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# Data Driven Determination of Reaction Conditions in Oxidative Coupling of Methane via Machine Learning

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**Abstract:** The challenge in catalytic reactions lies within its complexity coming from high dimensional experimental factors. In order to solve such complexity, machine learning is implemented to treat experimental conditions in high dimensions. Oxidative coupling of methane, methane to C<sub>2</sub> compounds (ethylene and ethane), is chosen as the prototype reaction where 156 data consisting of various experimental conditions is prepared. Machine learning reveals that the relationship between experimental conditions and C<sub>2</sub> yield is non-linear matter. In particular, extreme tree regression is found to accurately reproduce the experimental data. In addition, machine learning predictions can be a good indicator for designing experiments. Thus, machine learning can be a powerful approach towards understanding and determining experimental conditions in high dimension.

## Introduction

Understanding and controlling the catalytic reactions are considered to be challenging matters. Catalytic reactions involve multiple experimental factors and surface chemistries in a complex manner, making it difficult to create a complete model. However, the implementation of data science could potentially navigate and reveal such complex matter within catalysis as machine learning can treat multiple factors in high dimensions.<sup>[1]</sup> <sup>2]</sup> In earlier years, neural network was implemented to treat heterogeneous catalysis where such data science techniques

are proposed to be effective tools for simulating catalyst properties and the performance of solid materials.<sup>[3-8]</sup> Since then, rapid development of machine learning algorithms occurred due to the introduction of random forest and support vector machine, which greatly improve and expand the ways of understanding the data.<sup>[9-12]</sup> Thus, one can consider that such machine learning techniques could potentially solve the mystery of how reaction conditions determine the catalytic activities in heterogeneous catalysis.

Catalytic reactions depend on various parameters which can be classified into three categories: catalyst structure, reaction condition, and catalyst stability. The catalyst structure includes composition, oxidation state, particle size, shape, crystallinity, and strain; the reaction conditions include reactor shape, temperature, catalyst, reactant concentration, and flow rate; and the catalyst change during reactions includes aggregation/dispersion, redox, and surface reconstruction. Consequently, all of these parameters can be descriptor variables for representing catalytic reactions. In general, it is challenging to manipulate and handle high dimension descriptor variables by the human brain. Therefore, researchers design catalysts by considering few major descriptors such as particle size, d-band center, and reaction temperature.<sup>[13-15]</sup> For instance, in the case of gold catalysts, the particle size has been elucidated as the main descriptor of their catalytic performance for a variety of reactions including CO oxidation, aldehyde hydrogenation, and the water gas shift reaction.<sup>[16]</sup> Hence, gold catalysts under the guideline of particle size control can be well designed. Previous studies have also suggested, however, that factors other than particle size such as support effect, cluster size or single atom effect, and crystal structure also greatly contribute to the performance of gold catalysts.<sup>[17-19]</sup> In other words, the effect of the catalyst structure is a multi-dimensional problem. If such multi-dimensional problem can be treated within machine learning, further sophisticated catalyst design can be made achievable in principle. The same can be said about the effect of catalytic reaction conditions. One usually explores the influence and importance of each reaction parameter on the target products by conducting reactions under various conditions, and then either find the optimal experiment conditions empirically or instinctively when the data dimensions becomes high and complex. If the effects of the reaction conditions can be organized and if accurate models can be constructed using machine learning, then one could then survey the information surrounding the effects of each reaction parameter and select the optimum reaction conditions from predicted data, even if the range is not investigated through experiments.

Here, machine learning is implemented in order to determine the reaction conditions in heterogeneous catalysis. In particular, oxidative coupling of methane (OCM) is chosen as a prototype reaction where the reaction involves conversion of

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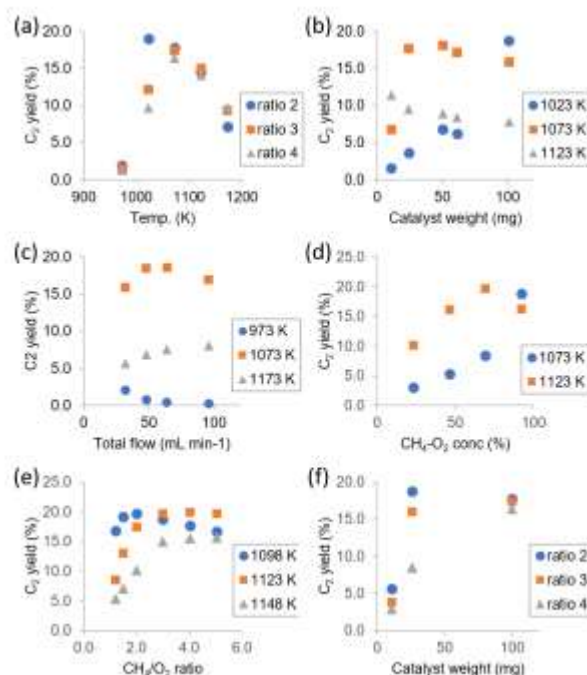
methane to  $C_2$  compounds ethylene and ethane. Typically, the OCM is performed on basic catalysts containing alkaline or alkaline earth metals at a very high temperature ranging from 973–1173 K for abstraction of H from  $CH_4$  to form  $CH_3$  radical intermediates of the  $C_2$  compounds.<sup>[20–22]</sup> To put the OCM towards an industrial application, the catalytic reaction systems should have high  $C_2$  selectivity by suppressing undesirable reactions— in particular, oxidation of  $CH_3$  radicals on catalyst surface as well as in gas phase— while maintaining  $CH_4$  conversion rate.<sup>[20]</sup> In addition, high durability is required for the catalyst materials to stably produce the  $C_2$  compounds at such high reaction temperatures.<sup>[23]</sup> In order to develop the OCM catalysts with these functions, hundreds of inorganic materials have been investigated as summarized in the previous review articles.<sup>[20, 21]</sup> Among the reported catalysts,  $Mn-Na_2WO_4/SiO_2$  exhibits relatively high activity, selectivity, and stability for the OCM.<sup>[23–26]</sup> The catalytic performance of  $Mn-Na_2WO_4/SiO_2$  has been further improved by meso-ordered structure of  $SiO_2$  support as well as by a membrane reactor with separated feeding of  $CH_4$  and  $O_2$ .<sup>[27, 28]</sup> However, no catalytic reaction systems affording sufficient  $C_2$  yield and selectivity for practical large-scale application have been developed.<sup>[20, 23]</sup> One can consider that OCM involves complex reaction conditions; therefore, machine learning is implemented to reveal how reaction conditions act in high dimension during the OCM reaction.  $Mn-Na_2WO_4/SiO_2$  catalysts are chosen due to high catalytic performance in OCM reaction.<sup>[21]</sup> Here, reaction conditions in the OCM reaction using  $Mn-Na_2WO_4/SiO_2$  are investigated in high dimension via machine learning while determination of the reaction conditions is performed.

## Results and Discussion

OCM reaction over  $Mn-Na_2WO_4/SiO_2$  is performed under various conditions; more specifically, a 156 data set is prepared at 156 experimental conditions by changing five reaction parameters including reaction temperature,  $CH_4/O_2$  ratio, concentration of  $CH_4$  and  $O_2$  gases ( $CH_4+O_2$  conc.), total flow rate, and catalyst weight. The total yields of ethylene and ethane ( $C_2$  yields) obtained under the various reaction conditions are listed in Table S1.  $C_2$  yield varies with every parameter of the reaction conditions. The  $C_2$  yields are consistent with previously reported yields obtained using  $Mn-Na_2WO_4$  catalysts under similar reaction conditions including the artificial neural network results, where the  $C_2$  yields of 22% reported in this work are consistent with  $C_2$  yields of 23% previously reported using artificial neural network.<sup>[23, 29, 30, 31]</sup> Given the nature of the random forest regression model, the impact of the descriptors are also further evaluated. During data acquisition, a reaction parameter value is changed until  $C_2$  yield reaches a local maximum or a plateau value as long as the variable parameter is within safety limits of the experiment (e.g. explosion limits); meanwhile, the other parameter values are kept constant. Several data at  $CH_4/O_2 < 2$  are obtained under low  $CH_4+O_2$  conc. to avoid explosion. It should also be noted that temperature  $< 973$  K is not investigated since  $Mn-Na_2WO_4/SiO_2$  hardly shows catalytic

activity. In addition, the catalyst weight of  $> ca. 100$  mg is not investigated due to concern of significant increase of back pressure by a thick catalyst bed. Each reaction parameter is changed to construct 156 data which is considered to form a parameter coordinate network capturing the reaction feature including the  $C_2$  maximum yield.

A part of the reaction data is picked up to present the complex effect of the reaction conditions on  $C_2$  yield as shown in Fig. 1. Fig. 1 (a) shows  $C_2$  yield dependence on reaction temperature. After the  $C_2$  compounds are generated from 973 K,  $C_2$  yield increases and then decreases as the temperature increases. It should be noted that the peak temperature for  $C_2$  yield is shifted by  $CH_4/O_2$  ratio as shown in Fig. 1(a). The result indicates that the effect of reaction temperature on  $C_2$  yield is influenced by the  $CH_4/O_2$  ratio.  $C_2$  yield also depends on reaction parameters other than reaction temperature as presented in Fig. 1(b)–(e). The figures also indicate that the effect of each parameter is affected by the reaction temperature. The effects of reaction parameters are changed by reaction parameters other than reaction temperature as represented by Fig. 1(f), which shows the effect of catalyst weight impacted by  $CH_4/O_2$  ratio. Thus, the effects of the five parameters on  $C_2$  yield cannot be described simply as they are intertwined. In the present case, the data set is six-dimensional including the five reaction parameters and  $C_2$  yield. Thus, it is a difficult task to organize the effects of the reaction parameters and to specify the optimum reaction conditions using the human brain.



**Figure 1.**  $C_2$  yield as (a) a function of reaction temperature for the OCM reaction over  $Mn-Na_2WO_4/SiO_2$  (catalyst weight: 50 mg, total flow: 32 mL min<sup>-1</sup>,  $CH_4+O_2$  conc.: 94%,  $CH_4/O_2 = 2$  (blue), 3 (orange), 4 (gray)); (b) a function of catalyst weight (total flow: 32 mL min<sup>-1</sup>,  $CH_4+O_2$  conc.: 94%,  $CH_4/O_2 = 3$ , temp.: 1023 (blue), 1073 (orange), 1123 K (gray)); (c) a function of total flow (catalyst



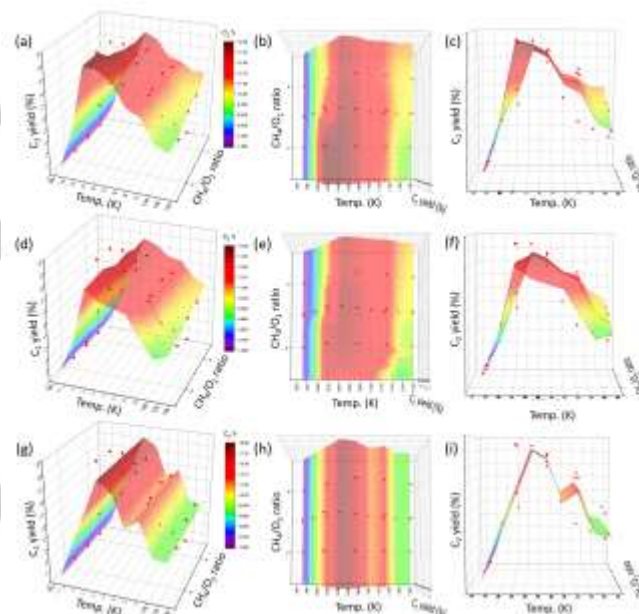
weight: 100 mg,  $\text{CH}_4\text{-O}_2$  conc.: 94%,  $\text{CH}_4/\text{O}_2 = 3$ , temp.: 973 (blue), 1073 (orange), and 1173 K (gray); (d) a function of  $\text{CH}_4\text{-O}_2$  conc. (catalyst weight: 26 mg, total flow: 26 mL  $\text{min}^{-1}$ ,  $\text{CH}_4/\text{O}_2$  ratio: 2, temp.: 1073 (blue) and 1123 K (orange)); (e) a function of  $\text{CH}_4/\text{O}_2$  ratio (catalyst weight: 40 mg, total flow: 30 mL  $\text{min}^{-1}$ ,  $\text{CH}_4\text{-O}_2$  conc.: 40%, temp.: 1098 (blue), 1123 (orange), 1148 K (gray)); (f) a function of catalyst weight (total flow: 26 mL  $\text{min}^{-1}$ ,  $\text{CH}_4\text{-O}_2$  conc.: 92%,  $\text{CH}_4/\text{O}_2 = 2$  (blue), 3 (orange), 4 (gray), temp: 1073 K).

Machine learning is implemented in order to understand how experimental conditions and  $\text{C}_2$  yields interact with each other in high dimensions. If machine learning can capture experimental conditions, one can interpolate or determine the catalytic activity such as in OCM reaction. In order to introduce machine learning, it is necessary to find appropriate machine learning methods for predicting  $\text{C}_2$  yield as there are numerous machine learning algorithms. Here, five linear and non-linear machine learning algorithms are applied to the prepared 156 data set where the average scores in cross validation and corresponding information are collected in Table 1 and Fig. S1. The following five descriptor variables are chosen: temperature, catalysts weight, total weight,  $\text{CH}_4\text{-O}_2$  concentration, and,  $\text{CH}_4/\text{O}_2$  ratio. Meanwhile,  $\text{C}_2$  yield is set to the objective variable. Note that basic experimental conditions are chosen as descriptors for  $\text{C}_2$  yield because the  $\text{Mn-Na}_2\text{WO}_4/\text{SiO}_2$  catalyst is known to have high stability for the OCM under harsh conditions; however, catalyst information including surface poisoning, particle size, and oxidation state could be potential descriptors for catalytic reactions involving catalyst degradation. The linear regression algorithms chosen include LSLR and SVR (L), and the non-linear regression algorithms chosen include SVR (RBF), RFR, and extreme tree regression ETR.<sup>[9, 10, 32]</sup> Table 1 indicates that two linear regression algorithms give low accuracy while three non-linear regression algorithms give relatively high accuracy. Thus, one can conclude that the relationship between experimental conditions and  $\text{C}_2$  yield is a non-linear matter. Furthermore, the ETR has the highest score among the non-linear machine learning with a score of 86%.

**Table 1.** Results of cross validation using various machine learning methods. Score is  $R^2$  and SD is standard deviation in cross validation.

Type	Machine	Score	SD	Hyper Parameter
Linear	Least Squares Linear Regression (LSLR)	0.32	0.16	N/A
Linear	Support Regression with Vector kernel (SVR (L))	0.27	0.19	N/A
Non-Linear	SVR (RBF)	0.77	0.10	$C = 10$ $\gamma = 0.001$
Non-Linear	Random Forest Regression (RFR)	0.78	0.12	Number of tree = 1000
Non-Linear	Extreme Tree Regression (ETR)	0.86	0.07	Number of tree = 1000

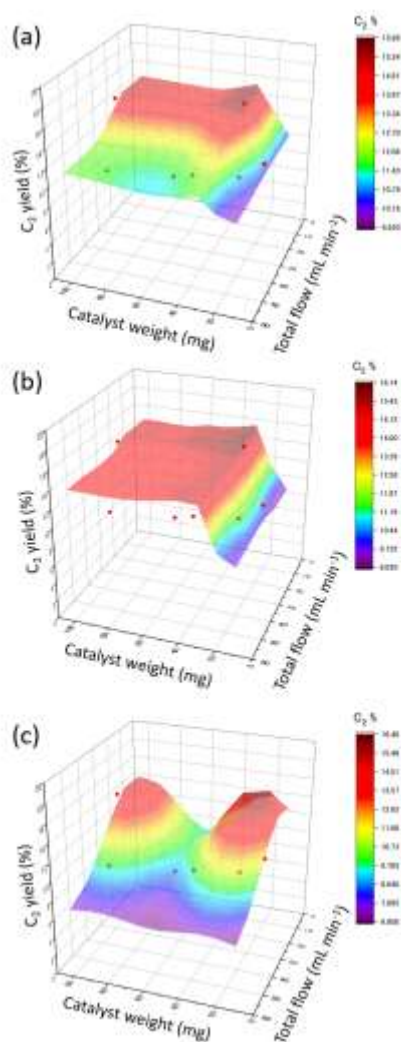
For further validation of the models created by the three nonlinear methods, prediction of  $\text{C}_2$  yield using the three nonlinear methods is performed in order to evaluate how each model represents the  $\text{C}_2$  prediction. The three-dimensional surface plots in Fig. 2 illustrate the predicted  $\text{C}_2$  yield using the non-linear machine learning models as a function of reaction temperature and  $\text{CH}_4/\text{O}_2$  ratio. The experimental data is superimposed onto the three-dimensional plots as indicated by red circles. The predictions by ETR (Fig. 2(a)-(c)) and RFR (Fig. 2(d)-(f)) present a shift of the peak reaction temperature for  $\text{C}_2$  yield where the peak temperature decreases with a decrease of  $\text{CH}_4/\text{O}_2$  ratio. This peak shift is the same as peak shift of the experimental data as clearly seen in Fig. 1(a). On the other hand, the prediction by SVR (RBF) (Fig. 2(g)-(i)) does not show such peak shift, and exhibits an unusual notched change around 1100 K. Thus, the ETR and RFR models are revealed to accurately reproduce the experimental data.



**Figure 2.** 3D surface plots of the predicted  $\text{C}_2$  yield against reaction temperature and  $\text{CH}_4/\text{O}_2$  ratio: (a-c) ETR; (d-f) RFR; (g-i) non-linear SVR prediction. (b), (e), (h): top view of (a), (d), (g). (c), (f) (i): side view of (a), (d), (g). The experimental data are over-layed on the figures as red circles. The other reaction parameters: catalyst weight 100 mg,  $\text{CH}_4\text{-O}_2$  conc 90%, total flow 30 mL  $\text{min}^{-1}$ .

Fig. 3 presents another three-dimensional surface plot of the predicted  $\text{C}_2$  yield against catalyst weight and total flow rate. In the ETR prediction (Fig. 3(a)), the surface plot exhibits a top and slopes on both sides of catalyst weight and total flow rate, capturing the feature of the experimental data. However, such feature is not observed in the RFR prediction (Fig. 3(b)), where a simple cliff-like change is seen along with the catalyst weight. In the case of the RFR prediction, a bimodal shape along with the catalyst weight, an unusual variation, is observed. Therefore, the ETR gives the most accurate model for OCM reactions for the

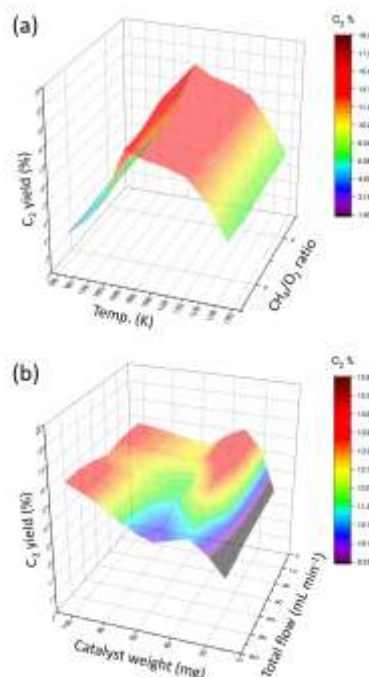
present set of catalysts and models tested, which is consistent with the cross validation score. In the ETR algorithm, the importance of descriptors is not weighted for making decision trees; however, it is weighted in the RFR algorithm. This difference can be viewed as the reason for the higher accuracy of the ETR model.



**Figure 3.** Surface 3D plots of the predicted  $C_2$  yield against the catalyst weight and the total flow rate: (a) ETR and (b) SVR prediction. The experimental data are over-layed on the figures as red circles. The other reaction parameters: temperature 1123K,  $CH_4+O_2$  conc 90%,  $CH_4/O_2$  ratio 3.

Construction of accurate predictive models using a small sampling of experimental data is very attractive for boosting the development of catalyst reaction systems. Here, model construction using a small number of data is investigated using ETR, where the data is selected from 156 data while keeping the diversity of the data as indicated on Table S1. Although the average cross validation score of the ETR model constructed

using 45 data is 0.45, which is lower than that reported for the 156 data, the predicted results are still relatively accurate enough to act as a good guideline for designing experiments as shown in Fig. S1(f). Fig. 4 illustrates  $C_2$  yield predicted by the ETR model based on the 45 data as a function of reaction temperature and  $CH_4/O_2$  ratio (Fig. 4(a)) and that as a function of catalyst weight and total flow rate (Fig. 4(b)). Although the figures do not capture the detailed variation of the experimental  $C_2$  yield by reaction conditions, they roughly agree with Fig. 2(a) and Fig. 3(a). Moreover, ETR with a small data set can be a good guideline for determining the next experimental conditions. In particular, Fig. 4(b) suggests that there might be hot spots for high  $C_2$  yield at 20–40 mg of catalysts weight with low total flow. Hence, machine learning with a small data set can be used to design experiments for achieving high  $C_2$  yield. Although generalizations of non-linear machine learning can be limited due to the nature of random forest regression, machine learning can be a powerful approach to accelerate the understanding of the effects of reaction conditions and for finding the optimal reaction conditions.



**Figure 4.** Surface 3D plots of the predicted  $C_2$  yield by the ETR based on 45 data (a) as a function of reaction temperature and  $CH_4/O_2$  ratio (catalyst weight 100 mg,  $CH_4+O_2$  conc 90%, total flow 30 mL min<sup>-1</sup>) and (b) the catalyst weight and the total flow rate (temperature 1123K,  $CH_4+O_2$  conc 90%,  $CH_4/O_2$  ratio 3).

The importance of the 5 descriptor variables in the ETR model with 156 data is evaluated and shown in Fig. 5. Reaction temperature shows the highest importance among the five descriptors, which is consistent with the experimental results in Fig. 1(a)–(e) showing  $C_2$  yield dependence on the temperature

as well as with the empirical rule of chemical reactions being very sensitive to temperature as usually represented by Arrhenius equation. After reaction temperature, catalyst weight exhibits high importance, but total flow rate shows a low degree of importance. These results suggest that a highly accurate model of the OCM reaction cannot be constructed only by using contact time calculated by catalyst weight and total flow. The higher importance of catalyst weight might reflect higher importance of the amount of active surface sites affected by the desorption rate of the fragments such as proton and hydroxyl groups on the catalyst surface simultaneously generated in the catalytic OCM reaction.<sup>[22]</sup> In fact, the previous studies have suggested that the desorption of the fragments needs higher energy than the activation of methane.<sup>[22]</sup> It is also interesting that  $\text{CH}_4 + \text{O}_2$  conc showed higher importance than  $\text{CH}_4/\text{O}_2$  ratio. This result might reflect that the adsorption of  $\text{CH}_4$  and  $\text{O}_2$  promotes the desorption of the fragments rather than  $\text{N}_2$ . It should be noted that this matter must be carefully investigated using theoretical calculations or experimental spectroscopies to confirm whether the importance reflect the reaction mechanism, since the importance of ETR are determined from contribution during the tree development on ETR.

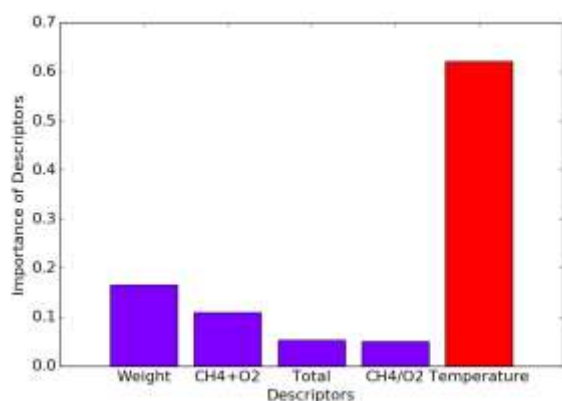


Figure 5. Importance of five descriptors in the ETR prediction.

## Conclusions

Accurate models describing the effect of the OCM reaction conditions on the  $\text{C}_2$  yield can be constructed by machine learning. Two linear regression methods (simple linear and linear SVR) and three non-linear regression methods (non-linear SVR, RFR, and ETR) of machine learning have been examined for constructing models using 156 data with six-dimensions composed of five reaction parameters as the descriptors and  $\text{C}_2$  yield as the objective variable. It is revealed that the relationship between experimental conditions and  $\text{C}_2$  yield lies upon non-linear matter where ETR is found to accurately predict the experimental data. Furthermore, ETR with a small data set of 45 data demonstrates that prediction from machine learning can be a good indicator for designing experiments for achieving high  $\text{C}_2$

yield. This observation suggests that machine learning can be used earlier in the research stage, allowing researchers to apply machine learning on a smaller data set. The machine can do interpolation which allows for gaps in the data to be filled, thereby suggesting potential areas for further investigation. Researchers can then use those preliminary findings to help inform how the next set of experiments should be designed and conducted. Such approach could potentially reduce the time spent on conducting experiments as well as make the experiment design process more efficient. Thus, one can consider that machine learning is an effective tool for understanding and determining experimental conditions in high dimensions, thereby acting as a great aid for designing experiments.

## Method

### Experiment

Catalyst precursors, silica gel (60N),  $\text{Mn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ , and  $\text{Na}_2\text{WO}_4 \cdot 2\text{H}_2\text{O}$  are supplied from Kanto Chemical Co., Fujifilm Wako Pure Chemical Co., and Sigma-Aldrich Co., respectively.  $\text{Mn-Na}_2\text{WO}_4/\text{SiO}_2$  is prepared by a co-impregnation method. A 300 mL of aqueous suspension containing 5 g of  $\text{SiO}_2$ , 0.50 g of  $\text{Mn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ , and 0.45 g of  $\text{Na}_2\text{WO}_4 \cdot 2\text{H}_2\text{O}$  is stirred at 323 K under stirring for 24 h. After evaporation of water at 338 K, the resulting solid is dried at 383 K overnight, and then calcined at 1273 K for 3 h to obtain  $\text{Mn-Na}_2\text{WO}_4/\text{SiO}_2$  containing 1.7wt% of Mn and 7.2wt% of  $\text{Na}_2\text{WO}_4$ .

OCM reaction is performed on conventional fixed bed reactors at atmospheric pressure. Before the reaction, the catalyst inside quartz tubes with 4 mm inside diameter is pretreated under  $\text{O}_2$  flow at 1173 K. OCM reaction is conducted under various conditions using 10–100 mg of the catalyst at 973–1173 K under  $\text{CH}_4/\text{O}_2/\text{N}_2$  with 1–10 of  $\text{CH}_4/\text{O}_2$  ratio and 8–94% of  $\text{CH}_4 + \text{O}_2$  conc. at total flow rate of 8–96  $\text{mL min}^{-1}$  (See Table S1). The effluent gas is analyzed by gas chromatograph. The  $\text{C}_2$  yield (%) is determined by  $((\text{effluent C}_2 \text{ conc} / \text{effluent N}_2 \text{ conc}) / (\text{initial CH}_4 \text{ conc} / \text{initial N}_2 \text{ conc})) \times 2 \times 100$ .

### Machine Learning

Scikit-learn (version 0.17) is implemented for machine learning. The following five machine learning algorithms are implemented: least squares linear regression (LSLR), support vector regression with linear kernel regression (SVR (L)), SVR with RBF kernel (SVR (RBF)), random forest regression (RFR), and extreme tree regression (ETR).<sup>[33]</sup> Hyperparameters of support vector regression with RBF kernel and RFR, and ETR are also optimized. C and gamma are set to 10 and 0.001 in SVR with RBF kernel, respectively. The number of trees in RFR and ETR are set to 1000 where the max depth of trees is set to none, meaning that the tree expands until the minimum numbers of samples to split reach 2. Cross validation is used to evaluate the accuracy of each machine learning algorithm where data is split into 20% test data and 80% trained data. The average  $R^2$  scores of ten random test and trained data are taken and evaluated. Descriptor importance is estimated during the random forest regression model. Random forest regression generates a bunch of decision trees. Within the decision tree, importance is defined according to the number of times each descriptor shows up throughout the decision tree as well as its place within the decision tree.



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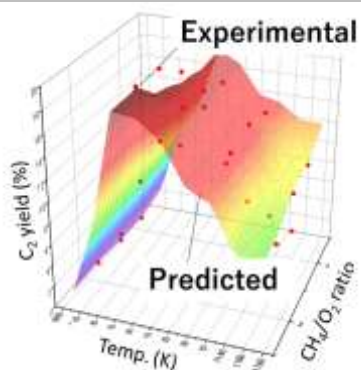
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## FULL PAPER

The challenge in catalytic reactions lies within its complexity coming from high dimensional experimental factors. In order to solve such complexity, machine learning is implemented to treat experimental conditions in high dimensions. Oxidative coupling of methane, methane to  $C_2$  compounds (ethylene and ethane), is chosen as the prototype reaction.



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**Data Driven Determination of Reaction Conditions in Oxidative Coupling of Methane via Machine Learning**