

## Homework #6

### FORMAT of the file to be submitted:

1. All the m-files should be named as pr1.m, pr2.m and so.
2. The results (figure, table, or individual result such as  $x = 2.653$ , ..., and any comment) should be placed in a WORD file named as yourlastname\_HW\_04.doc
3. All the m-files should be inserted at the end of the WORD file using COURIER 9 font.
4. The WORD file and all the m-files should ZIPPED together, and the file should be named as yourlastname\_HW\_06.zip or (yourlastname\_HW\_06.rar).
5. Place the file to the following folder:  
F:\COURSES\UGRADS\MECH\MECH307\HOMEWORK\...

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<b>Problem 1</b>	O.D.E.:	$\frac{dy}{dt} = 5 - 0.4t - te^{-0.10t}$
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	I.C.:	$y(0) = 10$
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- Plot  $y$  versus  $t$  until  $y$  becomes negative.
- $y_{\max} = \underline{\hspace{2cm}}$  m at  $t = \underline{\hspace{2cm}}$  s.
- $y = 0$  at  $t = \underline{\hspace{2cm}}$  s.

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<b>Problem 2</b>	O.D.E.:	$\frac{dy}{dt} = 5 - ct - te^{-0.10t}$
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	I.C.:	$y(0) = 10$
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- Plot  $y_{\max}$  versus  $c$ , which is a parameter in  $0.4 \leq c \leq 5$ .
- $y_{\max} = 15$  m when  $c = \underline{\hspace{2cm}}$  (with a +/- 0.1 error in it).

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### Problem 3

A mass-spring-damper system satisfies the following ODE and initial conditions:

O.D.E.:	$m \frac{d^2x}{dt^2} + c \frac{dx}{dt} + kx = 0$
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I.C.:	$x(0) = 0.5$ and $dx/dt(0) = 0$
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The parameters of the problem are given below:

$$\begin{aligned} m &= 10 \text{ kg,} \\ c &= 5 \text{ kg.s,} \\ k &= 40 \text{ N/m.} \end{aligned}$$

Calculate and plot the displacement of the mass,  $x(t)$  in  $0 \leq t \leq 20$ .  
Use a time step of 0.001 s.

Find the first four peaks of the vibration:

$$x_{\text{peak},1} = \underline{\quad 0.5 \quad} \text{ m} \quad \text{at } t = \underline{\quad 0.00 \quad} \text{ s.}$$

$$x_{\text{peak},2} = \underline{\hspace{2cm}} \text{ m} \quad \text{at } t = \underline{\hspace{2cm}} \text{ s.}$$

$$x_{\text{peak},3} = \underline{\hspace{2cm}} \text{ m} \quad \text{at } t = \underline{\hspace{2cm}} \text{ s.}$$

$$x_{\text{peak},4} = \underline{\hspace{2cm}} \text{ m} \quad \text{at } t = \underline{\hspace{2cm}} \text{ s.}$$

Then, calculate the period of the vibration:

$$t_{\text{peak},2} - t_{\text{peak},1} = \underline{\hspace{2cm}}$$

$$t_{\text{peak},3} - t_{\text{peak},2} = \underline{\hspace{2cm}}$$

$$t_{\text{peak},4} - t_{\text{peak},3} = \underline{\hspace{2cm}}$$

What is the amplitude ratios:

$$x_{\text{peak},1} / x_{\text{peak},2} = \underline{\hspace{2cm}}$$

$$x_{\text{peak},2} / x_{\text{peak},3} = \underline{\hspace{2cm}}$$

$$x_{\text{peak},3} / x_{\text{peak},4} = \underline{\hspace{2cm}}$$

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<b>Problem 4</b>	O.D.E.:	$\frac{dy}{dt} = \frac{30 e^{-0.10 t}}{1 + \sqrt{y}} - t e^{-0.25t}$
	I.C.:	$y(0) = 100$

What is the limit? That means,  $y$  approaches to  $\underline{\hspace{2cm}}$  as time goes to infinity.

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<b>Problem 5</b>	O.D.E.:	$\frac{dy}{dt} = \frac{c e^{-0.1 t}}{1 + \sqrt{y}} - t e^{-0.25t}$
	I.C.:	$y(0) = 100$

It was given that  $y(10) = 120$ .

Estimate the value of  $c = \underline{\hspace{2cm}}$  with a tolerance of  $\pm 0.1$ .

Plot  $y$  versus  $t$  for that particular value of  $c$ .

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**Problem 6**

O.D.E.:  $\frac{d^3 y}{dt^3} = -0.5y - 0.3t$

I.C.:  $y(0) = 10$   
 $dy/dt(0) = 100$   
 $d^2 y/dt^2(0) = 0$

- Plot  $y$  versus  $t$  in  $0 \leq t \leq 5$ .
- $y_{\max} = \underline{\hspace{2cm}}$  m at  $t = \underline{\hspace{2cm}}$  s.