

Reminders

- Questions about the assignments? Please post on the EdStem!
 - Clarification questions are helpful for everyone:)
 - If it's specific to your submission, you can post to instructors-only
- HW 1 is due on Wednesday
- HW 2 is out today, due next week Wednesday

Lecture Outline

- Table Review
 - Manipulating Tables
 - Operating on Tables
 - Functions
- Line Plots and Scatter Plots
- Bar Charts and Histograms

Table Review

Prof Lee's Cat Census

Professor Lee is in a cat picture group chat. She has collected data on the cats shared in this chat:

Name	Age	Weight	Coloring	Sex	Owner
Ruby	14	8	tuxedo	F	Alice
Gertrude	15	12	tuxedo	F	Alice
Hamby	8	16	tabby	М	Bob
Fig	3	7	tabby	F	Bob
Corina	6	10	tortie	F	Carol
Frito	2	8.5	tabby	М	Carol

Manipulating Tables

Keep or remove by columns:

```
- tbl.select(c1 ,c2, ...)
```

```
- tbl.drop(c1, c2, ...)
```

Keep or remove by row:

```
- tbl.where(c, predicate)
```

```
- tbl.take(row_indices)
```

Reorder table entries:

```
- tbl.sort(c[, descending=False])
```

Operating on Tables

Organize table entries by values in column c:

```
- tbl.group(c)
```

```
- tbl.group(c, func)
```

Apply a function func to all entries in a column c:

```
- tbl.apply(func, c)
```

Anatomy of a Function

Name, Parameters, Body, Return Statement

Example:

```
def convert_to_figs(weight):
   new_weight = (weight/fig_weight).round(1)
   return new weight
```

Anatomy of a Function

```
Name, Parameters, Body, Return Statement
Example:
def convert to figs (weight):
  new weight = (weight/fig weight).round(1)
 return new weight <
```

apply

Use apply to call a function on each element in a column

```
def convert_to_figs(weight):
    new_weight = (weight/fig_weight).round(1)
    return new_weight

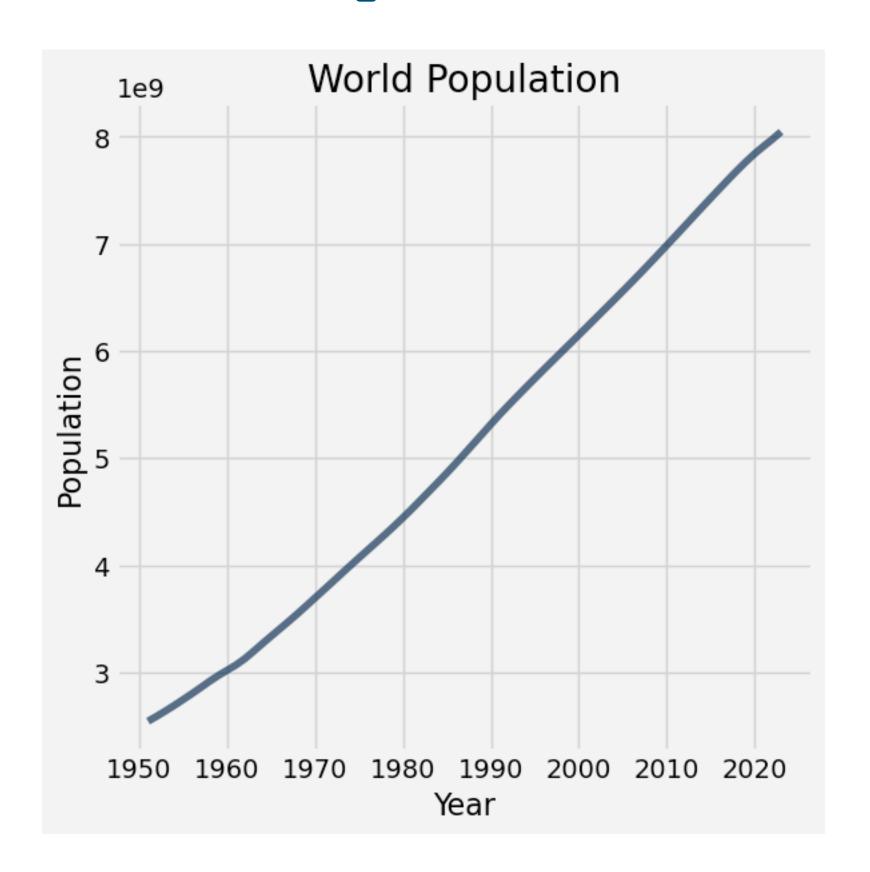
cat_tbl.apply(convert_to_figs, 'Weight')

    Returns an array with convert_to_figs called on each element in the 'Weight' column'
```

Plotting Relations Between Numerical Values

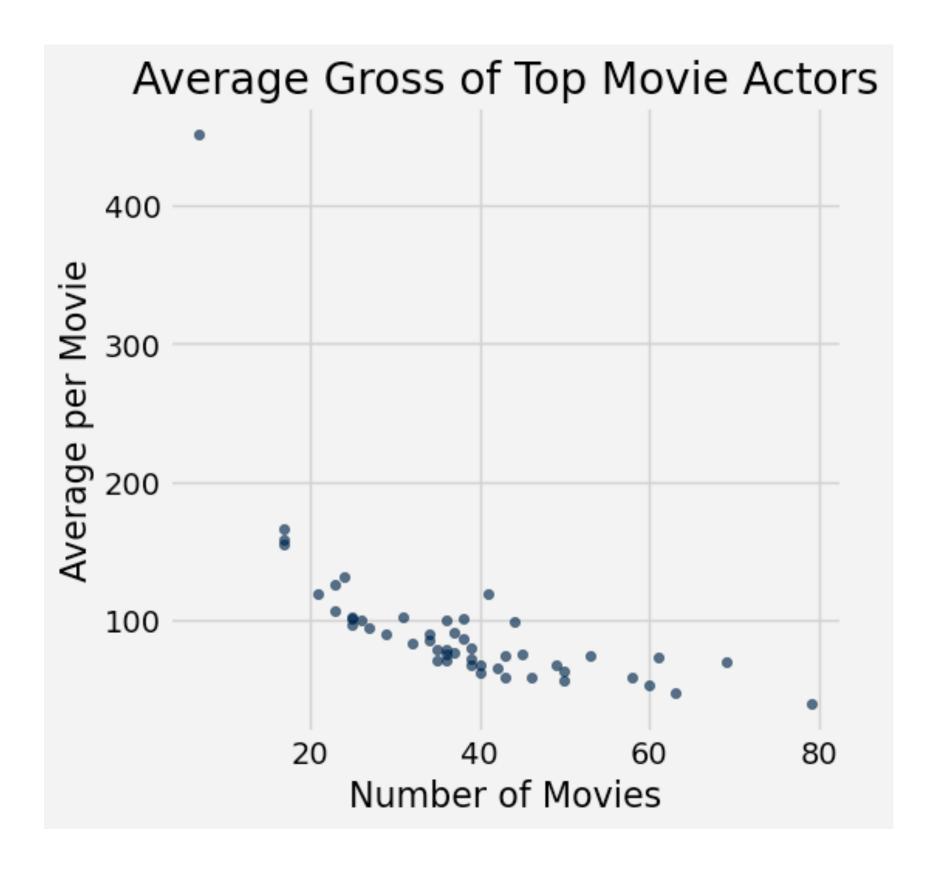
Line and Scatter Plots

Line Plot
plot



Scatter Plot

scatter



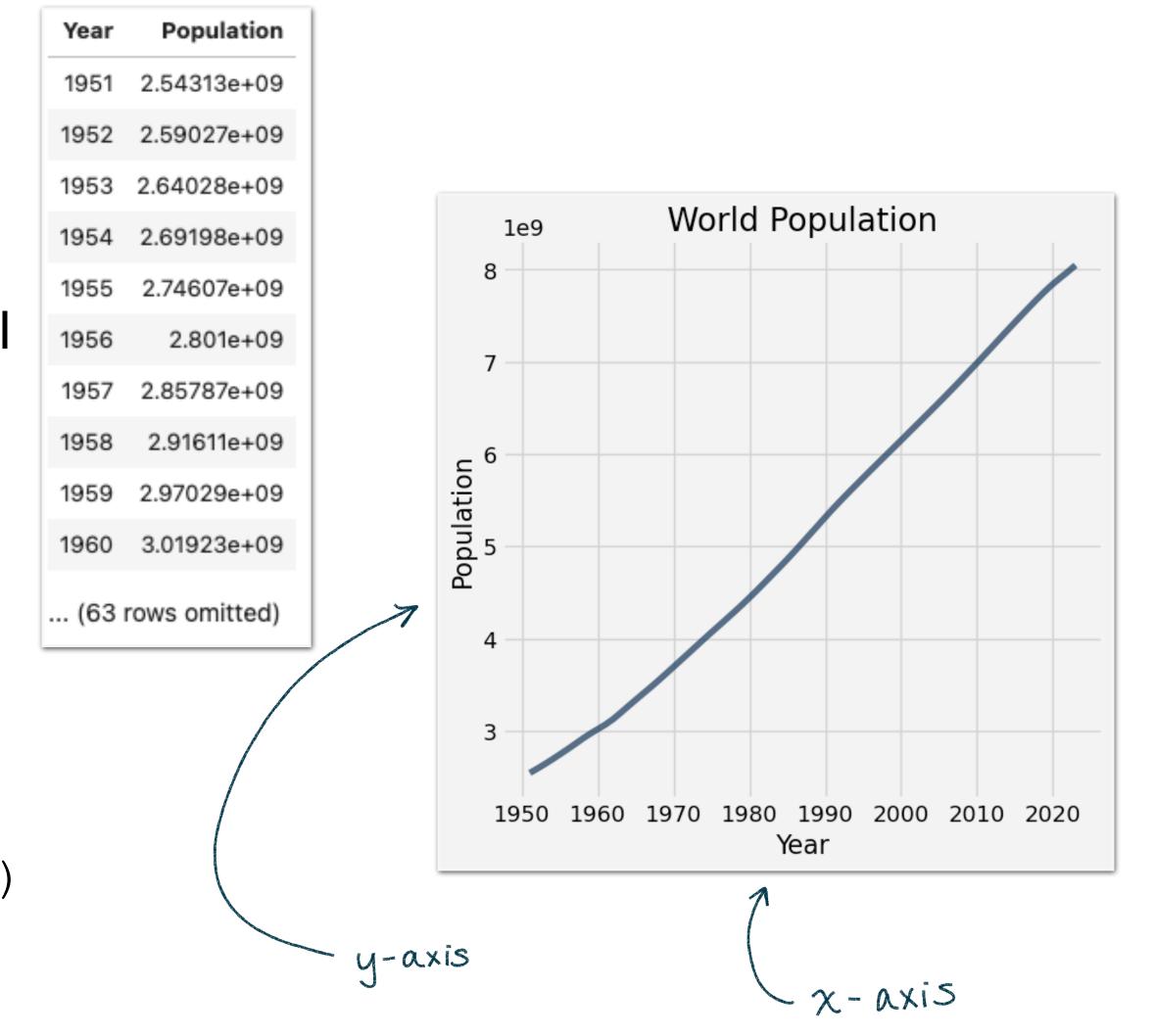
Line Plots

Line plots: good for sequential data if

- x-axis has an order (e.g., time, years, distance)
- sequential differences in y value are meaningful
- there's only one y-value for each x-value

```
tbl.plot(x_axis, y_axis)
```

- pop_data.plot('Year', 'Population')

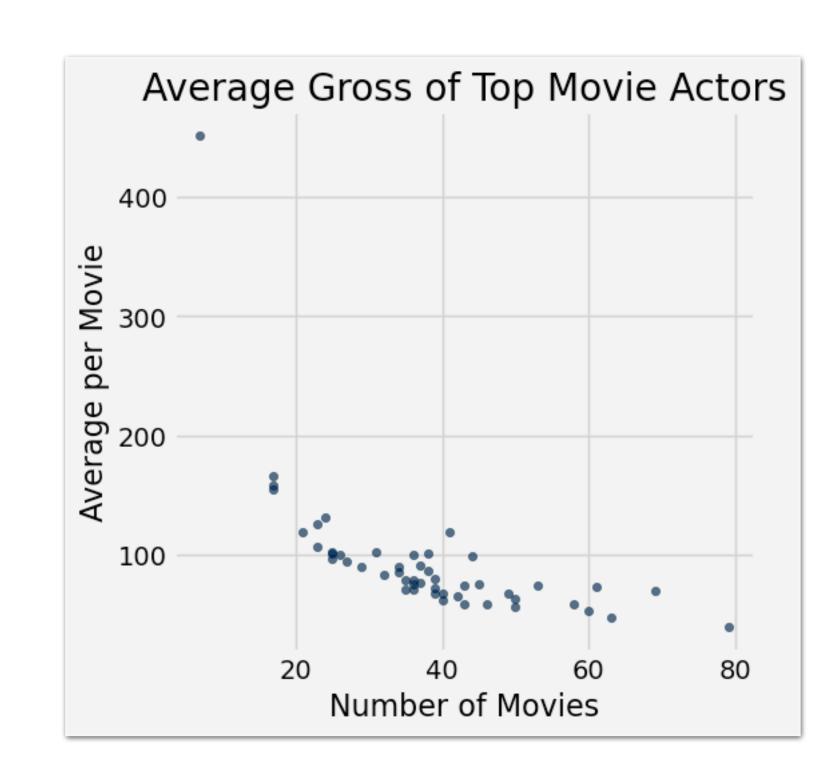


Scatter Plots

Scatter plots: good for non-sequential quantitative data

- Great for looking for associations

Gross N 4871.7 4772.8 4468.3	lumber of Movies 41 69	Average per Movie 118.8 69.2		Gross 936.7
4772.8				936.7
	69	69.2		
4468.3			The Avengers	623.4
	61	73.3	The Dark Knight	534.9
4340.8	44	98.7	Toy Story 3	415
3947.3	53	74.5	The Avengers	623.4
3810.4	38	100.3	Shrek 2	441.2
3587.2	36	99.6	War of the Worlds	234.3
3368.6	45	74.9	Dead Man's Chest	423.3
3351.5	58	57.8	The Dark Knight	534.9
3341.2	37	90.3	The Avengers	623.4
	3947.3 3810.4 3587.2 3368.6 3351.5	3947.3 53 3810.4 38 3587.2 36 3368.6 45 3351.5 58	3947.3 53 74.5 3810.4 38 100.3 3587.2 36 99.6 3368.6 45 74.9 3351.5 58 57.8	3947.3 53 74.5 The Avengers 3810.4 38 100.3 Shrek 2 3587.2 36 99.6 War of the Worlds 3368.6 45 74.9 Dead Man's Chest 58 57.8 The Dark Knight



tbl.scatter(x axis, y axis)

- actor.scatter('Number of Movies', 'Average per Movie')

Plot Notebook Demo

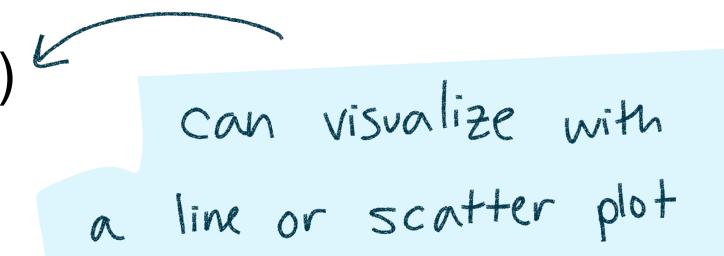
Visualizing Categorical Data

Recall: Types of Attributes

- Attributes are the names of columns in tables
- All values in a column should be the same type and comparable to each other
 - Numerical Values are on a numerical scale (e.g., years)
 - Values are *ordered*
 - Differences are meaningful
 - Categorical Each value is from a fixed inventory (e.g., material)
 - May not have an ordering
 - Categories are either the same or different

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Is this a numerical or categorical attribute?

Track and field: The distance a shotput is thrown (in feet)

[77, 54, 63, 70]

Is this a numerical or categorical attribute?

Gymnastics: Events that gymnasts can perform in

['floor exercise', 'pommel horse', 'rings', 'parallel bars']

Is this a numerical or categorical attribute?

Swimming: Race distances (in meters)

[50, 100, 200, 400, 800]

Terminology

- Individuals are rows in a column (instances of data)
- Categorical Variable are attributes (columns)
 - Each individual has exactly one value
 - Has a distribution
 - For each different value of a variable, there is a frequency of individuals that have that value

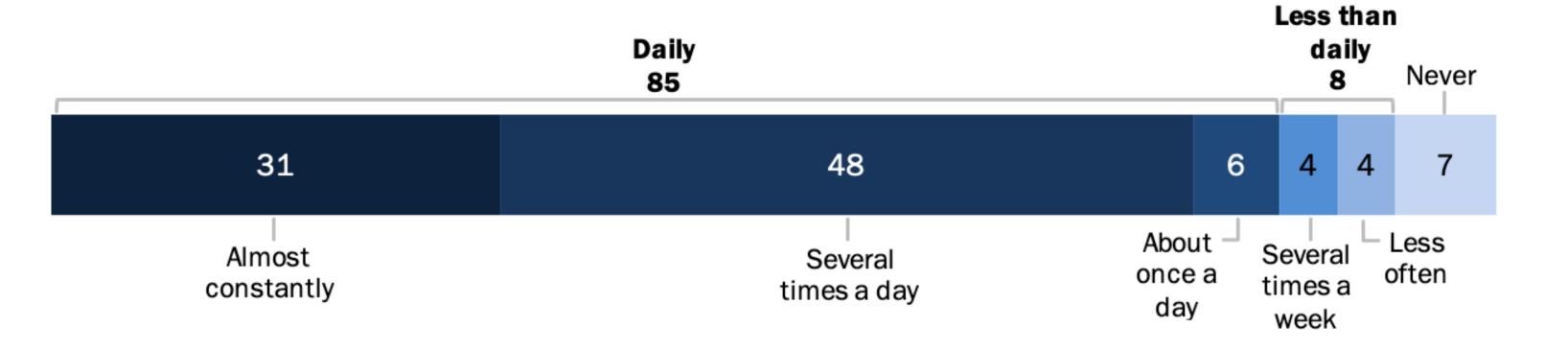
Distribution

Each individual has exactly one category

- Percents add to 100

More than eight-in-ten U.S. adults go online at least daily

% of U.S. adults who say they go online ...



Note: Respondents who did not give an answer are not shown. Source: Survey of U.S. adults conducted Jan. 25-Feb. 8, 2021.

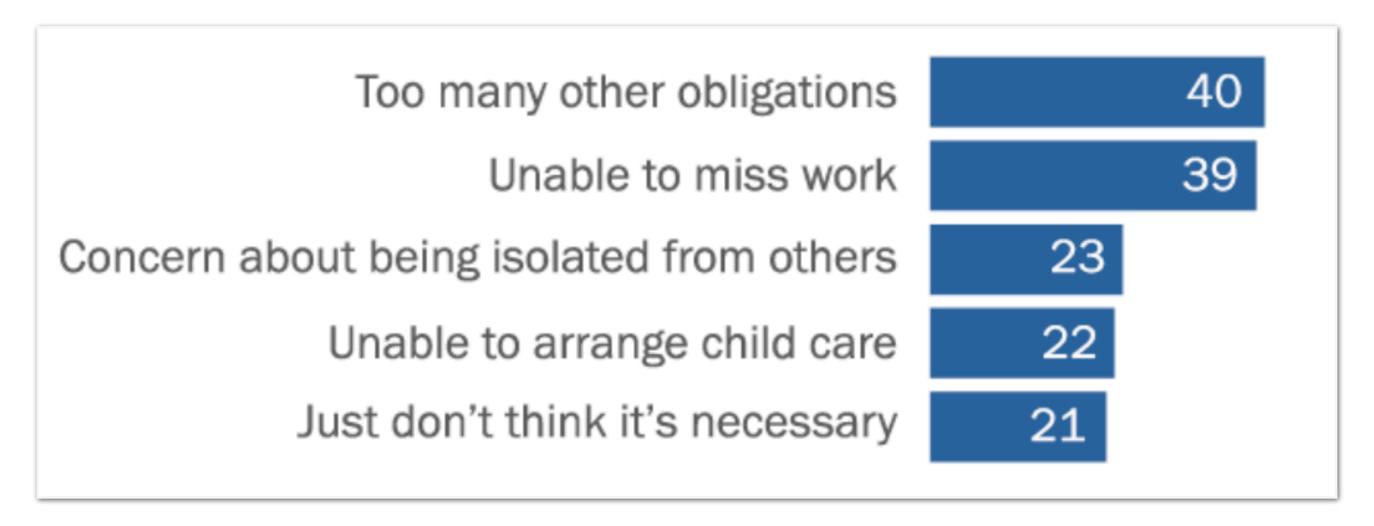
PEW RESEARCH CENTER

Not a distribution

When individuals can pick more than one answer

- Percents don't necessarily add up to 100

Survey question: "A major reason you would find it difficult to quarantine for 14 days"



Source: Pew Research

Bar Chart: Categorical Distributions

Bar charts: display categorical variables and frequencies

- One bar for each category
- Ordering of the bar can be specified (e.g. .sort)
- Length of bar is either count or % of individuals in that particular category

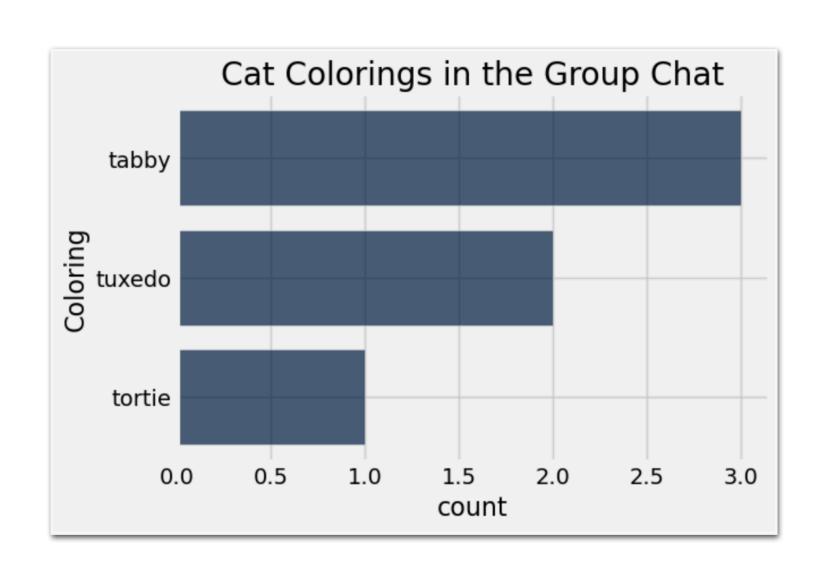
```
Coloring count

tabby 3

tuxedo 2

tortie 1
```

```
tbl.barh(category_label, freq_label)
- cat_tbl.barh('Coloring', 'count')
- cat_tbl.barh('Coloring')
```



Categorical Bar Chart Demo

Creating Histograms for Numerical Distributions

Visualizing Numerical Distributions

Let's say we have a data set containing grades students scored on an exam:

```
array([ 56, 83, 99, 87, 90, 73, 82, 88, 88, 90, 72, 77, 75, 85, 83, 88, 75, 93, 94, 86, 85, 87, 78, 63, 97, 96, 87, 66, 90, 91, 81, 81, 85, 70, 58, 77, 92, 66, 85, 93, 79, 85, 79, 90, 98, 75, 83, 76, 86, 82, 90, 67, 72, 90, 85, 91, 69, 94, 92, 99, 92, 92, 80, 72, 82, 91, 96, 90, 100, 90, 84, 80, 64, 71, 99, 92])
```

What if we want to know generally how students on the exam?

- Useful to sort these into groups (bins)
- Compare the size of these bins

Grouping Numerical Values into Bins

Binning is counting the number of numerical values that lie within a range (which is called bins)

- Bins are defined by their lower bounds (inclusive)
- The upper bound is the lower bound for the next bin)
 - Example: [10, 20)

[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

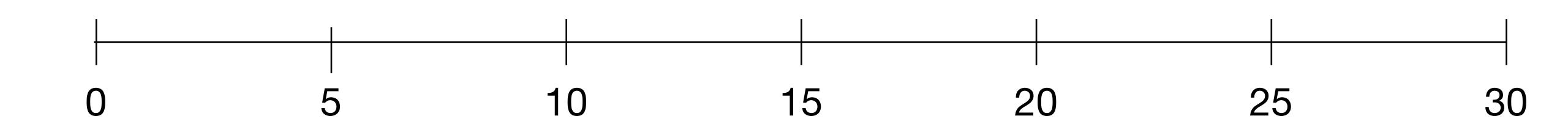
30

[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

Let's say we decide to use a bin size of 5

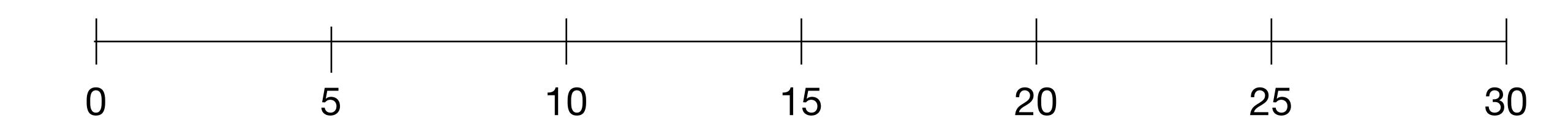
[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

Let's say we decide to use a bin size of 5



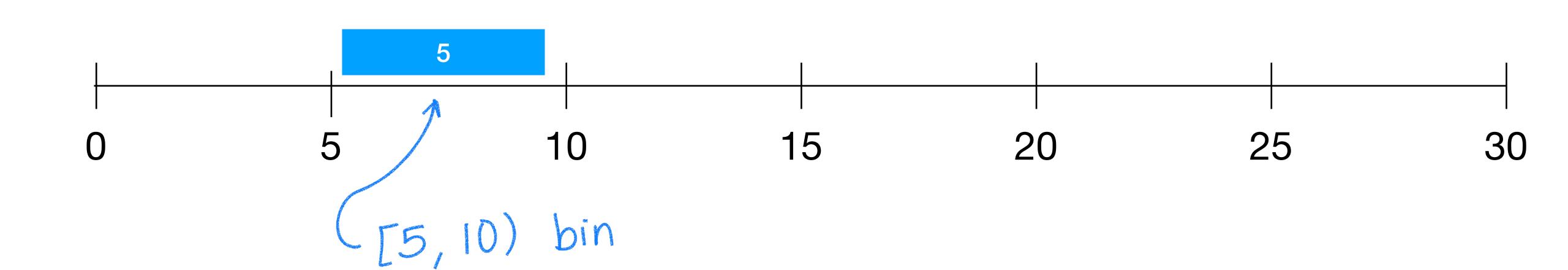
[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

What bin would 5 fall into?



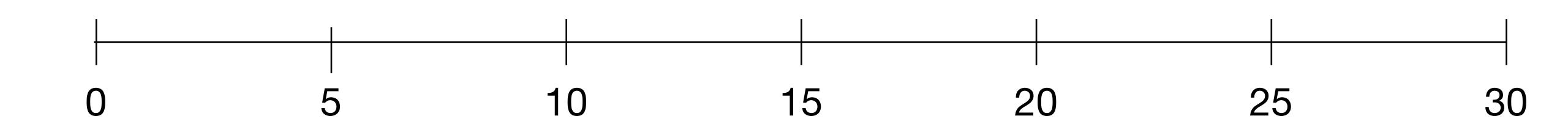
[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

What bin would 5 fall into?



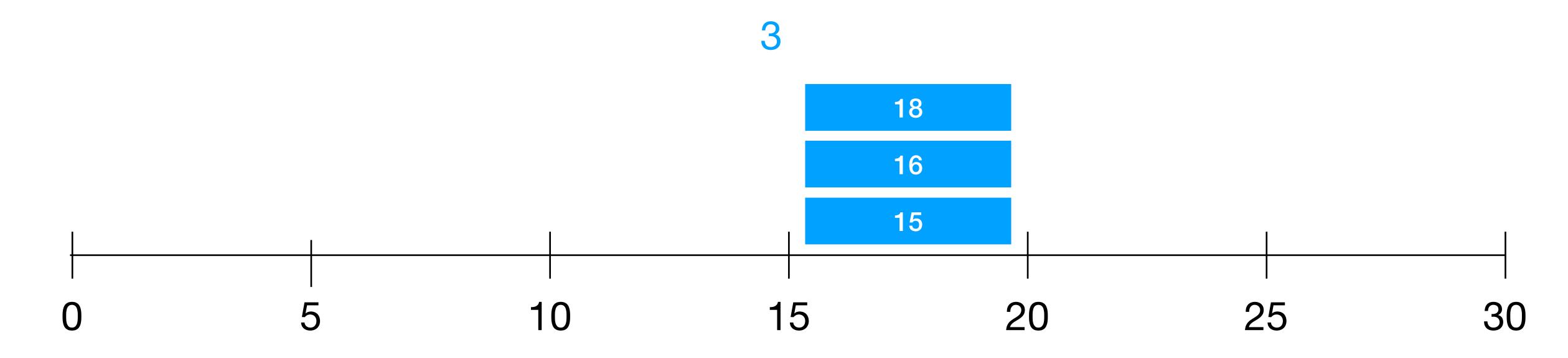
[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

How many individuals fall into bin 15-20?



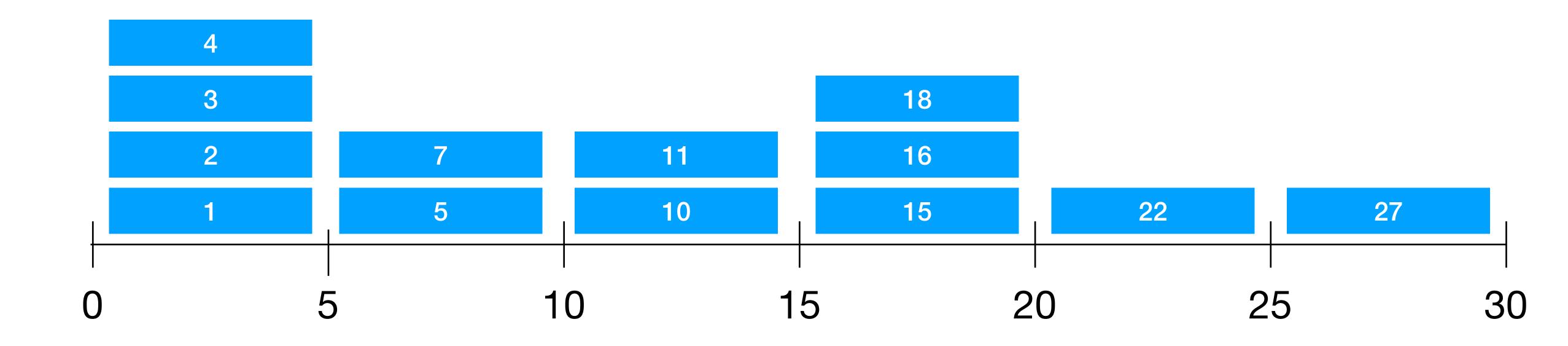
[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]

How many individuals fall into bin 15-20?



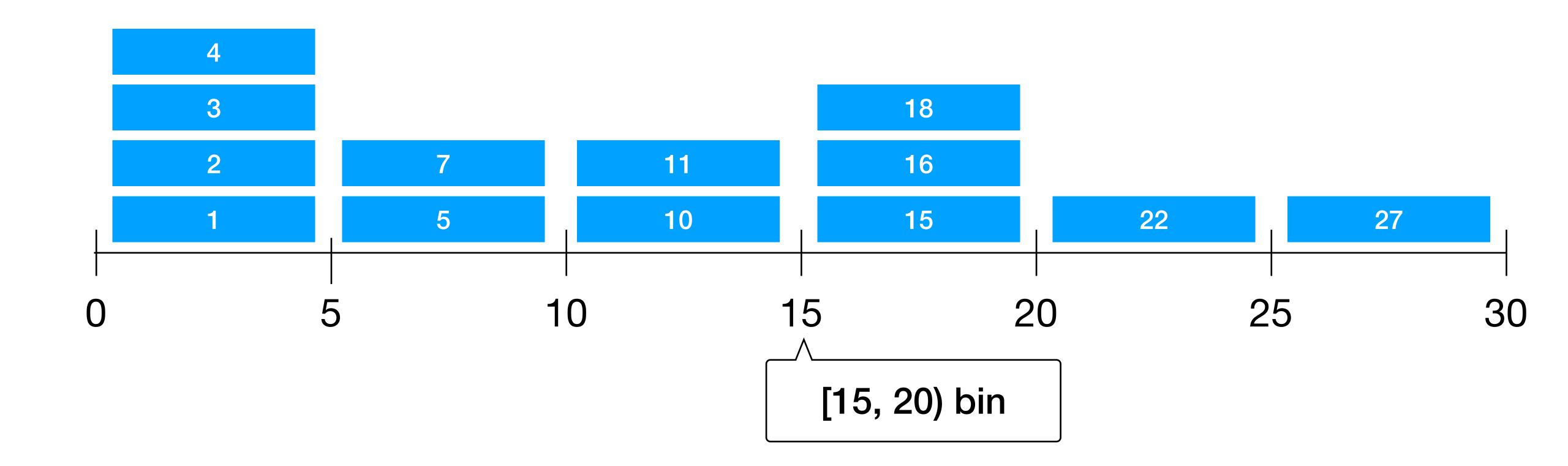
Binning: Example

[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]



Binning: Example

[1, 5, 7, 3, 2, 11, 18, 16, 15, 10, 22, 27, 4]



Choosing Bin Size

Let's go back to our data from before:

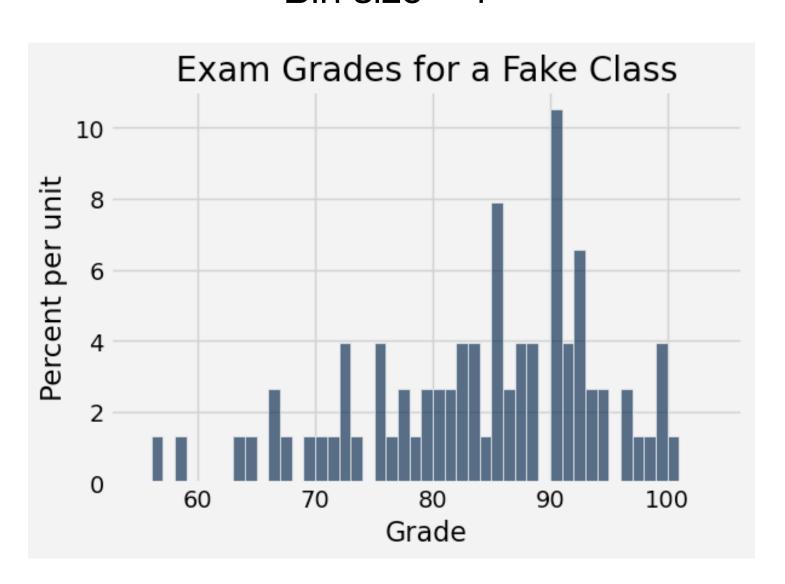
```
array([ 56, 83, 99, 87, 90, 73, 82, 88, 88, 90, 72, 77, 75, 85, 83, 88, 75, 93, 94, 86, 85, 87, 78, 63, 97, 96, 87, 66, 90, 91, 81, 81, 85, 70, 58, 77, 92, 66, 85, 93, 79, 85, 79, 90, 98, 75, 83, 76, 86, 82, 90, 67, 72, 90, 85, 91, 69, 94, 92, 99, 92, 92, 80, 72, 82, 91, 96, 90, 100, 90, 84, 80, 64, 71, 99, 92])
```

Choosing Bin Size

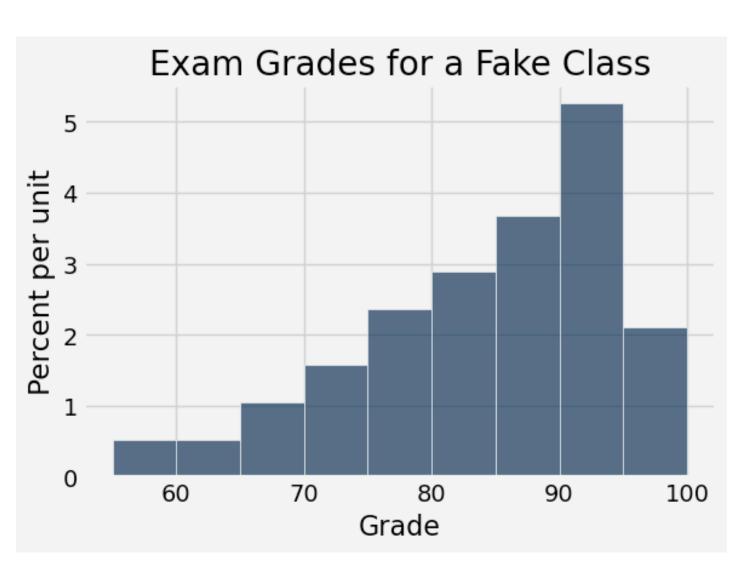
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```
array([ 56, 83, 99, 87, 90, 73, 82, 88, 88, 90, 72, 77, 75, 85, 83, 88, 75, 93, 94, 86, 85, 87, 78, 63, 97, 96, 87, 66, 90, 91, 81, 81, 85, 70, 58, 77, 92, 66, 85, 93, 79, 85, 79, 90, 98, 75, 83, 76, 86, 82, 90, 67, 72, 90, 85, 91, 69, 94, 92, 99, 92, 92, 80, 72, 82, 91, 96, 90, 100, 90, 84, 80, 64, 71, 99, 92])
```

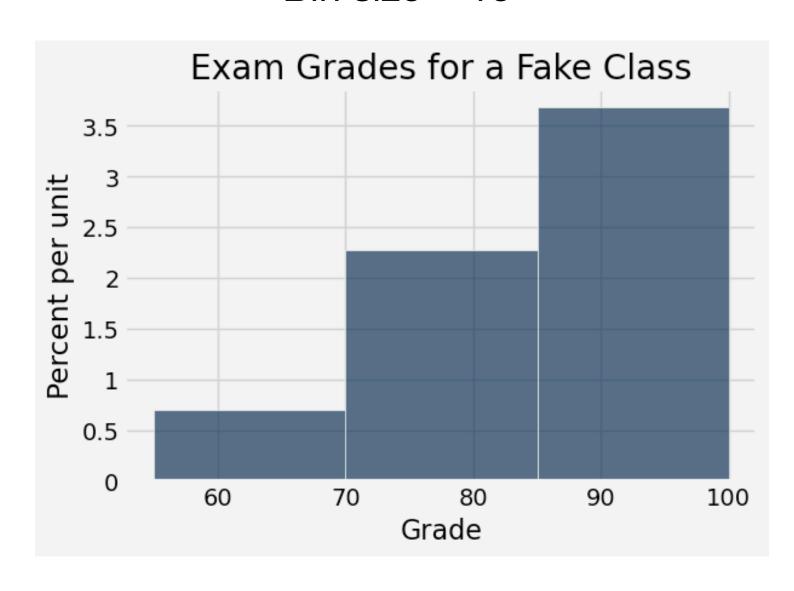
Bin size = 1



Bin size = 5

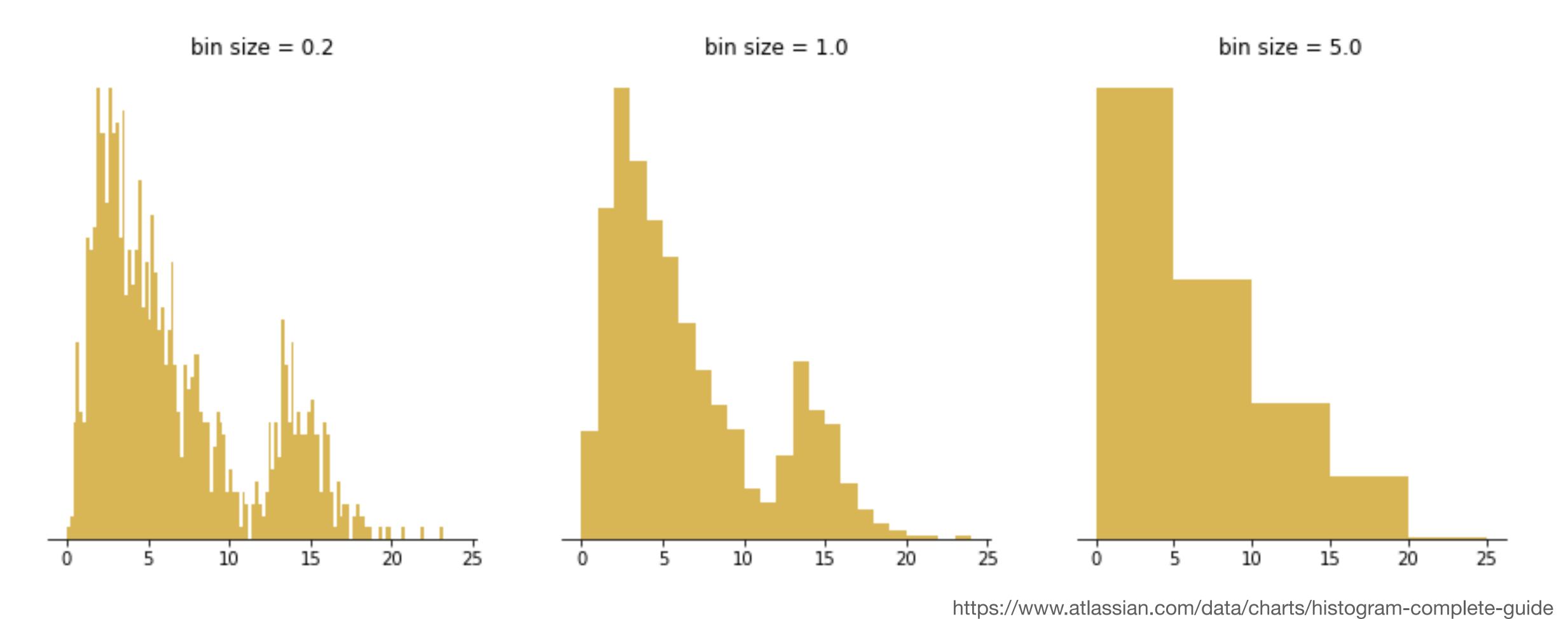


Bin size = 15



Choosing Bin Size

Chose so that it's representative of your data



bin

Group values in column c into 10 equally sized intervals:

- tbl.bin(c)

Create n equally wide bins:

- tbl.bin(c, bins=n)

Create bins of size step from start to end:

- tbl.bin(c, bins=np.arange(start, end, step))

hist

Create a histogram of numerical values in column c with 10 equal bins:

```
- tbl.hist(c)
```

Create a histogram with u as the x-axis:

```
- tbl.hist(c, unit=u)
```

Create a histogram with specified bins:

```
- tbl.hist(c, bins=np.arange(start, end, step))
```

Create a histogram with x-axis u and specified bins:

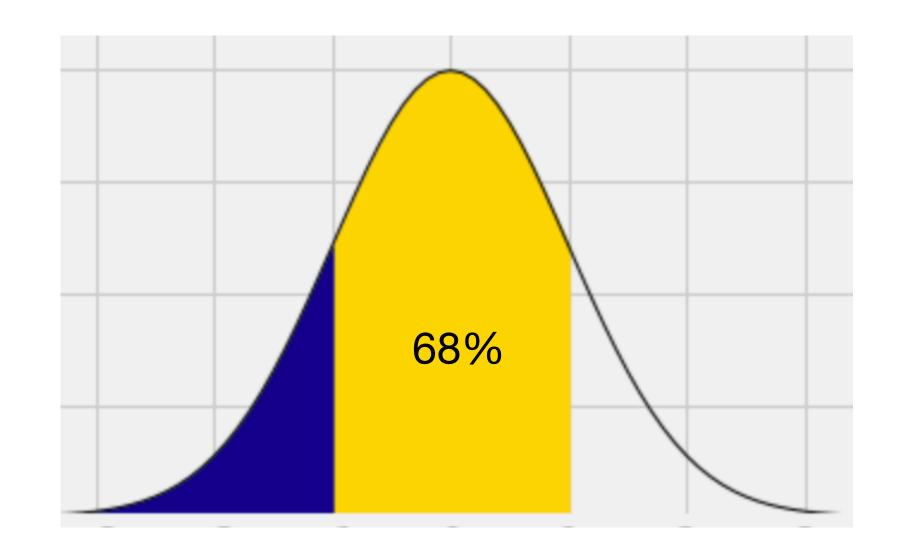
```
- tbl.hist(c, unit=u, bins=np.arange(start, end, step))
```

Histogram Notebook Demo -Bins

Areas should be *proportional* to the values they represent

In a histogram, the area of each bar is the percent of individuals in the corresponding bin

(Later on in the course, we will approximate histograms with smooth curves)

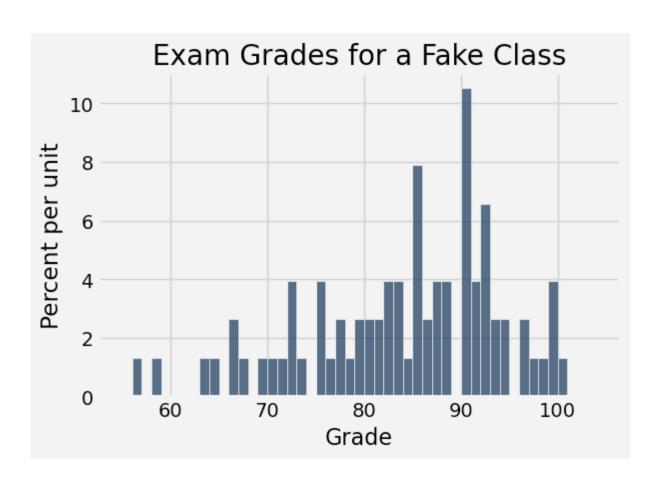


area of bar = percent of entries in bin

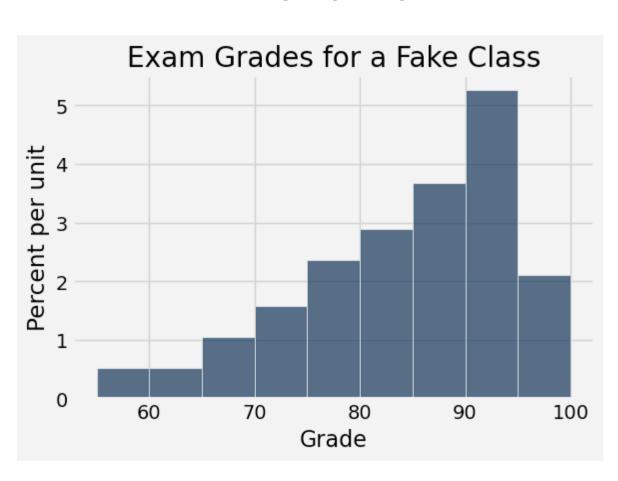
area of bar = (height of bar) \times (width of bin)

height of bar =
$$\frac{\text{area of bar}}{\text{width of bin}} = \frac{\text{percent of entries in bin}}{\text{width of bin}}$$

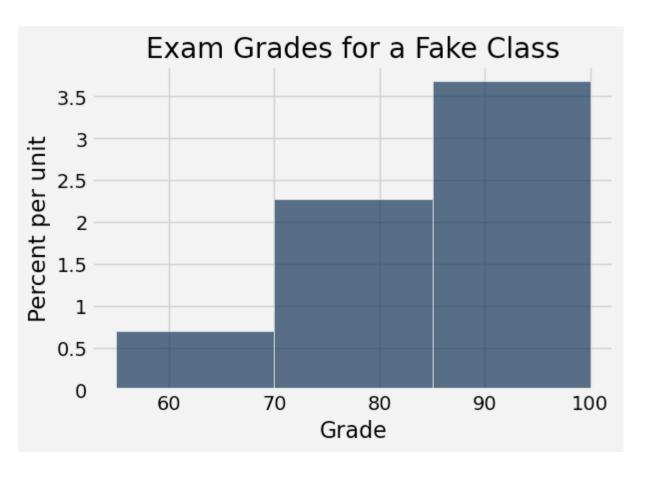
Bin size = 1



Bin size = 5



Bin size = 15

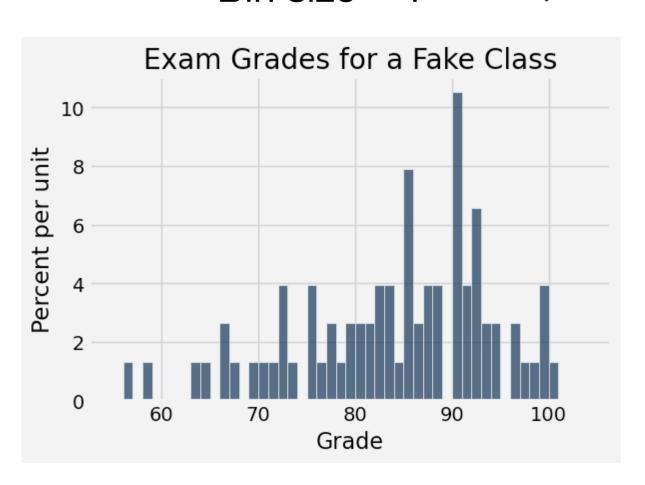


area of bar = percent of entries in bin

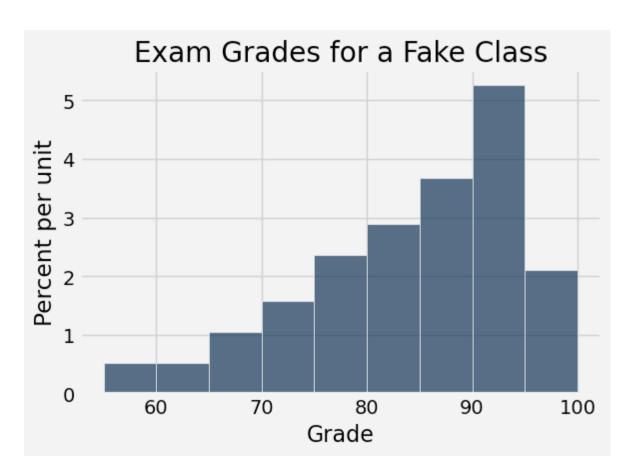
area of bar = (height of bar) \times (width of bin)

height of bar =
$$\frac{\text{area of bar}}{\text{width of bin}} = \frac{\text{percent of entries in bin}}{\text{width of bin}}$$

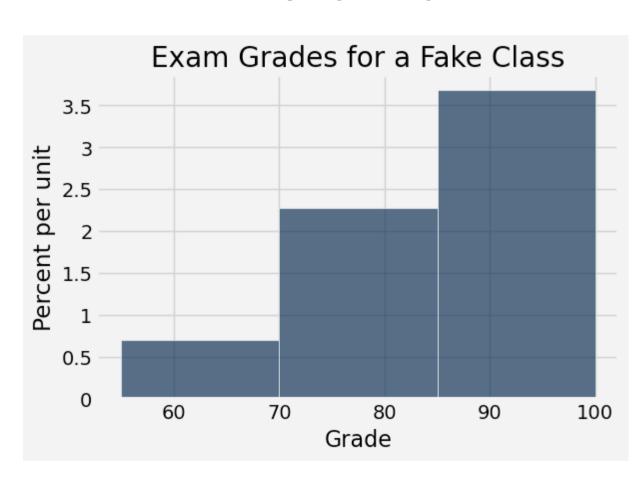
Bin size = 1



Bin size = 5



Bin size = 15



area of bar = percent of entries in bin area of bar = (height of bar) \times (width of bin)

When bin Size is 5:

height = \frac{\%}{5} \text{ entries in bin}

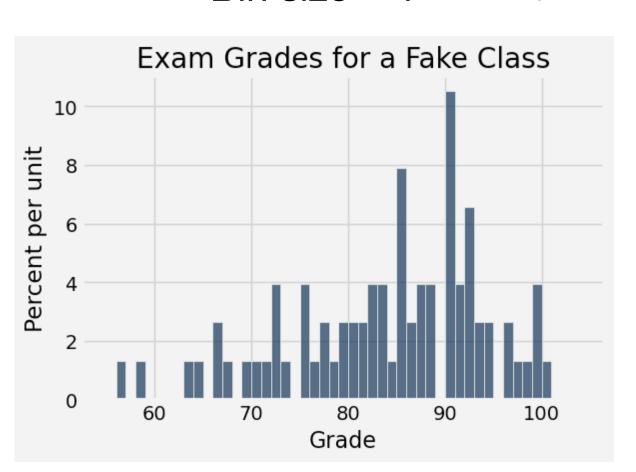
height of bar =
$$\frac{\text{area of bar}}{\text{width of bin}} = \frac{\text{percent of entries in bin}}{\text{width of bin}}$$

When bin Size is 15:

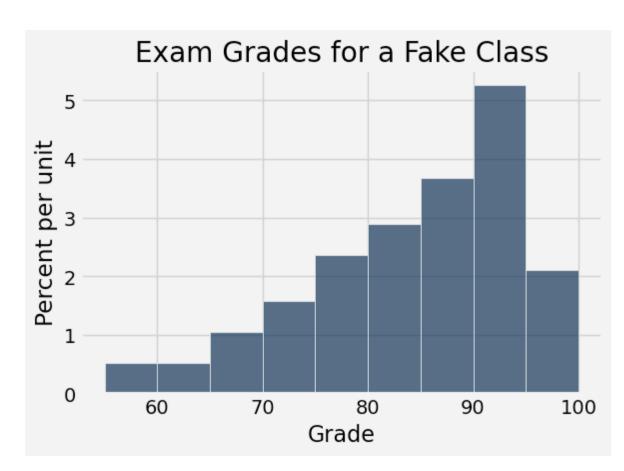
height = % entries in bin

15

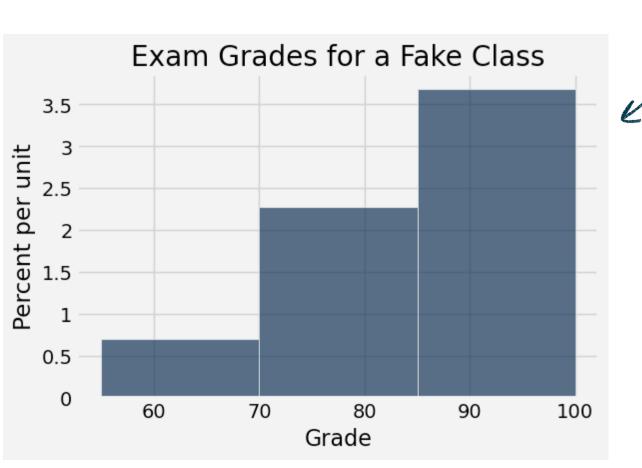
Bin size
$$= 1$$

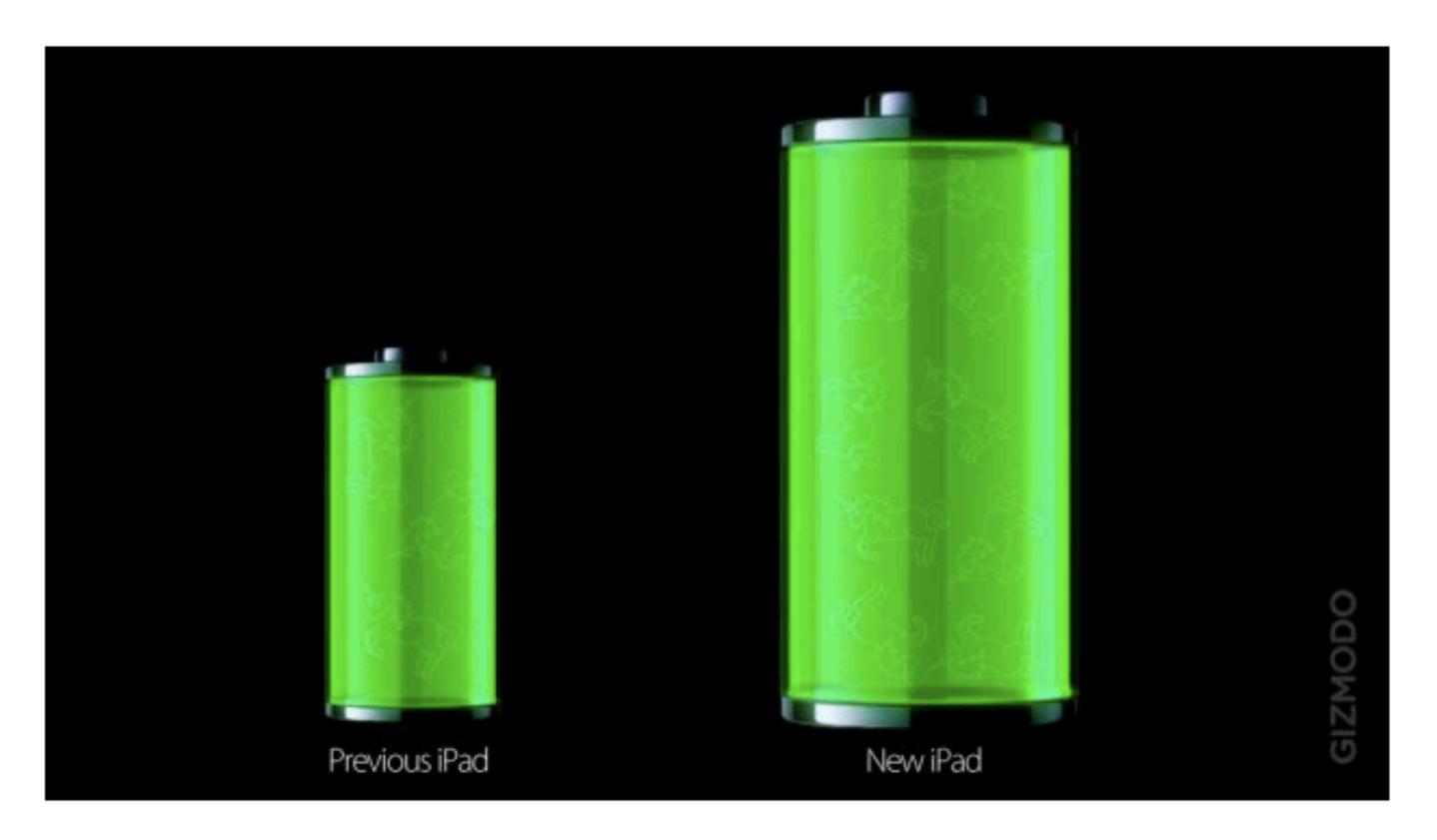


Bin size = 5

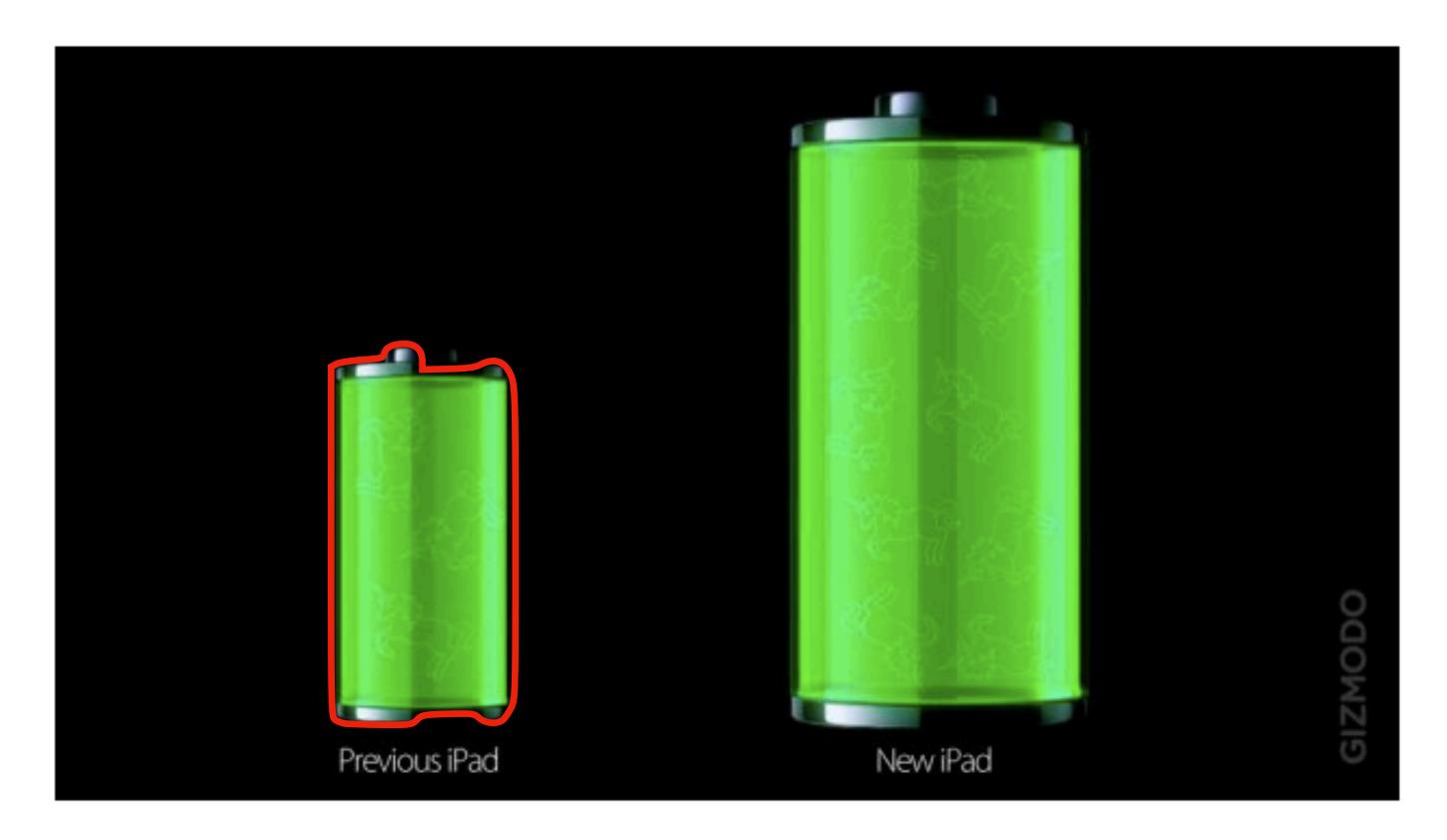


Bin size = 15

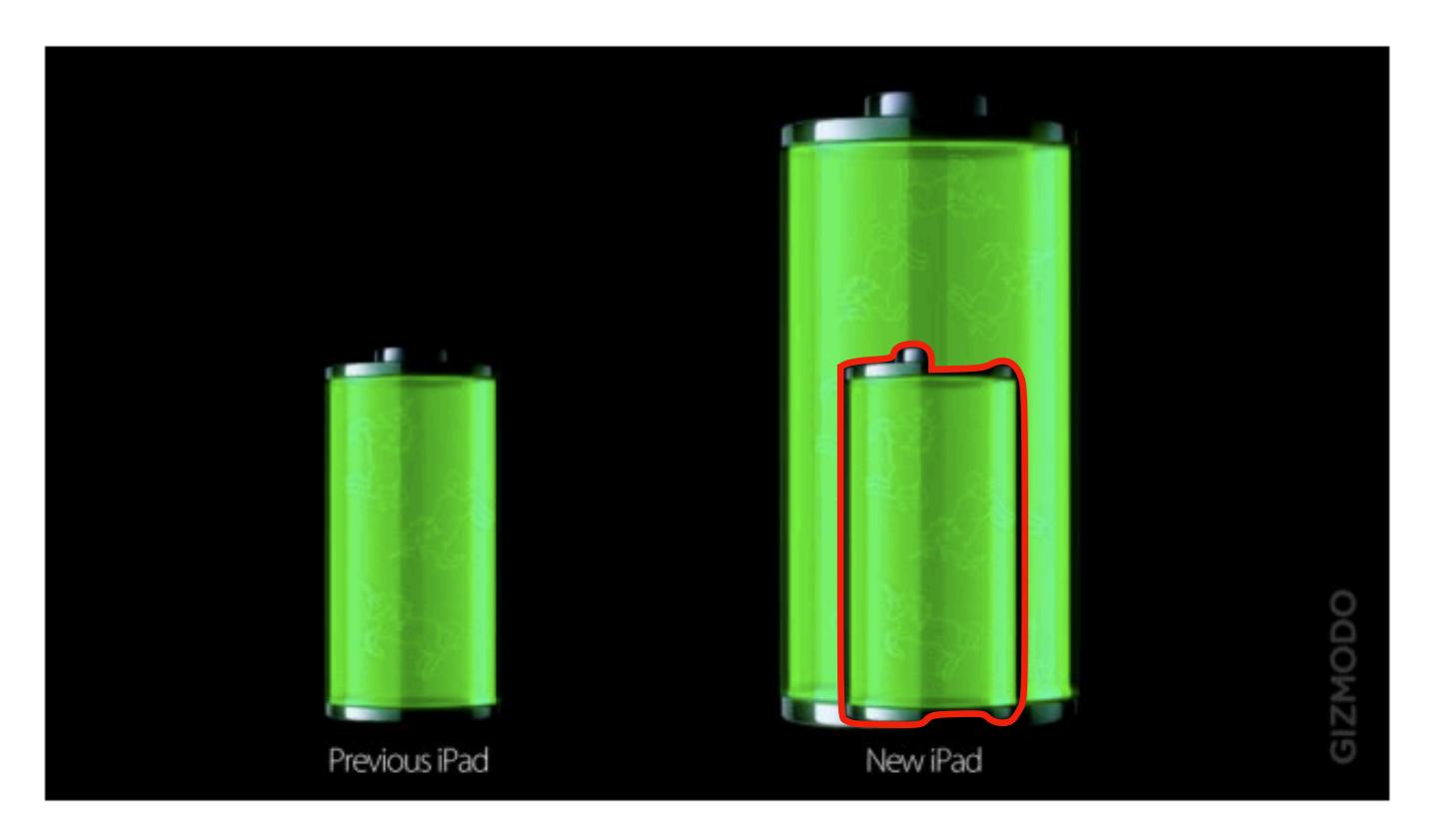




From <u>Gizmodo</u>, this shows battery size in the new iPad versus that of the iPad 2. The battery in the former is 70 percent bigger than that of the latter. Something's not right here.



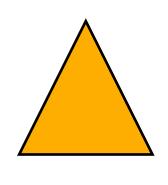
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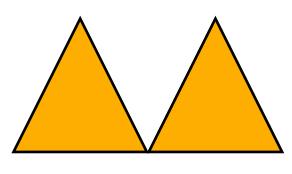


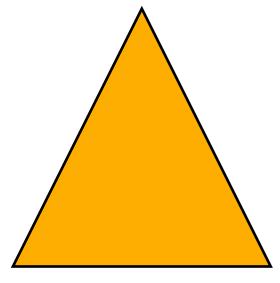
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Areas should be proportional to the values they represent

- For example
 - If you represent 20% of a population by:
 - Then 40% can be represented by:
 - But not by:

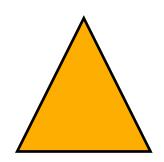


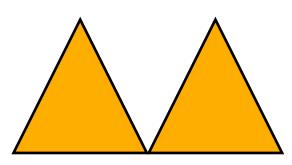


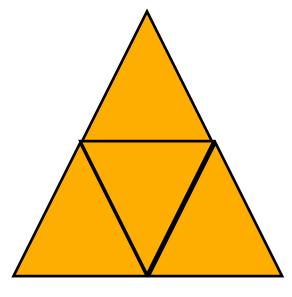


Areas should be proportional to the values they represent

- For example
 - If you represent 20% of a population by:
 - Then 40% can be represented by:
 - But not by:





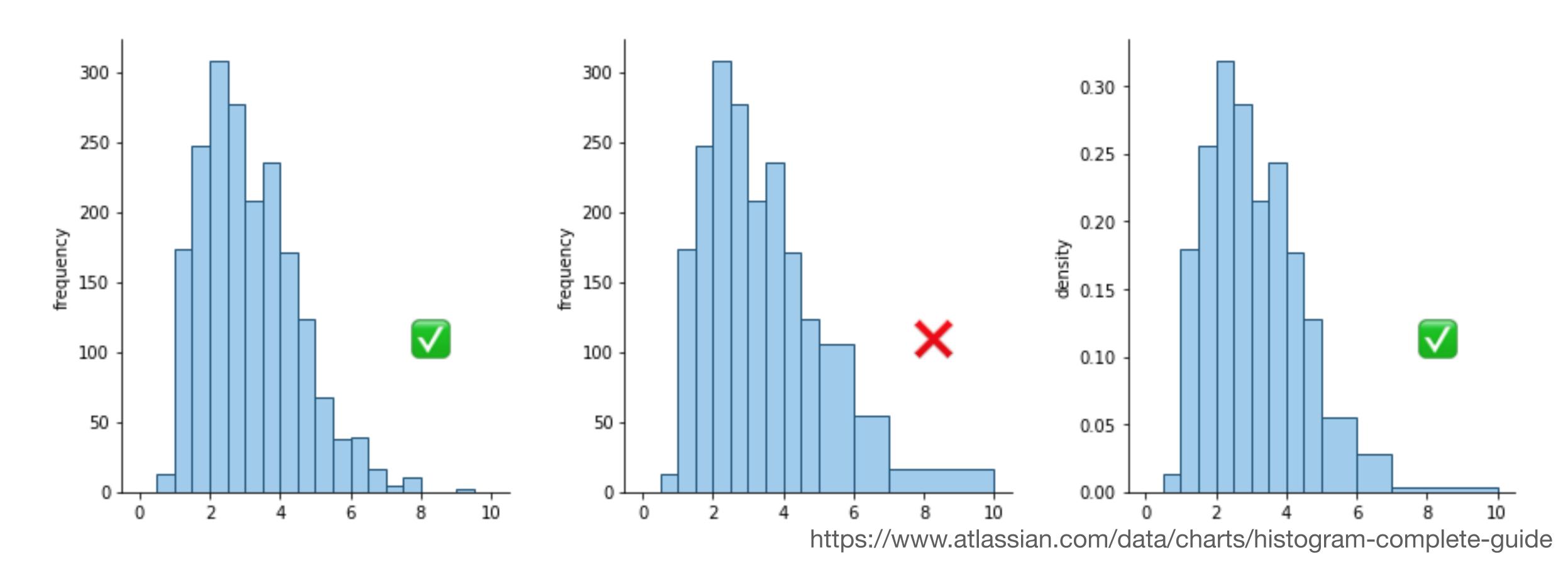


Unequal Bin Sizes

Bin sizes don't need to be equal

- unequal bin size is often used for better representing tails

For unequal bin sizes - vertical axis now represents density rather than frequency

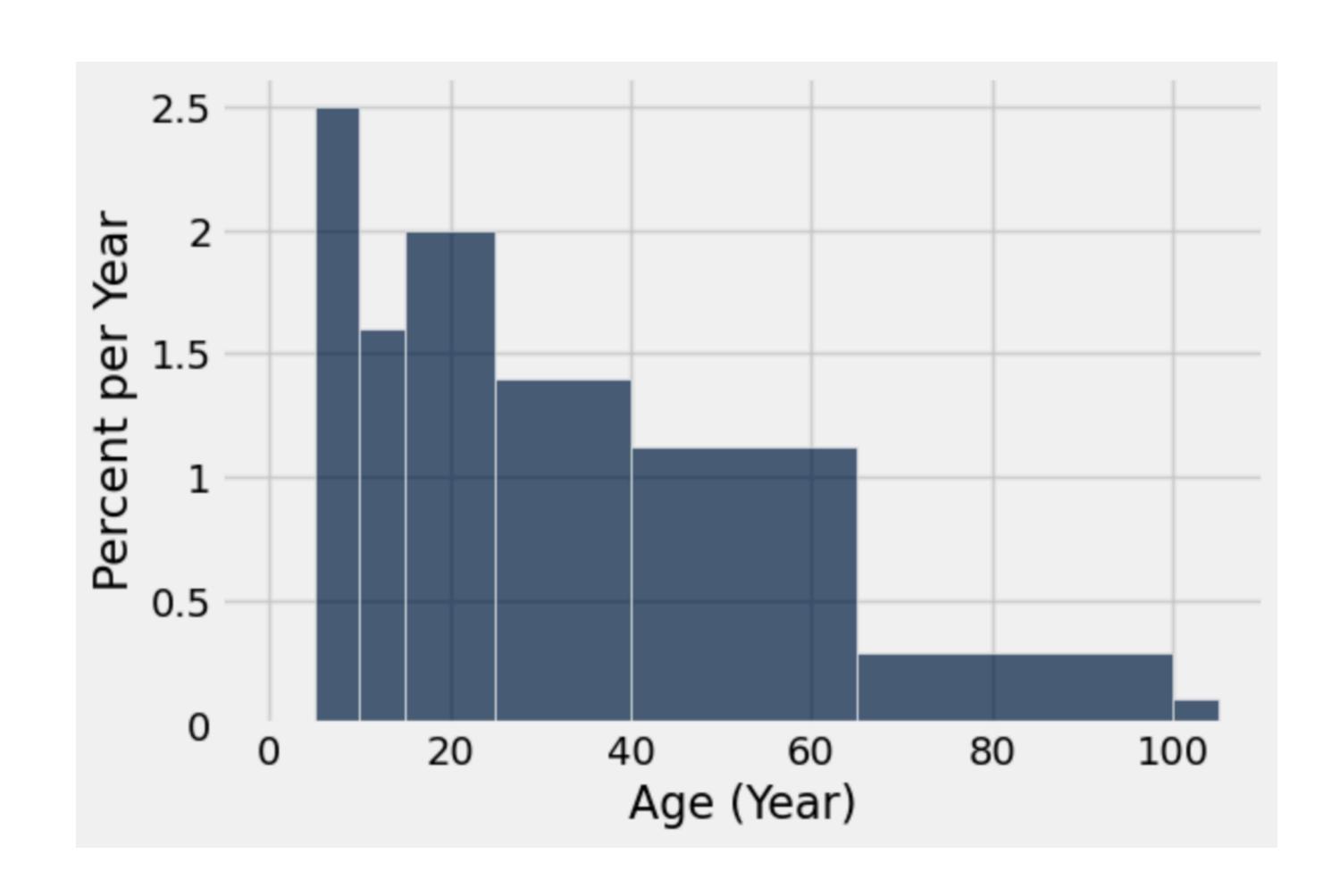


Histograms

The area of each bar is a percentage of the whole

The horizontal axis is a numerical distribution - the bins don't need to be of equal size

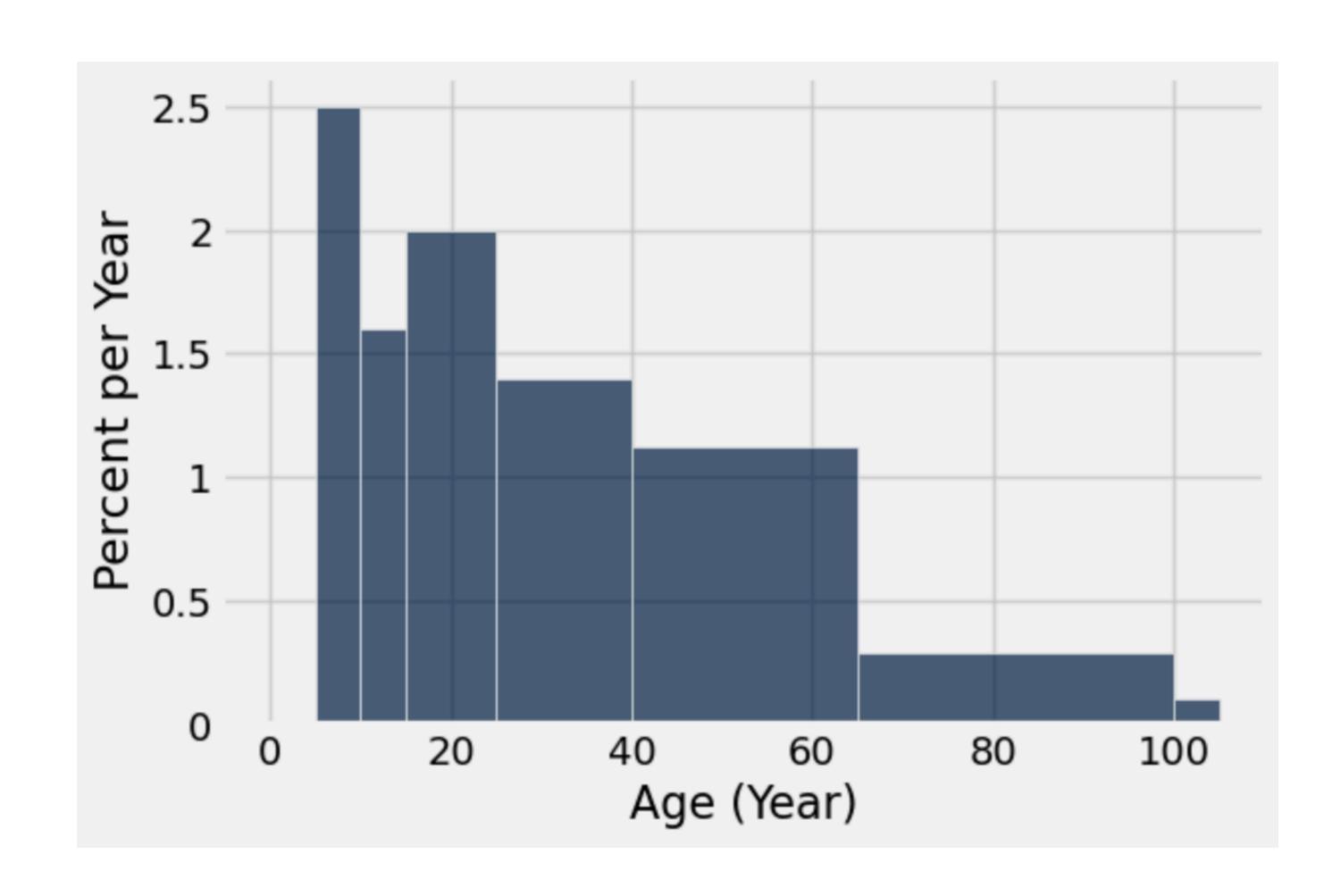
The vertical axis is a rate (e.g., percent/year) - density



Calculating Heights

The [40, 65) bin contains 56/200 items

- The bin is 28% (56/200) of the whole
- The bin width is 65-40 = 25 years



Area Notebook Demo

Bar Chart vs Histogram

Bar Chart

- Distribution of categorical variable
- Length of bars is proportional to the frequency / percent of individuals

Histogram

- Distribution of numerical variable
- Horizontal axis is numerical, bins can be unequal
- Area of bars is proportional of percent of individuals, height measures density

Next Class

- More charts