1 Human (PO)MDP

This is a MDP that the human runs in their mind. It can be formalized as a POMDP, but right now we have a weak POMDP with a a belief distribution over the robot's distribution of objects.

- 1. $S = \langle \iota, \mathcal{I}, d, H \rangle$
 - (a) Here \mathcal{I} is the set of items the robot can pass.
 - (b) Item ι is the object the human wants, and this is hidden information for the robot.
 - (c) d is the dialogue state what question was asked previously by the robot.
 - (d) Here $B(i \in \mathcal{I} == \iota)$ is the belief distribution of the robot over the items in \mathcal{I} . In the POMDP formulation B would be part of the state that is hidden from the human. Instead we model a distribution that tracks B allowing the human to solve an MDP instead of nested POMDPs. We will go back to the nested POMDP model repeatedly to make sure our MDP model is equivalent.
 - (e) Human's hunch of the robot's belief $H = P(\widehat{B}|\eta)$, where \widehat{B} is an estimate of the distribution of B, it is over the set of items \mathcal{I} . η is a set of priors that defines the distribution \widehat{B} , hence H is over the space of all possible priors values. We propose to use the Dirichlet distribution to model H.
- 2. $A_h = \langle l, g \rangle$, where A_h is the human action set and l and g are language and gesture actions respectively.
- 3. If this were a POMDP we would need observation functions and a observation set.
 - (a) $\Omega_h = \langle A_r \rangle$, where A_r is the set of robot actions and Ω_h is the set of human observations.
 - (b) $O = P(A_r|\iota, \mathcal{I}, d, H, B)$ is the observation function and it is hand coded by us so we know it, since we know the robots response to all the belief states.
 - (c) $T = P(\iota', \mathcal{I}', d', H', B' | \iota, \mathcal{I}, d, H, B, a_h, a_r) = P(\iota', \mathcal{I}', d' | \iota, \mathcal{I}, d, H, B, a_h, a_r) \times P(H' | \iota, \mathcal{I}, d, H, B, a_h, a_r) \times P(B' | \iota, \mathcal{I}, d, H, B, a_h, a_r)$
- 4. MDP formulation of this problem would not need the observation set or the observation functions, instead H would get updated based on A_r and A_h . This just has a transition function now defined as $T = P(\iota', \mathcal{I}', d', H'|\iota, \mathcal{I}, d, H, a_h, a_r) = P(\iota', \mathcal{I}', d'|\iota, \mathcal{I}, d, H, a_h, a_r) \times P(H'|\iota, \mathcal{I}, d, H, B, a_h, a_r)$ The conditional independence of the human's hunch H from the distribution over the required item, or set of items left over or the last question asked comes from visible robot actions. $P(H'|\iota, \mathcal{I}, d, H, B, a_h, a_r)$ is being

designed by us as an approximation and we need to think of data intensive methods of measuring this transition. $P(\iota', \mathcal{I}', d'|\iota, \mathcal{I}, d, H, a_h, a_r) =$

{ wait, pick(object), ask(property) }

5. $T = p(\omega', \mathcal{O}', ds' | \omega, \mathcal{O}, ds, a)$

If a is a pick action and $a.object == \omega$:

$$p(\omega', \mathcal{O}', ds' | \omega, \mathcal{O}, ds, a) = \begin{cases} 1/|\mathcal{O} \setminus \omega| & \text{if } \omega'! = \omega, ds = None, \mathcal{O}' = \mathcal{O} \setminus \omega \\ 0 & \text{otherwise} \end{cases}$$

If a is a pick action and a.object! = ω , we transition to the state where $s' = \langle \omega', \mathcal{O}', ds' \rangle = \langle \omega, \mathcal{O} \setminus a.object, ds \rangle$.

6.

$$R(\omega,\mathcal{O},ds,a) = \begin{cases} 10 & \text{if a == pick and a.object == } \omega \\ -80 & \text{if a == pick and a.object != } \omega \\ -1 & \text{if a == wait} \\ -3 & \text{if a == ask} \end{cases}$$

7.
$$\Omega = \langle l, g \rangle$$

8.
$$O = p(l, g|\omega, \mathcal{O}, ds, a) = p(l|\omega, \mathcal{O}, ds, a)p(g|\omega, \mathcal{O}, ds, a)$$

$$p(l|\mathcal{O}, \omega, a) = p(c|\omega^{t+1}, a^t) \prod_{w \in l} p(w|\omega, a)$$
 (1)

$$p(c|a^t) = \begin{cases} 0.8 & \text{if } a^t \text{ is a question} \\ 0.2 & \text{otherwise} \end{cases}$$
 (2)

 $p(w|\omega,a) = \frac{\text{Number of times } w \text{ is used to describe } \omega}{\text{Total counts for words describing } \omega}$