

1 Generator:

$$G = \langle X, Y, S, \delta_{ext}, \delta_{int}, \lambda, ta \rangle$$

$$Y = \{arrive\} \times \{port0\}$$

$$S = \mathbb{R}_0^+$$

$$\delta_{int}(s) = -(1/\lambda) \times \ln(1 - rand)$$

$$\lambda(s) = (arrive, 0)$$

$$ta(s) = s$$

2 Conveyor Belt:

$$M = \langle X, Y, S, \delta_{ext}, \delta_{int}, \lambda, ta \rangle$$

$$X = \{arrive\} \times \{port0\} \cup \{start, stop\} \times \{port1\}$$

$$Y = \{leave, detect\} \times \{port0\}$$

$$S = Queue \times \mathbb{R}_0^+ \times \mathbb{R}_0^+$$

$$where s = (q, v, \sigma);$$

'q' es la cola de las distancias

'v' es la velocidad de la cinta en un momento dado

$$\delta_{ext}((d1 \bullet q, v, \sigma), e, (x, port)) =$$

$$\left\{ \begin{array}{ll} (d1 \bullet q, v, \sigma) & \text{if } (x, port) = (arrive, 0) \wedge v = 0 \\ (map(+e * v)(d1 \bullet q), 0, \infty) & \text{if } (x, port) = (stop, 1) \\ (map(+e * v)(d1 \bullet q), V_c, (l' - d1')/V_c) & \text{if } (x, port) = (start, 1) \\ (map(+e * v)(d1 \bullet q) \bullet 0, v, (l' - d1')/V_c) & \text{if } (x, port) = (arrive, 0) \wedge v = V_c \end{array} \right.$$

$$where : d1' = d1 + e * v, \quad l' = \left\{ \begin{array}{ll} l & \text{if } d1 < l \\ l + \Delta l & \text{if } d1 \geq l \end{array} \right.$$

$$\delta_{int}(d1 \bullet d2 \bullet q, v, \sigma) =$$

$$\left\{ \begin{array}{ll} (map(+\sigma * v)(d1 \bullet d2 \bullet q), v, \Delta l/V_c) & \text{if } d1 < l \\ (map(+\sigma * v)(d2 \bullet q), v, (l - (d2 + \sigma * v))/V_c) & \text{if } d1 \geq l \wedge d2 \neq \emptyset \\ (\emptyset, v, \infty) & \text{if } d1 \geq l \wedge d2 = \emptyset \end{array} \right.$$

$$\lambda(d1 \bullet q, v, \sigma) = \left\{ \begin{array}{ll} (detect, 0) & \text{if } d1 < l \\ (leave, 0) & \text{if } d1 \geq l \end{array} \right.$$

$$ta(d1 \bullet q, v, \sigma) = \sigma$$

3 Rotary Table:

$$M = \langle X, Y, S, \delta_{ext}, \delta_{int}, \lambda, ta \rangle$$

$$X = \{arrive\} \times \{port0\} \cup \{rotateLeft, rotateRight, moveUp, moveDown\} \times \{port1\} \cup \{pick\} \times \{port2\}$$

$$Y = \{up, down, left, right, picked\} \times \{port0\} \cup \{ready\} \times \{port1\}$$

$$S = \{picking, notPicking, picked\} \times \{downLeft, downRight, upLeft, upRight\} \times \mathbb{R}_0^+ \times \mathbb{R}_0^+$$

where $s = (status, position, elapsed, \sigma)$

'status' es el estado del brazo robot

'position' es la posicion de la mesa rotatoria

'elapsed' lleva el tiempo transcurrido en un movimiento de la mesa rotatoria

$$\delta_{ext}((status, position, elapsed, \sigma), e, (x, port)) =$$

$$\left\{ \begin{array}{ll} (status, upLeft, 0, t_{mov}) & \text{if } (x, port) = (rotateLeft, 1) \\ (status, upRight, 0, t_{mov}) & \text{if } (x, port) = (moveUp, 1) \\ (status, downLeft, 0, t_{mov}) & \text{if } (x, port) = (moveDown, 1) \\ (picked, position, elapsed, 0) & \text{if } (x, port) = (pick, 2) \\ (status, downRight, 0, t_{mov}) & \text{if } (x, port) = ((arrive, 0) \vee (rotateRight, 1)) \\ (status, position, elapsed', \sigma') & \text{ow} \end{array} \right.$$

$$\text{where : } elapsed' = elapsed + e, \quad \sigma' = \begin{cases} t_{mov} - elapsed' & \text{if } elapsed < t_{mov} \\ \infty & \text{ow} \end{cases}$$

$$\delta_{int}(status, position, elapsed, \sigma) =$$

$$\left\{ \begin{array}{ll} (status, position, elapsed, \infty) & \text{if } status = picking \\ (notPicking, position, elapsed, \infty) & \text{if } status = picked \\ (picking, position, elapsed, 0) & \text{if } (status = notPicking) \wedge (position = upRight) \\ (status, position, elapsed + \sigma, \infty) & \text{ow} \end{array} \right.$$

$$\lambda(status, position, elapsed, \sigma) = \left\{ \begin{array}{ll} (ready, 1) & \text{if } status = picking \\ (picked, 0) & \text{if } status = picked \\ (down, 0) & \text{if } status = downLeft \\ (right, 0) & \text{if } status = downRight \\ (up, 0) & \text{if } status = upRight \\ (left, 0) & \text{if } status = upLeft \end{array} \right.$$

$$ta(status, position, elapsed, \sigma) = \sigma$$

4 System Control:

$$M = \langle X, Y, S, \delta_{ext}, \delta_{int}, \lambda, ta \rangle$$

$$X = \{leave, detect\} \times \{port0\} \cup \{up, down, left, right, picked\} \times \{port1\}$$

$$Y = \{start, stop\} \times \{port0\} \cup \{arrive\} \times \{port1\} \cup \{rotateLeft, rotateRight, moveUp, moveDown\} \times \{port2\}$$

$$S = \{leave, detect, up, down, left, right, picked\} \times \{upLeft, upRight, downLeft, downRight\} \times \mathbb{R}_0^+$$

where $s = (signal, position, \sigma)$

'signal' lleva un evento de entrada

'position' es la posicion de la mesa rotatoria

$$\delta_{ext}((signal, position, \sigma), e, (x, port)) =$$

$$\left\{ \begin{array}{ll} (detect, position, 0) & \text{if } (x, port) = (detect, 0) \wedge position \neq downLeft \\ (leave, downRight, 0) & \text{if } (x, port) = (leave, 0) \wedge position = downLeft \\ (left, upLeft, 0) & \text{if } (x, port) = (left, 1) \\ (down, downLeft, 0) & \text{if } (x, port) = (down, 1) \\ (right, downRight, 0) & \text{if } (x, port) = (right, 1) \\ (up, upRight, 0) & \text{if } (x, port) = (up, 1) \\ (picked, position, 0) & \text{if } (x, port) = (picked, 1) \end{array} \right.$$

$$\delta_{int}(signal, position, \sigma) = (signal, position, \infty)$$

$$\lambda(signal, position, \sigma) = \left\{ \begin{array}{ll} (stop, 1) & \text{if } signal = detect \\ (arrive, 1) & \text{if } signal = leave \\ (moveDown, 2) & \text{if } signal = left \\ (start, 0) & \text{if } signal = down \\ (moveUp, 2) & \text{if } signal = right \\ (rotateLeft, 2) & \text{if } signal = picked \end{array} \right.$$

$$ta(signal, position, \sigma) = \sigma$$

5 Robot:

$$M = \langle X, Y, S, \delta_{ext}, \delta_{int}, \lambda, ta \rangle$$

$$X = \{ready\} \times \{port0\}$$

$$Y = \{pick\} \times \{port0\}$$

$$S = \{busy, notBusy\} \times \mathbb{R}_0^+$$

where $s = (status, \sigma)$

'status' es el estado del brazo robot

$$\begin{aligned}
\delta_{ext}((status, \sigma), e, (x, port)) = & \\
\begin{cases} (busy, rand * (b - a) + a) & \text{if } (x, port) = (ready, 0) \wedge status = notBusy \\ (status, \sigma - e) & \text{ow } (x, port) = (down, 1) \end{cases} \\
\text{where : } a = 6 \wedge b = 16 \\
\delta_{int}(status, \sigma) = (notBusy, \infty) \\
\lambda(status, \sigma) = (pick, 0) \\
ta(status, \sigma) = \sigma
\end{aligned}$$

6 Conveyor Belt Statics:

$$\begin{aligned}
M &= \langle X, Y, S, \delta_{ext}, \delta_{int}, \lambda, ta \rangle \\
X &= \{arrive\} \times \{port0\} \cup \{start, stop\} \times \{port1\} \{leave\} \times \{port2\} \\
Y &= \mathbb{R} \times \{port0\} \cup \mathbb{R} \times \{port1\} \\
S &= N \times \{running, stopped\} \times N \times N \times N \times \mathbb{R}_0^+
\end{aligned}$$

where : $s = (print, status, counter, rejected, onBelt, \sigma)$

'print' dice el numero de puerto que se va a mostrar con gnuplot

'status' indica el estado de la cinta transportadora

'counter' cuenta la cantidad de arribos

'rejected' cuenta la cantidad de arribos rechazados dado que la cinta estaba detenida

'onBelt' cuenta la cantidad de piezas en la cinta transportadora

$$\begin{aligned}
\delta_{ext}((print, status, counter, rejected, onBelt, \sigma), e, (x, port)) = & \\
\begin{cases} (print, status, counter + 1, rejected, onBelt + 1, 0) & \text{if } (x, port) = (arrive, 0) \wedge status = running \\ (print, status, counter + 1, rejected + 1, onBelt, 0) & \text{if } (x, port) = (arrive, 0) \wedge status = stopped \\ (print, status, counter, rejected, onBelt - 1, 0) & \text{if } (x, port) = (leave, 2) \\ (print, running, counter, rejected, onBelt, \sigma) & \text{if } (x, port) = (start, 1) \\ (print, stopped, counter + 1, rejected, onBelt, \sigma) & \text{if } (x, port) = (stop, 1) \end{cases} \\
\delta_{int}(print, status, counter, rejected, onBelt, \sigma) = & \\
\begin{cases} (1, status, counter, rejected, onBelt, 0) & \text{if } print = 0 \\ (0, status, counter, rejected, onBelt, \infty) & \text{if } print = 1 \end{cases} \\
\lambda(print, status, counter, rejected, onBelt, \sigma) = \begin{cases} (rejected/counter, 0) & \text{if } print = 0 \\ (onBelt, 1) & \text{if } print = 1 \end{cases} \\
ta(print, status, counter, rejected, onBelt, \sigma) = \sigma
\end{aligned}$$