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Problem 1

$\varphi\{$
(a)
Domain: \mathbb{R}^3
Range: \mathbb{R}^4
Co-Domain: \mathbb{R}^4
One-to-one or Onto: One-to-one b/c pivots same domain

(b)
Domain: \mathbb{R}^6
Range: \mathbb{R}^3
Co-Domain: \mathbb{R}^3
One-to-one or Onto: Onto b/c range is the same as the codomain

(c)
Domain: \mathbb{R}^4
Range: \mathbb{R}^2
Co-Domain: \mathbb{R}^2
One-to-one or Onto: Onto b/c range is the same as the codomain

(d)
Domain: \mathbb{R}^4
Range: \mathbb{R}^3
Co-Domain: \mathbb{R}^3
One-to-one or Onto: Onto b/c range is the same as the codomain

(e)
Domain: \mathbb{R}^3
Range: \mathbb{R}^2
Co-Domain: \mathbb{R}^3
One-to-one or Onto: Onto b/c range is the same as the codomain

(f)
Domain: \mathbb{R}^4
Range: \mathbb{R}^4
Co-Domain: \mathbb{R}^4
One-to-one or Onto: Onto and One-to-one

One-to-one and Onto: To be both, the number of pivots has to be the same same as rows.

```
%}
```

Problem 2

```
%{  
(a)  
X = 3e1 + 2e2  
  
(b)  
No  
X cannot be made  
  
(c)  
No  
  
(d)  
No as we need 4 pivots but only have 3  
%}
```

Problem # 3 & 4

```
x_coords = [-1 1 1 -1]; % setting x coord for rectangle  
y_coords = [-1 -1 1 1]; % setting y coord for rectangle  
rectf = [x_coords; y_coords ; 1 1 1 1]; % creating rectangle  
figure; % creating figure  
fill(rectf(1,:),rectf(2,:), 'r') % filling in rectangle  
axis square;  
hold on;  
  
% Part a  
dx = -2;  
dy = 4;  
ang_deg = 45;  
t = [1 0 dx; 0 1 dy; 0 0 1];  
r = [cosd(ang_deg) -sind(ang_deg) 0; sind(ang_deg) cosd(ang_deg) 0; 0 0 1];  
% moved -2 in x-axis and +4 in y-axis, rotated by 45 degrees  
M1 = r * t % simplified matrix  
rectf1 = M1 * rectf; % new coordinates  
% rectf1 = r*(t*rectf); % same equation rewritten to reference  
fill(rectf1(1,:),rectf1(2,:), 'b') % filling in rectangle  
  
% Part b  
% rotated by 45 degrees, moved -2 in x-axis and +4 in y-axis,  
M2 = t * r % simplified matrix  
rectf2 = M2 * rectf; % new coordinates  
% rectf2 = t * (r * rectf); % same equation rewritten to reference  
fill(rectf2(1,:),rectf2(2,:), 'k') % filling in rectangle  
  
% Part c  
dx = 5;  
dy = 0;  
ang_deg = -90;
```

```
t = [1 0 dx; 0 1 dy; 0 0 1];
r = [cosd(ang_deg) -sind(ang_deg) 0; sind(ang_deg) cosd(ang_deg) 0; 0 0 1];
s = [0.5 0 0; 0 0.5 0; 0 0 1];
% scaled to 1/2, rotated by 45 degrees, moved -2 in x-axis and +4 in y-axis
M3 = t * r * s % simplified matrix
rectf3 = M3 * rectf; % new coordinates
% rectf3 = (t * (r * (s * rectf) ) ); % same equation rewritten to reference
fill(rectf3(1,:),rectf3(2,:), 'g')

% Part d
ang_deg = 10;
r = [cosd(ang_deg) -sind(ang_deg) 0; sind(ang_deg) cosd(ang_deg) 0; 0 0 1];
% rotated by 10 degrees 6 times
M4 = r^6
rectf4 = M4 * rectf;
% rectf4 = (r * (r * (r * (r * (r * (r * rectf) ) ) ) ) ); % same equation rewritten to reference
fill(rectf4(1,:),rectf4(2,:), 'cyan')

% Part e
dx = -2;
dy = 4;
t51 = [1 0 0; 0 1 dy; 0 0 1];
t52 = [1 0 dx; 0 1 0; 0 0 1];
% moving -2 in x-axis and +4 in y-axis
M51t = t51 * t52; % simplified
M52t = t52 * t51; % simplified
check1 = isequal(M51t, M52t)
% translation of points can be done in any order

ang_deg = 10;
r51 = [cosd(ang_deg) -sind(ang_deg) 0; sind(ang_deg) cosd(ang_deg) 0; 0 0 1];
r52 = [cosd(-ang_deg) -sind(-ang_deg) 0; sind(-ang_deg) cosd(-ang_deg) 0; 0 0 1];
% rotating 10 degrees and -10 degrees
M51r = r51 * r52; % simplified
M52r = r52 * r51; % simplified
check2 = isequal(M51r, M52r)
% just rotating points without translation can be done in any order

sd = [2 0 0; 0 2 0; 0 0 1];
sh = [0.5 0 0; 0 0.5 0; 0 0 1];
% scaling up by 2 and down by 1/2
M51s = sd * sh; % simplified
M52s = sh * sd; % simplified
check3 = isequal(M51s, M52s)
% just scaling points without translation can be done in any order

M51sr = sd * r51; % simplified
```

```
M52rs = r51 * sd; % simplified
check4 = isequal(M51sr, M52rs)
% scaling and rotating can be done in any order
```

M1 =

0.7071	-0.7071	-4.2426
0.7071	0.7071	1.4142
0	0	1.0000

M2 =

0.7071	-0.7071	-2.0000
0.7071	0.7071	4.0000
0	0	1.0000

M3 =

0	0.5000	5.0000
-0.5000	0	0
0	0	1.0000

M4 =

0.5000	-0.8660	0
0.8660	0.5000	0
0	0	1.0000

check1 =

logical

1

check2 =

logical

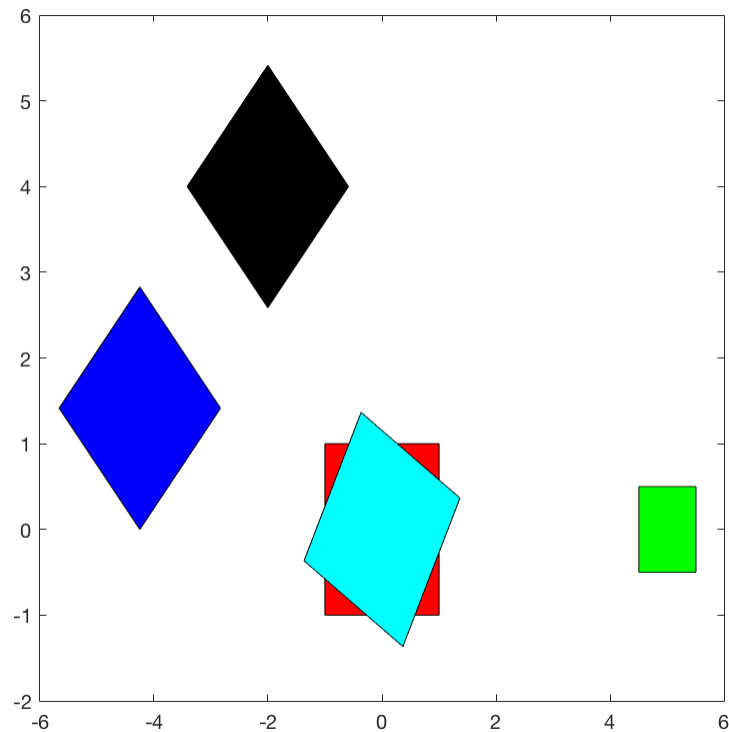
1

check3 =

logical

1

```
check4 =  
  
logical  
  
1
```

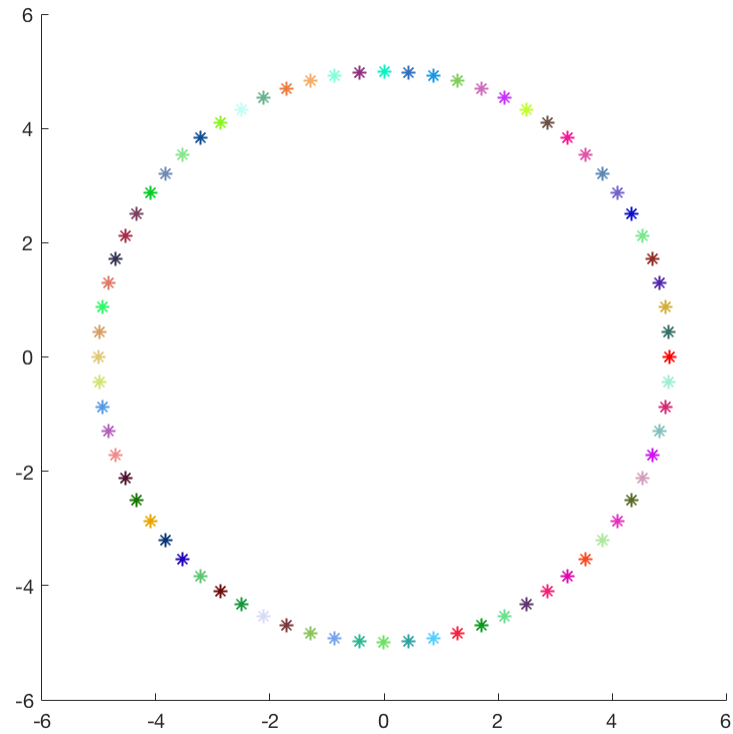


Problem # 4

Part b

```
figure;  
hold on;  
axis square;  
p = [5; 0; 1]; % defining p  
x = p(1,:); % defining x from p  
y = p(2,:); % defining y from p  
p1 = plot(x, y); % plotting x and y as initial point  
p1.Marker = '*';  
p1.Color = [1 0 0];  
  
for i = 1: 5: 355 % for loop  
    p = root(5)* p; % new p values every iteration  
    x = p(1,:); % new x every iteration from p  
    y = p(2,:); % new y every iteration from p  
    p2 = plot(x, y); % plotting new x and y in circle
```

```
p2.Marker = 's';  
p2.Color = [rand rand rand];  
end
```



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