



## Predictive Models and Decision Trees

# Lecture plan

- Predictive models
- Features and targets
- Supervised Segmentation
- Decision Trees
- ID3 algorithm

# Predictive Models

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- ***Predictive*** models apply statistics to predict outcomes
- The key criteria of evaluating a predictive model is its ability to ***forecast***, typically events in the future

# Data available on each loan application

- We think of these fields of information as attributes or property of the object of interest

## Debt consolidation for 149022957

[Sell Notes](#) [Glossary](#)

Loan ID: 137041539 (Joint Application<sup>1</sup>) | Lending Club Prospectus

« Previous | Next »

Add to Order

Amount Requested **\$20,000**  
Loan Purpose **Debt consolidation**  
Loan Grade **A2**  
Interest Rate **6.67%**  
Loan Length **5 years (60 payments)**  
Monthly Payment **\$392.92 / month**

Review Status **Approved** ✓  
Funding Received **\$9,625 (48.12% funded)**  
Investors **304 people funded this loan**  
Listing Expires in **29d 6h (8/27/18 2:00 PM)**

Note Status **In Funding**  
Loan Submitted on **7/18/18 8:06 AM**

### ■ Member\_156063942's Profile (all information not verified unless noted with an "\*\*\*\*")

Home Ownership **MORTGAGE**  
Job Title **Foreman**  
Length of Employment **10+ years**  
Location **898xx**

Gross Income **\$3,583 / month \***  
Debt-to-Income (DTI) **37.06%\*\***  
Joint Gross Income **\$7,333 / month**  
Joint Debt-to-Income (DTI) **21.29%**

### ■ Member\_156063942's Credit History (as reported by credit bureau on 7/18/18)

Credit Score Range: **735-739**  
Earliest Credit Line **03/1999**  
Open Credit Lines **6**  
Total Credit Lines **15**  
Revolving Credit Balance **\$16,727.00**  
Revolving Line Utilization **69.40%**  
Inquiries in the Last 6 Months **0**  
Accounts Now Delinquent **0**

Delinquent Amount **\$0.00**  
Delinquencies (Last 2 yrs) **0**  
Months Since Last Delinquency **n/a**  
Public Records On File **0**  
Months Since Last Record **n/a**  
Months Since Last Major Derogatory **n/a**  
Collections Excluding Medical **0**

# Attributes / Features of a model

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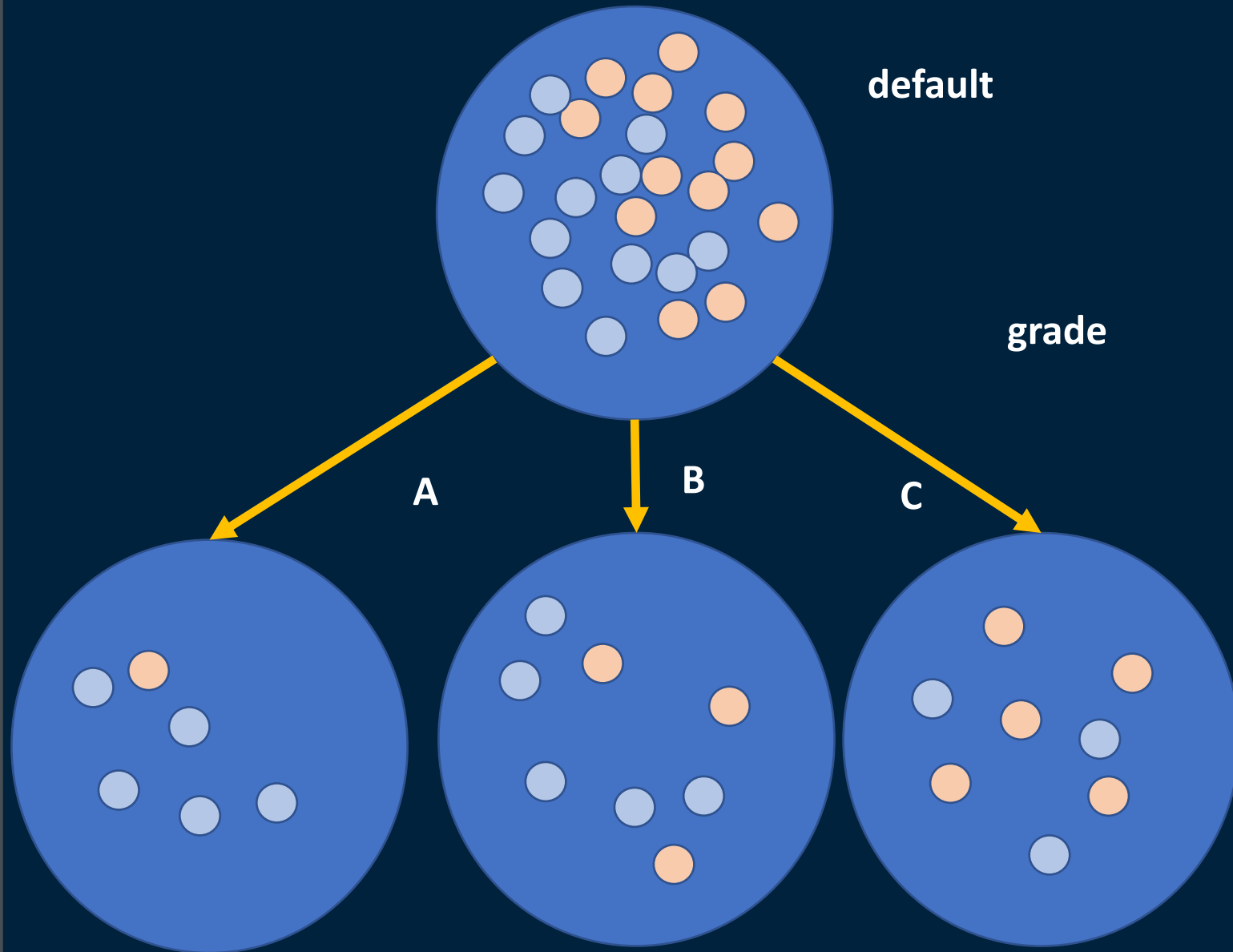
Attribute /  
independent variables

target attribute /  
dependent variables

	id	loan_amnt	funded_amnt	grade	fico_range_high	fico_range_low	default
0	84044117	35000.0	35000.0	E	694.0	690.0	False
1	84393373	5000.0	5000.0	C	674.0	670.0	False
3	83645580	16000.0	16000.0	C	714.0	710.0	True
4	83983220	20000.0	20000.0	D	674.0	670.0	False
6	83904318	8000.0	8000.0	C	684.0	680.0	False
7	83902702	10000.0	10000.0	B	684.0	680.0	False
10	84040775	4500.0	4500.0	B	664.0	660.0	False
11	84101628	1500.0	1500.0	D	714.0	710.0	False
12	83598178	20000.0	20000.0	A	709.0	705.0	False
13	84333354	9000.0	9000.0	C	669.0	665.0	True

# Informative Attributes

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# Informative Attributes

## Grade

grade	#defaults	default likelihood
A	3041.0	8.47%
B	12448.0	17.97%
C	19888.0	27.98%
D	13154.0	37.89%
E	7479.0	46.04%
F	3450.0	54.43%
G	1061.0	58.91%

# Informative Attributes

Fico

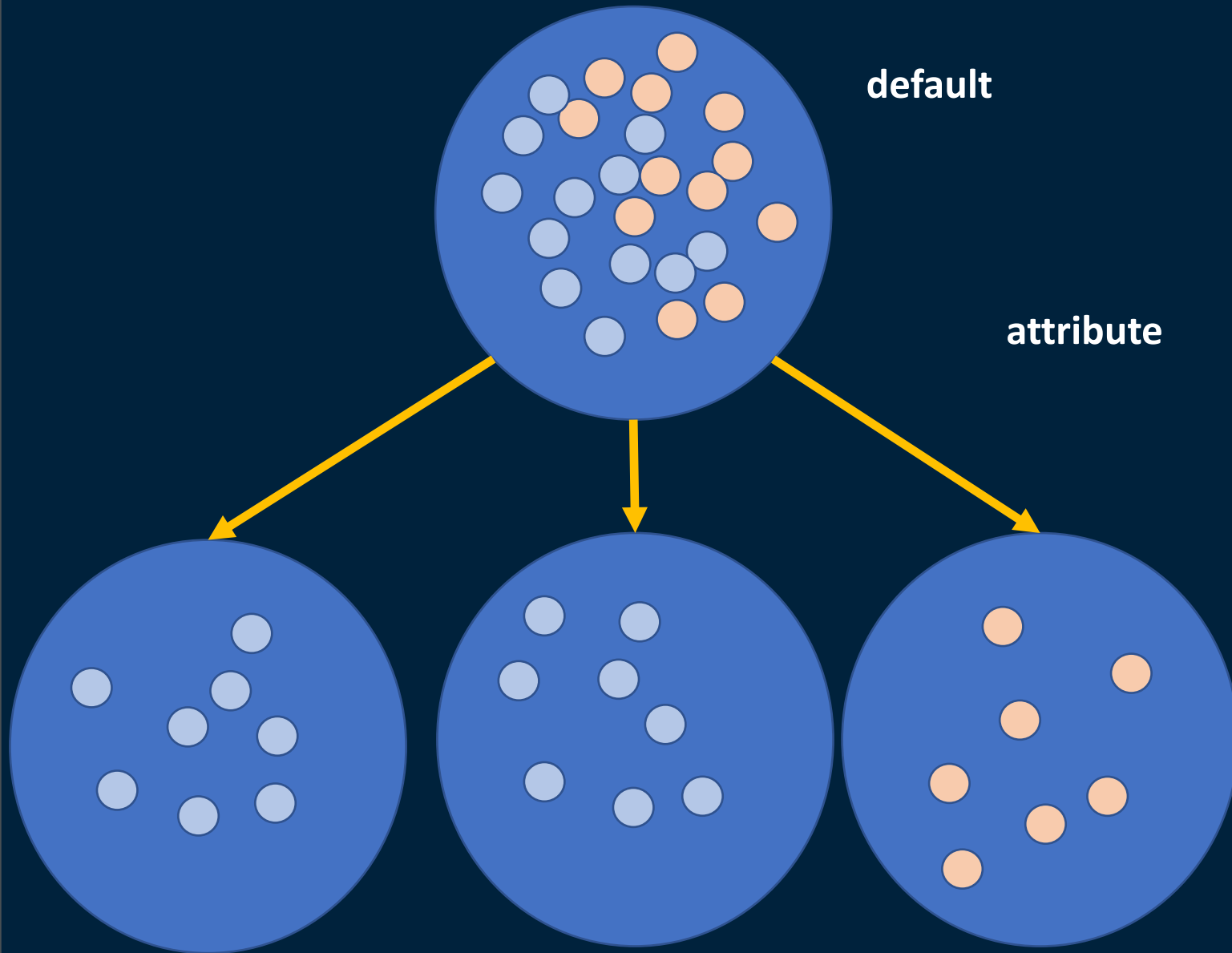
Fico	#defaults	default likelihood
<700	47401.0	29.76
700< <800	12978.0	17.55
>800	142.0	6.66



## Best case scenario

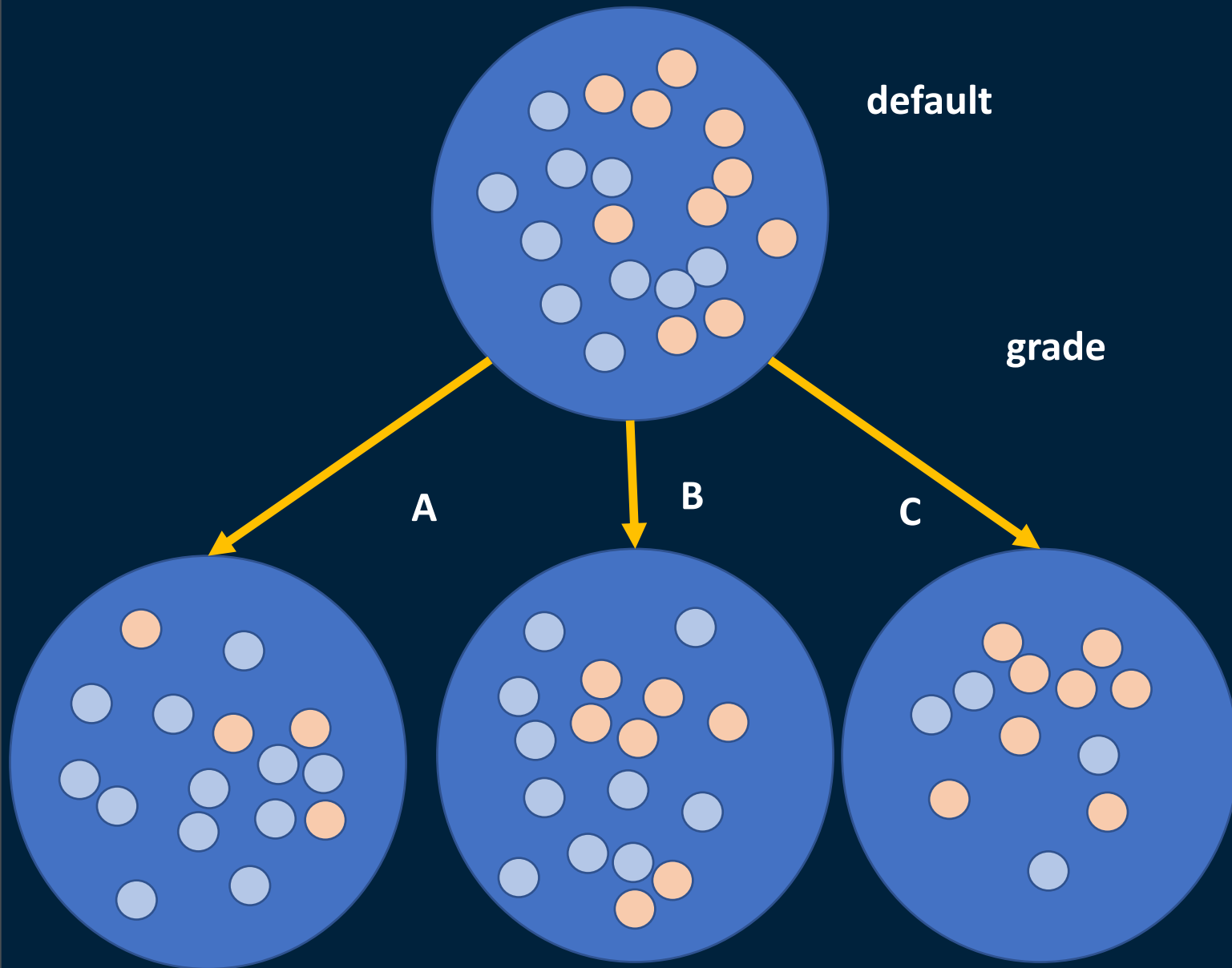
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- The attributes separate perfectly loans that will default and those that won't
- In other words attributes will separate instances into "pure" sets



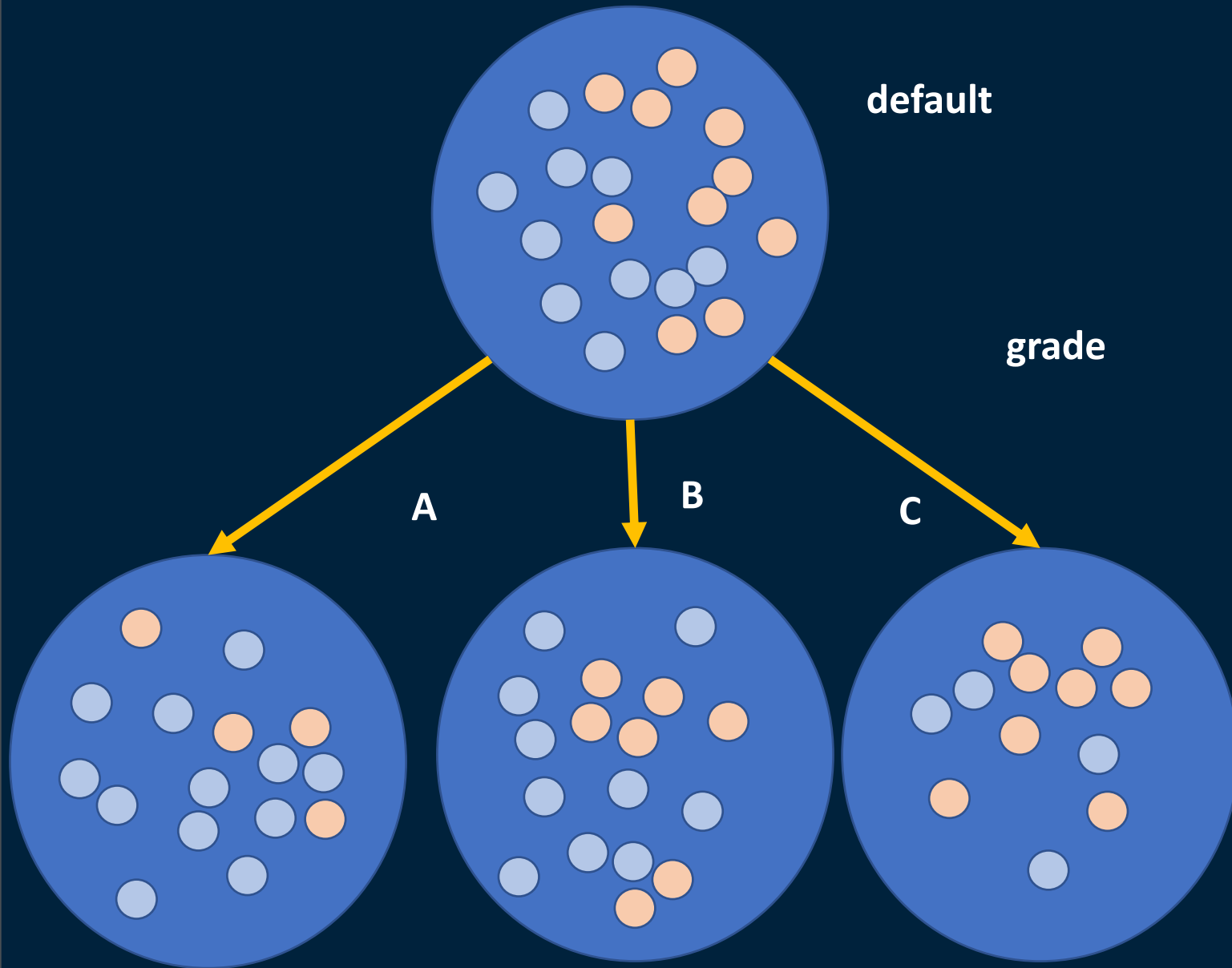
## Common case

- The attributes separate imperfectly loans that will default and those that won't
- In other words attributes will separate instances into "impure" sets
- There are many ways to separate into impure sets, how would we choose which one is best?



# Entropy

- Measures of impurity
- The notion of impurity is closely related to the notion of information

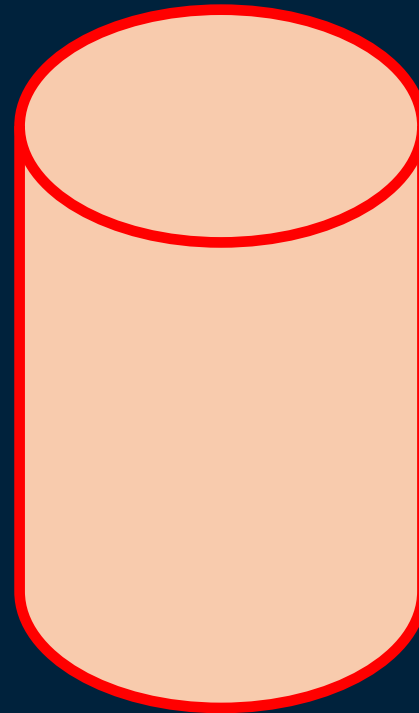


## Entropy and Information

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What is information?

By definition, information is *knowledge* about things, which may or may not be conceived by an observer

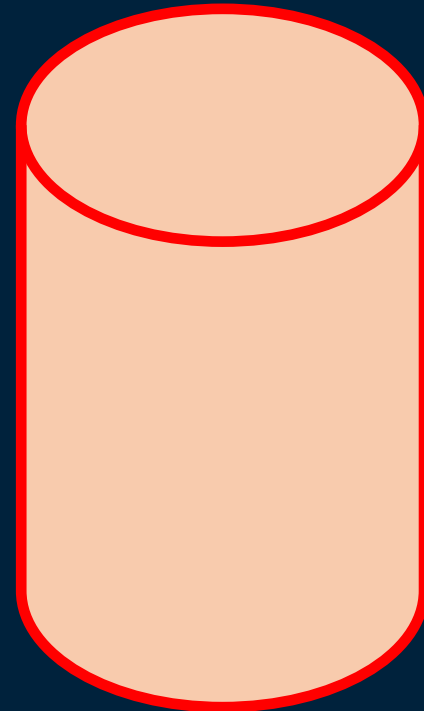


## Entropy and Information

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What is information?

- How much information do we gain from learning the type of the ball drawn from the urn below?
- What did we learn that we didn't know before?

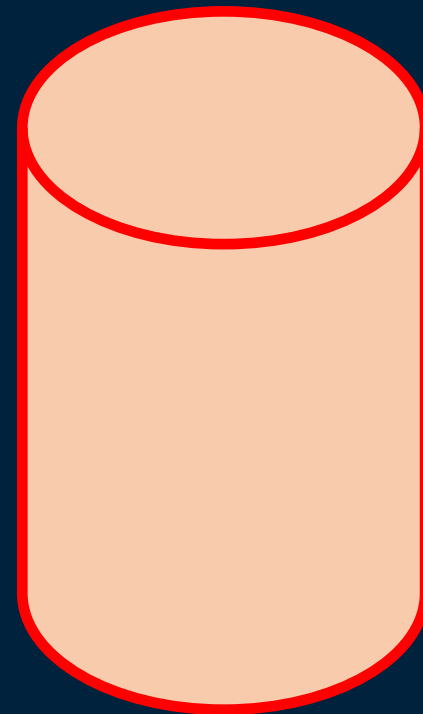


## Entropy and Information

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What is information?

Information is the *uncertainty* of the outcome

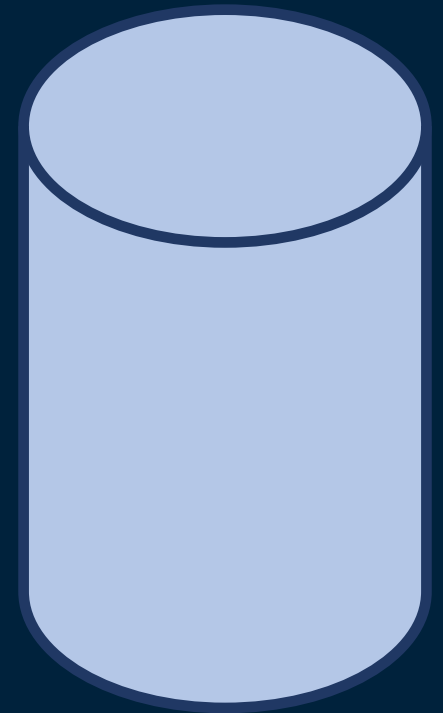
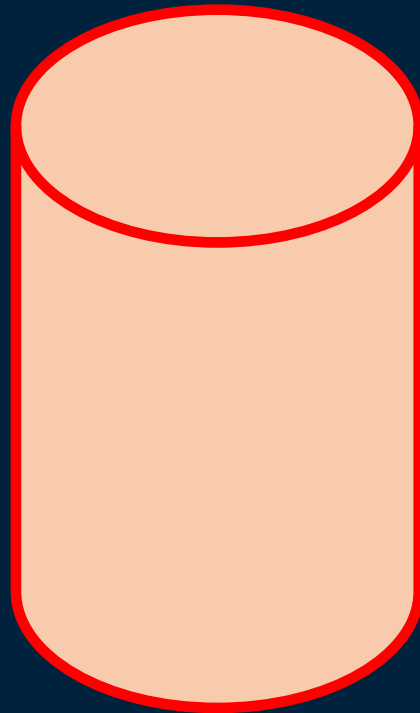


## Entropy and Information

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What is information?

There is greater uncertainty on the type of the ball drawn from the red urn vs the blue urn, therefore we would say that a draw from the red urn has ***greater information content***



# Information Measurement

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Let  $H$  be a measure of information

- $H$  should be **maximized** when the object is most unknown.
- **$H(X)=0$**  if  $X$  is determined/certain
- The information measure  $H$  should be **additive for independent objects**; i.e., with 2 information sources which has no relations with each other,  $H=H_1+H_2$ .

Entropy

- Entropy  $H(X)$  of a random variable  $X$  is defined by
$$H(X) = -\sum p(x) \log p(x)$$
- We can verify that the measure  $H(X)$  satisfies the three criterion stated.
- If we choose the logarithm in base 2, then the entropy may be claimed to be in the unit of **bits**; the use of the unit will be clarified later.

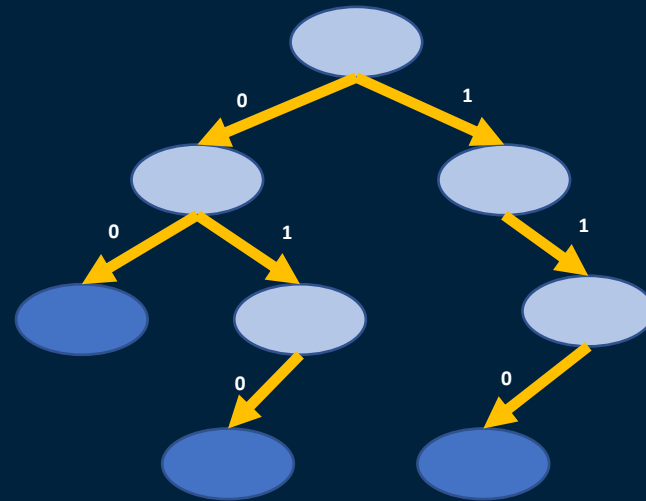


# Information Measurement

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## Shannon Entropy

- How many bits on average would required to describe a path from the root to a leaf?



## Entropy in thermodynamics or statistical mechanics

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- Entropy is the measure of disorder of a thermodynamic system
- The definition is identical with the information entropy, but the summation now runs on all possible physical states
- Actually, entropy is first introduced in thermodynamics and Shannon found out his measure is just entropy in physics

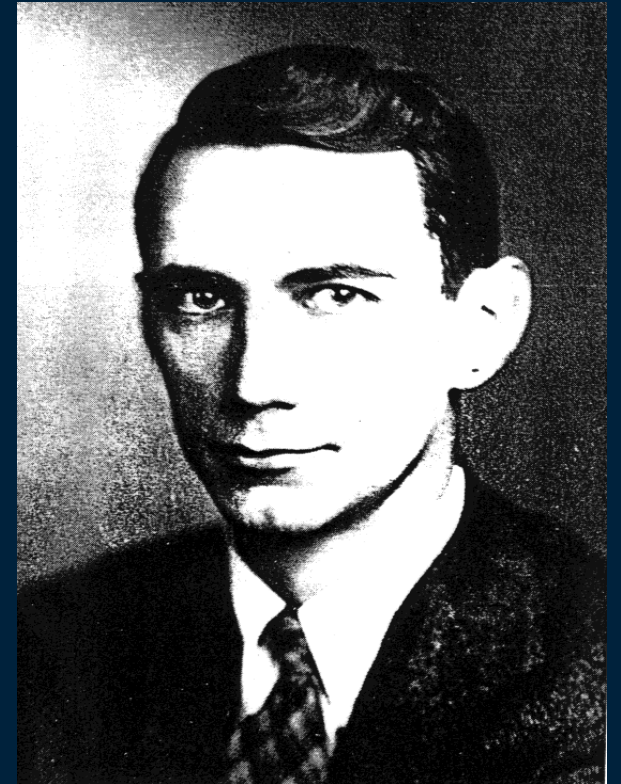
## Historical Notes

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Claude E. Shannon (1916-2001) himself in 1948, has established almost everything we will talk about today.

He was dealing with communication aspects.

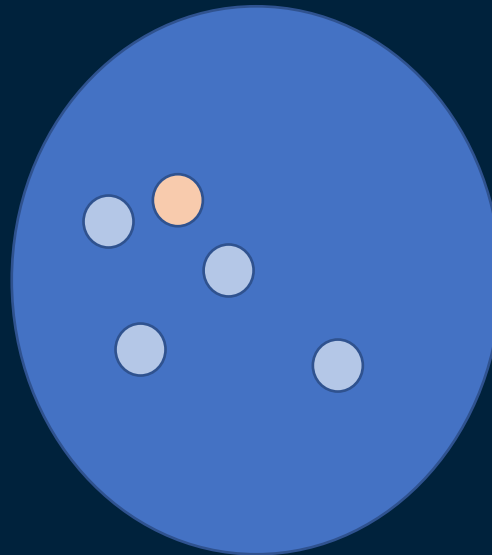
He first used the term “bit.”



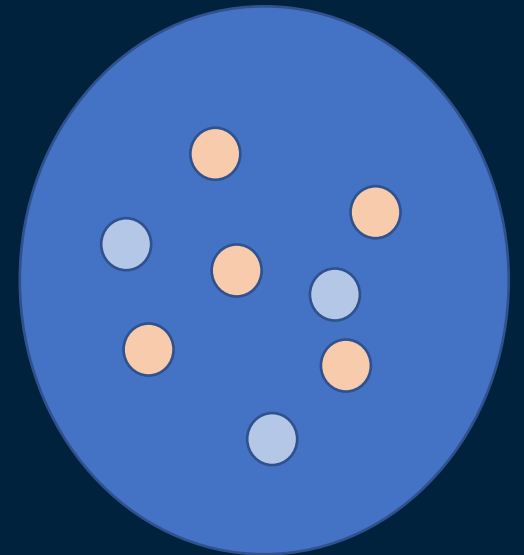
# Entropy

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$$entropy = \sum_i p_i \cdot \log p_i$$



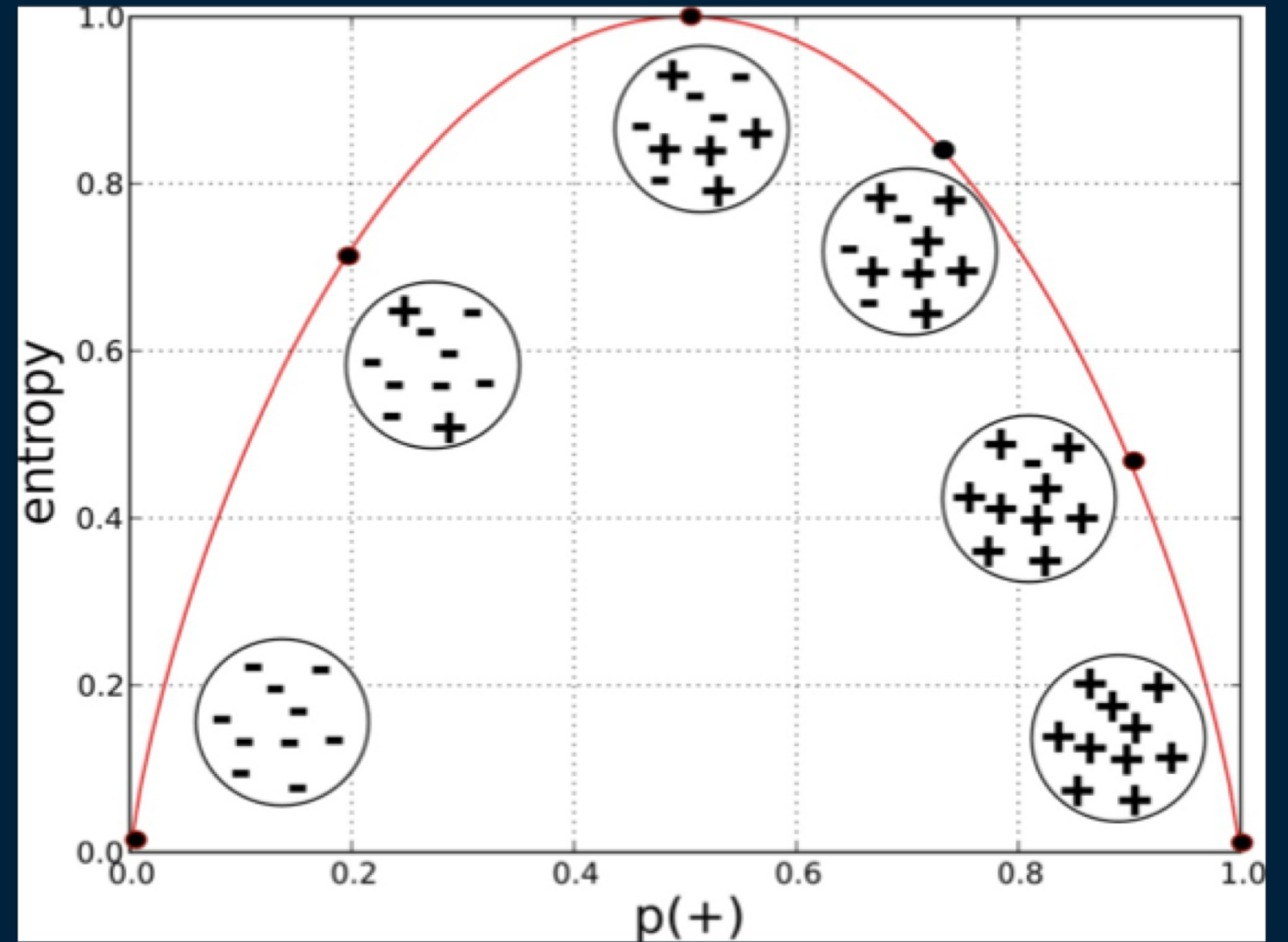
$$H = 0.8 \cdot \log 0.8 + 0.2 \cdot \log 0.2 = \mathbf{0.7219}$$



$$H = 0.625 \cdot \log 0.625 + 0.375 \cdot \log 0.375 = \mathbf{0.9544}$$

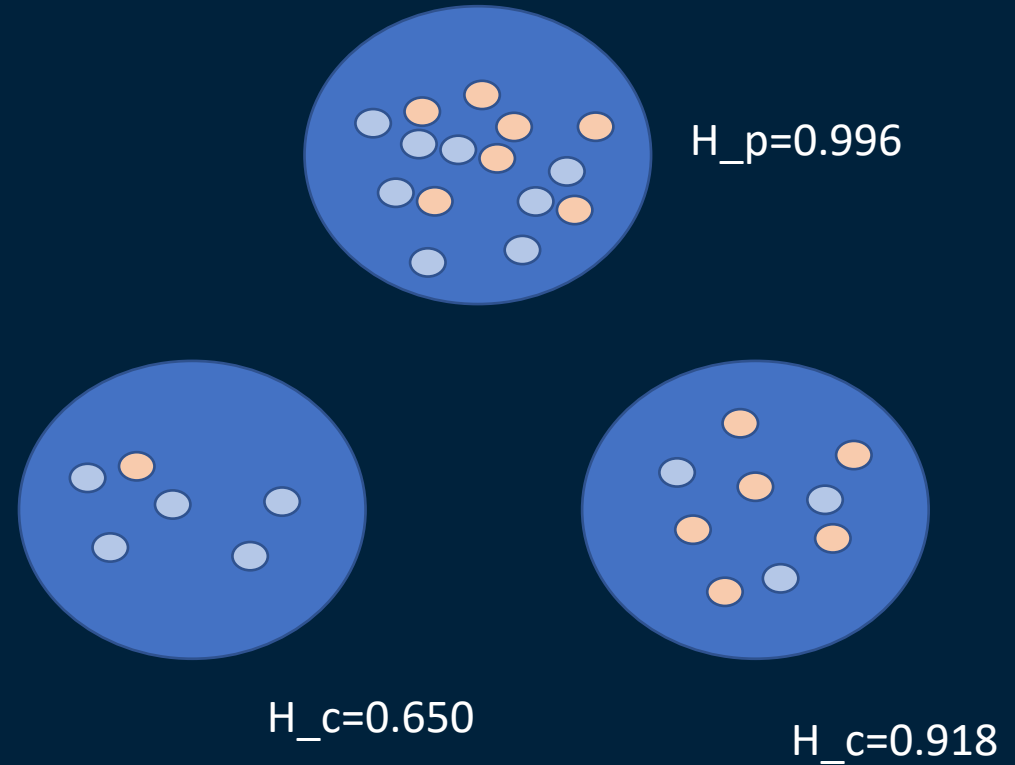
# Entropy

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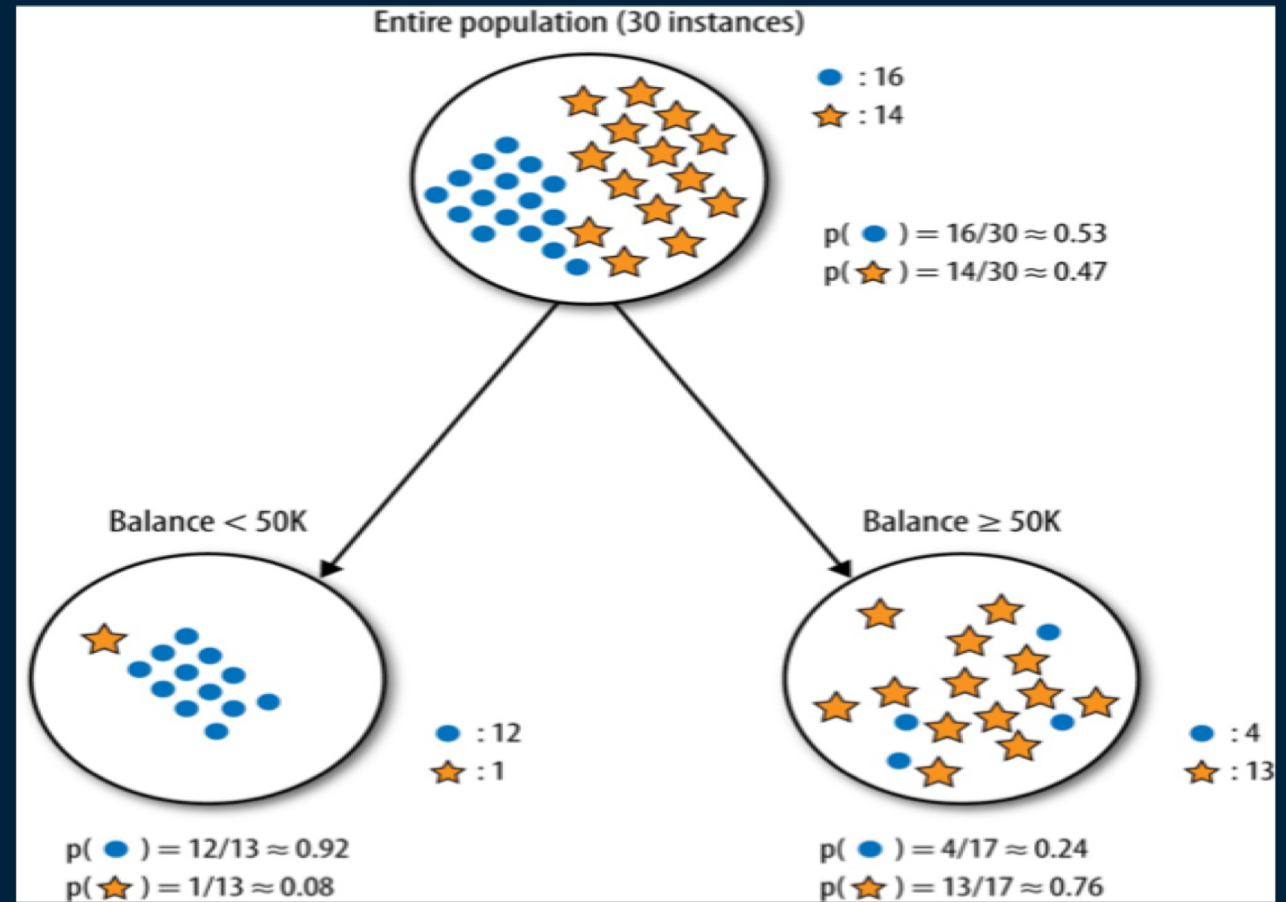
# Information Gain

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$$Ig = \sum p_{c_i} \cdot H_{c_1} - H_p = 0.1852$$

# Information Gain



$$\text{entropy}(\text{parent}) \approx 0.99$$

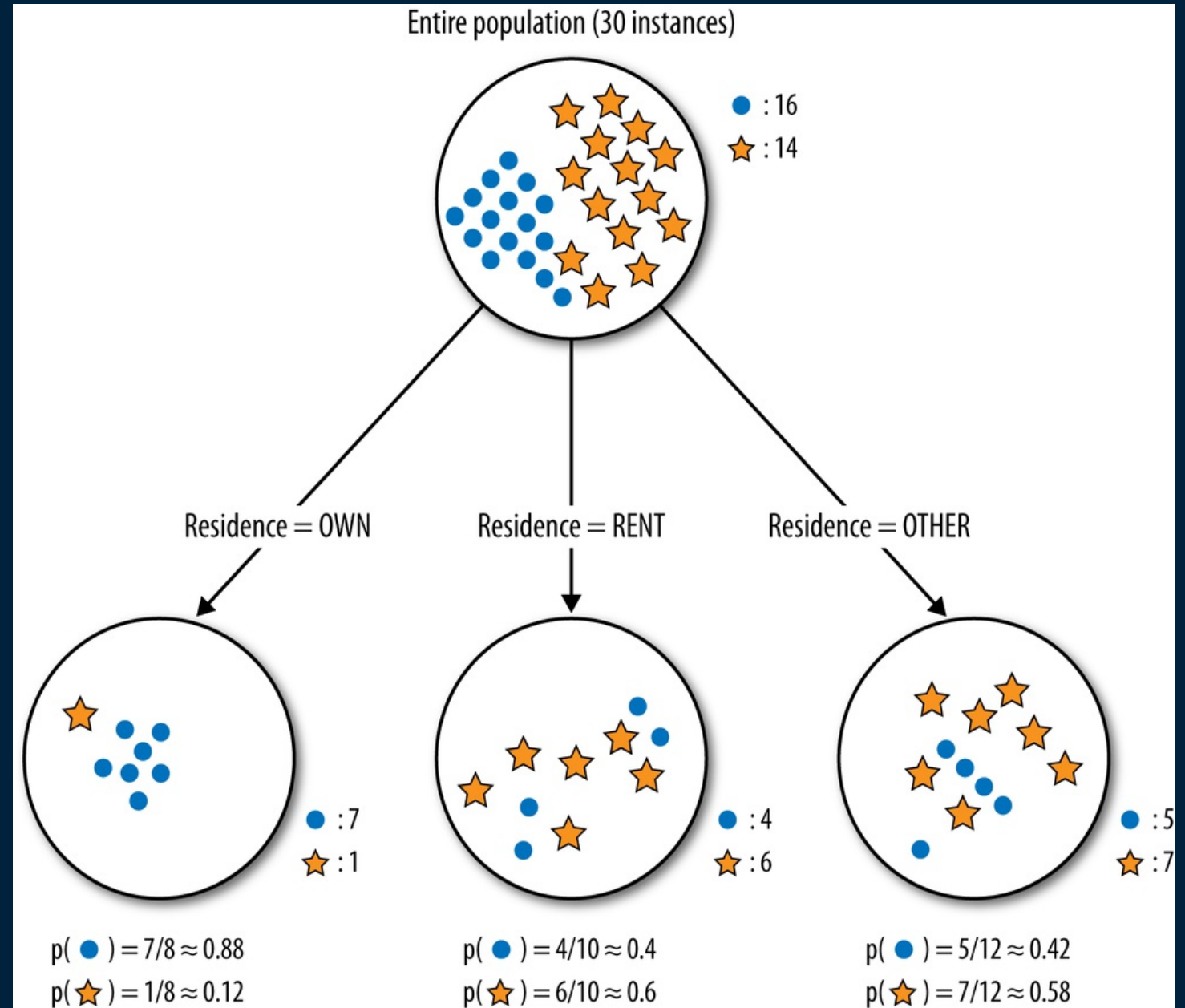
$$\text{entropy}(\text{Residence}=\text{OWN}) \approx 0.54$$

$$\text{entropy}(\text{Residence}=\text{RENT}) \approx 0.97$$

$$\text{entropy}(\text{Residence}=\text{OTHER}) \approx 0.98$$

$$IG \approx 0.13$$

# Information Gain

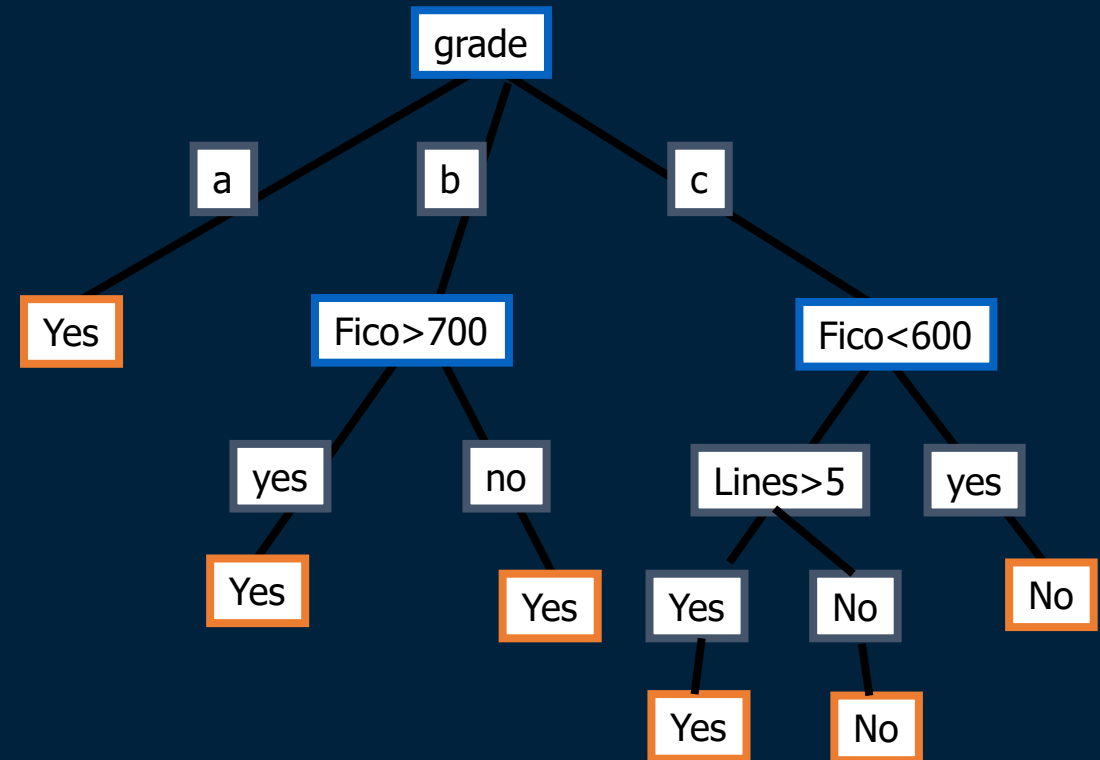




# ID3 algorithm

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ID3 algorithm: Repeatedly find the split maximizing the information gain on the residual set



## ID3 algorithm

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- The decision tree represents the classification of the table
- It can classify all the objects in the table
- Each internal node represents a test on some property
- Each possible value of that property corresponds to a branch of the tree
- An individual of unknown type may be classified by traversing this tree

## ID3 algorithm

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- In classifying any given instance, the tree does not use all the properties in the table
- Decision tree for credit risk assessment
  - If a person has a good credit history and low debit, we ignore her collateral income and classify her as low risk
  - In spite of omitting certain tests, the tree classifies all examples in the table

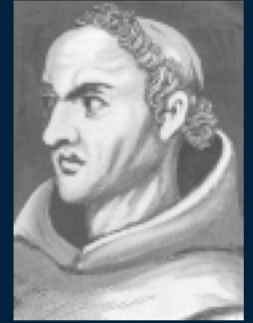
## ID3 algorithm

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- ID3 algorithm assumes that a good decision tree is the simplest decision tree
- Heuristic:
  - Preferring simplicity and avoiding unnecessary assumptions
  - Known as Occam's Razor

# Occam Razor

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- Occam Razor was first articulated by the medieval logician William of Occam in 1324
  - born in the village of Ockham in Surrey (England) about 1285, believed that he died in a convent in Munich in 1349, a victim of the Black Death
  - It is vain do with more what can be done with less..
- We should always accept the simplest answer that correctly fits our data
- The smallest decision tree that correctly classifies all given examples