# MIS 64018: Assignment\_4: Transportation / Transshipment problem

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### **Project Objective**

The purpose of this assignment is to formulate and solve a transportation / transshipment problem.

**Problem Formulation:** Since we are required to find a solution that minimizes the combined cost of production and shipment, this is obviously a minimization problem. In addition, we can see that Plants A and B have a combined production capacity (i.e. supply) of 220. Whereas, the warehouses have a combined demand of 210. This makes for an unbalanced problem which requires introducing a dummy warehouse. The formulation below puts that into consideration.

Plant	W1	W2	W3	W4*	Output
Plant A	22	14	30	M(0)	100
Plant B	16	20	24	M(0)	120
<del></del>	_	_	_	—-	
Demand	80	60	70	10	

### Objective function:

Min:  $Z = 622 \times 11 + 614 \times 12 + 630 \times 13 + 641 \times 21 + 645 \times 22 + 649 \times 23$  Subject to:

x11 + x12 + x13 + M14 = 100

x21 + x22 + x23 + M24 = 120

x11 + x21 = 80

x12 + x22 = 60

x13 + x23 = 70

M14 + M24 = 10

(x11,x12,x13,x21,x22,x23) >= 0

Solving the problem using lpsolve, or any other equivalent library in R.

Loading the lpSolveAPI library

#### library(lpSolveAPI)

```
/*Objective function*/
Min: 622 x11 + 614 x12 + 630 x13 + 641 x21 + 645 x22 + 649 x23;
/*Constraints*/
```

```
x11 + x12 + x13 + M14 = 100;

x21 + x22 + x23 + M24 = 120;

x11 + x21 = 80;

x12 + x22 = 60;

x13 + x23 = 70;

M14 + M24 = 10;
```

## [1] 0 60 40 80 0 30 0 10

Reading the lp formulation from HS.lp file and assign it to p

```
p <- read.lp("HS.lp")</pre>
p
## Model name:
                                     x21
                                            x22
                                                          M14
                                                                 M24
##
                x11
                       x12
                              x13
                                                   x23
## Minimize
                622
                       614
                              630
                                     641
                                            645
                                                   649
                                                            0
                                                                   0
## R1
                  1
                         1
                                1
                                       0
                                              0
                                                     0
                                                                          100
                  0
                         0
                                0
                                                                          120
## R2
                                       1
                                              1
                                                     1
                                                            0
                                                                   1
## R3
                  1
                         0
                                0
                                       1
                                              0
                                                     0
                                                            0
                                                                   0
                                                                           80
## R4
                  0
                         1
                                0
                                       0
                                              1
                                                     0
                                                            0
                                                                   0
                                                                           60
## R5
                  0
                         0
                                       0
                                              0
                                                     1
                                                            0
                                                                           70
                  0
                         0
                                0
                                       0
                                              0
                                                                           10
## R6
                                                     0
                                                            1
                                                                   1
## Kind
                Std
                      Std
                              Std
                                     Std
                                            Std
                                                   Std
                                                          Std
                                                                 Std
## Type
               Real
                     Real
                            Real
                                    Real
                                           Real
                                                 Real
                                                         Real
                                                                Real
## Upper
                Inf
                       Inf
                              Inf
                                     Inf
                                            Inf
                                                   Inf
                                                          Inf
                                                                 Inf
## Lower
                                       0
                                                            0
                  0
                         0
                                0
                                              0
                                                     0
                                                                   0
```

Question 1: Solve this transportation problem using lpsolve library in r.

```
## [1] 0

# the objective value for this problem is:
get.objective(p)

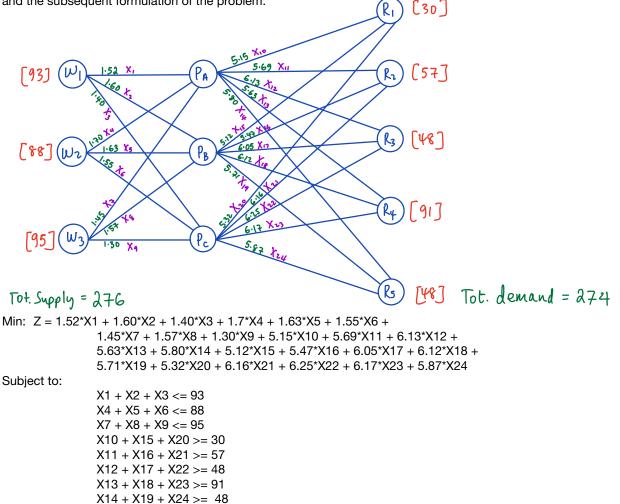
## [1] 132790

# the values of decision variables for the optimal solution are:
get.variables(p)
```

The overall total cost is \$132,790. As for shipments from plants to warehouses, Plant A should ship 60 AEDs to Warehouse2 and 40 AEDs to Warehouse3; Plant B should ship 80 AEDs to Warehouse1 and 30 to Warehouse3.

The last two values for the decision variables are shipments for the dummy Warehouse4.

**Q2.** Oil distribution transshipment problem: In this specific problem we can see that the supply is higher than the total demand, which indicates an unbalanced problem. Below the network diagram related to the problem and the subsequent formulation of the problem:



X1, X2, X3, ..., X27 >= 0Since there is an excess supply than demand (i.e. 276 > 274), we can re-write the constraints by introducing the concept of dummy refinery R6 in order to solve the problem. The constraints are as follows:

```
X1 + X2 + X3 = 93

X4 + X5 + X6 = 88

X7 + X8 + X9 = 95

X10 + X15 + X20 = 30

X11 + X16 + X21 = 57

X12 + X17 + X22 = 48

X13 + X18 + X23 = 91

X14 + X19 + X24 = 48

M16 + M26 + M36 = 2

X1 + X4 + X7 - X10 - X11 - X12 - X13 - X14 - M16 = 0

X2 + X5 + X8 - X15 - X16 - X17 - X18 - X19 - M26 = 0

X3 + X6 + X9 - X20 - X21 - X22 - X23 - X24 - M36 = 0

X1, X2, X3, ..., X27 >= 0
```

X1 + X4 + X7 - X10 - X11 - X12 - X13 - X14 = 0 X2 + X5 + X8 - X15 - X16 - X17 - X18 - X19 = 0 X3 + X6 + X9 - X20 - X21 - X22 - X23 - X24 = 0

In the next page, I have solved this transshipment people in R, using the IpSolveAPI library.

## Part 2: Oil Distribution transshipment problem.

```
/*Objective Function*/
Min: 1.52 X1 + 1.60 X2 + 1.40 X3 + 1.7 X4 + 1.63 X5 + 1.55 X6 + 1.45 X7 + 1.57 X8 + 1.30 X9 +
          5.15 \times 10 + 5.69 \times 11 + 6.13 \times 12 + 5.63 \times 13 + 5.80 \times 14 + 5.12 \times 15 + 5.47 \times 16 + 6.05 \times 17 + 6.12 \times 18 + 5.15 \times 10 + 5.69 \times 11 + 6.12 \times 18 + 5.12 \times 10 + 5.69 \times 11 + 6.12 \times 10 + 5.69 \times 10 + 5.69
          5.71 \times 19 + 5.32 \times 20 + 6.16 \times 21 + 6.25 \times 22 + 6.17 \times 23 + 5.87 \times 24;
/*Constraints*/
X1 + X2 + X3 = 93;
X4 + X5 + X6 = 88;
X7 + X8 + X9 = 95;
X10 + X15 + X20 = 30;
X11 + X16 + X21 = 57;
X12 + X17 + X22 = 48;
X13 + X18 + X23 = 91;
X14 + X19 + X24 = 48;
M16 + M26 + M36 = 2;
X1 + X4 + X7 - X10 - X11 - X12 - X13 - X14 - M16 = 0;
X2 + X5 + X8 - X15 - X16 - X17 - X18 - X19 - M26 = 0;
X3 + X6 + X9 - X20 - X21 - X22 - X23 - X24 - M36 = 0;
Reading the lp formulation from TOD.lp file and assign it to x
x <- read.lp("TOD2.lp")</pre>
## Model name:
```

Question 1: Solve this transportation problem using lpsolve library in r.

a linear program with 27 decision variables and 12 constraints

```
## [1] 0
# the objective value for this problem is:
get.objective(x)

## [1] 1966.68
# the values of decision variables for the optimal solution are:
get.variables(x)

## [1] 93 0 0 0 88 0 28 0 67 30 0 0 91 0 0 57 31 0 0 0 0 17 0 48 0
## [26] 0 2
```

The minimum cost is 1966.68. Note that the last three values for the decision variables are for the dummy refineries.