 & 2 \\ 5 & 7 & -2 \end{bmatrix}$. Compute $A - B$.

2.2.3. Multiplication

1. Let $A = \begin{bmatrix} -10 & -7 & -1 \\ -2 & -1 & -4 \\ -1 & 3 & 8 \end{bmatrix}$ and $B = \begin{bmatrix} -6 & -10 & -1 \\ -8 & -4 & 1 \\ 4 & -1 & -7 \end{bmatrix}$. Compute $A \cdot B$.
2. Let $A = \begin{bmatrix} 7 & 0 & -9 \\ 6 & 6 & -7 \\ -10 & 3 & 7 \end{bmatrix}$ and $B = \begin{bmatrix} 4 & 1 & 6 \\ 8 & 2 & -4 \\ -3 & 6 & -3 \end{bmatrix}$. Compute $A \cdot B$.
3. Let $A = \begin{bmatrix} 4 & -9 & 7 \\ 1 & 0 & 5 \\ 4 & -6 & 6 \end{bmatrix}$ and $B = \begin{bmatrix} -4 & -9 & -1 \\ 8 & 8 & 1 \\ 0 & -6 & 9 \end{bmatrix}$. Compute $A \cdot B$.
4. Let $A = \begin{bmatrix} 8 & 7 & -6 \\ -6 & -4 & 3 \\ -9 & 3 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & 6 & -3 \\ 0 & 1 & 2 \\ -2 & 5 & 9 \end{bmatrix}$. Compute $A \cdot B$.
5. Let $A = \begin{bmatrix} -2 & -1 & -5 \\ -2 & -1 & -8 \\ -6 & -9 & -1 \end{bmatrix}$ and $B = \begin{bmatrix} 0 & -3 & 5 \\ -6 & -5 & 4 \\ -4 & -3 & 4 \end{bmatrix}$. Compute $A \cdot B$.
6. Let $A = \begin{bmatrix} 8 & -6 & -10 \\ 3 & -9 & -2 \\ -8 & -4 & -5 \end{bmatrix}$ and $B = \begin{bmatrix} -9 & 3 & 0 \\ 4 & -9 & 8 \\ -1 & 1 & 1 \end{bmatrix}$. Compute $A \cdot B$.
7. Let $A = \begin{bmatrix} 6 & 4 & 8 \\ 1 & 1 & -1 \\ 3 & -9 & -5 \end{bmatrix}$ and $B = \begin{bmatrix} 4 & 4 & -3 \\ 9 & 4 & -4 \\ 5 & -7 & 0 \end{bmatrix}$. Compute $A \cdot B$.
8. Let $A = \begin{bmatrix} -3 & -3 & -6 \\ 1 & 5 & 8 \\ 2 & -8 & -8 \end{bmatrix}$ and $B = \begin{bmatrix} -2 & 7 & -2 \\ 2 & 5 & -6 \\ -6 & -5 & 8 \end{bmatrix}$. Compute $A \cdot B$.
9. Let $A = \begin{bmatrix} 5 & -5 & 8 \\ 3 & -5 & 6 \\ -10 & -5 & -7 \end{bmatrix}$ and $B = \begin{bmatrix} -9 & 3 & 2 \\ 4 & -2 & 2 \\ 8 & 8 & -9 \end{bmatrix}$. Compute $A \cdot B$.
10. Let $A = \begin{bmatrix} -2 & -3 & -1 \\ 3 & 5 & -5 \\ -8 & -1 & -8 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 8 & 2 \\ 9 & 2 & 7 \\ 8 & -9 & -1 \end{bmatrix}$. Compute $A \cdot B$.

3. Answer

3.1. Vector Arithmetic

3.1.1. Addition

1: $\begin{bmatrix} 2 \\ -3 \\ 4 \end{bmatrix}$ 2: $\begin{bmatrix} -1 \\ 14 \\ 2 \end{bmatrix}$ 3: $\begin{bmatrix} -18 \\ -1 \\ 3 \end{bmatrix}$ 4: $\begin{bmatrix} 17 \\ 4 \\ -9 \end{bmatrix}$ 5: $\begin{bmatrix} -6 \\ -9 \\ 20 \end{bmatrix}$

6: $\begin{bmatrix} -2 \\ -15 \\ 3 \end{bmatrix}$ 7: $\begin{bmatrix} 2 \\ -1 \\ 6 \end{bmatrix}$ 8: $\begin{bmatrix} -1 \\ -9 \\ 0 \end{bmatrix}$ 9: $\begin{bmatrix} -19 \\ 7 \\ -16 \end{bmatrix}$ 10: $\begin{bmatrix} 4 \\ 8 \\ -17 \end{bmatrix}$

3.1.2. Subtraction

1: $\begin{bmatrix} -11 \\ 9 \\ 6 \end{bmatrix}$ 2: $\begin{bmatrix} 3 \\ 7 \\ 0 \end{bmatrix}$ 3: $\begin{bmatrix} 6 \\ 9 \\ 11 \end{bmatrix}$ 4: $\begin{bmatrix} 1 \\ -2 \\ -7 \end{bmatrix}$ 5: $\begin{bmatrix} 3 \\ -11 \\ -1 \end{bmatrix}$

6: $\begin{bmatrix} 18 \\ 7 \\ -2 \end{bmatrix}$ 7: $\begin{bmatrix} 9 \\ 2 \\ -4 \end{bmatrix}$ 8: $\begin{bmatrix} -14 \\ -10 \\ -12 \end{bmatrix}$ 9: $\begin{bmatrix} 10 \\ 5 \\ 5 \end{bmatrix}$ 10: $\begin{bmatrix} -1 \\ -18 \\ 15 \end{bmatrix}$

3.1.3. Scalar Multiplication

1: $\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$ 2: $\begin{bmatrix} 0 \\ 10 \\ 0 \end{bmatrix}$ 3: $\begin{bmatrix} 18 \\ 30 \\ 30 \end{bmatrix}$ 4: $\begin{bmatrix} 14 \\ 35 \\ -28 \end{bmatrix}$ 5: $\begin{bmatrix} 4 \\ -36 \\ 0 \end{bmatrix}$

6: $\begin{bmatrix} -18 \\ -2 \\ -20 \end{bmatrix}$ 7: $\begin{bmatrix} 21 \\ 30 \\ -6 \end{bmatrix}$ 8: $\begin{bmatrix} 10 \\ 2 \\ 4 \end{bmatrix}$ 9: $\begin{bmatrix} 10 \\ 14 \\ -10 \end{bmatrix}$ 10: $\begin{bmatrix} 18 \\ -54 \\ 12 \end{bmatrix}$

3.2. Matrix Arithmetic

3.2.1. Addition

1: $\begin{bmatrix} 5 & -3 & -6 \\ -6 & -2 & 1 \\ -13 & 2 & -11 \end{bmatrix}$ 2: $\begin{bmatrix} 1 & -2 & 5 \\ -6 & -10 & 6 \\ 4 & 17 & -6 \end{bmatrix}$ 3: $\begin{bmatrix} 3 & 6 & -13 \\ -8 & 14 & 12 \\ 4 & 0 & 2 \end{bmatrix}$ 4: $\begin{bmatrix} 12 & 4 & -13 \\ -3 & 2 & 0 \\ -3 & -2 & -11 \end{bmatrix}$ 5: $\begin{bmatrix} -16 & 6 & 3 \\ -8 & 9 & -5 \\ -14 & -8 & 4 \end{bmatrix}$

6: $\begin{bmatrix} 11 & -6 & 3 \\ 3 & -8 & 1 \\ -7 & 10 & -2 \end{bmatrix}$ 7: $\begin{bmatrix} 9 & 0 & 7 \\ -2 & -3 & -3 \\ -16 & 5 & -17 \end{bmatrix}$ 8: $\begin{bmatrix} 13 & 3 & 0 \\ -8 & -11 & 4 \\ -10 & 7 & -1 \end{bmatrix}$ 9: $\begin{bmatrix} 9 & -11 & 3 \\ -15 & -6 & -14 \\ -10 & 3 & 11 \end{bmatrix}$ 10: $\begin{bmatrix} 5 & -5 & 2 \\ 6 & -2 & -4 \\ -3 & -1 & 1 \end{bmatrix}$

3.2.2. Subtraction

1: $\begin{bmatrix} 4 & -7 & 4 \\ -5 & 5 & -13 \\ 15 & -1 & -12 \end{bmatrix}$ 2: $\begin{bmatrix} 9 & -18 & 13 \\ -5 & -12 & 17 \\ -10 & 1 & -8 \end{bmatrix}$ 3: $\begin{bmatrix} -6 & -3 & -1 \\ 10 & 6 & -1 \\ -3 & -12 & 12 \end{bmatrix}$ 4: $\begin{bmatrix} 13 & -4 & 9 \\ 1 & 14 & -9 \\ 1 & 6 & 1 \end{bmatrix}$ 5: $\begin{bmatrix} -18 & 4 & -10 \\ -3 & 5 & -1 \\ 12 & -5 & 2 \end{bmatrix}$

6: $\begin{bmatrix} 4 & -9 & 10 \\ 9 & -1 & -7 \\ -12 & 2 & 8 \end{bmatrix}$ 7: $\begin{bmatrix} -13 & 4 & 6 \\ -9 & 6 & 2 \\ 4 & 6 & 2 \end{bmatrix}$ 8: $\begin{bmatrix} 16 & 14 & 7 \\ -4 & 0 & 10 \\ -11 & -1 & 2 \end{bmatrix}$ 9: $\begin{bmatrix} 7 & -13 & -13 \\ -3 & 4 & 0 \\ -1 & -12 & 10 \end{bmatrix}$ 10: $\begin{bmatrix} 7 & 15 & -6 \\ -11 & -7 & -8 \\ -15 & -4 & 5 \end{bmatrix}$

3.2.3. Multiplication

1: $\begin{bmatrix} 112 & 129 & 10 \\ 4 & 28 & 29 \\ 14 & -10 & -52 \end{bmatrix}$ 2: $\begin{bmatrix} 55 & -47 & 69 \\ 93 & -24 & 33 \\ -37 & 38 & -93 \end{bmatrix}$ 3: $\begin{bmatrix} -88 & -150 & 50 \\ -4 & -39 & 44 \\ -64 & -120 & 44 \end{bmatrix}$ 4: $\begin{bmatrix} 36 & 25 & -64 \\ -24 & -25 & 37 \\ -19 & -71 & -3 \end{bmatrix}$ 5: $\begin{bmatrix} 26 & 26 & -34 \\ 38 & 35 & -46 \\ 58 & 66 & -70 \end{bmatrix}$

6: $\begin{bmatrix} -86 & 68 & -58 \\ -61 & 88 & -74 \\ 61 & 7 & -37 \end{bmatrix}$ 7: $\begin{bmatrix} 100 & -16 & -34 \\ 8 & 15 & -7 \\ -94 & 11 & 27 \end{bmatrix}$ 8: $\begin{bmatrix} 36 & -6 & -24 \\ -40 & -8 & 32 \\ 28 & 14 & -20 \end{bmatrix}$ 9: $\begin{bmatrix} -1 & 89 & -72 \\ 1 & 67 & -58 \\ 14 & -76 & 33 \end{bmatrix}$ 10: $\begin{bmatrix} -37 & -13 & -24 \\ 8 & 79 & 46 \\ -81 & 6 & -15 \end{bmatrix}$