

Práctica 7
26-09-25

Ecuaciones Principales

$$v_e(t) = R i_1(t) + L \frac{d[i_1(t) - i_2(t)]}{dt} + R[i_1(t) - i_2(t)]$$

$$\frac{d[i_1(t) - i_2(t)]}{dt} + R[i_1(t) - i_2(t)] = R i_2(t) + R i_2(t) + \frac{1}{C} \int i_2(t) dt$$

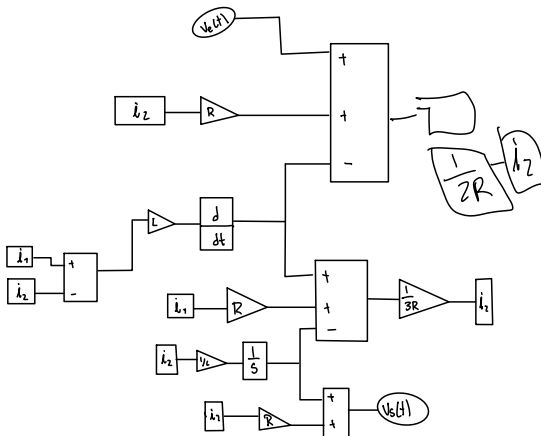
$$v_s(t) = R i_2(t) + \frac{1}{C} \int i_2(t) dt$$

Modelo de ecuaciones Integro-diferenciales

$$i_1(t) = \left[\frac{v_e(t) - L \frac{d[i_1(t) - i_2(t)]}{dt}}{2R} + R i_2(t) \right] \frac{1}{2R}$$

$$i_2(t) = \left[\frac{L \frac{d[i_2(t) - i_1(t)]}{dt} + R i_1(t) - \frac{1}{C} \int i_2(t) dt}{2R} \right] \frac{1}{2R}$$

$$v_s(t) = R i_2(t) + \frac{1}{C} \int i_2(t) dt$$



Transformada de Laplace

Práctica 7

$$\frac{V_s(s)}{V_c(s)} = \frac{?}{?}$$

Nota: No debe de haber términos negativos

$$V_c(s) = RI_1(s) + LS[I_1(s) - I_2(s)] + R[I_1(s) - I_2(s)]$$

$$LS[I_1(s) - I_2(s)] + R[I_1(s) - I_2(s)] = RI_2(s) + RI_2(s) + \frac{I_2(s)}{Cs}$$

$$V_c(s) = RI_2(s) + \frac{I_2(s)}{Cs}$$

Procedimiento algebraico

$$V_c(s) = (R + LS + R)I_1(s) - (LS + R)I_2(s)$$

$$= (LS + 2R)I_1(s) - (LS + R)I_2(s)$$

$$LSI_1(s) - LS I_2(s) + RI_1(s) + RI_2(s) = 2RI_2(s) + \frac{I_2(s)}{Cs}$$

$$LSI_1(s) + RI_1(s) = 3RI_2(s) + LS I_2(s) + \frac{I_2(s)}{Cs}$$

$$(LS + R)I_1(s) = (3R + LS + \frac{1}{Cs})I_2(s)$$

$$I_1(s) = \frac{3(CRs + Cs^2 + 1)}{Cs(Ls + R)} I_2(s) = \frac{Cs^2 + 3CRs + 1}{Cs(Ls + R)} I_2(s)$$

$$V_c(s) = \frac{(LS + 2R)(Cs^2 + 3CRs + 1)}{Cs(Ls + R)} I_2(s) - (LS + R)I_2(s)$$

$$= \left[\frac{(LS + 2R)(Cs^2 + 3CRs + 1) - Cs(Ls + R)(Cs + R)}{Cs(Ls + R)} \right] I_2(s)$$

$$CL^2s^3 + 3CLR s^2 + LS + 2CR s^2 + 6CR^2s + 2R$$

$$CL^2s^3 + 2CLR s^2 - CR^2s \quad 5CR^2s$$

— 0 — 0 — 0 — 0 — 0 — 0 — 0 — 0

$$V_c(s) = \frac{3CLR s^2 + (5CR^2 + L)s + 2R}{Cs(Ls + R)}$$

$$V_c(s) = \frac{CRs + 1}{Cs} I_2(s)$$

$$\frac{3CLR s^2 + (5CR^2 + L)s + 2R}{Cs(Ls + R)} I_2(s)$$

$$(CRS + 1)(LS + R)$$

$$\frac{V_s(s)}{V_e(s)} = \frac{CLRS^2 + (CR^2 + L)s + R}{3CLRS^2 + (SCR^2 + L)s + 2R}$$

$$R = 3.3 \text{ K}\Omega = 9 \text{ K}\Omega$$

$$C = 4.7 \text{ nF} \quad L = 3.3 \text{ mH}$$

$$22 \text{ nF}$$

$$33 \text{ mH}$$

$$\text{num} = [4.7 \cdot 10^{-6}] * [3.3 \cdot 10^{-3}] * [3.3 \cdot 10^{-3}], [4.7 \cdot 10^{-6}] * [3.3 \cdot 10^{-3}] * 22 + 3.3 \cdot 10^{-3} * 3.3 \cdot 10^{-3}$$

Estabilidad en lazo abierto

2-OCT-2025

calcular los polos de la función de transferencia

$$\frac{V_s(s)}{V_e(s)} = \frac{CLRS^2 + (CR^2 + L)s + R}{3CLRS^2 + (SCR^2 + L)s + 2R}$$

$$\text{den} = [3 * C * L * R, 5 * (R^2 * L + 2 * R)]$$

$$L = \text{np.roots}(\text{den})$$

→ F.print

$$\lambda_1 = -454545.117$$

$$\lambda_2 = -2.020$$

El sistema presenta una respuesta estable y sobreamortiguada

Error en el estado estacionario

$$e(s) = \lim_{s \rightarrow 0} s V_e(s) \left[1 - \frac{V_s(s)}{V_e(s)} \right]$$

$$= \lim_{s \rightarrow 0} s \cdot \frac{1}{s} \left[1 - \frac{CLRS^2 + (CR^2 + L)s + R}{3CLRS^2 + (SCR^2 + L)s + 2R} \right]$$

$$= \frac{R}{2R}$$

$$e(\infty) = \frac{1}{2} V$$

$$V_e(t) = 1V$$

$$V_e(s) = \frac{1}{s}$$

