## **Mathematical Exercise**

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**Abstract** This is **exercise** 1 for Foundations of Mathematical, WS24. Generated on 2024-10-28 with 10 problems per section.

## Introduction

Practice makes perfect.

We need many exercises to master the skill of mathmatical. However, it's not easy to find the exercise which just fit for you.

So, I create this repo to generate the exercise for you.

Just enjoy it!

The syntax of this document is Quarto syntax, which is a markdown-based language. It is designed to be human-readable and easy to write, while also being powerful enough to support complex document structures.

You can check the syllabus of this course in the following link: Syllabus.

### **Exercise**

#### **Vector Arithmetic**

#### Addition

1. Let 
$$\mathbf{u} = \begin{bmatrix} -6 \\ 6 \\ 5 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -2 \\ 9 \\ -8 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

2. Let  $\mathbf{u} = \begin{bmatrix} 6 \\ 4 \\ -4 \end{bmatrix}$  and  $\mathbf{v} = \begin{bmatrix} -7 \\ 10 \\ 1 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

3. Let  $\mathbf{u} = \begin{bmatrix} -9 \\ -4 \\ -8 \end{bmatrix}$  and  $\mathbf{v} = \begin{bmatrix} 10 \\ -6 \\ 6 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

4. Let 
$$\mathbf{u} = \begin{bmatrix} 8 \\ 5 \\ -4 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -10 \\ 4 \\ 5 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

5. Let 
$$\mathbf{u} = \begin{bmatrix} 1 \\ -7 \\ -2 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -9 \\ 4 \\ -5 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

6. Let 
$$\mathbf{u} = \begin{bmatrix} -4 \\ -2 \\ 3 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 7 \\ -9 \\ -3 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

7. Let 
$$\mathbf{u} = \begin{bmatrix} -9 \\ 0 \\ 2 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -3 \\ -10 \\ 9 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

8. Let 
$$\mathbf{u} = \begin{bmatrix} 5 \\ -10 \\ 10 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 5 \\ 10 \\ 1 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

9. Let 
$$\mathbf{u} = \begin{bmatrix} -4 \\ 2 \\ -1 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -6 \\ -4 \\ 0 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

10. Let 
$$\mathbf{u} = \begin{bmatrix} 10 \\ -2 \\ 0 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 4 \\ -2 \\ 7 \end{bmatrix}$ . Compute  $\mathbf{u} + \mathbf{v}$ .

#### **Subtraction**

1. Let 
$$\mathbf{u} = \begin{bmatrix} -1 \\ -1 \\ 6 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 6 \\ -1 \\ 5 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

2. Let 
$$\mathbf{u} = \begin{bmatrix} 4 \\ -2 \\ 2 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 4 \\ -8 \\ 3 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

3. Let 
$$\mathbf{u} = \begin{bmatrix} -9 \\ 1 \\ -7 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 2 \\ 5 \\ -2 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

4. Let 
$$\mathbf{u} = \begin{bmatrix} 6 \\ 2 \\ -2 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -8 \\ 1 \\ 6 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

5. Let 
$$\mathbf{u} = \begin{bmatrix} -2 \\ 4 \\ -5 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 6 \\ 9 \\ -2 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

6. Let 
$$\mathbf{u} = \begin{bmatrix} 3 \\ -7 \\ 10 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 6 \\ -10 \\ -1 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

7. Let 
$$\mathbf{u} = \begin{bmatrix} -9 \\ -8 \\ 5 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 2 \\ -2 \\ 8 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

8. Let 
$$\mathbf{u} = \begin{bmatrix} 4 \\ -10 \\ -7 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} -2 \\ 7 \\ 1 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

9. Let 
$$\mathbf{u} = \begin{bmatrix} 10 \\ 0 \\ 0 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 8 \\ 9 \\ -10 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

10. Let 
$$\mathbf{u} = \begin{bmatrix} -10 \\ 3 \\ 7 \end{bmatrix}$$
 and  $\mathbf{v} = \begin{bmatrix} 8 \\ 5 \\ -7 \end{bmatrix}$ . Compute  $\mathbf{u} - \mathbf{v}$ .

### **Scalar Multiplication**

1. Let 
$$\mathbf{u} = \begin{bmatrix} -9 \\ 2 \\ 1 \end{bmatrix}$$
. Compute  $2\mathbf{v}$ .

2. Let 
$$\mathbf{u} = \begin{bmatrix} 5 \\ -10 \\ -9 \end{bmatrix}$$
. Compute  $2\mathbf{v}$ .

3. Let 
$$\mathbf{u} = \begin{bmatrix} -7 \\ -3 \\ -5 \end{bmatrix}$$
. Compute  $3\mathbf{v}$ .

4. Let 
$$\mathbf{u} = \begin{bmatrix} 8 \\ -6 \\ -9 \end{bmatrix}$$
. Compute  $1\mathbf{v}$ .

5. Let 
$$\mathbf{u} = \begin{bmatrix} 5 \\ 1 \\ 3 \end{bmatrix}$$
. Compute  $-3\mathbf{v}$ .

6. Let 
$$\mathbf{u} = \begin{bmatrix} 0 \\ 9 \\ -3 \end{bmatrix}$$
. Compute 1v.

7. Let 
$$\mathbf{u} = \begin{bmatrix} -5 \\ 3 \\ -2 \end{bmatrix}$$
. Compute  $10\mathbf{v}$ .

8. Let 
$$\mathbf{u} = \begin{bmatrix} 5 \\ -1 \\ 0 \end{bmatrix}$$
. Compute  $-1\mathbf{v}$ .

9. Let 
$$\mathbf{u} = \begin{bmatrix} -3 \\ 5 \\ -1 \end{bmatrix}$$
. Compute  $-3\mathbf{v}$ .

10. Let 
$$\mathbf{u} = \begin{bmatrix} -10 \\ 9 \\ -3 \end{bmatrix}$$
. Compute  $10\mathbf{v}$ .

## **Matrix Arithmetic**

#### Addition

1. Let 
$$A = \begin{bmatrix} 4 & -10 & -8 \\ -5 & 0 & -10 \\ 8 & 7 & 0 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 9 & -2 & -3 \\ -5 & 6 & -4 \\ -9 & 4 & 0 \end{bmatrix}$ . Compute  $A + B$ .

2. Let 
$$A = \begin{bmatrix} 8 & 2 & -2 \\ -8 & -9 & 5 \\ -10 & -7 & -10 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 2 & 5 & -9 \\ -9 & -6 & -9 \\ -5 & -5 & -3 \end{bmatrix}$ . Compute  $A + B$ .

3. Let 
$$A = \begin{bmatrix} 8 & 7 & -3 \\ -1 & -2 & -3 \\ -8 & 2 & 3 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 8 & 6 & 6 \\ 6 & 7 & 5 \\ 0 & 5 & -10 \end{bmatrix}$ . Compute  $A + B$ .

4. Let 
$$A = \begin{bmatrix} 9 & 8 & -9 \\ 2 & -6 & -6 \\ -6 & -5 & -9 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 3 & -2 & 2 \\ 7 & -7 & -1 \\ 9 & -4 & 2 \end{bmatrix}$ . Compute  $A + B$ .

5. Let 
$$A = \begin{bmatrix} -6 & -2 & 5 \\ 1 & 6 & 0 \\ 0 & -8 & -10 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -8 & -10 & 6 \\ -4 & 9 & -3 \\ -5 & -1 & -2 \end{bmatrix}$ . Compute  $A + B$ .

6. Let 
$$A = \begin{bmatrix} -4 & 9 & -6 \\ -5 & 0 & -2 \\ -2 & -10 & 1 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -9 & -6 & -10 \\ -8 & 9 & -5 \\ 5 & -3 & -3 \end{bmatrix}$ . Compute  $A + B$ .

7. Let 
$$A = \begin{bmatrix} 9 & -1 & 4 \\ 2 & 9 & -7 \\ 5 & -3 & -9 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 3 & 8 & 4 \\ 8 & -10 & 0 \\ -2 & 0 & 8 \end{bmatrix}$ . Compute  $A + B$ .

8. Let 
$$A = \begin{bmatrix} 9 & -10 & -4 \\ 7 & 4 & 8 \\ -8 & 3 & -10 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 8 & 8 & 5 \\ 0 & 5 & 2 \\ 9 & 8 & 7 \end{bmatrix}$ . Compute  $A + B$ .

9. Let 
$$A = \begin{bmatrix} 7 & -7 & -7 \\ -10 & 9 & 0 \\ -10 & 9 & -6 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 2 & -5 & -5 \\ -5 & -1 & 2 \\ 6 & 5 & -9 \end{bmatrix}$ . Compute  $A + B$ .

10. Let 
$$A = \begin{bmatrix} 5 & 8 & -8 \\ -10 & -2 & 7 \\ 2 & 2 & -1 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 3 & -4 & 7 \\ 4 & -7 & 2 \\ 3 & 6 & -1 \end{bmatrix}$ . Compute  $A + B$ .

1. Let 
$$A = \begin{bmatrix} 3 & -4 & -8 \\ -3 & -2 & 7 \\ -5 & 5 & -8 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -6 & -6 & 7 \\ 2 & -5 & -8 \\ 5 & 1 & 9 \end{bmatrix}$ . Compute  $A - B$ .

2. Let 
$$A = \begin{bmatrix} 0 & -4 & -1 \\ 1 & -5 & -5 \\ -8 & 9 & 6 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 3 & 4 & -6 \\ -7 & 1 & -10 \\ -8 & 2 & 0 \end{bmatrix}$ . Compute  $A - B$ .

3. Let 
$$A = \begin{bmatrix} -5 & -5 & 6 \\ -9 & -5 & -5 \\ 2 & -6 & 4 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -6 & -3 & -6 \\ -3 & 2 & 0 \\ 1 & 4 & 0 \end{bmatrix}$ . Compute  $A - B$ .

4. Let 
$$A = \begin{bmatrix} -9 & -5 & 5 \\ -4 & 8 & -10 \\ -4 & 2 & 2 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -10 & -2 & 7 \\ 6 & 8 & -1 \\ -4 & -2 & 0 \end{bmatrix}$ . Compute  $A - B$ .

5. Let 
$$A = \begin{bmatrix} -8 & -10 & 4 \\ 1 & -7 & -9 \\ -3 & 5 & -5 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -8 & 1 & 0 \\ -4 & -6 & 0 \\ 0 & -9 & 7 \end{bmatrix}$ . Compute  $A - B$ .

6. Let  $A = \begin{bmatrix} 6 & 5 & -9 \\ -4 & -10 & 4 \\ 8 & 4 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} 2 & -6 & 3 \\ 0 & -4 & 6 \\ -2 & 4 & -6 \end{bmatrix}$ . Compute  $A - B$ .

6. Let 
$$A = \begin{bmatrix} 6 & 5 & -9 \\ -4 & -10 & 4 \\ 8 & 4 & 5 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 2 & -6 & 3 \\ 0 & -4 & 6 \\ -2 & 4 & -6 \end{bmatrix}$ . Compute  $A - B$ .

7. Let 
$$A = \begin{bmatrix} -3 & -1 & -4 \\ -9 & -2 & 3 \\ 5 & -6 & -3 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 6 & 7 & -1 \\ -9 & -6 & -2 \\ -3 & -6 & -2 \end{bmatrix}$ . Compute  $A - B$ .

8. Let 
$$A = \begin{bmatrix} 8 & 2 & 0 \\ 9 & -4 & -3 \\ 1 & -4 & -8 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 4 & -5 & 7 \\ -9 & 6 & -7 \\ 3 & 6 & 8 \end{bmatrix}$ . Compute  $A - B$ .

9. Let 
$$A = \begin{bmatrix} -6 & -9 & -6 \\ 2 & 3 & -8 \\ -7 & 4 & 9 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -4 & 7 & 1 \\ -6 & -2 & -4 \\ -8 & -10 & -10 \end{bmatrix}$ . Compute  $A - B$ .

10. Let 
$$A = \begin{bmatrix} 4 & 8 & -10 \\ -9 & 6 & -5 \\ 6 & -5 & 5 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 6 & 5 & -6 \\ -6 & 3 & -1 \\ 9 & -9 & -6 \end{bmatrix}$ . Compute  $A - B$ .

#### Multiplication

1. Let 
$$A = \begin{bmatrix} 6 & 4 & -10 \\ 4 & -6 & 4 \\ -10 & 0 & -3 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -9 & -2 & -3 \\ 3 & -3 & -3 \\ -6 & -1 & 6 \end{bmatrix}$ . Compute  $A \cdot B$ .

2. Let 
$$A = \begin{bmatrix} 2 & 5 & -9 \\ -2 & -9 & 7 \\ -1 & 7 & 8 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 2 & -5 & -5 \\ -7 & 6 & 7 \\ 8 & -9 & 3 \end{bmatrix}$ . Compute  $A \cdot B$ .

3. Let 
$$A = \begin{bmatrix} 4 & -3 & -1 \\ 1 & 1 & 6 \\ 6 & -1 & -5 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -6 & 2 & 0 \\ 2 & 0 & 3 \\ 5 & -8 & 3 \end{bmatrix}$ . Compute  $A \cdot B$ .

4. Let 
$$A = \begin{bmatrix} 9 & 1 & 9 \\ 3 & 4 & -10 \\ 0 & -2 & -5 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 5 & -5 & -8 \\ 5 & 2 & -10 \\ -2 & 9 & 3 \end{bmatrix}$ . Compute  $A \cdot B$ .

5. Let 
$$A = \begin{bmatrix} -6 & -5 & -7 \\ -8 & -10 & -10 \\ -10 & -8 & -4 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -7 & 1 & 8 \\ -8 & -6 & 0 \\ -10 & 6 & -4 \end{bmatrix}$ . Compute  $A \cdot B$ .

6. Let 
$$A = \begin{bmatrix} 5 & 6 & -8 \\ 0 & 2 & -2 \\ -2 & 1 & -4 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -2 & -1 & -8 \\ 8 & -5 & 8 \\ 1 & 1 & -8 \end{bmatrix}$ . Compute  $A \cdot B$ .

7. Let 
$$A = \begin{bmatrix} -3 & -10 & -5 \\ -5 & 7 & -3 \\ -3 & -10 & 2 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -1 & -7 & -7 \\ 2 & 5 & -5 \\ 6 & -10 & -10 \end{bmatrix}$ . Compute  $A \cdot B$ .

8. Let  $A = \begin{bmatrix} -1 & -10 & -7 \\ 4 & -10 & -3 \\ -2 & 8 & -3 \end{bmatrix}$  and  $B = \begin{bmatrix} 5 & -6 & -9 \\ 1 & 0 & 2 \\ -2 & -2 & -8 \end{bmatrix}$ . Compute  $A \cdot B$ .

9. Let  $A = \begin{bmatrix} -6 & -7 & 7 \\ -10 & -6 & 3 \\ -6 & 8 & -4 \end{bmatrix}$  and  $B = \begin{bmatrix} 7 & -5 & -3 \\ -5 & -7 & 9 \\ 0 & -5 & -2 \end{bmatrix}$ . Compute  $A \cdot B$ .

8. Let 
$$A = \begin{bmatrix} -1 & -10 & -7 \\ 4 & -10 & -3 \\ -2 & 8 & -3 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 5 & -6 & -9 \\ 1 & 0 & 2 \\ -2 & -2 & -8 \end{bmatrix}$ . Compute  $A \cdot B$ .

9. Let 
$$A = \begin{bmatrix} -6 & -7 & 7 \\ -10 & -6 & 3 \\ -6 & 8 & -4 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 7 & -5 & -3 \\ -5 & -7 & 9 \\ 0 & -5 & -2 \end{bmatrix}$ . Compute  $A \cdot B$ .

10. Let 
$$A = \begin{bmatrix} -6 & 8 & -4 \\ 5 & -3 & -10 \\ -1 & -2 & 2 \\ 1 & -8 & -5 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 0 & -5 & -2 \\ -1 & 0 & 6 \\ -5 & 7 & -8 \\ 1 & -5 & 0 \end{bmatrix}$ . Compute  $A \cdot B$ .

# Answer

## **Vector Arithmetic**

#### Addition

1: 
$$\begin{bmatrix} -8 \\ 15 \\ -3 \end{bmatrix}$$
 2:  $\begin{bmatrix} -1 \\ 14 \\ -3 \end{bmatrix}$  3:  $\begin{bmatrix} 1 \\ -10 \\ -2 \end{bmatrix}$  4:  $\begin{bmatrix} -2 \\ 9 \\ 1 \end{bmatrix}$  5:  $\begin{bmatrix} -8 \\ -3 \\ -7 \end{bmatrix}$  6:  $\begin{bmatrix} 3 \\ -11 \\ 0 \end{bmatrix}$  7:  $\begin{bmatrix} -12 \\ -10 \\ 11 \end{bmatrix}$  8:  $\begin{bmatrix} 10 \\ 0 \\ 11 \end{bmatrix}$  9:  $\begin{bmatrix} -10 \\ -2 \\ -1 \end{bmatrix}$  10:  $\begin{bmatrix} 14 \\ -4 \\ 7 \end{bmatrix}$ 

1: 
$$\begin{bmatrix} -7 \\ 0 \\ 1 \end{bmatrix}$$
 2:  $\begin{bmatrix} 0 \\ 6 \\ -1 \end{bmatrix}$  3:  $\begin{bmatrix} -11 \\ -4 \\ -5 \end{bmatrix}$  4:  $\begin{bmatrix} 14 \\ 1 \\ -8 \end{bmatrix}$  5:  $\begin{bmatrix} -8 \\ -5 \\ -3 \end{bmatrix}$ 
6:  $\begin{bmatrix} -3 \\ 3 \end{bmatrix}$  7:  $\begin{bmatrix} -11 \\ -6 \\ 3 \end{bmatrix}$  8:  $\begin{bmatrix} 6 \\ -17 \\ 9 \end{bmatrix}$  9:  $\begin{bmatrix} 2 \\ -9 \\ 10 \end{bmatrix}$  10:  $\begin{bmatrix} -18 \\ -2 \\ 14 \end{bmatrix}$ 

**Scalar Multiplication** 

1: 
$$\begin{bmatrix} -18 \\ 4 \\ 2 \end{bmatrix}$$
 2:  $\begin{bmatrix} 10 \\ -20 \\ -18 \end{bmatrix}$  3:  $\begin{bmatrix} -21 \\ -9 \\ -15 \end{bmatrix}$  4:  $\begin{bmatrix} 8 \\ -6 \\ -9 \end{bmatrix}$  5:  $\begin{bmatrix} -15 \\ -3 \\ -9 \end{bmatrix}$ 

$$6: \begin{bmatrix} 0 \\ 9 \\ -3 \end{bmatrix} 7: \begin{bmatrix} -50 \\ 30 \\ -20 \end{bmatrix} 8: \begin{bmatrix} -5 \\ 1 \\ 0 \end{bmatrix} 9: \begin{bmatrix} 9 \\ -15 \\ 3 \end{bmatrix} 10: \begin{bmatrix} -100 \\ 90 \\ -30 \end{bmatrix}$$

#### **Matrix Arithmetic**

#### Addition

$$1: \begin{bmatrix} 13 & -12 & -11 \\ -10 & 6 & -14 \\ -1 & 11 & 0 \end{bmatrix} 2: \begin{bmatrix} 10 & 7 & -11 \\ -17 & -15 & -4 \\ -15 & -12 & -13 \end{bmatrix} 3: \begin{bmatrix} 16 & 13 & 3 \\ 5 & 5 & 2 \\ -8 & 7 & -7 \end{bmatrix} 4: \begin{bmatrix} 12 & 6 & -7 \\ 9 & -13 & -7 \\ 3 & -9 & -7 \end{bmatrix} 5: \begin{bmatrix} -14 & -12 & 11 \\ -3 & 15 & -3 \\ -5 & -9 & -12 \end{bmatrix}$$

$$6: \begin{bmatrix} -13 & 3 & -16 \\ -13 & 9 & -7 \\ 3 & -13 & -2 \end{bmatrix} 7: \begin{bmatrix} 12 & 7 & 8 \\ 10 & -1 & -7 \\ 3 & -3 & -1 \end{bmatrix} 8: \begin{bmatrix} 17 & -2 & 1 \\ 7 & 9 & 10 \\ 1 & 11 & -3 \end{bmatrix} 9: \begin{bmatrix} 9 & -12 & -12 \\ -15 & 8 & 2 \\ -4 & 14 & -15 \end{bmatrix} 10: \begin{bmatrix} 8 & 4 & -1 \\ -6 & -9 & 9 \\ 5 & 8 & -2 \end{bmatrix}$$

#### **Subtraction**

$$1: \begin{bmatrix} 9 & 2 & -15 \\ -5 & 3 & 15 \\ -10 & 4 & -17 \end{bmatrix} 2: \begin{bmatrix} -3 & -8 & 5 \\ 8 & -6 & 5 \\ 0 & 7 & 6 \end{bmatrix} 3: \begin{bmatrix} 1 & -2 & 12 \\ -6 & -7 & -5 \\ 1 & -10 & 4 \end{bmatrix} 4: \begin{bmatrix} 1 & -3 & -2 \\ -10 & 0 & -9 \\ 0 & 4 & 2 \end{bmatrix} 5: \begin{bmatrix} 0 & -11 & 4 \\ 5 & -1 & -9 \\ -3 & 14 & -12 \end{bmatrix}$$

$$6: \begin{bmatrix} 4 & 11 & -12 \\ -4 & -6 & -2 \\ 10 & 0 & 11 \end{bmatrix} 7: \begin{bmatrix} -9 & -8 & -3 \\ 0 & 4 & 5 \\ 8 & 0 & -1 \end{bmatrix} 8: \begin{bmatrix} 4 & 7 & -7 \\ 18 & -10 & 4 \\ -2 & -10 & -16 \end{bmatrix} 9: \begin{bmatrix} -2 & -16 & -7 \\ 8 & 5 & -4 \\ 1 & 14 & 19 \end{bmatrix} 10: \begin{bmatrix} -2 & 3 & -4 \\ -3 & 3 & -4 \\ -3 & 4 & 11 \end{bmatrix}$$

Multiplication

$$1: \begin{bmatrix} 18 & -14 & -90 \\ -78 & 6 & 30 \\ 108 & 23 & 12 \end{bmatrix} 2: \begin{bmatrix} -103 & 101 & -2 \\ 115 & -107 & -32 \\ 13 & -25 & 78 \end{bmatrix} 3: \begin{bmatrix} -35 & 16 & -12 \\ 26 & -46 & 21 \\ -63 & 52 & -18 \end{bmatrix} 4: \begin{bmatrix} 32 & 38 & -55 \\ 55 & -97 & -94 \\ 0 & -49 & 5 \end{bmatrix} 5: \begin{bmatrix} 152 & -18 & -20 \\ 236 & -8 & -24 \\ 174 & 14 & -64 \end{bmatrix}$$

$$6: \begin{bmatrix} 30 & -43 & 72 \\ 14 & -12 & 32 \\ 8 & -7 & 56 \end{bmatrix} 7: \begin{bmatrix} -47 & 21 & 121 \\ 1 & 100 & 30 \\ -5 & -49 & 51 \end{bmatrix} 8: \begin{bmatrix} -1 & 20 & 45 \\ 16 & -18 & -32 \\ 4 & 18 & 58 \end{bmatrix} 9: \begin{bmatrix} -7 & 44 & -59 \\ -40 & 77 & -30 \\ -82 & -6 & 98 \end{bmatrix} 10: \begin{bmatrix} 0 & 29 & 54 \\ 13 & -24 & 10 \\ 34 & -31 & 70 \end{bmatrix}$$

# **Bibliography**