
Table of Contents

| | |
|-------------------|---|
| Eric Wan | 1 |
| Question 12 | 1 |
| Question 13 | 4 |

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clc, clear, close all

Question 12

```
X=[1.6978 7.7368 8.7591 1.9001 0.7486 0.2048 6.1228, 1.6926 2.2690
    13.2931];
Y=[11.4976,4.5624,17.0159,5.1402,8.9841,8.9526,2.0939,6.1407];
X = sort(X);
Y = sort(Y);

for i = [3, 5, 6]
    thr = i; % threshold
    Nx = numel(X); % # of elements in X (No target)
    Ny = numel(Y); % # of elements in Y (W/ target)
    N = Nx + Ny; % # of total elements

    Nf = X > thr; % samples X > threshold
    count = sum(X > thr); % # of samples X > threshold
    pTa = Nx/N; % a priori probability for X (no target was present)
    pF = count/Nx; % probability of false alarm (X > thr / count X)

    Nc = Y > thr; % samples Y- > threshold
    count = sum(Y > thr); % # of samples Y > threshold
    pTp = Ny/N; % a priori probability for Y (target was present)
    pD = count/Ny; % probability of detection (Y > thr / count Y)
    pM = 1 - pD;

    pE = pM * pTp + pF * pTa; % prob error = prob miss * a priori prob
    present + prob fail * apriori prob not present
    % a priori prob, false alarm, miss, error rate
    % thresh of 3, 5, 6
    sprintf("a priori probability for X (target was not present) of
threshold (%f): %f", thr, pTa)
    sprintf("a priori probability for Y (target was present) of
threshold (%f): %f", thr, pTp)
    sprintf("probability for a false alarm (target was not present but
detects as such) of threshold (%f): %f", thr, pF)
    sprintf("probability for a miss (target was present but not
detects) of threshold (%f): %f", thr, pM)
    sprintf("probability of error of threshold (%f): %f", thr, pE)
end
```

```
[x, xt] = ksdensity(X);
[y, yt] = ksdensity(Y);
figure;
hold on;
plot(xt, x);
plot(yt, y);
title("Question 12")
xlabel("Values");
ylabel("Counts");
legend("Target Absent", "Target Present");
```

```
ans =
```

```
    "a priori probabilty for X (target was not present) of threshold  
(3.000000): 0.555556"
```

```
ans =
```

```
    "a priori probabilty for Y (target was present) of threshold  
(3.000000): 0.444444"
```

```
ans =
```

```
    "probability for a false alarm (target was not present but detects  
as such) of threshold (3.000000): 0.400000"
```

```
ans =
```

```
    "probability for a miss (target was present but not detects) of  
threshold (3.000000): 0.125000"
```

```
ans =
```

```
    "probability of error of threshold (3.000000): 0.277778"
```

```
ans =
```

```
    "a priori probabilty for X (target was not present) of threshold  
(5.000000): 0.555556"
```

```
ans =
```

```
    "a priori probabilty for Y (target was present) of threshold  
(5.000000): 0.444444"
```

```
ans =
```

"probability for a false alarm (target was not present but detects as such) of threshold (5.000000): 0.400000"

ans =

"probability for a miss (target was present but not detects) of threshold (5.000000): 0.250000"

ans =

"probability of error of threshold (5.000000): 0.333333"

ans =

"a priori probability for X (target was not present) of threshold (6.000000): 0.555556"

ans =

"a priori probability for Y (target was present) of threshold (6.000000): 0.444444"

ans =

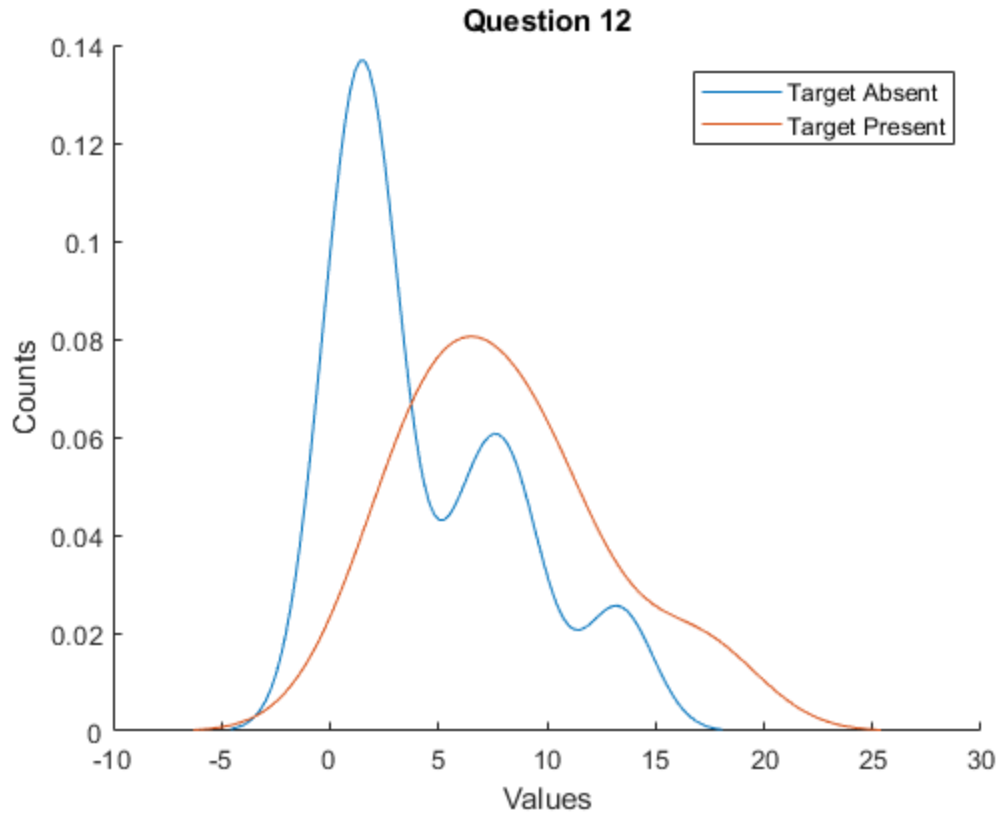
"probability for a false alarm (target was not present but detects as such) of threshold (6.000000): 0.400000"

ans =

"probability for a miss (target was present but not detects) of threshold (6.000000): 0.375000"

ans =

"probability of error of threshold (6.000000): 0.388889"



Question 13

```
data = xlsread("HW2_data_shankar_Spring.xlsx", "hw5data_", "CE:CE");
data1 = data(1:40); % target is not present
data1 = sort(data1);
data2 = data(41:70); % target is present
data2 = sort(data2);
thr = (median(data1) + median(data2))/2;

figure;
hold on;
grid on;
histogram(data1, 6);
histogram(data2, 6);
line(thr, 10, 'Color', 'red', 'LineWidth', 3);
title("Question 13: WAN");
xlabel("Values");
ylabel("Counts");
legend("Target Absent", "Target Present");

Nx = numel(data1); % # of elements in d2 (No target)
Ny = numel(data2); % # of elements in d1 (W/ target)
N = Nx + Ny; % # of total elements

Nf = sum(data1 > thr); % samples d2 > threshold
```

```

pTa = Nx/N; % a priori probability for d2 (no target was present)
pF = Nf/Nx; % probability of false alarm (d2 > thr / count d2)

Nc = sum(data2 > thr); % samples d1 > threshold
pTp = Ny/N; % a priori probability for d1 (target was present)
pD = Nc/Ny; % probability of detection (d1 > thr / count d1)
pM = 1 - pD; % probability of miss

pSens = Nf/Ny; % # of correct positive detections / # of positive
cases
pSpec = Nc/Nx; % # of correct negative detections / # of negative
cases
PPV = Nc / (Nc + Nf); % # of correct positive detections / # of
positive detections
pACC = (Nc + (Nx - Nf)) / N; % # of correct detections / # of cases

pE = pM * pTp + pF * pTa; % prob error = prob miss * a priori prob
present + prob fail * a priori prob not present
% a priori prob, false alarm, miss, sensitivity, specificity, positive
predictive value, accuracy
sprintf("a priori probability for X of threshold (%f): %f", thr, pTa)
sprintf("a priori probability for Y of threshold (%f): %f", thr, pTp)
sprintf("probability for a false alarm of threshold (%f): %f", thr, pF)
sprintf("probability for a miss of threshold (%f): %f", thr, pM)
sprintf("sensitivity of threshold (%f): %f", thr, pSens)
sprintf("specificity of threshold (%f): %f", thr, pSpec)
sprintf("positive predictive value of threshold (%f): %f", thr, PPV)
sprintf("accuracy of threshold (%f): %f", thr, pACC)

fprintf('-----Confusion Matrix for Histogram w/ Threshold %f-----
\n', thr);
fprintf('%-15s\t %-15s\t %-15s\t %-15s
\n', 'Data', 'Target', 'Target', 'Total')
fprintf('%-15s\t %-15s\t %-15s\t %-15s
\n', 'Collected', 'Detected', 'Not Detected', 'Count')
fprintf('%-15s\t %-15d\t %-15d\t %-15d\n', 'Target Absent', Nf, Nx -
Nf, Nx)
fprintf('%-15s\t %-15d\t %-15d\t %-15d\n', 'Target Present', Nc, Ny -
Nc, Ny)
fprintf('%-15s\t %-15d\t %-15d\t %-15d\n', 'Total Count', Nf + Nc, Ny
- Nf + Ny - Nc, N)

pt = 0:0.0001:10;
npt = 0:0.0001:25;
p = ksdensity(data1, pt);
np = ksdensity(data2, npt);
thr = sum((pt((abs(p - np(1:numel(p)))) < 0.00001)) + npt((abs(p -
np(1:numel(p)))) < 0.00001)))/2)/2;
figure;
hold on;
plot(pt, p); % absent
plot(npt, np); % present
area(pt(pt>thr & pt<pt(end)), p(pt>thr & pt<pt(end))); % miss

```

```

area(npt(npt<thr & npt>npt(1)), np(npt<thr & npt>npt(1))); % false
alarm
title("Question 13: WAN");
xlabel("Values");
ylabel("Est. Density");
legend("Target Absent", "Target Present", "False Alarm", "Miss");

Nx = numel(data1); % # of elements in d2 (No target)
Ny = numel(data2); % # of elements in d1 (W/ target)
N = Nx + Ny; % # of total elements

Nf = sum(data1 > thr); % samples d2 > threshold
pTa = Nx/N; % a priori probability for d2 (no target was present)
pF = Nf/Nx; % probability of false alarm (d2 > thr / count d2)

Nc = sum(data2 > thr); % samples d1 > threshold
pTp = Ny/N; % a priori probability for d1 (target was present)
pD = Nc/Ny; % probability of detection (d1 > thr / count d1)
pM = 1 - pD; % probability of miss

pSens = Nf/Ny; % # of correct positive detections / # of positive
cases
pSpec = Nc/Nx; % # of correct negative detections / # of negative
cases
PPV = Nc / (Nc + Nf); % # of correct positive detections / # of
positive detections
pACC = (Nc + (Nx - Nf)) / N; % # of correct detections / # of cases

pE = pM * pTp + pF * pTa; % prob error = prob miss * a priori prob
present + prob fail * apriori prob not present
% a priori prob, false alarm, miss, sensitivity, specificity, positive
predictive value, accuracy
sprintf("a priori probability for X of threshold (%f): %f", thr, pTa)
sprintf("a priori probability for Y of threshold (%f): %f", thr, pTp)
sprintf("probability for a false alarm of threshold (%f): %f", thr, pF)
sprintf("probability for a miss of threshold (%f): %f", thr, pM)
sprintf("sensitivity of threshold (%f): %f", thr, pSens)
sprintf("specificity of threshold (%f): %f", thr, pSpec)
sprintf("positive predictive value of threshold (%f): %f", thr, PPV)
sprintf("accuracy of threshold (%f): %f", thr, pACC)

fprintf('-----Confusion Matrix for kDensity w/ Threshold %f-----\n',
thr);
fprintf('%-15s\t %-15s\t %-15s\t %-15s\n', 'Data', 'Target', 'Target', 'Total')
fprintf('%-15s\t %-15s\t %-15s\t %-15s\n', 'Collected', 'Detected', 'Not Detected', 'Count')
fprintf('%-15s\t %-15d\t %-15d\t %-15d\n', 'Target Absent', Nf, Nx -
Nf, Nx)
fprintf('%-15s\t %-15d\t %-15d\t %-15d\n', 'Target Present', Nc, Ny -
Nc, Ny)
fprintf('%-15s\t %-15d\t %-15d\t %-15d\n', 'Total Count', Nf + Nc, Ny
- Nf + Ny - Nc, N)

```

```

ans =

    "a priori probabilty for X of threshold (3.961607): 0.571429"

ans =

    "a priori probabilty for Y of threshold (3.961607): 0.428571"

ans =

    "probabilty for a false alarm of threshold (3.961607): 0.125000"

ans =

    "probabilty for a miss of threshold (3.961607): 0.233333"

ans =

    "sensitivity of threshold (3.961607): 0.166667"

ans =

    "specificity of threshold (3.961607): 0.575000"

ans =

    "positive predictive value of threshold (3.961607): 0.821429"

ans =

    "accuracy of threshold (3.961607): 0.828571"

-----Confusion Matrix for Histogram w/ Threshold 3.961607-----
Data          Target          Target          Total
Collected    Detected          Not Detected    Count
Target Absent    5              35             40
Target Present   23             7              30
Total Count     28             32             70

ans =

    "a priori probabilty for X of threshold (4.189250): 0.571429"

ans =

```

```

    "a priori probabiltiy for Y of threshold (4.189250): 0.428571"

ans =

    "probabilty for a false alarm of threshold (4.189250): 0.125000"

ans =

    "probabilty for a miss of threshold (4.189250): 0.300000"

ans =

    "sensitivity of threshold (4.189250): 0.166667"

ans =

    "specificity of threshold (4.189250): 0.525000"

ans =

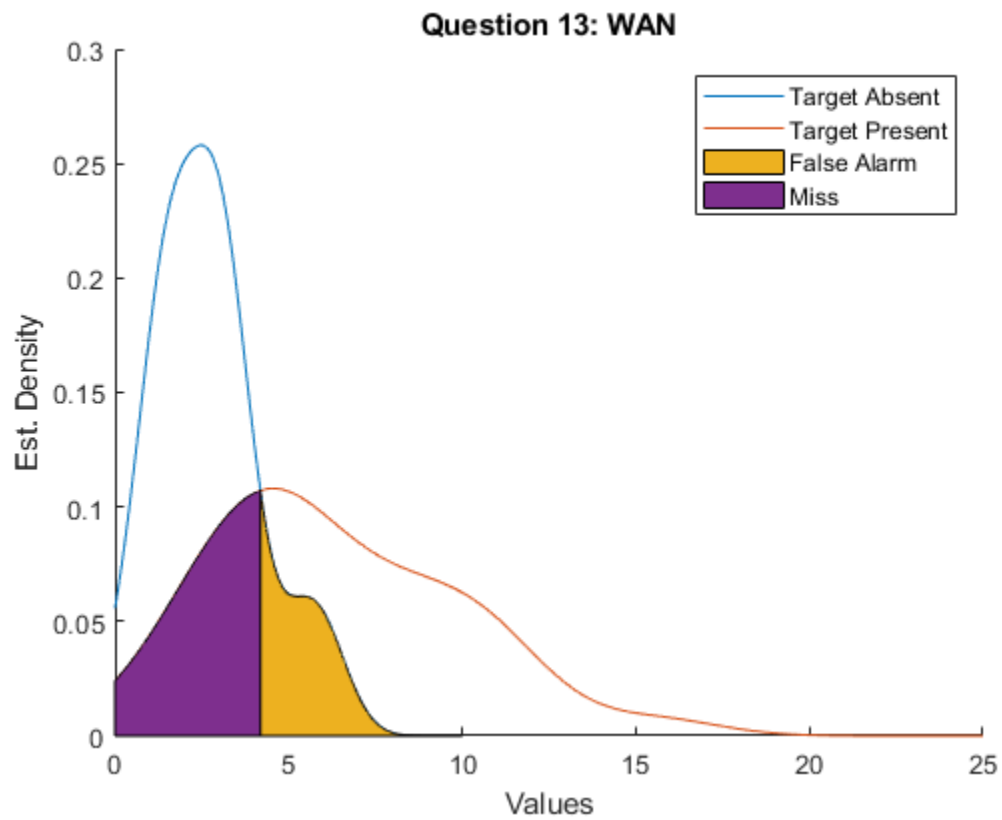
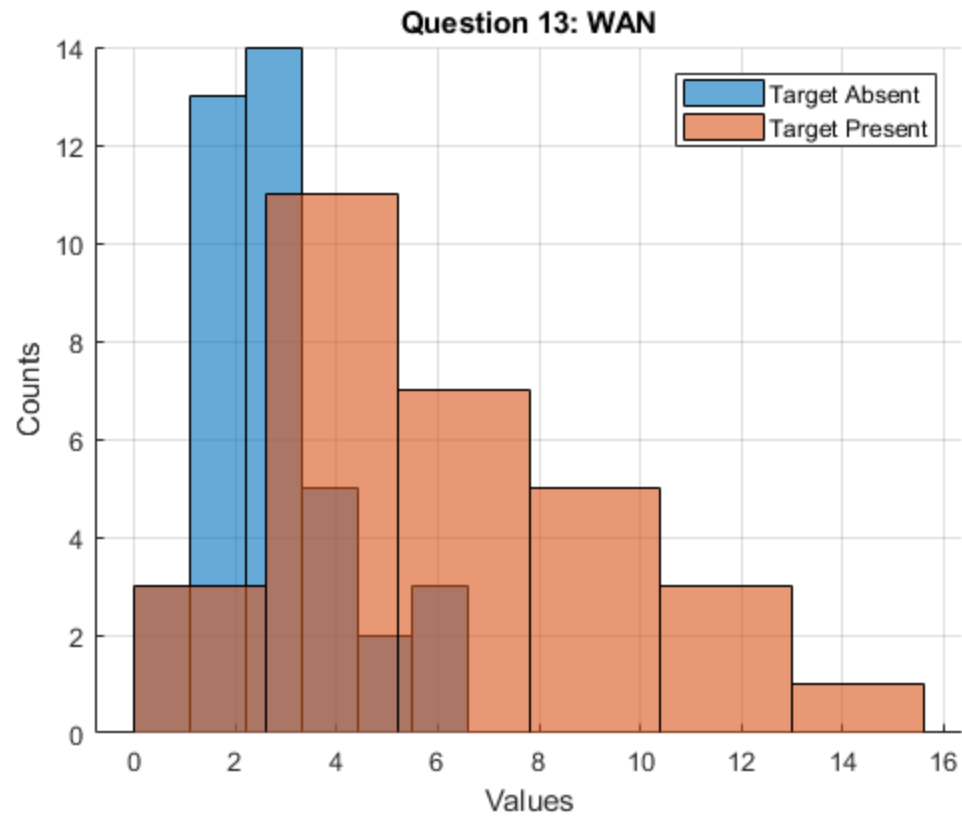
    "positive predictive value of threshold (4.189250): 0.807692"

ans =

    "accuracy of threshold (4.189250): 0.800000"

-----Confusion Matrix for kDensity w/ Threshold 4.189250-----
Data      Target      Target      Total
Collected Detected    Not Detected Count
Target Absent  5          35         40
Target Present 21          9         30
Total Count   26         34         70

```

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