

# Bifurcation Equations

## Kuznetzov Cancer Model

$$\dot{x} = \lambda y + \frac{\rho xy}{\eta + y} - \mu xy - \delta x + \sigma,$$

$$\dot{y} = \alpha y(1 - \beta y)(y - \beta_0) - \mu_1 xy,$$

$$\begin{aligned}
& \text{SN} = -4 \beta \eta^2 \lambda^5 \mu \mu^5 + \alpha^5 (-1 + \beta \beta \theta)^2 (\beta^2 \delta \eta + \mu + \beta (\delta + \eta \mu - \rho))^2 \\
& \quad (\delta \eta + \beta \theta^2 \mu + \beta \theta (\delta + \eta \mu - \rho))^2 (\delta^2 + (-\eta \mu + \rho)^2 - 2 \delta (\eta \mu + \rho)) + \\
& \quad \alpha \eta \lambda^4 \mu^4 (\eta \mu^2 + 2 \beta \mu (\eta (9 \delta - 4 \eta \mu - 5 \rho) + \beta \theta (4 \delta - 9 \eta \mu + 4 \rho))) + \\
& \quad \beta^2 \eta (\delta^2 + \beta \theta^2 \mu^2 - 8 \eta^2 \mu^2 + 2 \delta (9 \beta \theta \mu + 4 \eta \mu - \rho) - 20 \eta \mu \rho + \rho^2 - 2 \beta \theta \mu (4 \eta \mu + 5 \rho)) - \\
& \quad 2 \alpha^2 \lambda^3 \mu^3 (\eta \mu^2 (\beta \theta (\delta - 2 \eta \mu + \rho) - \eta (-2 \delta + \eta \mu + \rho))) + \\
& \quad \beta \mu (\beta \theta \eta (14 \delta^2 - 25 \delta \eta \mu + 13 \eta^2 \mu^2 - 4 \delta \rho - 10 \rho^2) + 2 \beta \theta^2 (\delta^2 - 7 \delta \eta \mu + 8 \eta^2 \mu^2 - \\
& \quad 2 \delta \rho - 7 \eta \mu \rho + \rho^2) + \eta^2 (16 \delta^2 - 13 \delta \eta \mu + \eta^2 \mu^2 - 18 \delta \rho - 5 \eta \mu \rho + 4 \rho^2)) + \\
& \quad \beta^3 \eta^2 (-\beta \theta^3 \mu^2 (-2 \delta + \eta \mu + \rho) + \beta \theta^2 \mu (16 \delta^2 - 13 \delta \eta \mu + \eta^2 \mu^2 - 18 \delta \rho - 5 \eta \mu \rho + 4 \rho^2)) + \\
& \quad \eta (\delta^3 + \delta^2 (\eta \mu - 4 \rho) + 2 (\eta \mu - \rho)^3 - \delta (4 \eta^2 \mu^2 + \eta \mu \rho - 5 \rho^2)) + \\
& \quad \beta \theta (2 \delta^3 + \delta^2 (13 \eta \mu - 5 \rho) + (4 \eta \mu - \rho) (-\eta \mu + \rho)^2 + \delta (-18 \eta^2 \mu^2 - 31 \eta \mu \rho + 4 \rho^2)) + \\
& \quad \beta^2 \eta (\beta \theta^3 \mu^2 (\delta - 2 \eta \mu + \rho) + \beta \theta^2 \mu (14 \delta^2 - 25 \delta \eta \mu + 13 \eta^2 \mu^2 - 4 \delta \rho - 10 \rho^2)) + \\
& \quad \beta \theta (\delta^3 + 18 \eta^3 \mu^3 + \delta^2 (25 \eta \mu - \rho) + 4 \eta^2 \mu^2 \rho - 23 \eta \mu \rho^2 + \rho^3 - \delta (46 \eta^2 \mu^2 + 30 \eta \mu \rho + \rho^2)) + \\
& \quad \eta (2 \delta^3 + \delta^2 (13 \eta \mu - 5 \rho) + (4 \eta \mu - \rho) (-\eta \mu + \rho)^2 + \delta (-18 \eta^2 \mu^2 - 31 \eta \mu \rho + 4 \rho^2)) + \alpha^3 \lambda^2 \\
& \mu^2 (\mu^2 (\eta^2 (6 \delta^2 + (-\eta \mu + \rho)^2 - 6 \delta (\eta \mu + \rho))) + \beta \theta^2 (\delta^2 + 6 \eta^2 \mu^2 - 6 \eta \mu \rho + \rho^2 - 2 \delta (3 \eta \mu + \rho))) + \\
& \quad 2 \beta \theta \eta (3 \delta^2 + 3 \eta^2 \mu^2 - \eta \mu \rho - 2 \rho^2 - \delta (5 \eta \mu + \rho)) - \\
& \quad 2 \beta \mu (\beta \theta^3 \mu (5 \delta^2 + 14 \eta^2 \mu^2 - 18 \eta \mu \rho + 5 \rho^2 - 2 \delta (9 \eta \mu + 5 \rho))) + \\
& \quad \beta \theta \eta (-18 \delta^3 + (\eta \mu - 8 \rho) (-\eta \mu + \rho)^2 + 4 \delta^2 (6 \eta \mu + 7 \rho) + \delta (-8 \eta^2 \mu^2 + 9 \eta \mu \rho - 2 \rho^2)) + \\
& \quad \eta^2 (-14 \delta^3 - (\eta \mu - \rho)^3 + 3 \delta^2 (5 \eta \mu + 8 \rho) - \delta (\eta^2 \mu^2 - 12 \eta \mu \rho + 11 \rho^2)) - \beta \theta^2 (5 \delta^3 - \\
& \quad 15 \eta^3 \mu^3 + 18 \eta^2 \mu^2 \rho + 2 \eta \mu \rho^2 - 5 \rho^3 - 15 \delta^2 (\eta \mu + \rho) + \delta (24 \eta^2 \mu^2 + 13 \eta \mu \rho + 15 \rho^2)) + \\
& \quad \beta^4 \eta^2 (\beta \theta^4 \mu^2 (6 \delta^2 + (-\eta \mu + \rho)^2 - 6 \delta (\eta \mu + \rho))) + \delta^2 \eta^2 (\delta^2 + (-\eta \mu + \rho)^2 - 2 \delta (\eta \mu + \rho)) + \\
& \quad 2 \beta \theta^3 \mu (14 \delta^3 + (\eta \mu - \rho)^3 - 3 \delta^2 (5 \eta \mu + 8 \rho) + \delta (\eta^2 \mu^2 - 12 \eta \mu \rho + 11 \rho^2)) + \\
& \quad 2 \beta \theta \delta \eta (3 \delta^3 + \delta^2 (\eta \mu - 11 \rho) + 5 (\eta \mu - \rho)^3 + \delta (-9 \eta^2 \mu^2 - 4 \eta \mu \rho + 13 \rho^2)) + \\
& \quad \beta \theta^2 (6 \delta^4 + 6 \delta^3 (5 \eta \mu - 3 \rho) + 2 \delta (9 \eta \mu - 4 \rho) (-\eta \mu + \rho)^2 + \\
& \quad (-\eta \mu + \rho)^4 + \delta^2 (-54 \eta^2 \mu^2 - 72 \eta \mu \rho + 19 \rho^2)) - \\
& \quad 2 \beta^3 \eta (\beta \theta^4 \mu^2 (-3 \delta^2 - 3 \eta^2 \mu^2 + \eta \mu \rho + 2 \rho^2 + \delta (5 \eta \mu + \rho))) + \delta \eta^2 (-3 \delta^3 - 5 (\eta \mu - \rho)^3 + \\
& \quad \delta^2 (-\eta \mu + 11 \rho) + \delta (9 \eta^2 \mu^2 + 4 \eta \mu \rho - 13 \rho^2)) + \beta \theta \eta (-5 \delta^4 + 5 (-\eta \mu + \rho)^4 - \\
& \quad 5 \delta (-\eta \mu + \rho)^2 (6 \eta \mu + \rho) + \delta^3 (-8 \eta \mu + 15 \rho) + \delta^2 (39 \eta^2 \mu^2 + 12 \eta \mu \rho - 10 \rho^2)) + \\
& \quad \beta \theta^3 \mu (-18 \delta^3 + (\eta \mu - 8 \rho) (-\eta \mu + \rho)^2 + 4 \delta^2 (6 \eta \mu + 7 \rho) + \delta (-8 \eta^2 \mu^2 + 9 \eta \mu \rho - 2 \rho^2)) +
\end{aligned}$$

$$\begin{aligned}
& \beta\theta^2 (-3\delta^4 + (9\eta\mu - 2\rho)(\eta\mu - \rho)^3 + \delta^3(-24\eta\mu + 7\rho) + \\
& \quad \delta^2(58\eta^2\mu^2 + 50\eta\mu\rho - 3\rho^2) - \delta(39\eta^3\mu^3 - 53\eta^2\mu^2\rho + 11\eta\mu\rho^2 + 3\rho^3)) + \\
& \beta^2 (\beta\theta^4\mu^2(\delta^2 + 6\eta^2\mu^2 - 6\eta\mu\rho + \rho^2 - 2\delta(3\eta\mu + \rho)) + 2\beta\theta^3\mu(5\delta^3 - 15\eta^3\mu^3 + 18\eta^2\mu^2\rho + 2\eta\mu \\
& \quad \rho^2 - 5\rho^3 - 15\delta^2(\eta\mu + \rho) + \delta(24\eta^2\mu^2 + 13\eta\mu\rho + 15\rho^2)) + \eta^2(6\delta^4 + 6\delta^3(5\eta\mu - 3\rho) + \\
& \quad 2\delta(9\eta\mu - 4\rho)(-\eta\mu + \rho)^2 + (-\eta\mu + \rho)^4 + \delta^2(-54\eta^2\mu^2 - 72\eta\mu\rho + 19\rho^2)) + \\
& \beta\theta^2(\delta^4 + \delta^3(30\eta\mu - 4\rho) - (-\eta\mu + \rho)^2(54\eta^2\mu^2 + 28\eta\mu\rho - \rho^2) + \\
& \quad \delta^2(-99\eta^2\mu^2 - 90\eta\mu\rho + 6\rho^2) + 2\delta(58\eta^3\mu^3 - 21\eta^2\mu^2\rho + 45\eta\mu\rho^2 - 2\rho^3)) + \\
& 2\beta\theta\eta(3\delta^4 + \delta^3(24\eta\mu - 7\rho) - (9\eta\mu - 2\rho)(\eta\mu - \rho)^3 + \delta^2(-58\eta^2\mu^2 - 50\eta\mu\rho + 3\rho^2) + \\
& \quad \delta(39\eta^3\mu^3 - 53\eta^2\mu^2\rho + 11\eta\mu\rho^2 + 3\rho^3))) - 2\alpha^4\lambda\mu_1 \\
& (\mu^2(-\beta\theta^3\mu(\delta^2 - 3\delta\eta\mu + 2\eta^2\mu^2 - 2\delta\rho - 3\eta\mu\rho + \rho^2) + \delta\eta^2(2\delta^2 + (-\eta\mu + \rho)^2 - 3\delta(\eta\mu + \rho)) + \\
& \quad \beta\theta\eta(3\delta^3 - (\eta\mu - \rho)^3 - \delta^2(4\eta\mu + 5\rho) + \delta(2\eta^2\mu^2 - 3\eta\mu\rho + \rho^2)) + \\
& \quad \beta\theta^2(\delta^3 - (-\eta\mu + \rho)^2(3\eta\mu + \rho) - \delta^2(2\eta\mu + 3\rho) + \delta(4\eta^2\mu^2 + 3\eta\mu\rho + 3\rho^2)) + \\
& \beta^5\beta\theta\delta\eta^2(\beta\theta^4\mu^2(2\delta^2 + (-\eta\mu + \rho)^2 - 3\delta(\eta\mu + \rho)) + \delta^2\eta^2(\delta^2 + (-\eta\mu + \rho)^2 - 2\delta(\eta\mu + \rho)) + \\
& \quad \beta\theta^3\mu(6\delta^3 + 2(\eta\mu - \rho)^3 - 7\delta^2(\eta\mu + 2\rho) - \delta(\eta^2\mu^2 + 9\eta\mu\rho - 10\rho^2)) + \beta\theta^2(2\delta^4 + 7\delta^3 \\
& \quad (\eta\mu - \rho) + \delta(6\eta\mu - 5\rho)(-\eta\mu + \rho)^2 + (-\eta\mu + \rho)^4 + \delta^2(-16\eta^2\mu^2 - 19\eta\mu\rho + 9\rho^2)) + \\
& \quad \beta\theta\delta\eta(3\delta^3 + 4(\eta\mu - \rho)^3 - \delta^2(\eta\mu + 10\rho) + \delta(-6\eta^2\mu^2 - 5\eta\mu\rho + 11\rho^2)) + \\
& \beta\mu(2\beta\theta^4\mu^2(2\delta^2 - 5\delta\eta\mu + 3\eta^2\mu^2 - 4\delta\rho - 5\eta\mu\rho + 2\rho^2) - \beta\theta\eta(-10\delta^4 - 4\delta(2\eta\mu - \rho) \\
& \quad (-\eta\mu + \rho)^2 + 2(-\eta\mu + \rho)^4 + \delta^3(9\eta\mu + 28\rho) + \delta^2(7\eta^2\mu^2 + 15\eta\mu\rho - 24\rho^2)) + \\
& \quad \delta\eta^2(6\delta^3 + 2(\eta\mu - \rho)^3 - 7\delta^2(\eta\mu + 2\rho) - \delta(\eta^2\mu^2 + 9\eta\mu\rho - 10\rho^2)) + \\
& \quad \beta\theta^3\mu(2\delta^3 - 6\delta^2\rho + (7\eta\mu - 2\rho)(-\eta\mu + \rho)^2 + \delta(-9\eta^2\mu^2 - 11\eta\mu\rho + 6\rho^2)) + \\
& \quad \beta\theta^2(4\delta^4 - 16\delta^3\rho - (\eta\mu - \rho)^3(\eta\mu + 4\rho) + \delta^2(-10\eta^2\mu^2 - 11\eta\mu\rho + 24\rho^2) + \\
& \quad \delta(7\eta^3\mu^3 - 13\eta^2\mu^2\rho + 22\eta\mu\rho^2 - 16\rho^3))) - \\
& \beta^4\eta(-\delta^3\eta^3(\delta^2 + (-\eta\mu + \rho)^2 - 2\delta(\eta\mu + \rho)) + \beta\theta^4\mu(-10\delta^4 - 4\delta(2\eta\mu - \rho)(-\eta\mu + \rho)^2 + \\
& \quad 2(-\eta\mu + \rho)^4 + \delta^3(9\eta\mu + 28\rho) + \delta^2(7\eta^2\mu^2 + 15\eta\mu\rho - 24\rho^2)) + \\
& \beta\theta^5\mu^2(-3\delta^3 + (\eta\mu - \rho)^3 + \delta^2(4\eta\mu + 5\rho) - \delta(2\eta^2\mu^2 - 3\eta\mu\rho + \rho^2)) + \\
& 2\beta\theta\delta^2\eta^2(-\delta^3 + (\eta\mu - \rho)^3 + \delta^2(4\eta\mu + \rho) + \delta(-4\eta^2\mu^2 + 3\eta\mu\rho + \rho^2)) + \beta\theta^2\delta\eta \\
& (-4\delta^4 + 10\delta\rho(-\eta\mu + \rho)^2 - 2(-\eta\mu + \rho)^4 + 7\delta^3(\eta\mu + 2\rho) - \delta^2(\eta^2\mu^2 - 5\eta\mu\rho + 18\rho^2)) + \\
& \beta\theta^3(-3\delta^5 + (\eta\mu - \rho)^5 - \delta(\eta\mu - \rho)^3(8\eta\mu + \rho) + \delta^4(-9\eta\mu + 11\rho) + \\
& \quad \delta^3(18\eta^2\mu^2 + 33\eta\mu\rho - 14\rho^2) + \delta^2(\eta^3\mu^3 + 27\eta^2\mu^2\rho - 34\eta\mu\rho^2 + 6\rho^3))) - \\
& \beta^2(\beta\theta^5\mu^3(\delta^2 - 3\delta\eta\mu + 2\eta^2\mu^2 - 2\delta\rho - 3\eta\mu\rho + \rho^2) + \beta\theta^4\mu^2 \\
& \quad (-2\delta^3 + 6\delta^2\rho - (7\eta\mu - 2\rho)(-\eta\mu + \rho)^2 + \delta(9\eta^2\mu^2 + 11\eta\mu\rho - 6\rho^2)) - \\
& \quad \delta\eta^2(2\delta^4 + 7\delta^3(\eta\mu - \rho) + \delta(6\eta\mu - 5\rho)(-\eta\mu + \rho)^2 + (-\eta\mu + \rho)^4 + \\
& \quad \delta^2(-16\eta^2\mu^2 - 19\eta\mu\rho + 9\rho^2)) + 2\beta\theta^3\mu(\delta^4 - (\eta\mu - \rho)^3(8\eta\mu + \rho) - \\
& \quad \delta^3(3\eta\mu + 4\rho) + \delta^2(\eta^2\mu^2 + 11\eta\mu\rho + 6\rho^2) + \delta(9\eta^3\mu^3 + 8\eta^2\mu^2\rho - 13\eta\mu\rho^2 - 4\rho^3)) + \\
& \beta\theta^2(-\delta^5 + 5\delta^4\rho - (6\eta\mu - \rho)(-\eta\mu + \rho)^4 - \delta(-\eta\mu + \rho)^2(\eta^2\mu^2 - 20\eta\mu\rho + 5\rho^2)) - \\
& \quad 2\delta^3(\eta^2\mu^2 - 5\eta\mu\rho + 5\rho^2) + 2\delta^2(5\eta^3\mu^3 + 9\eta^2\mu^2\rho - 15\eta\mu\rho^2 + 5\rho^3)) + \\
& \beta\theta\eta(-3\delta^5 + (\eta\mu - \rho)^5 - \delta(\eta\mu - \rho)^3(8\eta\mu + \rho) + \delta^4(-9\eta\mu + 11\rho) + \\
& \quad \delta^3(18\eta^2\mu^2 + 33\eta\mu\rho - 14\rho^2) + \delta^2(\eta^3\mu^3 + 27\eta^2\mu^2\rho - 34\eta\mu\rho^2 + 6\rho^3))) + \\
& \beta^3(\beta\theta^5\mu^2(\delta^3 - (-\eta\mu + \rho)^2(3\eta\mu + \rho) - \delta^2(2\eta\mu + 3\rho) + \delta(4\eta^2\mu^2 + 3\eta\mu\rho + 3\rho^2)) + \\
& \quad \delta^2\eta^3(3\delta^3 + 4(\eta\mu - \rho)^3 - \delta^2(\eta\mu + 10\rho) + \delta(-6\eta^2\mu^2 - 5\eta\mu\rho + 11\rho^2)) + \beta\theta\delta\eta^2 \\
& \quad (4\delta^4 - 10\delta\rho(-\eta\mu + \rho)^2 + 2(-\eta\mu + \rho)^4 - 7\delta^3(\eta\mu + 2\rho) + \delta^2(\eta^2\mu^2 - 5\eta\mu\rho + 18\rho^2)) +
\end{aligned}$$

$$\begin{aligned}
& 2 \beta \theta^2 \eta (\delta^5 + 2(\eta \mu - \rho)^5 - 9 \delta (\eta \mu - \rho)^3 \rho - \delta^4 (5 \eta \mu + 6 \rho) + \\
& \quad \delta^3 (5 \eta^2 \mu^2 + 3 \eta \mu \rho + 14 \rho^2) + \delta^2 (-3 \eta^3 \mu^3 + 19 \eta \mu \rho^2 - 16 \rho^3)) + \\
& \beta \theta^3 (\delta^5 - 5 \delta^4 \rho + (6 \eta \mu - \rho) (-\eta \mu + \rho)^4 + \delta (-\eta \mu + \rho)^2 (\eta^2 \mu^2 - 20 \eta \mu \rho + 5 \rho^2)) + \\
& \quad 2 \delta^3 (\eta^2 \mu^2 - 5 \eta \mu \rho + 5 \rho^2) - 2 \delta^2 (5 \eta^3 \mu^3 + 9 \eta^2 \mu^2 \rho - 15 \eta \mu \rho^2 + 5 \rho^3)) - \\
& \beta \theta^4 \mu (-4 \delta^4 + 16 \delta^3 \rho + (\eta \mu - \rho)^3 (\eta \mu + 4 \rho) + \delta^2 (10 \eta^2 \mu^2 + 11 \eta \mu \rho - 24 \rho^2)) + \\
& \quad \delta (-7 \eta^3 \mu^3 + 13 \eta^2 \mu^2 \rho - 22 \eta \mu \rho^2 + 16 \rho^3))) ;
\end{aligned}$$

$$\begin{aligned}
In[=] := \text{Hoff} = & -\lambda^2 \mu^3 \mu \mathbf{1}^2 + \alpha^6 \beta \theta (-1 + \beta \beta \theta)^2 (\beta \theta + \eta) (1 + \beta \eta) \\
& ((1 + \beta (\beta \theta + 2 \eta)) (2 \beta \delta + \mu + \beta \beta \theta \mu) - 2 \beta (1 + \beta \beta \theta) \rho) - 2 \alpha \beta \lambda^2 \mu \mathbf{1}^2 (-3 \delta \mu + 2 \lambda \mu \mathbf{1} + 3 \mu \rho) - \\
& \alpha^5 (\delta (\beta \theta + \eta) \mu - \beta \theta \mu \rho + \beta^5 \beta \theta^2 \delta \eta (\beta \theta + \eta) ((\beta \theta + 2 \eta) (2 \delta + \beta \theta \mu) - 2 \beta \theta \rho) + \\
& \beta ((\beta \theta + \eta) (2 \delta^2 + 3 \delta \eta \mu + 4 \beta \theta \lambda \mu \mathbf{1}) - 2 (2 \beta \theta \delta + \delta \eta + \beta \theta \eta \mu) \rho + 2 \beta \theta \rho^2) + \\
& 2 \beta^2 (-((\beta \theta + \eta) (\delta (\beta \theta^2 \mu + \beta \theta (\delta + \eta \mu) - \eta (3 \delta + \eta \mu)) - 2 \beta \theta (2 \beta \theta + 3 \eta) \lambda \mu \mathbf{1})) + \\
& (\delta (2 \beta \theta^2 - 2 \beta \theta \eta - \eta^2) + \beta \theta^2 (\beta \theta + \eta) \mu) \rho - \beta \theta^2 \rho^2) + \\
& 2 \beta^3 ((\beta \theta + \eta) (\delta (-\delta (\beta \theta^2 + 5 \beta \theta \eta - 2 \eta^2) - \beta \theta \eta (2 \beta \theta + \eta) \mu) + 2 \beta \theta (\beta \theta^2 + 4 \beta \theta \eta + 2 \eta^2) \lambda \mu \mathbf{1}) + \\
& \beta \theta (6 \beta \theta \delta \eta + \delta \eta^2 + \beta \theta^2 (2 \delta + \eta \mu)) \rho - \beta \theta^3 \rho^2) + \\
& \beta^4 \beta \theta ((\beta \theta + \eta) (\delta (-8 \delta \eta^2 + \beta \theta^3 \mu + 2 \beta \theta \eta (\delta - \eta \mu) + 2 \beta \theta^2 (\delta + \eta \mu)) + 4 \beta \theta \eta (\beta \theta + 2 \eta) \lambda \mu \mathbf{1}) - \\
& \beta \theta (4 \beta \theta \delta \eta - 2 \delta \eta^2 + \beta \theta^3 \mu + 2 \beta \theta^2 (2 \delta + \eta \mu)) \rho + 2 \beta \theta^3 \rho^2) ) - \\
& \alpha^3 \lambda \mu \mathbf{1} (\mu (\delta - \rho) + \beta (2 \delta^2 + 4 (2 \beta \theta + \eta) \lambda \mu \mathbf{1} + (7 \beta \theta - 2 \eta) \mu \rho + 2 \rho^2 - \delta (7 \beta \theta \mu + 6 \eta \mu + 4 \rho)) + \\
& \beta^2 (6 \eta^2 (-3 \delta \mu + 2 \lambda \mu \mathbf{1}) + \beta \theta^2 (-7 \delta \mu + 8 \lambda \mu \mathbf{1} + 7 \mu \rho) - \\
& 4 \beta \theta (\delta^2 + 6 \delta \eta \mu - 4 \eta \lambda \mu \mathbf{1} - 2 \delta \rho - \eta \mu \rho + \rho^2)) + \\
& \beta^3 (6 \beta \theta \eta^2 (-3 \delta \mu + 2 \lambda \mu \mathbf{1}) + \beta \theta^3 \mu (\delta - \rho) + 4 \eta^2 (-3 \delta \eta \mu + 2 \eta \lambda \mu \mathbf{1} + 3 \delta \rho) + \\
& 2 \beta \theta^2 (\delta^2 - 3 \delta \eta \mu + 2 \eta \lambda \mu \mathbf{1} - 2 \delta \rho - \eta \mu \rho + \rho^2)) ) - \\
& \alpha^2 \lambda \mu \mathbf{1} (\mu (-\lambda \mu \mathbf{1} + \mu (\delta + 2 \beta \theta \mu + \eta \mu - \rho)) + \beta (3 \delta^2 \mu + 4 \beta \theta \delta \mu^2 + 2 \beta \theta^2 \mu^3 + 4 \beta \theta \eta \mu^3 + \\
& 3 \eta^2 \mu^3 - 6 \delta \lambda \mu \mathbf{1} + 2 \beta \theta \lambda \mu \mathbf{1} - 2 \mu (3 \delta + 2 \beta \theta \mu + 3 \eta \mu) \rho + 6 \lambda \mu \mathbf{1} \rho + 3 \mu \rho^2) + \\
& \beta^2 (2 \delta^3 + \eta (\beta \theta + \eta) (\beta \theta + 2 \eta) \mu^3 - \beta \theta^2 \lambda \mu \mu \mathbf{1} + 3 \delta^2 (\beta \theta \mu - 2 \rho) - \\
& (\beta \theta^2 + 6 \beta \theta \eta + 6 \eta^2) \mu^2 \rho + 6 (\beta \theta + 2 \eta) \lambda \mu \mathbf{1} \rho + 3 (\beta \theta + 2 \eta) \mu \rho^2 - \\
& 2 \rho^3 + \delta (\beta \theta (\beta \theta \mu^2 - 6 \lambda \mu \mathbf{1}) - 6 (\beta \theta + \eta) \mu \rho + 6 \rho^2)) ) - \\
& \alpha^4 (\mu (\beta \theta^2 \mu^2 - 2 \beta \theta \lambda \mu \mathbf{1} + \eta (\delta \mu - \lambda \mu \mathbf{1}) + \beta \theta \mu (\delta + \eta \mu - \rho)) + \\
& \beta^4 \eta ((\beta \theta + \eta) (\beta \theta + 2 \eta) (\delta (\delta + \beta \theta \mu) (2 \delta + \beta \theta \mu) - \beta \theta \lambda (6 \delta + \beta \theta \mu) \mu \mathbf{1}) - \\
& \beta \theta (\delta (6 \delta \eta + 3 \beta \theta^2 \mu + 4 \beta \theta (\delta + \eta \mu)) - 2 \beta \theta (\beta \theta + \eta) \lambda \mu \mathbf{1}) \rho + 2 \beta \theta^2 \delta \rho^2) + \beta (2 \beta \theta^3 \mu^3 + \\
& \beta \theta^2 \mu (2 \lambda \mu \mathbf{1} + 5 \mu (\delta + \eta \mu - \rho)) + \eta (3 \delta^2 \mu + \lambda \mu \mathbf{1} (-3 \eta \mu + 2 \rho) + 3 \delta (\eta \mu^2 - 2 \lambda \mu \mathbf{1} - \mu \rho)) + \\
& \beta \theta (3 \delta^2 \mu + 3 \eta^2 \mu^3 + \delta (8 \eta \mu^2 - 8 \lambda \mu \mathbf{1} - 6 \mu \rho) - 2 \eta \mu (\lambda \mu \mathbf{1} + 3 \mu \rho) + \rho (8 \lambda \mu \mathbf{1} + 3 \mu \rho)) ) + \\
& \beta^2 (\beta \theta^4 \mu^3 + \beta \theta^3 \mu (2 \lambda \mu \mathbf{1} + 5 \mu (\delta + \eta \mu - \rho)) + 2 \beta \theta^2 \\
& (3 \delta^2 \mu + 3 \eta^2 \mu^3 + \delta (9 \eta \mu^2 - 4 \lambda \mu \mathbf{1} - 6 \mu \rho) + 3 \eta \mu (\lambda \mu \mathbf{1} - 2 \mu \rho) + \rho (4 \lambda \mu \mathbf{1} + 3 \mu \rho)) + \\
& \eta (2 \delta^3 + \delta^2 (9 \eta \mu - 4 \rho) + 2 \eta \lambda \mu \mathbf{1} (-\eta \mu + \rho) + 2 \delta (\eta^2 \mu^2 - 9 \eta \lambda \mu \mathbf{1} - 2 \eta \mu \rho + \rho^2)) + \\
& \beta \theta (2 \delta^3 + 2 \eta^3 \mu^3 + 3 \delta^2 (5 \eta \mu - 2 \rho) - 2 \rho^3 + 3 \eta^2 \mu (\lambda \mu \mathbf{1} - 2 \mu \rho) + \\
& 2 \eta \rho (5 \lambda \mu \mathbf{1} + 3 \mu \rho) + 3 \delta (5 \eta (\eta \mu^2 - 2 \lambda \mu \mathbf{1}) - 7 \eta \mu \rho + 2 \rho^2)) ) + \\
& \beta^3 (\beta \theta^4 \mu (-2 \lambda \mu \mathbf{1} + \mu (\delta + \eta \mu - \rho)) + 6 \delta \eta^2 (\delta^2 + \delta \eta \mu - 2 \eta \lambda \mu \mathbf{1} - \delta \rho) + \\
& \beta \theta^3 (3 \delta^2 \mu + 3 \eta^2 \mu^3 + \delta (8 \eta \mu^2 - 8 \lambda \mu \mathbf{1} - 6 \mu \rho) - 2 \eta \mu (\lambda \mu \mathbf{1} + 3 \mu \rho) + \rho (8 \lambda \mu \mathbf{1} + 3 \mu \rho)) + \\
& \beta \theta^2 (2 \delta^3 + 2 \eta^3 \mu^3 + 3 \delta^2 (5 \eta \mu - 2 \rho) - 2 \rho^3 + 3 \eta^2 \mu (\lambda \mu \mathbf{1} - 2 \mu \rho) + \\
& 2 \eta \rho (5 \lambda \mu \mathbf{1} + 3 \mu \rho) + 3 \delta (5 \eta (\eta \mu^2 - 2 \lambda \mu \mathbf{1}) - 7 \eta \mu \rho + 2 \rho^2)) ) + \\
& 2 \beta \theta \eta (4 \delta^3 + \delta^2 (9 \eta \mu - 8 \rho) + 2 \eta \lambda \mu \mathbf{1} (\eta \mu - \rho) + 2 \delta (2 \eta^2 \mu^2 - 9 \eta \lambda \mu \mathbf{1} - 4 \eta \mu \rho + 2 \rho^2)) ) ;
\end{aligned}$$

$$\begin{aligned}
In[=] := \text{BT} = & -3 \eta \lambda^2 \mu^3 \mu \mathbf{1}^2 \rho + \alpha^6 (-1 + \beta \beta \theta)^2 \eta (\beta \theta + \eta) \\
& (1 + \beta \eta) ((1 + \beta (\beta \theta + 2 \eta))^2 \mu - 4 \beta^2 \eta \rho) (\delta (\eta + \beta \beta \theta \eta) + \beta \theta (-\eta \mu + \rho)) +
\end{aligned}$$

$$\begin{aligned}
& \alpha \lambda \mu 1 (\beta \theta \mu^2 (3 \beta \eta^3 \mu^3 + 3 \delta^2 (\mu + \beta \eta \mu) + 3 \mu \rho^2 - 6 \delta (1 + \beta \eta) \mu (\eta \mu + \rho) + 3 \eta^2 \mu^2 (\mu - 2 \beta \rho) + \\
& \quad \eta \rho (-6 \mu^2 + 2 \beta \lambda \mu 1 + 3 \beta \mu \rho)) + \eta (3 \beta \eta^3 \mu^5 + 3 \eta^2 \mu^4 (\mu - 3 \beta \rho) + 3 \delta^2 \mu^2 (\mu + \beta \eta \mu - \beta \rho) + \\
& \quad 3 \eta \mu^3 \rho (-2 \mu + 3 \beta \rho) + \rho (-4 \beta \lambda^2 \mu 1^2 + 2 \lambda \mu \mu 1 (\mu - 8 \beta \rho) + 3 \mu^2 \rho (\mu - \beta \rho))) - \\
& \quad 2 \delta (3 \eta \mu^4 + 3 \beta \eta^2 \mu^4 + \mu \rho (3 \mu^2 - 8 \beta \lambda \mu 1 - 3 \beta \mu \rho))) ) + \\
& \alpha^5 \eta (\beta \theta + \eta) (1 + \beta \eta) (-\mu (-2 \delta^2 + \eta \lambda \mu 1 + 2 \delta (\beta \theta \mu - \eta \mu + \rho))) + \\
& \quad 2 \beta (5 \delta^2 \eta \mu + \delta (\beta \theta^2 \mu^2 + 2 \beta \theta \mu (-\eta \mu + \rho) + 2 \eta (3 \eta \mu^2 - \lambda \mu 1 - 3 \mu \rho)) - \\
& \quad 2 (\eta^2 \lambda \mu \mu 1 + 2 \beta \theta^2 \mu^2 (\eta \mu - \rho) + \beta \theta (\eta \mu - \rho) (\eta \mu^2 - \lambda \mu 1 - \mu \rho))) + \\
& \beta^4 (32 \delta^3 \eta^3 + 8 \beta \theta \delta \eta^2 (4 \delta^2 + 3 \delta \eta \mu - 2 \eta \lambda \mu 1 - 3 \delta \rho) + \beta \theta^4 \mu (2 \delta^2 + 2 \delta \eta \mu - \eta \lambda \mu 1 - 2 \delta \rho) + \\
& \quad 2 \beta \theta^3 \eta (5 \delta^2 \mu - 2 \eta \lambda \mu \mu 1 + \delta (6 \eta \mu^2 - 2 \lambda \mu 1 - 6 \mu \rho)) + \\
& \quad 4 \beta \theta^2 \eta (2 \delta^3 + 6 \delta^2 (\eta \mu - \rho) + \eta \lambda \mu 1 (-\eta \mu + \rho) + 4 \delta (\eta^2 \mu^2 - \eta \lambda \mu 1 - 2 \eta \mu \rho + \rho^2)) + \\
& \quad 2 \beta^2 (4 \delta^3 \eta + 4 \beta \theta^3 \mu^2 (-\eta \mu + \rho) + 2 \eta^2 \lambda \mu 1 (-\eta \mu + \rho) + \delta^2 (-2 \beta \theta^2 \mu + 12 \eta (\eta \mu - \rho) + \\
& \quad \beta \theta (7 \eta \mu + 4 \rho)) - 2 \beta \theta (2 \eta^3 \mu^3 - 2 \rho^3 + 2 \eta \rho (2 \lambda \mu 1 + 3 \mu \rho) - \eta^2 \mu (5 \lambda \mu 1 + 6 \mu \rho)) + \\
& \quad \beta \theta^2 (-12 \eta^2 \mu^3 - 4 \rho (\lambda \mu 1 + 3 \mu \rho) + \eta \mu (5 \lambda \mu 1 + 24 \mu \rho)) + \delta (\beta \theta^3 \mu^2 + 2 \beta \theta^2 \mu (\eta \mu + 7 \rho) + \\
& \quad 8 \eta (\eta^2 \mu^2 - \eta \lambda \mu 1 - 2 \eta \mu \rho + \rho^2) - 2 \beta \theta (3 \eta^2 \mu^2 + 3 \eta \lambda \mu 1 - 7 \eta \mu \rho + 4 \rho^2)) - 2 \beta^3 \\
& (\beta \theta^4 \delta \mu^2 + 4 \delta \eta^2 (-4 \delta^2 - 3 \delta \eta \mu + 2 \eta \lambda \mu 1 + 3 \delta \rho) + 2 \beta \theta^3 (\eta \mu - \rho) (\delta \mu + \eta \mu^2 - \lambda \mu 1 - \mu \rho) + \\
& \quad 4 \beta \theta \eta (-2 \delta^3 + 3 \eta \lambda \mu 1 (-\eta \mu + \rho) - 2 \delta^2 (3 \eta \mu + \rho) + 4 \delta (\eta^2 \mu^2 + \eta \lambda \mu 1 - 2 \eta \mu \rho + \rho^2)) + \\
& \quad \beta \theta^2 (4 \eta^3 \mu^3 - 4 \rho^3 - \delta^2 (7 \eta \mu + 4 \rho) + 4 \eta \rho (2 \lambda \mu 1 + 3 \mu \rho) - \\
& \quad 2 \eta^2 \mu (5 \lambda \mu 1 + 6 \mu \rho) + 2 \delta (3 \eta^2 \mu^2 + 3 \eta \lambda \mu 1 - 7 \eta \mu \rho + 4 \rho^2))) + \\
& \alpha^2 (\mu (3 \beta \theta^2 \mu^3 (\delta^2 + (-\eta \mu + \rho)^2 - 2 \delta (\eta \mu + \rho)) + \eta (3 \delta^3 \mu^2 - 2 \delta^2 \mu (3 \eta \mu^2 + \lambda \mu 1 + 3 \mu \rho) + \\
& \quad \delta \mu (3 \eta^2 \mu^3 + 2 \eta \mu (5 \lambda \mu 1 - 3 \mu \rho) + \rho (-2 \lambda \mu 1 + 3 \mu \rho)) + \\
& \quad \lambda \mu 1 (-8 \eta^2 \mu^3 + 4 \eta \mu^2 \rho + \rho (\lambda \mu 1 + 4 \mu \rho))) + \\
& \beta \theta \mu (3 \delta^3 \mu + 3 \eta^3 \mu^4 - \rho^2 (2 \lambda \mu 1 + 3 \mu \rho) - \delta^2 (3 \eta \mu^2 + 2 \lambda \mu 1 + 9 \mu \rho) + \eta \mu \rho (4 \lambda \mu 1 + 9 \mu \rho) - \\
& \quad \eta^2 \mu^2 (8 \lambda \mu 1 + 9 \mu \rho) + \delta (-3 \eta^2 \mu^3 + 2 \eta \mu (5 \lambda \mu 1 - 3 \mu \rho) + \rho (4 \lambda \mu 1 + 9 \mu \rho))) - \\
& \beta^2 \eta (-3 \delta^4 \eta \mu^2 + 4 \delta \lambda \mu 1 (\eta^3 \mu^3 - 3 \eta \mu \rho^2 + 6 \rho^3 + 2 \eta^2 \mu (\lambda \mu 1 - 2 \mu \rho)) + \\
& \quad 2 \delta^3 (3 \eta^2 \mu^3 + 4 \lambda \mu 1 \rho + \eta \mu (8 \lambda \mu 1 + 3 \mu \rho)) + \\
& \quad 4 \lambda \mu 1 (3 \eta^4 \mu^4 - 2 \rho^4 + 3 \eta^2 \mu \rho (\lambda \mu 1 + \mu \rho) + \eta \rho^2 (4 \lambda \mu 1 + 3 \mu \rho) - \eta^3 \mu^2 (\lambda \mu 1 + 7 \mu \rho)) - \\
& \quad \delta^2 (3 \eta^3 \mu^4 + 24 \lambda \mu 1 \rho^2 + 2 \eta^2 \mu^2 (16 \lambda \mu 1 - 3 \mu \rho) + \eta (4 \lambda^2 \mu 1^2 + 16 \lambda \mu \mu 1 \rho + 3 \mu^2 \rho^2)) - \\
& \beta \theta^2 \mu (3 \delta^3 \mu^2 - 2 \delta^2 \mu (3 \eta \mu^2 + \lambda \mu 1 + 3 \mu \rho)) + \\
& \quad \delta \mu (3 \eta^2 \mu^3 + 2 \eta \mu (5 \lambda \mu 1 - 3 \mu \rho) + \rho (-2 \lambda \mu 1 + 3 \mu \rho)) + \lambda \mu 1 \\
& \quad (-8 \eta^2 \mu^3 + 4 \eta \mu^2 \rho + \rho (\lambda \mu 1 + 4 \mu \rho))) + \beta \theta (-3 \delta^4 \mu^2 + \delta^3 \mu (3 \eta \mu^2 + 16 \lambda \mu 1 + 9 \mu \rho)) + \\
& \quad \delta^2 (3 \eta^2 \mu^4 - 4 \lambda^2 \mu 1^2 - 26 \lambda \mu \mu 1 \rho - 9 \mu^2 \rho^2 + 6 \eta \mu^2 (-5 \lambda \mu 1 + \mu \rho)) + \\
& \quad 2 \lambda \mu 1 (10 \eta^3 \mu^4 + 4 \eta \mu \rho (\lambda \mu 1 + \mu \rho) + \rho^2 (2 \lambda \mu 1 + 3 \mu \rho) - \eta^2 \mu^2 (2 \lambda \mu 1 + 17 \mu \rho)) + \\
& \quad \delta \mu (-3 \eta^3 \mu^4 + \rho^2 (4 \lambda \mu 1 + 3 \mu \rho) + \eta^2 (-6 \lambda \mu^2 \mu 1 + 9 \mu^3 \rho) + \eta (8 \lambda^2 \mu 1^2 - 9 \mu^2 \rho^2))) + \\
& \beta (\beta \theta^2 \mu^2 (3 \delta^3 \mu + 3 \eta^3 \mu^4 - \rho^2 (2 \lambda \mu 1 + 3 \mu \rho) - \delta^2 (3 \eta \mu^2 + 2 \lambda \mu 1 + 9 \mu \rho)) + \\
& \quad \eta \mu \rho (4 \lambda \mu 1 + 9 \mu \rho) - \eta^2 \mu^2 (8 \lambda \mu 1 + 9 \mu \rho) + \\
& \quad \delta (-3 \eta^2 \mu^3 + 2 \eta \mu (5 \lambda \mu 1 - 3 \mu \rho) + \rho (4 \lambda \mu 1 + 9 \mu \rho))) + \beta \theta (3 \delta^4 \mu^2 + 3 \eta^4 \mu^6 - \\
& \quad 4 \delta^3 \mu (4 \lambda \mu 1 + 3 \mu \rho) - 4 \eta^3 \mu^4 (7 \lambda \mu 1 + 3 \mu \rho) + \rho^2 (4 \lambda^2 \mu 1^2 + 16 \lambda \mu \mu 1 \rho + 3 \mu^2 \rho^2)) - \\
& \quad 2 \eta \mu \rho (5 \lambda^2 \mu 1^2 + 12 \lambda \mu \mu 1 \rho + 6 \mu^2 \rho^2) + 2 \eta^2 \mu^2 (2 \lambda^2 \mu 1^2 + 18 \lambda \mu \mu 1 \rho + 9 \mu^2 \rho^2) + \\
& \quad \delta^2 (-6 \eta^2 \mu^4 + 4 \lambda^2 \mu 1^2 + 48 \lambda \mu \mu 1 \rho + 18 \mu^2 \rho^2 + 4 \eta \mu^2 (7 \lambda \mu 1 - 3 \mu \rho)) + \\
& \quad 4 \delta (\eta^2 \mu^3 (4 \lambda \mu 1 - 3 \mu \rho) - \rho (2 \lambda^2 \mu 1^2 + 12 \lambda \mu \mu 1 \rho + 3 \mu^2 \rho^2)) + \eta \mu \\
& \quad (-2 \lambda^2 \mu 1^2 - \lambda \mu \mu 1 \rho + 6 \mu^2 \rho^2))) + \eta (3 \delta^4 \mu^2 - \delta^3 \mu (3 \eta \mu^2 + 16 \lambda \mu 1 + 9 \mu \rho)) +
\end{aligned}$$

$$\begin{aligned}
& \delta^2 (-3 \eta^2 \mu^4 + 4 \lambda^2 \mu \mu 1^2 + 26 \lambda \mu \mu 1 \rho + 9 \mu^2 \rho^2 - 6 \eta \mu^2 (-5 \lambda \mu 1 + \mu \rho)) + \\
& 2 \lambda \mu 1 (-10 \eta^3 \mu^4 - 4 \eta \mu \rho (\lambda \mu 1 + \mu \rho) - \rho^2 (2 \lambda \mu 1 + 3 \mu \rho) + \eta^2 \mu^2 (2 \lambda \mu 1 + 17 \mu \rho)) + \\
& \delta \mu (3 \eta^3 \mu^4 + 3 \eta^2 \mu^2 (2 \lambda \mu 1 - 3 \mu \rho) - \rho^2 (4 \lambda \mu 1 + 3 \mu \rho) + \eta (-8 \lambda^2 \mu 1^2 + 9 \mu^2 \rho^2))) + \\
& \alpha^3 (-\mu (2 \beta \theta^2 \mu^2 (\delta^2 - 5 \delta \eta \mu + 4 \eta^2 \mu^2 - 2 \delta \rho - 5 \eta \mu \rho + \rho^2) + \eta (-4 \delta^3 \mu + \delta^2 (2 \eta \mu^2 + \lambda \mu 1 + 8 \mu \rho)) + \\
& 2 \delta \mu (\eta^2 \mu^2 + \eta \lambda \mu 1 + \eta \mu \rho - 2 \rho^2) - \lambda \mu 1 (6 \eta^2 \mu^2 + 2 \eta \mu \rho + \rho^2)) + \\
& \beta \theta (-4 \delta^3 \mu + 8 \eta^3 \mu^4 - 2 \eta \lambda \mu \mu 1 \rho - 6 \eta^2 \mu^2 (\lambda \mu 1 + 2 \mu \rho) + \rho^2 (\lambda \mu 1 + 4 \mu \rho) + \\
& \delta^2 (4 \eta \mu^2 + \lambda \mu 1 + 12 \mu \rho) - 2 \delta (4 \eta^2 \mu^3 + \eta \mu (-\lambda \mu 1 + 2 \mu \rho) + \rho (\lambda \mu 1 + 6 \mu \rho))) + \\
& \beta^3 \eta (\beta \theta^3 \mu (4 \delta^3 \mu - \delta^2 (2 \eta \mu^2 + \lambda \mu 1 + 8 \mu \rho) - 2 \delta \mu (\eta^2 \mu^2 + \eta \lambda \mu 1 + \eta \mu \rho - 2 \rho^2) + \\
& \lambda \mu 1 (6 \eta^2 \mu^2 + 2 \eta \mu \rho + \rho^2)) + \\
& 4 \eta (2 \delta^5 - 2 \delta^4 (2 \eta \mu + 3 \rho) + 4 \delta \eta \lambda \mu 1 (4 \eta^2 \mu^2 + \eta \lambda \mu 1 - 3 \eta \mu \rho - \rho^2) + \\
& \eta \lambda \mu 1 (\eta \mu - \rho) (3 \eta^2 \mu^2 - 4 \eta \lambda \mu 1 - 6 \eta \mu \rho + 3 \rho^2) + \delta^3 (5 \eta^2 \mu^2 + 3 \eta \mu \rho + 6 \rho^2) + \\
& \delta^2 (-3 \eta^3 \mu^3 - 2 \rho^3 + 4 \eta^2 \mu (-4 \lambda \mu 1 + \mu \rho) + \eta \rho (4 \lambda \mu 1 + \mu \rho))) + \\
& \beta \theta^2 (6 \delta^4 \mu - 2 \delta^3 (\eta \mu^2 + 2 \lambda \mu 1 + 9 \mu \rho) + \eta \lambda \mu \mu 1 (26 \eta^2 \mu^2 - 8 \eta \lambda \mu 1 - 29 \eta \mu \rho + 3 \rho^2) + \\
& \delta^2 (10 \eta^2 \mu^3 + \eta \mu (-25 \lambda \mu 1 + 4 \mu \rho) + 2 \rho (4 \lambda \mu 1 + 9 \mu \rho)) - 2 \delta (7 \eta^3 \mu^4 + \rho^2 \\
& (2 \lambda \mu 1 + 3 \mu \rho) - \eta^2 \mu^2 (9 \lambda \mu 1 + 11 \mu \rho) + \eta (-4 \lambda^2 \mu 1^2 - 12 \lambda \mu \mu 1 \rho + \mu^2 \rho^2))) + \\
& 2 \beta \theta (4 \delta^5 - \delta^4 (5 \eta \mu + 16 \rho) + \delta^3 (7 \eta^2 \mu^2 - 2 \eta \lambda \mu 1 + 4 \eta \mu \rho + 24 \rho^2) + \\
& \delta^2 (-16 \rho^3 + \eta \rho (10 \lambda \mu 1 + 7 \mu \rho) + \eta^2 \mu (-44 \lambda \mu 1 + 9 \mu \rho)) + \\
& 2 \eta \lambda \mu 1 (8 \eta^3 \mu^3 - \rho^3 + 2 \eta \rho (2 \lambda \mu 1 + 5 \mu \rho) - \eta^2 \mu (6 \lambda \mu 1 + 17 \mu \rho)) - 2 \delta (3 \eta^4 \mu^4 - 2 \rho^4 + \\
& 3 \eta \rho^2 (\lambda \mu 1 + \mu \rho) - 7 \eta^3 \mu^2 (3 \lambda \mu 1 + \mu \rho) + \eta^2 (-6 \lambda^2 \mu 1^2 + 5 \lambda \mu \mu 1 \rho + 3 \mu^2 \rho^2))) + \\
& \beta (-2 \beta \theta^3 \mu^3 (\delta^2 - 5 \delta \eta \mu + 4 \eta^2 \mu^2 - 2 \delta \rho - 5 \eta \mu \rho + \rho^2) + 2 \beta \theta^2 \mu (-4 \delta^3 \mu - 14 \eta^3 \mu^4 + \\
& 3 \delta^2 (4 \eta \mu^2 + \lambda \mu 1 + 4 \mu \rho) + \rho^2 (3 \lambda \mu 1 + 4 \mu \rho) - 2 \eta \mu \rho (3 \lambda \mu 1 + 11 \mu \rho) + \\
& 2 \eta^2 \mu^2 (5 \lambda \mu 1 + 16 \mu \rho) + 2 \delta (3 \eta^2 \mu^3 + 5 \eta \mu (-\lambda \mu 1 + \mu \rho) - 3 \rho (\lambda \mu 1 + 2 \mu \rho))) + \\
& \eta (6 \delta^4 \mu - 2 \delta^3 (\eta \mu^2 + 2 \lambda \mu 1 + 9 \mu \rho) + \eta \lambda \mu \mu 1 (26 \eta^2 \mu^2 - 8 \eta \lambda \mu 1 - 29 \eta \mu \rho + 3 \rho^2) + \\
& \delta^2 (10 \eta^2 \mu^3 + \eta \mu (-25 \lambda \mu 1 + 4 \mu \rho) + 2 \rho (4 \lambda \mu 1 + 9 \mu \rho)) - 2 \delta (7 \eta^3 \mu^4 + \rho^2 \\
& (2 \lambda \mu 1 + 3 \mu \rho) - \eta^2 \mu^2 (9 \lambda \mu 1 + 11 \mu \rho) + \eta (-4 \lambda^2 \mu 1^2 - 12 \lambda \mu \mu 1 \rho + \mu^2 \rho^2))) + \\
& \beta \theta (6 \delta^4 \mu - 20 \eta^4 \mu^5 + \eta \mu \rho^2 (3 \lambda \mu 1 + 2 \mu \rho) + 2 \rho^3 (2 \lambda \mu 1 + 3 \mu \rho) - 2 \delta^3 (5 \eta \mu^2 + \\
& 2 \lambda \mu 1 + 12 \mu \rho) + 2 \eta^3 \mu^3 (23 \lambda \mu 1 + 27 \mu \rho) - 2 \eta^2 \mu (4 \lambda^2 \mu 1^2 + 23 \lambda \mu \mu 1 \rho + 21 \mu^2 \rho^2) + \\
& \delta^2 (36 \eta^2 \mu^3 + 12 \rho (\lambda \mu 1 + 3 \mu \rho) + \eta \mu (-19 \lambda \mu 1 + 22 \mu \rho)) - 2 \delta (6 \eta^3 \mu^4 + \eta^2 \\
& \mu^2 (\lambda \mu 1 - 25 \mu \rho) + 6 \rho^2 (\lambda \mu 1 + 2 \mu \rho) + \eta (-4 \lambda^2 \mu 1^2 - 8 \lambda \mu \mu 1 \rho + 7 \mu^2 \rho^2))) + \\
& \beta^2 (\beta \theta^3 \mu (4 \delta^3 \mu - 8 \eta^3 \mu^4 + 2 \eta \lambda \mu \mu 1 \rho + 6 \eta^2 \mu^2 (\lambda \mu 1 + 2 \mu \rho) - \rho^2 (\lambda \mu 1 + 4 \mu \rho) - \\
& \delta^2 (4 \eta \mu^2 + \lambda \mu 1 + 12 \mu \rho) + 2 \delta (4 \eta^2 \mu^3 + \eta \mu (-\lambda \mu 1 + 2 \mu \rho) + \rho (\lambda \mu 1 + 6 \mu \rho))) + \\
& 2 \eta (4 \delta^5 - \delta^4 (5 \eta \mu + 16 \rho) + \delta^3 (7 \eta^2 \mu^2 - 2 \eta \lambda \mu 1 + 4 \eta \mu \rho + 24 \rho^2) + \\
& \delta^2 (-16 \rho^3 + \eta \rho (10 \lambda \mu 1 + 7 \mu \rho) + \eta^2 \mu (-44 \lambda \mu 1 + 9 \mu \rho)) + \\
& 2 \eta \lambda \mu 1 (8 \eta^3 \mu^3 - \rho^3 + 2 \eta \rho (2 \lambda \mu 1 + 5 \mu \rho) - \eta^2 \mu (6 \lambda \mu 1 + 17 \mu \rho)) - 2 \delta (3 \eta^4 \mu^4 - 2 \rho^4 + \\
& 3 \eta \rho^2 (\lambda \mu 1 + \mu \rho) - 7 \eta^3 \mu^2 (3 \lambda \mu 1 + \mu \rho) + \eta^2 (-6 \lambda^2 \mu 1^2 + 5 \lambda \mu \mu 1 \rho + 3 \mu^2 \rho^2))) + \\
& \beta \theta^2 (6 \delta^4 \mu - 20 \eta^4 \mu^5 + \eta \mu \rho^2 (3 \lambda \mu 1 + 2 \mu \rho) + 2 \rho^3 (2 \lambda \mu 1 + 3 \mu \rho) - 2 \delta^3 (5 \eta \mu^2 + \\
& 2 \lambda \mu 1 + 12 \mu \rho) + 2 \eta^3 \mu^3 (23 \lambda \mu 1 + 27 \mu \rho) - 2 \eta^2 \mu (4 \lambda^2 \mu 1^2 + 23 \lambda \mu \mu 1 \rho + 21 \mu^2 \rho^2) + \\
& \delta^2 (36 \eta^2 \mu^3 + 12 \rho (\lambda \mu 1 + 3 \mu \rho) + \eta \mu (-19 \lambda \mu 1 + 22 \mu \rho)) - 2 \delta (6 \eta^3 \mu^4 + \eta^2 \\
& \mu^2 (\lambda \mu 1 - 25 \mu \rho) + 6 \rho^2 (\lambda \mu 1 + 2 \mu \rho) + \eta (-4 \lambda^2 \mu 1^2 - 8 \lambda \mu \mu 1 \rho + 7 \mu^2 \rho^2))) + \\
& 2 \beta \theta (4 \delta^5 - 6 \eta^5 \mu^5 - 4 \rho^5 - 2 \delta^4 (\eta \mu + 10 \rho) + 2 \eta \rho^3 (4 \lambda \mu 1 + 5 \mu \rho) + \\
& 4 \eta^4 \mu^3 (9 \lambda \mu 1 + 5 \mu \rho) + \eta^2 \lambda \mu 1 \rho (8 \lambda \mu 1 + 17 \mu \rho) -
\end{aligned}$$

$$\begin{aligned}
& 4 \delta^3 (\eta \lambda \mu 1 + \eta \mu \rho - 10 \rho^2) - \eta^3 \mu (16 \lambda^2 \mu 1^2 + 61 \lambda \mu \mu 1 \rho + 20 \mu^2 \rho^2) + \\
& \delta^2 (20 \eta^3 \mu^3 - 40 \rho^3 + 8 \eta \rho (2 \lambda \mu 1 + 3 \mu \rho) + \eta^2 \mu (-53 \lambda \mu 1 + 20 \mu \rho)) - 2 \delta (8 \eta^4 \mu^4 - 10 \\
& \rho^4 + 2 \eta \rho^2 (5 \lambda \mu 1 + 7 \mu \rho) - \eta^3 \mu^2 (21 \lambda \mu 1 + 22 \mu \rho) + \eta^2 (-8 \lambda^2 \mu 1^2 + 10 \mu^2 \rho^2))) + \\
& \alpha^4 (\mu (\delta \eta (\delta^2 + 6 \delta \eta \mu - 4 \eta^2 \mu^2 - 2 \eta \lambda \mu 1 - 2 \delta \rho - 6 \eta \mu \rho + \rho^2) - \beta \theta^2 \mu \\
& (\delta^2 + 2 \delta \eta \mu - 6 \eta^2 \mu^2 - 2 \delta \rho + 5 \eta \mu \rho + \rho^2) + \beta \theta (\delta^3 + 6 \eta^3 \mu^3 + \delta^2 (5 \eta \mu - 3 \rho) - \\
& 4 \eta^2 \mu^2 \rho - \eta \mu \rho^2 - \rho^3 - \delta (6 \eta^2 \mu^2 + 2 \eta \lambda \mu 1 + 4 \eta \mu \rho - 3 \rho^2))) + \\
& \beta^4 \eta (\beta \theta^4 \delta \mu (\delta^2 + 6 \delta \eta \mu - 4 \eta^2 \mu^2 - 2 \eta \lambda \mu 1 - 2 \delta \rho - 6 \eta \mu \rho + \rho^2) + \\
& 4 \eta^3 (8 \delta^4 + 4 \eta^2 \lambda^2 \mu 1^2 - 16 \delta \eta \lambda \mu 1 (\eta \mu - \rho) + 3 \delta^2 (-\eta \mu + \rho)^2 - 4 \delta^3 (2 \eta \mu + 3 \rho)) + \\
& \beta \theta^2 \eta (16 \delta^4 + 4 \delta^3 (5 \eta \mu - 13 \rho) - \delta^2 (5 \eta^2 \mu^2 + 24 \eta \lambda \mu 1 + 67 \eta \mu \rho - 56 \rho^2)) + \\
& 4 \eta \lambda \mu 1 (-3 \eta^2 \mu^2 - 2 \rho^2 + 5 \eta (\lambda \mu 1 + \mu \rho)) + \\
& 4 \delta (2 \eta^3 \mu^3 - 5 \rho^3 + 12 \eta \rho (\lambda \mu 1 + \mu \rho) - 3 \eta^2 \mu (5 \lambda \mu 1 + 3 \mu \rho)) + \\
& 4 \beta \theta \eta^2 (12 \delta^4 - \delta^3 (6 \eta \mu + 25 \rho) - 4 \delta^2 (\eta \lambda \mu 1 + 4 \eta \mu \rho - 4 \rho^2) - 2 \eta \lambda \mu 1 (\eta^2 \mu^2 + \rho^2 - \\
& 2 \eta (2 \lambda \mu 1 + \mu \rho)) + \delta (3 \eta^3 \mu^3 - 3 \rho^3 + \eta \rho (26 \lambda \mu 1 + 9 \mu \rho) - \eta^2 \mu (28 \lambda \mu 1 + 9 \mu \rho))) + \\
& \beta \theta^3 \eta (13 \delta^3 \mu + \delta^2 (13 \eta \mu^2 - 8 \lambda \mu 1 - 28 \mu \rho) + 4 \eta \lambda \mu 1 (-\eta \mu^2 + \lambda \mu 1 + \mu \rho) + \\
& \delta (-8 \eta^2 \mu^3 - 7 \eta \mu (2 \lambda \mu 1 + \mu \rho) + \rho (8 \lambda \mu 1 + 15 \mu \rho))) + \\
& \beta (2 \beta \theta^3 \mu^2 (\delta^2 + 8 \eta^2 \mu^2 - 9 \eta \mu \rho + \rho^2 - 2 \delta (3 \eta \mu + \rho)) + \beta \theta^2 \mu \\
& (-\delta^3 + 42 \eta^3 \mu^3 + \rho^3 + \delta^2 (-5 \eta \mu + 3 \rho) - 4 \eta^2 \mu (4 \lambda \mu 1 + 19 \mu \rho) + \\
& \eta \rho (8 \lambda \mu 1 + 33 \mu \rho) - \delta (6 \eta^2 \mu^2 - 10 \eta \lambda \mu 1 + 28 \eta \mu \rho + 3 \rho^2)) + \\
& \beta \theta \eta (12 \delta^3 \mu + 26 \eta^3 \mu^4 - 3 \mu \rho^3 + \delta^2 (6 \eta \mu^2 - 8 \lambda \mu 1 - 27 \mu \rho) - 5 \eta^2 \mu^2 (4 \lambda \mu 1 + 11 \mu \rho) + \\
& 4 \eta (\lambda^2 \mu 1^2 + 3 \lambda \mu \mu 1 \rho + 8 \mu^2 \rho^2) - 2 \delta (\eta^2 \mu^3 + 2 \eta \mu (\lambda \mu 1 + 8 \mu \rho) - \rho (4 \lambda \mu 1 + 9 \mu \rho))) + \\
& \eta^2 (13 \delta^3 \mu + \delta^2 (13 \eta \mu^2 - 8 \lambda \mu 1 - 28 \mu \rho) + 4 \eta \lambda \mu 1 (-\eta \mu^2 + \lambda \mu 1 + \mu \rho) + \\
& \delta (-8 \eta^2 \mu^3 - 7 \eta \mu (2 \lambda \mu 1 + \mu \rho) + \rho (8 \lambda \mu 1 + 15 \mu \rho))) - \\
& \beta^2 (\beta \theta^4 \mu^2 (\delta^2 + 2 \delta \eta \mu - 6 \eta^2 \mu^2 - 2 \delta \rho + 5 \eta \mu \rho + \rho^2) + \beta \theta^3 \mu (\delta^3 - 42 \eta^3 \mu^3 + \delta^2 (5 \eta \mu - 3 \rho) - \rho^3 + \\
& 4 \eta^2 \mu (4 \lambda \mu 1 + 19 \mu \rho) - \eta \rho (8 \lambda \mu 1 + 33 \mu \rho) + \delta (6 \eta^2 \mu^2 - 10 \eta \lambda \mu 1 + 28 \eta \mu \rho + 3 \rho^2)) + \\
& \eta^2 (-16 \delta^4 + \delta^3 (-20 \eta \mu + 52 \rho) + \delta^2 (5 \eta^2 \mu^2 + 24 \eta \lambda \mu 1 + 67 \eta \mu \rho - 56 \rho^2)) + \\
& 4 \eta \lambda \mu 1 (3 \eta^2 \mu^2 + 2 \rho^2 - 5 \eta (\lambda \mu 1 + \mu \rho)) - \\
& 4 \delta (2 \eta^3 \mu^3 - 5 \rho^3 + 12 \eta \rho (\lambda \mu 1 + \mu \rho) - 3 \eta^2 \mu (5 \lambda \mu 1 + 3 \mu \rho)) - \\
& 2 \beta \theta^2 \eta (11 \delta^3 \mu + 34 \eta^3 \mu^4 - \rho^2 (8 \lambda \mu 1 + 19 \mu \rho) - 3 \eta^2 \mu^2 (12 \lambda \mu 1 + 29 \mu \rho) - \\
& \delta^2 (30 \eta \mu^2 + 8 \lambda \mu 1 + 41 \mu \rho) + 4 \eta (\lambda^2 \mu 1^2 + 9 \lambda \mu \mu 1 \rho + 18 \mu^2 \rho^2) + \\
& \delta (30 \eta^2 \mu^3 + 2 \eta \mu (7 \lambda \mu 1 - 47 \mu \rho) + \rho (16 \lambda \mu 1 + 49 \mu \rho))) + \\
& \beta \theta \eta (-16 \delta^4 + \delta^3 (-43 \eta \mu + 52 \rho) + \delta^2 (61 \eta^2 \mu^2 - 60 \rho^2 + 8 \eta (5 \lambda \mu 1 + 19 \mu \rho))) + \\
& \delta (-72 \eta^3 \mu^3 + 28 \rho^3 - \eta \rho (80 \lambda \mu 1 + 153 \mu \rho) + \eta^2 \mu (42 \lambda \mu 1 + 197 \mu \rho)) - \\
& 4 (8 \eta^4 \mu^4 + \rho^4 - \eta \rho^2 (6 \lambda \mu 1 + 11 \mu \rho) - \eta^3 \mu^2 \\
& (17 \lambda \mu 1 + 25 \mu \rho) + \eta^2 (7 \lambda^2 \mu 1^2 + 21 \lambda \mu \mu 1 \rho + 27 \mu^2 \rho^2))) + \\
& \beta^3 (\beta \theta^4 \mu (\delta^3 + 6 \eta^3 \mu^3 + \delta^2 (5 \eta \mu - 3 \rho) - 4 \eta^2 \mu^2 \rho - \eta \mu \rho^2 - \rho^3 - \\
& \delta (6 \eta^2 \mu^2 + 2 \eta \lambda \mu 1 + 4 \eta \mu \rho - 3 \rho^2)) + \\
& \beta \theta^3 \eta (12 \delta^3 \mu + 26 \eta^3 \mu^4 - 3 \mu \rho^3 + \delta^2 (6 \eta \mu^2 - 8 \lambda \mu 1 - 27 \mu \rho) - 5 \eta^2 \mu^2 (4 \lambda \mu 1 + 11 \mu \rho) + \\
& 4 \eta (\lambda^2 \mu 1^2 + 3 \lambda \mu \mu 1 \rho + 8 \mu^2 \rho^2) - 2 \delta (\eta^2 \mu^3 + 2 \eta \mu (\lambda \mu 1 + 8 \mu \rho) - \rho (4 \lambda \mu 1 + 9 \mu \rho))) + \\
& 4 \eta^3 (12 \delta^4 - \delta^3 (6 \eta \mu + 25 \rho) - 4 \delta^2 (\eta \lambda \mu 1 + 4 \eta \mu \rho - 4 \rho^2) - \\
& 2 \eta \lambda \mu 1 (\eta^2 \mu^2 + \rho^2 - 2 \eta (2 \lambda \mu 1 + \mu \rho)) + \\
& \delta (3 \eta^3 \mu^3 - 3 \rho^3 + \eta \rho (26 \lambda \mu 1 + 9 \mu \rho) - \eta^2 \mu (28 \lambda \mu 1 + 9 \mu \rho))) + 2 \beta \theta \eta^2
\end{aligned}$$

$$\begin{aligned}
& \left( 32 \delta^4 + 6 \eta^4 \mu^4 + 4 \delta^3 (\eta \mu - 19 \rho) + 6 \rho^4 - 8 \eta \rho^2 (2 \lambda \mu 1 + 3 \mu \rho) - 4 \eta^3 \mu^2 (7 \lambda \mu 1 + 6 \mu \rho) - \right. \\
& \quad \delta^2 (31 \eta^2 \mu^2 + 24 \eta \lambda \mu 1 + 95 \eta \mu \rho - 62 \rho^2) + 4 \eta^2 (7 \lambda^2 \mu 1^2 + 11 \lambda \mu \mu 1 \rho + 9 \mu^2 \rho^2) + \\
& \quad \left. 4 \delta (10 \eta^3 \mu^3 - 6 \rho^3 + 22 \eta \rho (\lambda \mu 1 + \mu \rho) - \eta^2 \mu (19 \lambda \mu 1 + 26 \mu \rho)) \right) + \\
& \beta \theta^2 \eta (16 \delta^4 + \delta^3 (43 \eta \mu - 52 \rho) - \delta^2 (61 \eta^2 \mu^2 - 60 \rho^2 + 8 \eta (5 \lambda \mu 1 + 19 \mu \rho)) + \\
& \quad \delta (72 \eta^3 \mu^3 - 28 \rho^3 + \eta \rho (80 \lambda \mu 1 + 153 \mu \rho) - \eta^2 \mu (42 \lambda \mu 1 + 197 \mu \rho)) + \\
& \quad 4 (8 \eta^4 \mu^4 + \rho^4 - \eta \rho^2 (6 \lambda \mu 1 + 11 \mu \rho) - \eta^3 \mu^2 \\
& \quad (17 \lambda \mu 1 + 25 \mu \rho) + \eta^2 (7 \lambda^2 \mu 1^2 + 21 \lambda \mu \mu 1 \rho + 27 \mu^2 \rho^2)) \Big) ;
\end{aligned}$$