

## CS4750/7750 HW #4 (20 points)

Implement minimax algorithm to play a two-player, four-in-a-row game, which is a variation of tic-tac-toe: two players, *X* and *O*, take turns marking the spaces in a 5×6 grid. The player who succeeds in placing 4 of their marks consecutively in a horizontal, vertical, or diagonal row wins the game. See an example below where *X* player plays first and wins the game.

Successor function: a player may place a piece at any empty space next to an existing piece horizontally, vertically, or diagonally on the board.

Tie-breaking of moves: break ties in increasing order of column number first (smaller column number has higher priority) and then increasing order of row number (smaller row number has higher priority).

	1	2	3	4	5	6
1						
2		o	x		x	
3		o	o	<b><u>x</u></b>		
4	o	x	x	o		
5		x				

This is a group assignment. You may use any programming language in your implementation.

You are asked to do the following tasks:

- 1) (6 points) Implement the minimax algorithm to play the game. Describe the implementation in your report.
- 2) (4 points) Implement Player 1 (*X* player) as follows.
  - Player 1 makes the first move and puts the first piece ‘x’ at [3,4] position on the board (the bold x position in the example).
  - Run the minimax algorithm on a 2-ply game tree, i.e., looking ahead 2 moves (one move by the player and one move by the opponent).
  - Use the following heuristic evaluation function on the states (if not a terminal state) of the cut-off nodes in the game tree. For terminal nodes, return their utility value: -1000 for lose, 0 for tie, or 1000 for win. Here, the “me” in the formula refers to Player 1.

$$\begin{aligned} h(n) = & 200 * [\text{number of two-side-open-3-in-a-row for me}] \\ & - 80 * [\text{number of two-side-open-3-in-a-row for opponent}] \\ & + 150 * [\text{number of one-side-open-3-in-a-row for me}] \\ & - 40 * [\text{number of one-side-open-3-in-a-row for opponent}] \\ & + 20 * [\text{number of two-side-open-2-in-a-row for me}] \\ & - 15 * [\text{number of two-side-open-2-in-a-row for opponent}] \\ & + 5 * [\text{number of one-side-open-2-in-a-row for me}] \end{aligned}$$

$$- 2*[number\ of\ one-side-open-2-in-a-row\ for\ opponent]$$

where

- “one-side-open-3-in-a-row”: there is an empty space next to one end of a 3-in-a-row to potentially make it 4-in-a row in the next move.
- “two-side-open-3-in-a-row”: there are empty spaces next to both ends of a 3-in-a-row to potentially make it 4-in-a row in the next move.
- “one-side-open-2-in-a-row”: there is an empty space next to one end of a 2-in-a-row to potentially make it 3-in-a row in the next move.
- “two-side-open-2-in-a-row”: there are empty spaces next to both ends of a 2-in-a-row to potentially make it 3-in-a row in the next move.

For example, for player ‘X’, the value of the following state is

$$h = 200*0 - 80*1 + 150*1 - 40*0 + 20*1 - 15*0 + 5*0 - 2*3 = 84$$

		o	x		
		o	o	x	
	o	x	x	o	
		x			

- 3) (4 points) Implement Player 2 (O player) as follows.
  - Player 2 puts the first ‘o’ piece at [3,3] position on the board (to the left of the bold x position in the example).
  - Use the same heuristic function as Player 1, i.e., the function  $h(n)$  given above. Now, the “me” in the formula refers to Player 2.
  - Run minimax algorithm on a 4-ply game tree, i.e., looking ahead 4 moves (two moves by the player and two moves by the opponent).
- 4) (4 points) Play a game between Player 1 and Player 2. Print out the following:
  - a) every move made by the two players throughout the whole game,
  - b) for each move, the number of nodes generated by minimax algorithm and the CPU execution time.

Submission:

- a) (18 points) A pdf file of your report containing descriptions of your implementation and result.
- b) (2 points) A zip file containing your code with appropriate comments.